

A Workflow for Characterizing Nanoparticle Monolayers for Biosensors: Machine Learning on Real and Artificial SEM Images

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ABSTRACT

A persistent challenge in materials science is the characterization of a large ensemble of heterogeneous nanostructures in a set of images. This often leads to practices such as manual particle counting, and sampling bias of a favorable region of the “best” image. Herein, we present the open-source software, imaging criteria and workflow necessary to fully characterize an ensemble of SEM nanoparticle images. Such characterization is critical to nanoparticle biosensors, whose performance and characteristics are determined by the distribution of the underlying nanoparticle film. We utilize novel artificial SEM images to objectively compare commonly-found image processing methods through each stage of the workflow: acquisition, preprocessing, segmentation, labeling and object classification. Using the semi-supervised machine learning application, Ilastik, we demonstrate the decomposition of a nanoparticle image into particle subtypes relevant to our application: singles, dimers, flat aggregates and piles. We outline a workflow for characterizing and classifying nanoscale features on low-magnification images with thousands of nanoparticles. This work is accompanied by a repository of supplementary materials, including videos, a bank of real and artificial SEM images, and ten IPython Notebook tutorials to reproduce and extend the presented results.

Keywords: Image Processing, Gold Nanoparticles, Biosensor, Plasmonics, Electron Microscopy, Microscopy, Ilastik, Segmentation, Bioengineering, Reproducible Research, IPython Notebook

1 INTRODUCTION

Metallic colloids, especially gold nanoparticles (AuNPs) continue to be of high interdisciplinary interest, ranging in application from biosensing(Sai et al., 2009)(Nath and Chilkoti, 2002) to photovoltaics(Shahin et al., 2012), even to heating water(McKenna, 2012). The optical properties of nanoparticles are highly sensitive to their morphology. In sensing applications, nanorods(Becker et al., 2010) and nanoshells(Kessentini and Barchiesi, 2012) show demonstrable enhancement over their spherical counterparts; even the AuNP dimer exhibits a central “hot spot”(Cheng et al., 2011). In addition to individual particle morphology, ensemble properties also drastically affect the response of a nanosystem. While nanofilm sensors exhibit an optimal monolayer fill fraction at which sensitivity peaks(Shahin et al., 2012)(Jeong et al., 2011)(Moirangthem et al., 2011), they are also susceptible to degradation through film contamination and aggregation. Since nanoparticle aggregation processes are difficult to control(Kim et al., 2008)(Pease et al., 2010), one must experimentally characterize a nanosystem to ensure quality and consistency between samples. While there are several approaches, including spectral methods(Lopatynskiy et al., 2011)(Khlebtsov, 2008), small-angle X-ray scattering(Gleber et al., 2010), and dynamic light scattering(Jans et al., 2009)(Khlebtsov and Khlebtsov, 2011)¹, high-resolution microscopy (HRM) is still the most direct way to obtain detailed nanoscale structural information.

In this context, quantitation of SEM data can be painstaking, with simple approach involving hand-counting of the particles in a typical image(Sciaccia and Monroe, 2014). Advances in image analysis have enabled the automatic counting and sizing of particles in high contrast images such as transmission electron micrographs(Reetz et al., 2000) utilizing prewritten routines in software packages such as MATLAB™(MathWorks, 2013) or Fiji(Schindelin et al., 2012). In biomedical applications, image

¹For an excellent comparison of AuNP measurements methods, see Ref. (Meli et al., 2012).

analysis from in-house algorithms has been used to classify relevant features in mesoporous silicon for protein delivery (Alexander et al., 2009). In direct relation to particle identification from SEM images, hybrid approaches combining MATLAB routines and custom code have been used to successfully segment nanoparticles images (Singh, 2013).

Despite advances in HRM and image processing, it remains challenging to rigorously and consistently measure and classify nanoscale features in an image which itself is many thousands of times larger. The domain knowledge interrelating microscopy, nanotechnology and image processing is broad, and image processing guides are often very general (Sankur and Lent, 2004), or focused primarily on biology (Acunto and Salvetti, 2010) (Eliceiri et al., 2012) and medicine (Lehmann, 1999). Herein, we present a modern workflow for nanoparticle image processing based on recent advances in open-source software. We first compare several image preprocessing and segmentation techniques based on their performance on both real and novel *artificial* SEM images, then demonstrate how to classify different types of nanoparticles in the same image using the machine-learning application, Ilastik (Sommer et al., 2011). From acquisition to classification, we identify which image processing techniques are the most useful for AuNP characterization. These techniques combined into a single workflow are used to automatically identify tens of thousands of nanoparticles in low-magnification images, group them by species, and eliminate the need for manual counting and biased sampling.

The manuscript is outlined as follows: Section 2 describes best-practices in sample preparation and scanning electron microscope (SEM) imaging of AuNP films, followed by an overview of open-source image processing software. We then present novel artificial SEM images, subsequently used in Section 3 to objectively quantify and compare segmentation and classification tools. Section 3 first describes caveats and best practices for SEM imaging, and follows with a comparative survey of segmentation techniques, including thresholding, edge-based, seeded and semi-supervised learning approaches. Following a discussion on preprocessing, we utilized machine learning applications to classify single particles, dimers and aggregates in both real and artificial SEM images. Section 4 discusses image processing workflows and the role of image processing in HRM techniques other than SEM. For training and dissemination (Editorial, 2014) (Mascarelli, 2014), all results and analysis are available as supplemental IPython (Perez and Granger, 2007) Notebook tutorials (Hughes, 2014a), enumerated in Table 1 and henceforth referred to simply as Notebooks.

2 MATERIALS AND METHODS

2.1 Sample Preparation

Citrate-capped gold nanoparticles (AuNPs) of mean diameter 21 nm were synthesized according to the standard reduction protocol (Turkevich et al., 1951). Size distributions were ascertained through careful centroid-centroid distance measurements of dimer particles in TEM and SEM images; complimentary size and concentration data were obtained through empirical spectroscopic approaches (Khlebtsov, 2008) (Haiss et al., 2007) (Amendola and Meneghetti, 2009). AuNPs were deposited onto amino-functionalized optical fibers [GIF-625 Thorlabs] using a protocol similar to Ref. (Shahin et al., 2012). Prior to imaging, fibers were immersed in ethanol to remove contaminants like those found in Fig. (1b), which absorb quickly onto the highly-charged, functionalized glass.

2.2 Software

There are numerous software tools for image processing (Eliceiri et al., 2012). Popular open-source libraries include Fiji, scikit-image (van der Walt et al., 2014) and Octave (Kovesi, 2000), while commercial solutions in MATLAB™ and Mathematica™ are also available. Fiji is a distribution of the highly successful ImageJ (Schneider, C.A., Rasband, W.S., Eliceiri, 2012) platform with an impressive suite of plugins geared towards biology and microscopy, such as MOSAIC (Sbalzarini and Kournoutsakos, 2005) for particle tracking, and Weka (Arganda-Carreras, I., Cardona, A., Kaynig, V., Schindelin, 2011) for trainable segmentation. Scikit-image is a functional library that boasts an elegant API and integration with the scientific Python (Peterson, 2001) stack. Mahotas (Coelho, 2013), another Python imaging library, has been recently employed in the analysis of SEM images of block copolymer nanocomposites (Ploshnik et al., 2013). Fiji and scikit-image were used predominately the results presented here; a related library, pyparty (Hughes, 2014c), assisted in artificial image generation and particle analysis. Supervised segmentation was performed in Ilastik.

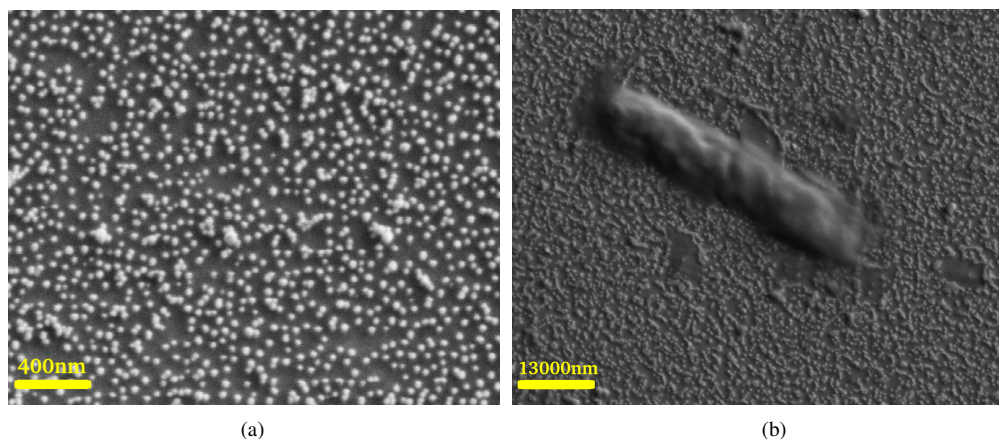


Figure 1. Clean vs. contaminated AuNP films. Typical 22nm monolayer of AuNPs at 100000X (a), and 30000X monolayer with microbial contamination (b). Several examples of other commonly observed surface contaminants and defects are available in supplemental data. One can see examples of small AuNP aggregates forming.

2.3 Test and Sample Images

To compare image processing methods objectively, three high-resolution (3072 x 2304) artificial SEM images were created. The benefit of using artificial images is the exact particle brightness and sizes are known a priori, so segmentation errors can be quantified to the pixel. Each image consists of circles of nominal diameter 30 pixels ($\sigma = 3$) arranged into singles (50%), dimers (25%), trimers (12.5%) and tetramers (12.5%) of varying particle size and orientation. 1170 non-overlapping² particles were overlaid onto a mesh of periodically varying brightness ranging from 80-170, resulting in a surface coverage of 21.4%. The particle brightness ranges from 190 to 250 based on a scaled beta-distribution, $\beta(a=2, b=2)$, slightly biased towards brighter clusters. Brightness variation was chosen to reflect observed distributions in actual samples. Brightness in this context refers to the monochromatic pixel intensity range between 0 and 255.

Fig. (2) shows the three test images, referred to as RASTER, SMOOTH and NOISY, and will be referred to in this special font throughout. RASTER depicts particles with sharp, distinct boundaries. The SMOOTH test image applies a Gaussian filter ($\sigma = 3\text{px}$) to RASTER, resulting in blended, realistic boundaries. The NOISY test image is the SMOOTH image with Gaussian noise added to 25% coverage. In practice, actual electron microscope noise may not be normally distributed (Nemota, 2012). Notebook 1 is provided to generate artificial SEM or TEM images.

Twelve real SEM images ranging in magnification from 30-100kX are included in the supplemental data. These include ideal and flawed images with defects of low and varying contrast, non-circular particles due to astigmatism, striations from detector discharge (JEOL, 2014) and noise. The real SEM images are utilized primarily for comparing *thresholding* methods in the next section, and are available for download in the supplemental data.

3 RESULTS

It is difficult to generalize the workflow of image processing,³ as the optimal approach is often reached after cycles of trial and error. Most often, the final workflow involves 5 steps: **Acquisition** → **Preprocessing** → **Segmentation** → **Labeling** → **Measurement and Object Classification**. In the context of AuNPs, this corresponds to first obtaining a suitable image, then separating the particles from background (segmentation), followed by labeling and grouping the particle subtypes (classification), and finally

²Intra-cluster overlap was allowed and ranged to about 20%, for example in tetramers, but overlap between trimer A and dimer B was avoided.

³Woods presents image processing in 11 chapters (Woods, 2002), but notes that segmentation and enhancement are not necessarily separate. In addition, some segmentation algorithms incorporate preprocessing; for example, the Canny filter uses Gaussian smoothing.

Notebook	Description
1	Generating Test Images
2	Measuring Digitization Errors in Small Particles
3	Quantifying Segmentation in Binary Images
4	Thresholding, Edge, and Seeded Segmentation
5	Denoising and Filtering
6	Contrast Enhancement
7	Intro to Particle Classification
8	Segmentation Error in Ilastik
9	Classifying Nanoparticles: Ilastik vs. User Partitioning
10	Fourier Filtering of the Noisy Test Image

Table 1. Hyperlinks to supplemental IPython Notebooks.

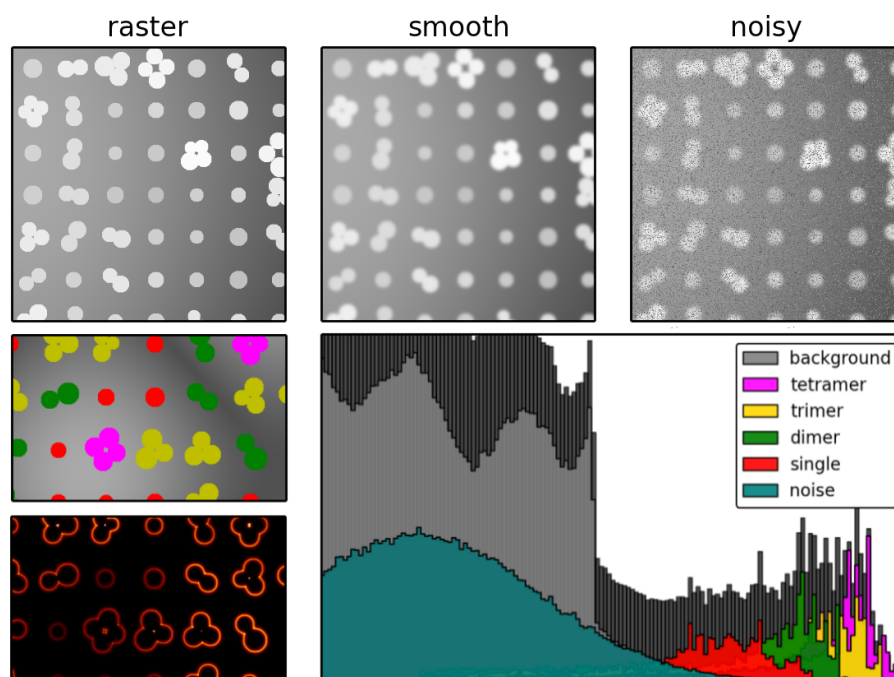


Figure 2. Three artificial test images referred to as RASTER, SMOOTH and NOISY. **Top:** Cropped (512 x 512) region of each image. **Left:** Color-coded particle species and artificially colored smoothed edges. **Bottom right:** Brightness histogram decomposed by source, shown from 80 to 255 pixels. The noise and smoothing effectively mix the background and particle populations which makes segmentation more challenging on these images. The color scheme of red, green, yellow and magenta will be used consistently to refer to singles, dimers, trimers and tetramer particle types, respectively.

producing distributions based on size, shape, brightness and other object features (measurement). Each of the subsequent sections corresponds to one of these steps⁴, with segmentation and object classification receiving the most attention. We deviate from the step order by discussing segmentation prior to preprocessing, since shortcomings in the segmentation naturally motivate a discussion of noise removal and contrast enhancement, two important preprocessing techniques.

⁴Labeling is not discussed in detail because particle labeling routines (connected-component algorithms) are easy accessed, and give mostly identical across image processing libraries.

3.1 Acquisition

Images (3072 x 2304) were acquired using a Zeiss™ EVO LS 25 SEM using the SE2 detector⁵ at 1kV over a range of magnifications. Nominal line integration and scan average settings resulted in roughly a three minute acquisition time. The SEM chamber vacuum was pumped for at least an hour before imaging; and the working distance was 5.5mm. AuNPs of diameter under 20nm in diameter may prove difficult to image reliably, due to their low contrast and distinct halo, which has been previously discussed from a theoretical standpoint(Klein et al., 2011). In such cases, we obtained sharper edges using an annular secondary electron detector, but at the cost of higher sensitivity to charging. While the theoretical resolution of a 1kV beam is about half of the wavelength, or .02nm(Barlow, 2004); the pragmatic value for low-voltage is still about 2nm(Microscopy, 2014). Improvements in optics and detectors are narrowing this gap by overcoming issues related to beam widening,⁶ chromatic aberration, and insufficient escape volume of the signal carriers(Amako et al., 2002)(Dellby et al., 2001). For a comprehensive evaluation of SEM imaging aberrations and their causes, consult Ref. (JEOL, 2014). Of those we encountered, charging, astigmatism, and detector discharging were the most difficult to correct for, as they induce particle warping and local contrast variations simultaneously.

While it is advantageous to image at a large field of view, this lowers particle resolution and leads to at least two types of digitization errors. The first type is intrinsic to measuring digitized particles (i.e. squaring the circle), and is described in more detail in Section 3.5. The second type is related to the particle size distribution (i.e. size histogram). At low magnification, the particles are too pixelated, resulting in sparse binning. This is illustrated in Fig. (3), which shows the particle area distributions of the same sample, imaged at 5000X and 30000X. The measured mean, variance and other important statistical parameters are no longer reliable. We observed that suitable particles distributions were obtained when the object of interest is *at least 10 pixels across*. Ergo, for 22nm diameter AuNPs, the magnification and resolution settings should result in a scale no larger than 2.2 nm per pixel. At such a scale, just under 15000 non-overlapping 22nm diameter AuNPs could fit in a 3072 x 2304 resolution image, covering a surface area of 34 μm^2 . Images can be regenerated or modified using notebook 1.

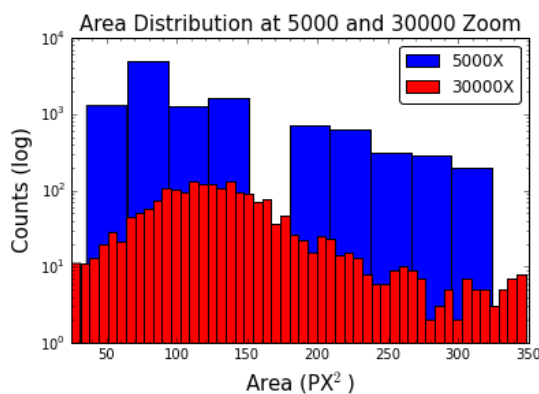


Figure 3. The effect of a 6-fold magnification change on the particle area distribution in same sample. The profile of the distribution is lost at low resolution.

3.2 Segmentation

To group the many approaches to segmentation(Narkhede, 2013), we've chosen the following categorization: *thresholding* refers to the segmentation algorithms that primarily analyze pixel brightness. *Edge-based* segmentation operates on object boundaries, related to the image gradient or Laplacian. Morphological watershedding(Beucher, S ; Lantuejoul, 1979) and random walk segmentation(Grady, 2006) have been paired due to phenomenological similarities. Such approaches treat the image as a topographic barrier; in watershedding the analogue is to water basins, in random walks to a diffusion

⁵The SE2 is an Everhart-Thornley detector that collects a combination of secondary and back-scattered electrons to give both compositional and topographical resolution, respectively.

⁶The repulsion between low-energy electrons make them difficult to focus into a narrow beam.

barrier, and both approaches require user-provided *seeds*.⁷ These segmentation algorithms represent a broad sampling of various segmentation methodologies; they are straightforward to implement in scikit-image and/or Fiji, and they provide a natural segue into the topic of semi-supervised segmentation. Our overview of segmentation is non-exhaustive. Some popular methods we did not examine include unsupervised clustering (Tan et al., 2013), various region-based techniques and several graph methods such as normalized cuts (Malik, 2000).

We assessed performance based on accuracy in segmenting the artificial images. Since the exact particle extents in the test images are known a priori, segmentation performance can be evaluated objectively. Overthresholding and underthresholding are quantified as the false positives (fp), negatives (fn) and net (fp + fn) of the pixels in the segmented image (Γ_1) as compared to the binary version of the RASTER test image (Γ_2). Since the binarized images are boolean arrays, this is equivalent to the set intersection ($\Gamma_1 \cap \Gamma_2$), as demonstrated in Notebook 3. Because the comparison is to the rastered particles, and not the smoothed particles, we expect the majority of segmentation methods to overestimate the boundary size.

3.2.1 Thresholding

Fiji is distributed with an auto-thresholding plugin (Landini, 2013) that can simultaneously apply 25 segmentation algorithms on a single image. Of these, 16 segment based on information in the overall, or *global*, image brightness, while the remaining 9 parse *local* brightness information to segment subregions of the image separately. We ranked the 25 algorithms based on their performance on real SEM images, **and selected only the top performing methods for further comparison on the artificial images**. A collage summarizing these results is available in the supplemental material. In short, we found that most of Fiji's global auto-thresholding routines failed in the presence of the contrast gradients found in real AuNP SEM images. A global brightness cutoff; that is, setting a brightness value and screening all pixels below it, performed well within a narrow cutoff range.

In regard to the 9 local auto-thresholding algorithms, Otsu (Otsu, 1975) performed the best on the real SEM images, followed by the Bensen and MidGrey methods. Additionally, scikit-image's Gaussian adaptive threshold function performed reasonably well on some of the sample SEM images.⁸ Therefore, we chose a global pixel cutoff, Gaussian adaptive thresholding and local Otsu thresholding as three methods for further evaluation on the artificial test images.

Both adaptive and Otsu thresholding performed poorly on all three of the test images, as they were highly sensitive to noise, as well as local contrast variations in the background gradient as illustrated in Fig. (4). A global brightness cutoff segmented the test images quite well, when set at or near the optimal cutoff value. For the noisy test image, the optimal threshold value is 187 grayscale, reaching only 7.4% net error as shown in Fig. (5). Unfortunately, finding the optimal threshold often requires manual tuning, limiting its utility in batch processing; although we acknowledge that automated approaches to locating the optimal global threshold based on summing weighted normal distributions have been proposed (Woods, 2002) (Dickerson, 2001). It is important to recognize that the test images were designed such that the dimmest particle is still brighter than the brightest region of the background. Thus, the artificial images favor the global cutoff method by design. In reality, local electronic variations in SEM images blur the global separation of background and particles, rendering them impossible to threshold via global cutoff.

3.2.2 Edge-based segmentation

It is often useful to work with the gradient or Laplacian of an image, rather than the image itself. The gradient emphasizes regions of rapid brightness changes, such as the border between nanoparticle edges and image background. Edge segmentation techniques are well developed in commercial and open access packages, and are well-suited to resolve surface features in SEM images (Midoh et al., 2007). Since nanoparticles are nonporous, if their outlines can be accurately identified, then segmentation follows merely from filling in the bound regions. Since it is straightforward to fill an enclosed region of a binary image with the standard morphological operations (Cressie and Serra, 1988) found in scikit image, the successfulness of this approach depends on how accurately the particle boundaries can be identified. We chose the Sobel (Sobel and Feldman, 1968) and Canny (Canny, 1986) filters as candidates for edge detection on the three test images.

⁷While watershedding without user-specified seeds is possible, it tends to result in oversegmentation (Woods, 2002).

⁸scikit-image's adaptive thresholding "method" parameter (Gaussian, mean, median etc...) specifies how the threshold value is determined from the local pixel neighbourhood. Gaussian provided the best results for our images.

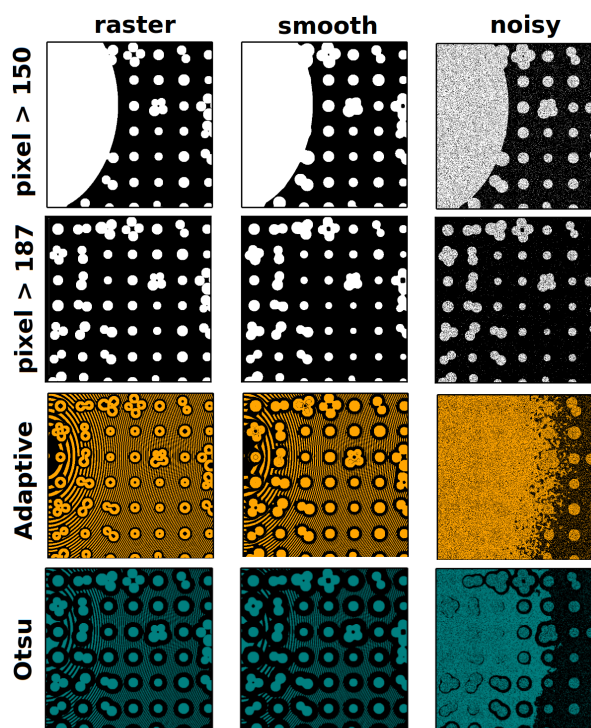


Figure 4. Three thresholding methods applied to the RASTER, SMOOTH and NOISY test images. **Row 1:** Cutting out all pixels below a brightness of 150 leads to significant over-thresholding. **Row 2:** An optimal cutoff of 187 gives lowest segmentation error achievable when applying the global cutoff method to the NOISY image: about 7.4% error as shown in Fig. (5a). **Rows 3/4:** Gaussian adaptive thresholding and local Otsu thresholding both fail in the presence of the complex background and noise.

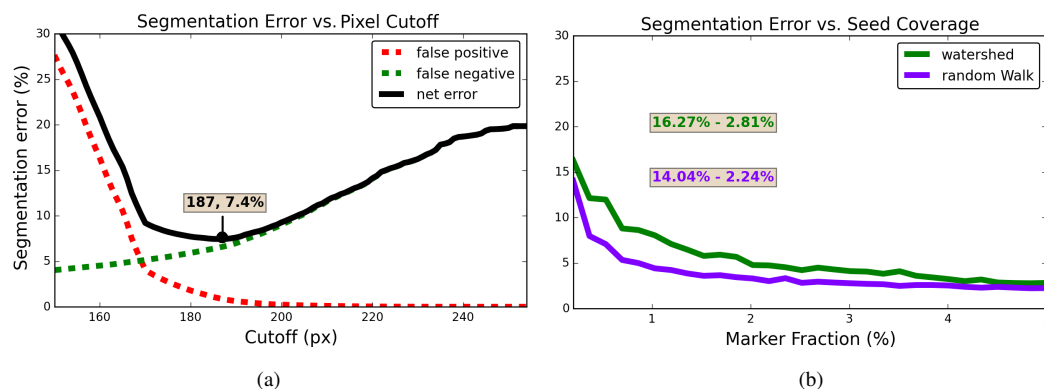


Figure 5. Comparing segmentation error on NOISY between the global cutoff, watershed and random walk methods: **(a)** Pixel false positives and negatives for a global brightness cutoff shows minimal segmentation error of 7.4% at brightness 187. **(b)** Segmentation error for random walk and watershed methods as a function of seed marker fraction.

The Canny filter is a widely-used edge-detection technique, known for its sensitivity to weak edges and robustness to noise. Canny works by first smoothing an image, then tracing edges based on the strength of the image gradient (Green, 2002). Canny employs a hysteresis filter to remove small unconnected fragments, or “streaks”, and retain real edges (Ding and Goshtasby, 2001). The Sobel operator does not find edges directly; it computes the gradient of the image, and then one must apply a cutoff (masking) to

retain the strongest gradients, which in the case of nanoparticles occur at the particle edges. Following both methods, a binary closing operator must be applied to fill the connected components. Fig. 6 from top to bottom shows the Sobel outlines, corresponding masks, and filled outlines from both the Sobel and Canny edges. Canny has three tunable parameters: σ for the Gaussian smoothing, and the upper and lower thresholds in hysteresis, and the results in Fig. 6 are based on the best results after a basic parameter sweep (Notebook 4).

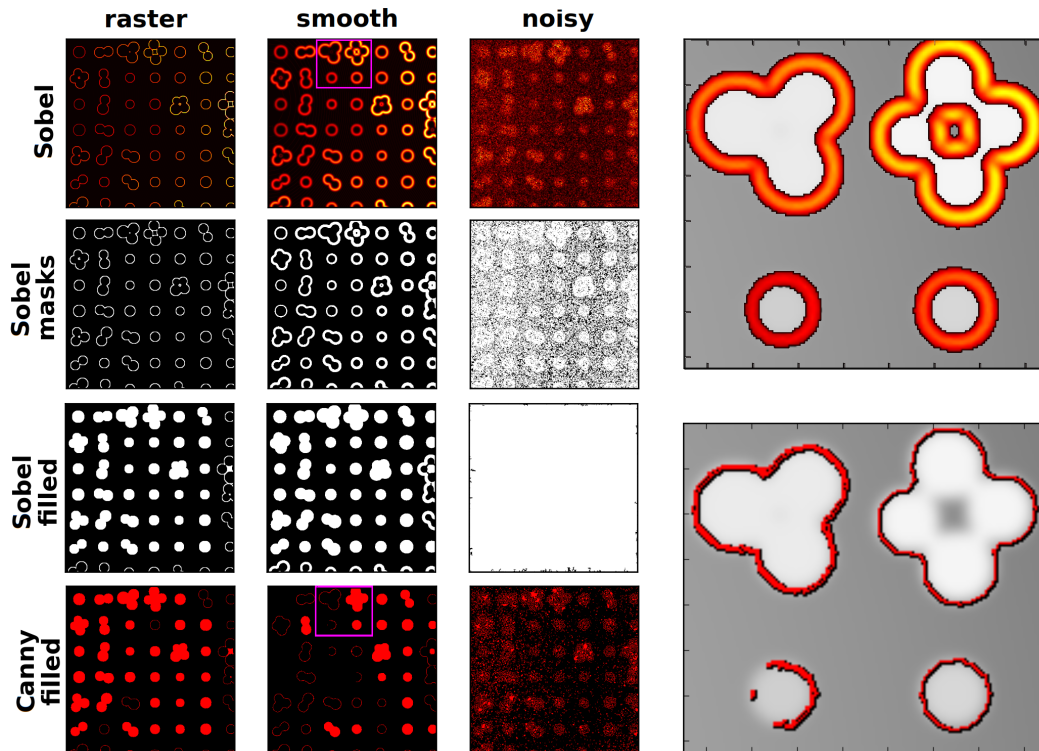


Figure 6. Sobel and Canny edge detection and segmentation applied to RASTER, SMOOTH, NOISY, respectively. **Left (top to bottom):** Sobel gradient with color proportional to gradient intensity; masks corresponding regions where the gradient is stronger than a cutoff value; binary filling of Sobel masks; Canny edges and subsequent binary filling. **Right:** Sobel (top) and Canny (bottom) edges superimposed onto the original SMOOTH image, corresponding to the rectangles in the left plot. Canny edges are sharp, but prone to “streaking” and difficult to fill. Sobel edges are very thick, tend to overestimate particle bounds, and require an additional masking step.

As with pixel thresholding, edge-segmentation also fails in the presence of noise. Absent of noise, both the Sobel and Canny filters produced sensible particle edges. Canny’s edges are thin and precise, but many outlines are not fully connected, and hence cannot be filled. This effect is more pronounced in the SMOOTH image, which has less sharply defined boundaries to begin with. Sobel on the other hand produces thick edges, which overextend the true particles boundaries, but are less susceptible to streaking. Binary filling yielded more particles from the Sobel outlines, but not all the particles could be filled. Even the Sobel edges have small breaks, especially around dim particles on bright background. These results could potentially be improved through fine-tuning some of the morphological filling parameters, or employing a multi-scale edge-finding routine (Sumengen and Manjunath, 2005), but as it stands, edge-filling was unsuccessful at segmenting the test images. Even still, edge features are vital to the seeded and semi-supervised segmentation techniques that will be discussed in the next sections; their general importance to image processing should not be understated.

3.2.3 Seeded segmentation

In seeding, one specifies a collection of marker pixels corresponding to the objects of interest, and a collection corresponding to the background. Seeds were acquired by random sampling from the binarized

RASTER image at marker densities ranging from 10% down to 0.4% of the total pixel count and were split evenly between object and background (i.e. 10% = 5% object, 5% background). The Sobel operator was used to assign elevations for watershedding. Segmentations of the test images by the watershed and random walk methods are shown in Fig. (7).

Both of these methods outperformed thresholding and edge-segmentation on the NOISY image. Watershed actually performed better around SMOOTH particle boundaries, rather than the sharp edges of RASTER. Fig. (5b) shows the accuracy of the segmentations on the noisy test image as a function marker density. For the test images, random walks outperforms watershedding; however, both worsen asymptotically for marker densities less than 1%. Likewise, the segmentation error converges to about 2%; that is, 98% of the pixels in the image were correctly assigned to particles or background. The segmentation error is mostly false positives since the smoothing of the particle edges leads to an overprediction of particle extents. This is illustrated in Fig. (10).

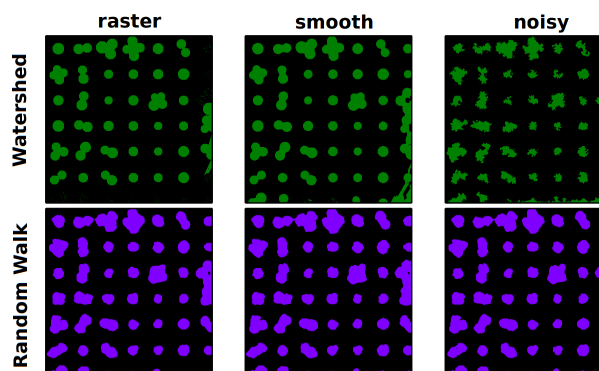


Figure 7. Watershed and random walk segmentation results for 1% marker fraction on all three test images. Watershed basins were set as the Sobel gradient of each image, as shown in Fig. 6 (top left). The predicted particles from watershed and random-walk segmentation are shown in rows two and three, respectively.

3.3 Preprocessing: Contrast Enhancement and Denoising

Because of the likelihood of contrast variation in SEM images, we considered what effects contrast enhancement would have on a low-contrast AuNP image, and how they might effect the subsequent segmentation step. We applied the following three scikit-image histogram correction methods on the dim sample image: *global equalization*, *adaptive equalization* and *contrast stretching* (Robert Fisher, Simon Perkins, Ashley Walker, 2003). Since this image has a very narrow brightness distribution, each technique resulted in broadening as seen in Fig. (8a). To test how the segmentation would be affected, we applied global Otsu thresholding using the default parameters in Fiji to the original and corrected images.

Fig. (8b) illustrates that Otsu sufficiently segments both the original and stretched images; but poorly segments the equalized image. It shows that image dimness did not correspond with poor segmentation. This is not true in general, as there are several examples of contrast correction improving segmentation accuracy (Salihah and Mashor, 2010) (Humayun and Malik, 2013). Furthermore, workflows involving human judgements, particularly in medical imaging, benefit from contrast correction in another facet: it mitigates bias arising from perceived image quality (Isa et al., 2003). Differences in images, segmentation styles and contrast correction techniques make it difficult to conclude if contrast correction is generally favorable or unfavorable in AuNP workflows.

By far, the noisy test image was the most difficult to segment, and so was the subject of four denoising approaches, starting with mean and median rank filters (Soille, 2001). Mean filtering tends to degrade particle boundaries by oversmoothing. The median filter sharpens boundaries and works well for sparse noise, but performs poorly for the 25% corruption of the noisy image. Next, we applied a bilateral filter (Tomasi, C., Manduchi, 1998) and the Chambolle (Chambolle, 2004) total variation filter. The bilateral filter smooths while preserving boundaries, so it combines the strengths of both the mean and median filters. Both the bilateral and Chambolle methods outperformed standard rank filters and are shown in Fig. (8b). These four filters are all spatial-domain techniques. In Notebook 10, we demonstrate

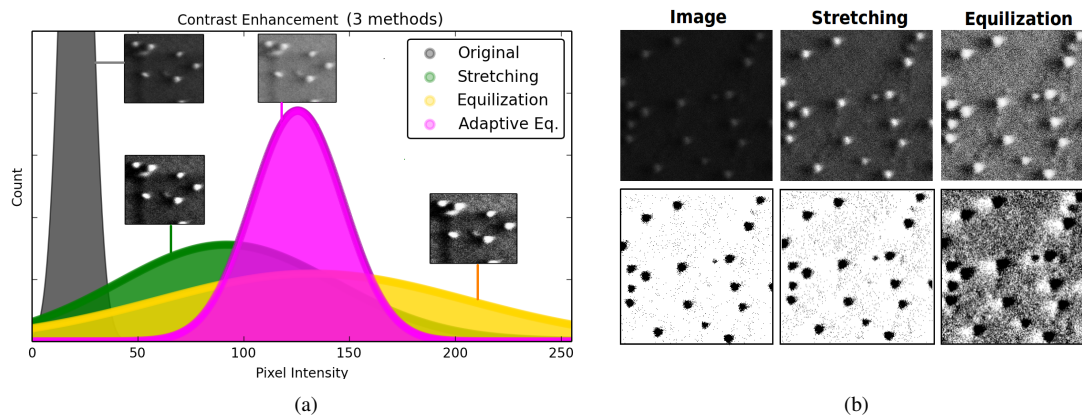


Figure 8. (a) The effects of contrast enhancement, stretching, equalization and adaptive equalization on a low contrast AuNP SEM image. Inlays show a cropped region of the image after enhancement. (b) Global Otsu thresholding applied on the original, stretched and equalized images. After equalization, Otsu segmentation is no longer effective.

low-pass and band-pass filters in the frequency-domain, and find that with the correct set of parameters, the band-pass filter removes contrast variation from the background and eliminate most of the noise, but also distorts the shape of the particles. More in-depth presentations of denoising and contrast enhancement are available in Notebooks 5 and 6, respectively.

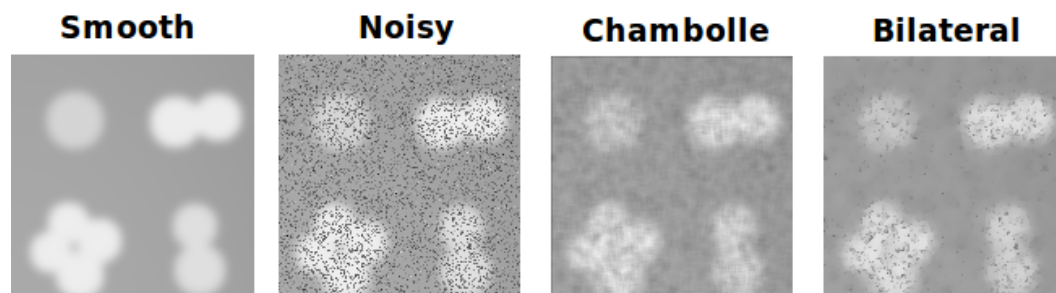


Figure 9. From left to right: 150px² region of SMOOTH, NOISY, Chambolle (weight = 0.3) and bilateral ($\sigma = 0.35$) filters.

3.4 Semi-Supervised Segmentation

In recent years, open-source libraries like scikit-learn (Pedregosa, F. and Varoquaux, G. and Gramfort, A. and Michel et al., 2011) and SimpleCV (Demaagd et al., 2012) have made great strides in assimilating machine-learning utilities into a comprehensive API, while interactive applications like Ilastik and Weka have made semi-supervised learning quite accessible. In semi-supervised learning, one first labels a few objects of interest, akin to seeding in Section 3.2.3. Weka and Ilastik both provide a wand tool to simplify this task. Next, one selects the feature or features that distinguish the objects from the background. Features may incorporate brightness, edge, size, orientation and texture information, among others; however, for segmentation, brightness and size features are usually sufficient. The features and labels are then used to train a random forest (Breiman, 2001) classifier, which predicts the remaining object groups and finally returns the labeled image. To reduce uncertainty, more labels are added and the classifier is updated iteratively. Once adequately trained, a classifier can be stored and reused for batch processing.

An Ilastik classifier based on size and brightness features was trained on the noisy test image. Two background and two particles labels were sufficient to produce a segmentation error of only 2.7%. Eight additional labels reduced error to 2.5%. These ten labels make up less than 0.1% of the extent of the image, or about 5000 pixels. By contrast, random walker segmentation required 3% marker fraction

(2×10^5 pixels) to reach the same accuracy, and the labels were spread out more uniformly across the image. Size and brightness features worked well in segmenting our NOISY test image because, while the noise can be as bright as the particles in some regions, it is still composed of singular pixels. Therefore, it can be distinguished based on size features. A classifier privy to brightness information alone could not segment NOISY. This is reflected in Fig. 2 where the noise contribution to the overall brightness effectively *couples* the background and particles distributions, which are otherwise separate and can be segmented trivially through a pixel threshold cutoff.

A salient restriction of classification approaches is the requisite of feature consistency between images. This is illustrated in Fig. (10), in which a classifier trained on the noisy image is used to segment the smoothed image, resulting in a doubling of overthresholding (false positives). This has important implications for classification in batch processing, since even under careful SEM operation, it can be difficult to obtain images with brightness and sharpness, especially for small particles on rough surfaces. In such cases, preprocessing, in particular contrast equalization, can improve sample-to-sample consistency prior to segmentation. A workflow that incorporated contrast equalization would complement a classifier trained on evenly illuminated images. When switching between magnifications or detectors, we recommend separate classifier for each case.

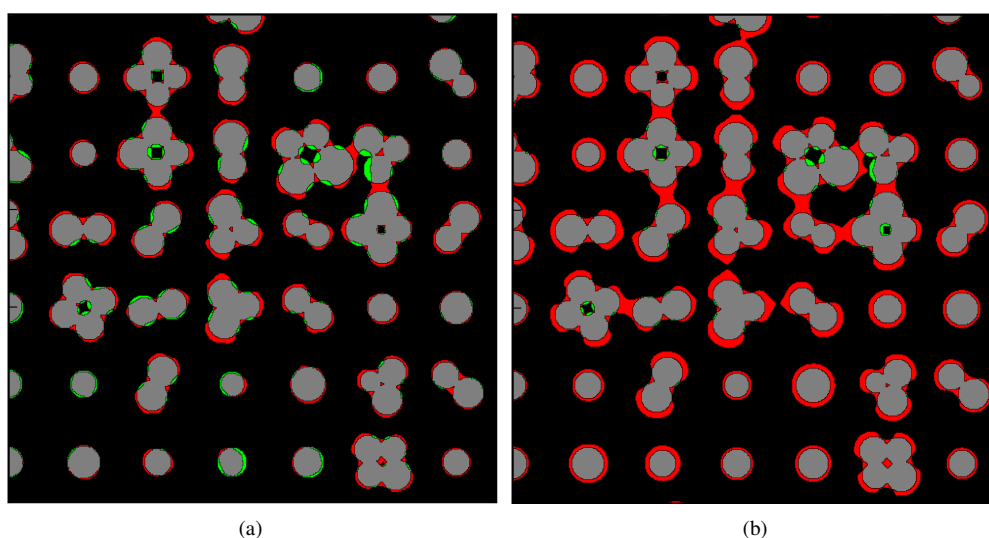


Figure 10. Segmentation error visualized: an Ilastik classifier was trained on, and subsequently used to segment, the NOISY test image (a). The same classifier was then used to segment the SMOOTH test image (b). Since the classifier is trained to expect noise, it actually performs worse on a noise-free image like SMOOTH. In general, the predictive power of a classifier will decline with the degree of dissimilarity between the training data and the sample data. The true particle extents are shown in grey, while red and green depict regions of overthresholding (fp) and underthresholding (fn), respectively.

3.5 Descriptors and Measurements

Once the particles have been segmented and labeled via connected-component algorithms (Wagner and Lipinski, 2013), one typically generates distributions and statistics based on particle descriptors such as area, perimeter and circularity ($C = 4\pi \times \text{Area}/\text{Perim}^2$). Particle descriptors are returned from encoding methods (K Benkrid, 2000) based on generalized morphological operations. This may result in errant descriptors for small particles, especially those with curved edges. For circular particles, one may expect the deviation to vary geometrically; that is, from a single pixel square ($C=0.785$) to a perfectly rastered circle ($C=1.0$), but this tends not to be the case (Hughes, 2014b). Fig. (11) shows the circularity as a function of radius measured with the default encoding methods of scikit-image, Fiji/ImageJ and the a separate algorithm in the ImageJ Particles8 plugin (Landini, 2008). Fiji's default encoding actually corrects for small-pixel circularity and results in $C=1$ for circles of radii 50 pixels or greater. The Particles8 plugin correctly estimates the single pixel square circularity. It is therefore very important be aware of measurement errors arising from the encoding and digitization of the particles themselves.

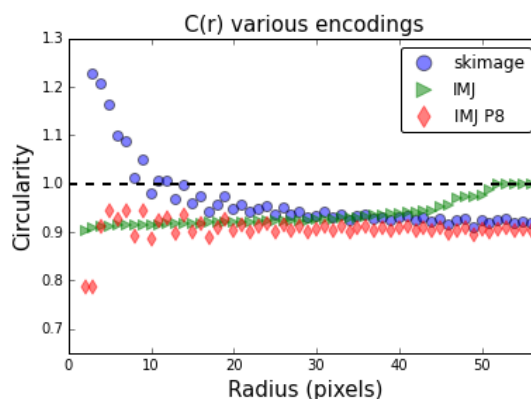


Figure 11. Circularity of rastered circles(Zingl, 2012) of increasing radius with encoding methods used by scikit-image, Fiji/ImageJ and the ImageJ Particles 8 (IMJ P8) plugin. IMJ P8 correctly predicts the single-pixel circularity ($C=0.785$), while the default Fiji encoding converges to $C=1$ for $r \geq 50$.

3.6 Classification

After segmenting and labeling the particles, the next step is to classify them. To classify objects, one first must determine which features best distinguish one type of object from another. For us, it is quite important to characterize the distributions of the following subgroups: *singles*, *dimers*, *flat aggregates* and *piles* (aggregates, in which nanoparticles are visibly stacking), as each contributes differently to the overall optical response, and hence sensitivity and dynamic range, of our plasmonic biosensor. The following description shows how to group particles of similar features.

3.6.1 Classifying Aggregates in SEM Images

In Section 3.4.4, we showed that Ilastik was able to discern particles from background using a semi-supervised classifier, trained with brightness and size features. With *only* brightness and size information, is it possible to further separate the particles into the aforementioned subgroups? To answer this, we employed Ilastik's *pixel classification workflow*. Using the AuNP image in Fig. (1a), we labeled several particles as singles, dimers, flat aggregates and piles, and classified based on size and several brightness features, such as mean particle brightness. The group predictions failed, as shown in Fig. (1a). This reflects that size and brightness are not correlated with these particle classes; for example, piles are not always brighter or bigger than flat aggregates.

Recently, Ilastik introduced the *object classification workflow*. This workflow introduces new shape and texture features, underpinned by the feature accumulator library, VIGRA(Köthe, 2013), and enforces the constraint that the entire extent of a particle fit one of the predicted groups, rather than partially belonging to several groups as was the case in (Fig. 1a). After incorporating the *RegionRadii* descriptor, which makes use of the principal components axes of each object, our retrained classifier predicted much more sensible nanoparticle groups as shown in Fig. (1b). A step-by-step video tutorial for predicting these groups is included in the supplemental materials.

3.6.2 Object Classification in Test Images

The test images are composed of four particle types: *singles*, *dimers*, *trimers* and *tetramers* of varying brightness, size and orientation. This offers a unique opportunity measure Ilastik's predictive power in regard to object classification and illustrate its advantages over a user-defined classifier. A simple example of what is meant by a user-defined classifier would be to classify all particles of diameter $< 50\text{nm}$ as *type A* and all $\geq 50\text{nm}$ as *type B*.

For manual classification in the test images, we looked for a pair of particle descriptors to optimally distinguish the four particle types. We limited our pairings to size (e.g. area) and shape (e.g. eccentricity) descriptors. Poor pairings occurred between redundant descriptors, for example area and perimeter as shown in Fig. (13a). A suitable pairing turned out to be *circularity* (C) and the *semi-minor axis length* (β) of an ellipse fit to the particle, as this pair nicely incorporates size and shape information.

Based on clustering observed in the scatter plot of particle circularity vs. minor axis length (Fig. 13b), we used *pyparty* to define the following partition (shown as white dotted lines):

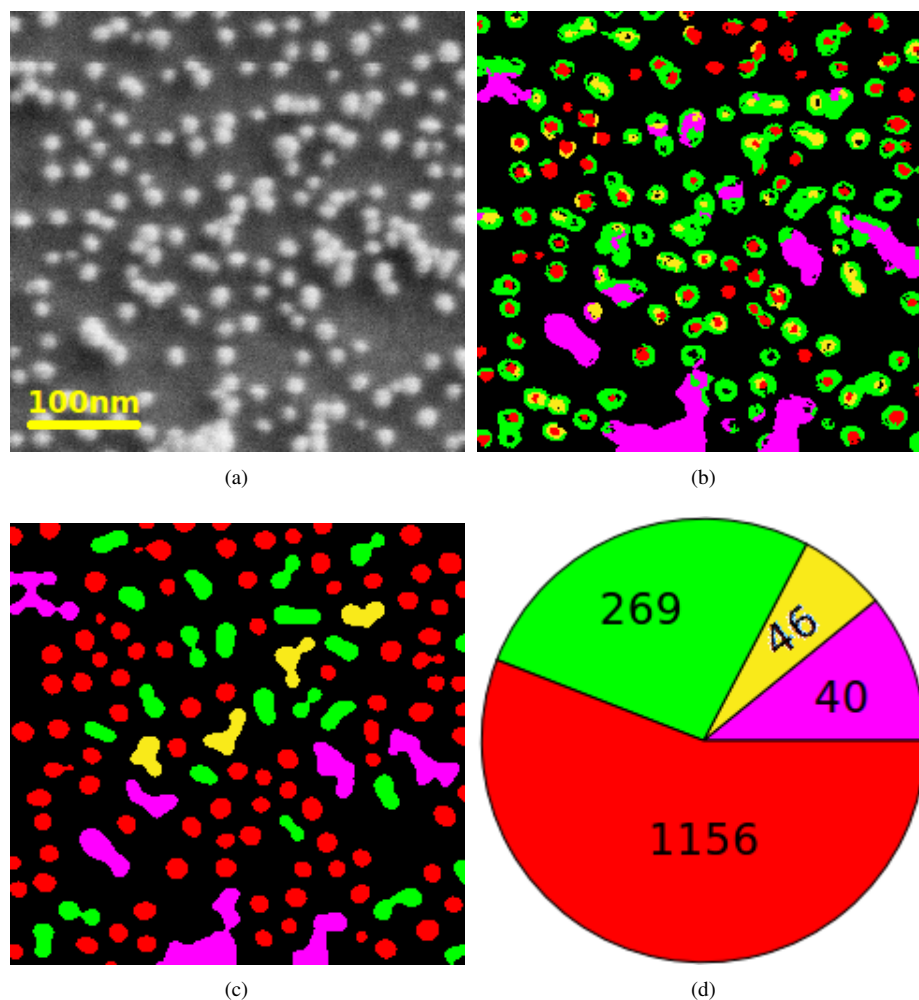


Figure 12. Ilastik predictions of **singles**, **dimers**, **flat aggregates** and **piles** on a zoomed region of image from Fig. (1a). Predictions from pixel classification workflow (b) and object classification workflow (c). Pie chart (d) indicates the number of particles identified in the full image. Wedge size is proportional to the area covered by each group. The net particle area is 24.93% of the total image area.

$$\begin{aligned}
 \text{Singles} &= (\beta < 42, C > 0.85) & \text{Dimers} &= (\beta < 42, C < 0.85) \\
 \text{Trimers} &= (\beta > 42, C > 0.6) & \text{Tetramers} &= (\beta > 42, C < 0.6)
 \end{aligned}
 \tag{1}$$

Ten particles were labeled to train the Ilastik classifier: 3 tetramers, 3 trimers, 2 singles and 2 dimers, using the descriptors *Count*⁹ and *RegionRadii*, rather than circularity and minor axis length. The descriptors are different because the manual partitioning was done in pyparty, which utilizes descriptors defined in scikit-image, rather than VIGRA. Two challenges with manual partitioning are apparent: first, for more than two feature dimensions, one must define an n-dimensional feature space, and the cuts become hyperplanes which are impractical to implement. Secondly, finding the optimal cuts is non-trivial. Ilastik nicely automates both of these tasks.

Ilastik's predictions and the true groups are shown in Fig. (14). The manually assigned partitions are filled in with bold color. It is clear that the fixed partition poorly separates the trimers and tetramers, as it misidentified 53 trimers and tetramers or about 18% of the total trimer/tetramer population. By

⁹In VIGRA, the *Count* descriptor is merely the number of pixels in the object, so it is equivalent to the *Area* descriptor in scikit-image.

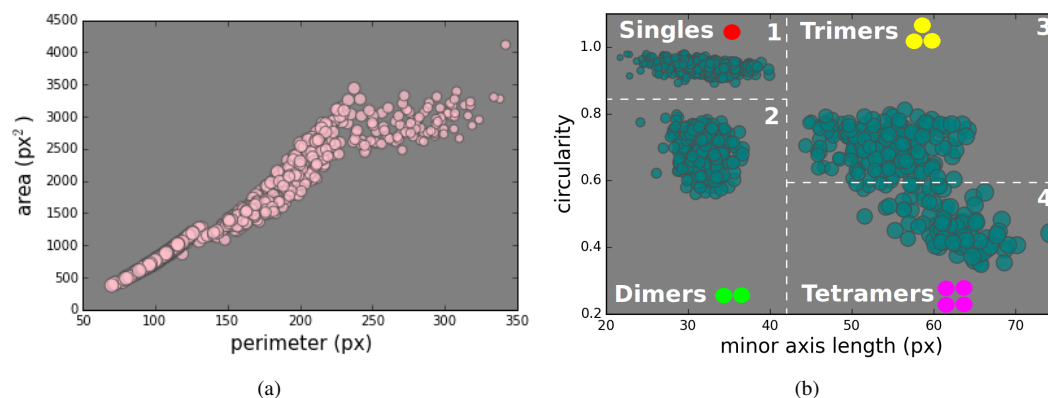


Figure 13. Scatter plots for particle features pairs. **(a)** Area and *perimeter* descriptors are too correlated to resolve particle groups. **(b)** Circularity and *semi-minor axis* lead to natural clustering in the test image. Based on these clusters, one can draw a partition and predict particle grouping; although, the trimer and tetramer distinction is rather arbitrary. The text inlays **(b)** illustrate which particle groups we intend to assign to each region of the partition (i.e. we believe the cluster in quadrant 1 is single particles, the cluster in 2 is dimers, and so on). Marker size is proportional to circularity in **(a)** and proportional to particle area in **(b)**.

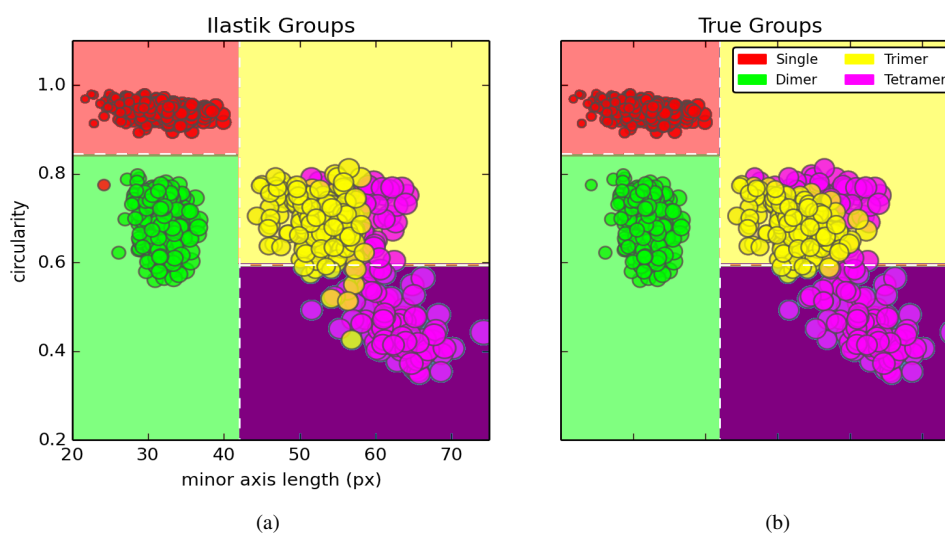


Figure 14. **(a)** Particle groups predicted by Ilastik overlaid on the user-set partitions. **(b)** Actual particle groups. It is clear that the trimers and tetramers are difficult to disentangle, but Ilastik was able to distinguish many trimers and tetramers belonging to the same cluster in the scatterplot. Background color corresponds to the groups that would have been predicted by the pyparty partition.

comparison, Ilastik only misidentified 14 tetramers and trimers, and mistook one dimer for a single. After trying other features and adding more labels, our optimal Ilastik predictor performed even better, as illustrated in Fig. (15). As with semi-supervised segmentation, image consistency is paramount when applying a pre-made classifier to a new image.

4 DISCUSSION

4.1 Choosing a Workflow

While there is no one-size-fits-all workflow, obtaining the optimal segmentation is a fairly ubiquitous task. Our results indicate that thresholding is the most simple and computationally efficient approach; however,

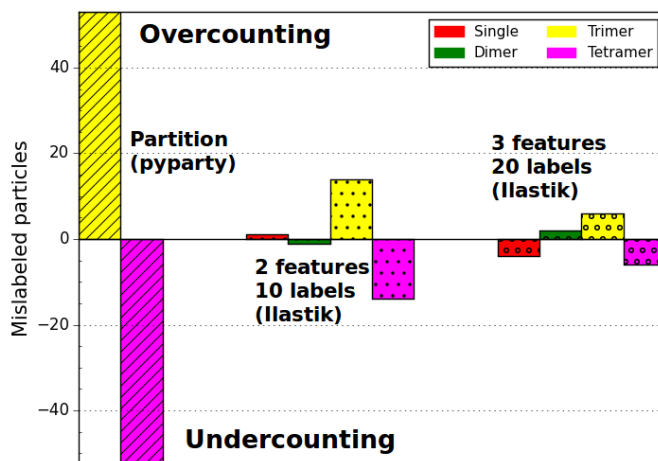


Figure 15. Incorrect predictions for particle groups in the test images. The trimers and tetramers were misidentified more often than the singles and dimers. Ilastik clearly outperforms the fixed partition approach (Fig. 13b), which mislabeled 53 of the trimers as tetramers. Predictions based on 10 labeled particles in Ilastik using *Count* and *RegionRadii* features mislabeled only 14 trimer/tetramers and 1 single/double. An optimal predictor based on 20 labeled particles and the additional feature of *Mean in neighborhood* mislabeled only six trimers.

it demands that particles are necessarily brighter than the background and the image is fairly noise-free. Whenever objects and background have intersecting brightness distributions, they can no longer be delineated through brightness features alone. In the test images, noise and smoothing resulted in this convolution (see the overlapping regions in Fig. 2 histogram); therefore, it is not surprising that seeding and semi-supervised methods performed much better on these images. In many cases, preprocessing can improve the workflow; however, care should be taken to understand any compounding effects or constraints it may impose on the subsequent segmentation step. In regard to classifying different groups of nanoparticle species, Ilastik's object classification workflow is quite powerful; we recommend it highly. In cases of poor image consistently, it may still be advantageous to classify particles based on a hard-set partition (e.g. radius ≥ 50 px & circularity < 0.8), and straightforward API for such tasks.

Because of the subjective nature of image processing (Woods, 2002), discovering an optimal, robust workflow usually requires trial and error. It is important to choose tools commensurate with research goals and programming experience. Graphical interfaces like those found in Fiji and Ilastik offer a user-friendly avenue to rapidly explore a variety of techniques. Working directly with the scikit-image API provides a nice trade-off between productivity and flexibility, and is great for building customized workflows. Ultimately, as customizability becomes more important, the tradeoff between flexibility and productivity leads away from graphical applications like Fiji and Ilastik, towards flexible API's like those found in scikit-image. In high-performance applications, OpenCV (Bradski, 2000) or GPU-accelerated libraries (NVIDIA, 2014) may offer the best framework. In any case, optimizing the image processing workflow is time consuming, so obtaining a good image is better than relying on processing to compensate.

4.2 Imaging Beyond SEM

In addition to SEM, one may also consider using TEM or STEM (scanning transmission electron microscopy) to enhance contrast and reduce charging; however, transmission microscopy requires transparent samples, or in the case of STEM, distributing the nanoparticles onto a carbon support film (Pennycook et al., 2007). Scanning probe techniques like atomic force microscopy (AFM) offer a viable alternative to electron microscopy. Nanopositioning stages facilitate wide-field AFM imaging, while maintaining resolutions comparable to, or better than, those of typical SEM images at the same magnification (Andrade et al., 2013). AFM yields new operational constraints, such as considerations in regard to tip size and

geometry, long-scan thermal drift correction¹⁰ and even particles sticking to the probe itself. Contrast disparity, hazy edges, drift, noise and other artifacts of SEM also manifest in scanning probe images. This is illustrated in Fig. (16), which shows quantum dots measured with AFM side-by-side with a SEM image of gold nanoparticles; from an image processing standpoint, they have similar particle features and could be analyzed with the same techniques.

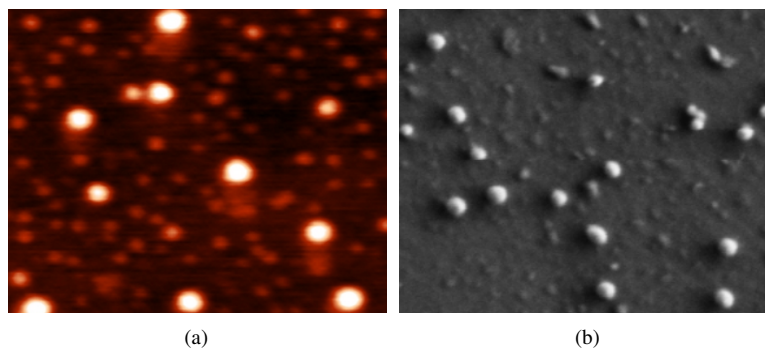


Figure 16. (a) Various sized quantum dots measured with AFM (reproduced with permission from Ref. (Yu. Kudriavstev, R. Asomoza, O. Koudriavtseva, Ya. Parkhomenko, 2013)). (b) Gold nanoparticles on polymerized silane layer. Although depicting very different systems, these images would be analyzed in a nearly identical fashion.

5 CONCLUSIONS

Progress in nanotechnology, high-resolution microscopy and open-source image processing has enabled nanosystem characterization at scales ranging from the individual particle to the entire composite; however, to do so effectively requires a breadth of interrelated domain knowledge. To streamline nanostructure characterization, we identified the most relevant preprocessing, segmentation and object classification techniques for nanoparticle images. Artificial test images were utilized to assess a variety of segmentation techniques, ranging from thresholding to semi-supervised learning. The NOISY SEM image proved the most difficult to segment; only the random walk method and Ilastik's semi-supervised pixel classification were able to achieve a low segmentation error ($\approx 2.5\%$), and Ilastik required fewer seed markers and provides a wand tool for easier labeling. In general, particle sizes were overestimated due to enlarged boundaries in the smoothed test image. This "halo effect" is commonly encountered in SEM, predominantly when the beam is unfocused or of low energy.

Ilastik succeeded in classifying nanoparticles into singles, dimers and flat and piled aggregates in real SEM images. On the artificial image, a manually-set classifier misidentified trimer and tetramer aggregates about 20% of the time, even with the optimal feature pair and partition hand-selected. Meanwhile, Ilastik's predictions were correct to within a 2.5-5% error range; 2.5% error was achievable after labeling only 10 particles and specifying *Count*, *RegionRadii* and *Brightness* as the identifying features. Both methods successfully distinguished singles from dimers.

With the addition of machine-learning applications to the already rich open-source image processing ecosystem, researchers are well-equipped to characterize their nanosystems over a range of length scales. This work is a branching-off point for materials scientists looking to incorporate automated, wide-field image analysis into their research. To aid in this process, ten supplemental IPython Notebooks tutorials (Table 1), videos, a variety of SEM AuNP images and our artificial images are freely available as supplemental data. We encourage researchers to reuse our artificial image set to benchmark new techniques and workflows.

¹⁰Consult Ref. (Acunto and Salvetti, 2010) for a nice explanation of the source of thermal drift in SPM and Ref. (Snella, 2010) for drift correction techniques in SEM.

6 SUPPLEMENTAL

Supplemental Notebooks (Table 1), figures and videos are hosted at: https://github.com/hugadams/imgproc_supplemental. The Notebooks are presented in tutorial format to provide a launching point into particle analysis.

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