

## Towards a Quantitative Model of Epidemics during Conflicts

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### Abstract

Epidemics may both contribute to and arise as a result of conflict. The effects of conflict on infectious diseases are complex and there have been confounding observations of both increase and decrease in disease outbreaks during and after conflicts. However there is no unified mathematical model that explains all these counter-intuitive observations. There is an urgent need for a quantitative framework for modelling conflicts and epidemics.

We introduce a set of mathematical models to understand the role of conflicts in epidemics. Our mathematical framework has the potential to explain the counter-intuitive observations and the complex role of human conflicts in epidemics. Our work suggests that aid and peacekeeping organizations should take an integrated approach that combines public health measures, socio-economic development, and peacekeeping in the conflict zone.

Our approach exemplifies the role of non-linear thinking in complex systems like human societies. We view our work as a step towards a quantitative model of disease spread in conflicts.

### Introduction

Epidemics and conflicts are closely connected. Epidemics may both contribute to conflict and also arise as a result of violence in human societies. The effects of conflict on infectious diseases is multi-faceted and complex. There have been counter-intuitive observations of both increase and decrease in disease outbreaks during and after conflicts (McInnes, 2009). For example, epidemics have been observed to be both initiated and diminished by conflicts. Paradoxically, epidemics have been observed to rebound, even after conflicts have ended. However there is no unified quantitative model that explains all these counter-intuitive observations.

There is an urgent need for a quantitative framework for modelling conflicts and epidemics. The recent appearance of emerging pathogens like Zika and Ebola virus in conflict-prone regions highlights the need for a quantitative framework that combines the effects of both disease spread and conflicts.

Such models can be a first step towards shaping public health policy, spreading public awareness and may also be a tool for public health professionals in conflict zones. Quantitative techniques like these may also help predict possible emerging hotspots for emerging diseases (Banerjee, Guedj, Ribeiro, Moses, & Perelson, 2016; Banerjee,

Perelson, & Moses, 2017). Models of joint epidemic and conflict risk would be of considerable interest to future humanitarian and peacekeeping missions.

## Materials and Methods

### Models

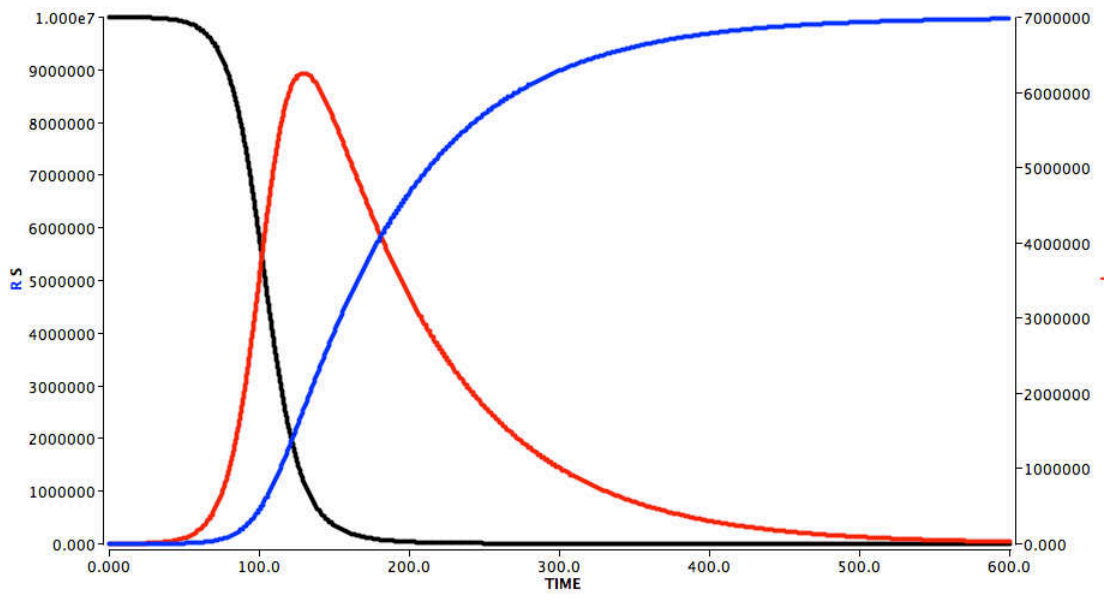
We start with a basic susceptible-infected-recovered (SIR) model. The density of susceptible people who are healthy but can be infected by a pathogen is denoted by  $S$ . The density of people who are infected is represented by the compartment  $I$ . The interaction between infected and susceptible causes more infections which is represented by the mass action term  $-\beta IS$  (the rate at which susceptibles become infected). This shows up as influx term in the infected compartment ( $+\beta IS$ ). The density of people who recover from infections is represented by  $R$ . This is composed of an influx from the infected population at a rate of  $\nu I$ . The model is shown below.

$$\frac{dS}{dt} = -\beta IS$$

$$\frac{dI}{dt} = \beta IS - \nu I$$

$$\frac{dR}{dt} = \nu I$$

We assume in this simple model that those who recover never become infected again. Additionally, we neglect birth and death processes in this simple model. All these assumptions can be relaxed in more involved models. A simulation of this simple model is shown below.



**Figure 1.** A simulation of the basic SIR model showing how the density of infected people ( $I$ , in red) rises and then decreases. The density of susceptible people ( $S$ , in black) declines causing the infection to start declining. The density of people who recover ( $R$ , in blue) increases throughout the process.

The basic reproductive number ( $R_0$ ) is the expected number of new infections produced by a single infected individual over the individual's productively infected lifespan (in a completely susceptible population). It is given by the following quantity

$$R_0 = \frac{\beta S}{\nu}$$

This can be derived by observing that the infection can be sustained if the rate of change of infected individuals ( $I$ ) is greater than 0

$$\frac{dI}{dt} = \beta IS - \nu I > 0$$

$$\beta IS > \nu I$$

This finally gives us the following relationship

$$\frac{\beta S}{\nu} > 1$$

## Methods

The dynamical models were implemented in Berkeley Madonna (Macey & Oster., 2001) and have been made available online (Banerjee, 2019).

## Results

### 1. Coupled models of disease and conflict

We introduce the following model of two populations in conflict with each other.  $S_1$  and  $S_2$  refers to susceptible populations of the two nations or communities within a nation (combines both civilians and combatants). The first term in each of these compartments simulates removal due to infection. The second term models influx or efflux of people: this could be due to refugees fleeing from one country to another or the invasion of an army. This is modelled as a piecewise linear function ( $X$ ).

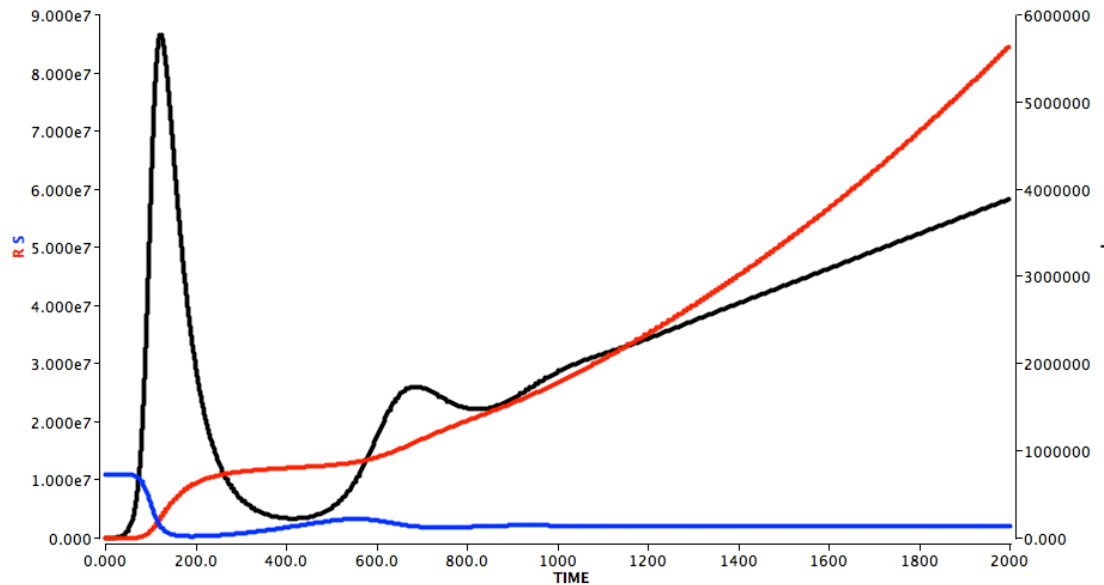
$$\frac{dS_1}{dt} = -\beta I S_1 + \alpha_1 X$$

$$\frac{dS_2}{dt} = -\beta I S_2 + \alpha_2 X$$

$$\frac{dI}{dt} = \beta I S_1 + \beta I S_2 - \nu I$$

$$\frac{dR}{dt} = \nu I$$

$$X = \begin{cases} 0, & t < t_i \\ \delta(t - t_i), & t \geq t_i \end{cases}$$



**Figure 2.** A simulation of the basic two-nation model showing how the density of infected people ( $I$ , in black) rises and then decreases and then increases again. The density of susceptible people ( $S$ , in blue) declines initially causing the infection to start declining. It then starts increasing due to influx of soldiers and refugees causing the rebound in infections. The density of people who recover ( $R$ , in red) increases throughout the process.

We note that some of these parameters might be correlated, e.g. increased migration might breakdown already strained medical services (parameter  $\nu$  in the SIR model). We look at this in a later model.

We only show representative plots to demonstrate this case. We note that this model is not specific to any disease nor do we estimate model parameters specific to any pathogen. Our objective is only to demonstrate that such a situation is indeed feasible. It would be possible to fit these mathematical models to data, should adequate data become available.

## 2. An epidemic can be decreased during times of conflict

It is a common assumption that conflicts can worsen an epidemic but cannot initiate a new epidemic (with the exception of biological warfare agents) (Altman, 2010). Epidemics could be reduced for some time during conflicts. This could happen due to:

- a) mobility of people being reduced. For example, lower incidence of HIV has been reported in Angola and is attributed to reduced mobility due to conflicts (McInnes, 2009).
- b) increase in susceptible population during conflict due to mortality from the conflict, and
- c) increase in migration.

We show this effect can be simulated by an increase in the value of  $S(t)$  after some time. The increase ( $X$ ) is modelled as a piecewise linear function: it is 0 before some time and increases linearly after some time. The model is shown below.

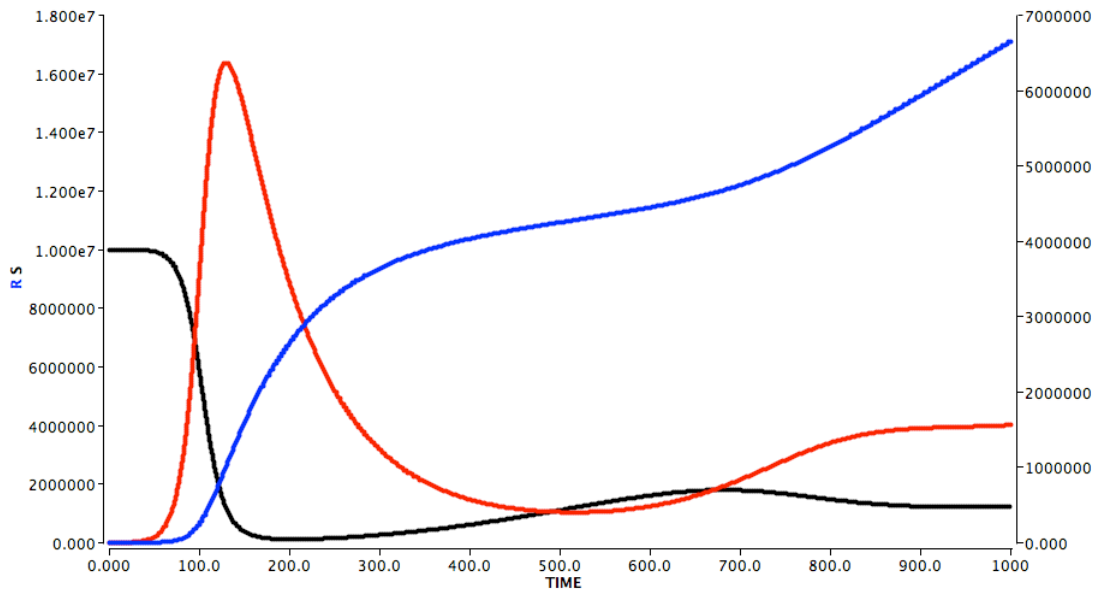
$$\frac{dS}{dt} = -\beta IS + \alpha X$$

$$\frac{dI}{dt} = \beta IS - \nu I$$

$$\frac{dR}{dt} = \nu I$$

$$X = \begin{cases} 0, & t < t_i \\ \delta(t - t_i), & t \geq t_i \end{cases}$$

A simulation of this outcome is shown in Figure 3 and it can be seen that the density of infections declines (after 100 time units) and then comes back up again.



**Figure 3.** A simulation of the migration model showing how the density of infected people ( $I$ , in red) rises and then decreases. The density of susceptible people ( $S$ , in blue) declines initially causing the infection to start declining. It then starts increasing due to migration causing the rebound in infections. The density of people who recover ( $R$ , in red) increases throughout the process.

### 3. Epidemics could reappear or be diminished after the end of conflicts

Epidemics could reappear after the end of conflicts due to migration of aid workers or return of refugees displaced during the conflict. This highlights the need for sustained humanitarian and aid missions even after conflicts have ceased.

This effect can be simulated by an increase in  $S(t)$ . The model has been introduced in the previous section. Figure 3 shows that the infection can decline over certain periods of time; in the simulation it declines between 100 and 500 time units, before rebounding again.

After a conflict ends, there could also be migration of refugees and peacekeepers, all of whom could either add to the susceptible or infected pool. This could cause a resurgence of the epidemic. We show another plausible model for this below. This model has an influx (after a certain time) in the susceptible ( $S$ ) and infected ( $I$ ) compartments. The increase is modelled as a piecewise linear function.

$$\frac{dS}{dt} = -\beta IS + \alpha_1 X_1$$

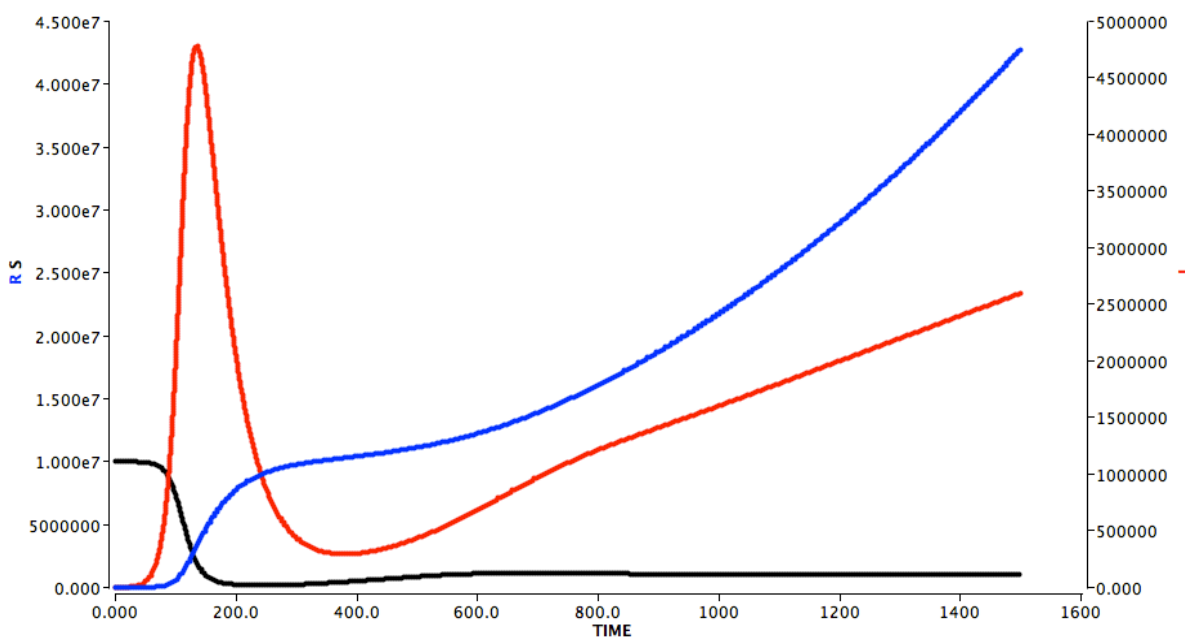
$$\frac{dI}{dt} = \beta IS - \nu I + \alpha_2 X_2$$

$$\frac{dR}{dt} = \nu I$$

$$X_1 = \begin{cases} 0, & t < t_i \\ \delta_1(t - t_i), & t \geq t_i \end{cases}$$

$$X_2 = \begin{cases} 0, & t < t_i \\ \delta_2(t - t_i), & t \geq t_i \end{cases}$$

We show a simulation below. The plot shows how the density of infected people rises, then decreases and then increases again.



**Figure 4.** A simulation of a model after a conflict with migration of refugees and peacekeepers in both the infected and susceptible populations. The simulation shows how the density of infected people ( $I$ , in red) rises, then decreases and then increases again. The density of susceptible people ( $S$ , in black) declines and then increases again after a conflict due to migration of refugees and peacekeepers. The density of people who recover ( $R$ , in blue) increases throughout the duration of the simulation.

#### 4. The effects of migration on diseases

As the previous cases demonstrate, migration has a significant effect on disease spread during and after conflicts. Here we examine in more detail the different effects migration can have on spread of infectious diseases. Other additional factors that can compound recovery from epidemics caused in part by both migration and conflicts are:

- a) breakdown of medical infrastructure
- b) over-crowding, and
- c) unsanitary facilities

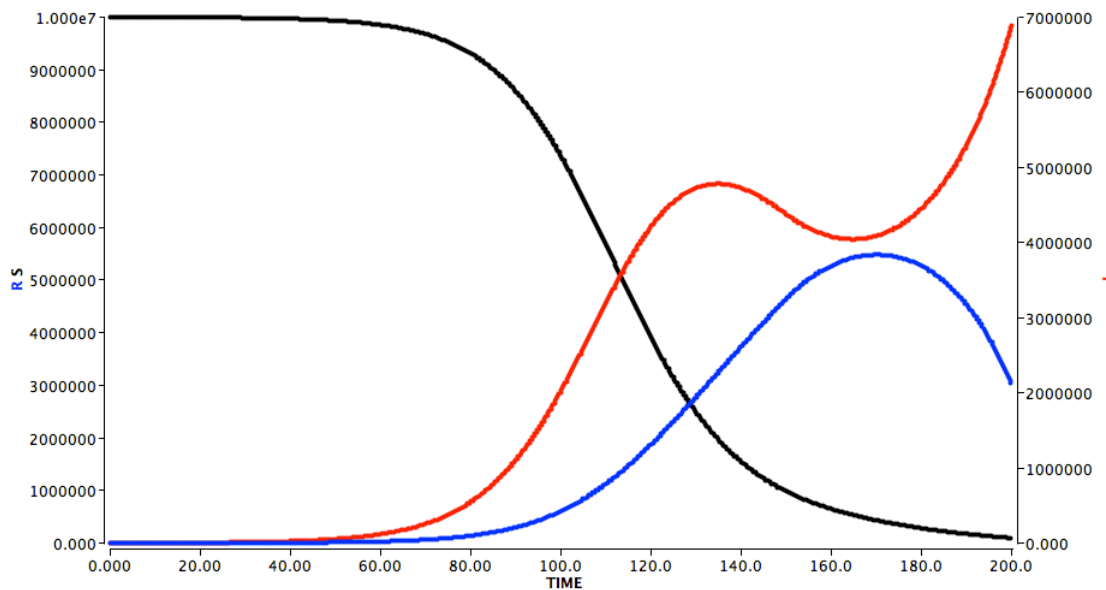
Most of these would affect the rate of recovery (parameter  $\nu$ ) in the model. We can simulate these effects by lowering the value of  $\nu$  in the model. The rate of recovery ( $\nu$ ) is at baseline before some time and then is assumed to decrease linearly with time afterwards. We can look at other functional forms but this is a very basic and simple formulation. In the future when data becomes available, we can fit more complex functions.

The model is shown below

$$\begin{aligned}\frac{dS}{dt} &= -\beta IS \\ \frac{dI}{dt} &= \beta IS - \nu I \\ \frac{dR}{dt} &= \nu I \\ \nu &= \begin{cases} \nu_0, & t < t_i \\ \nu_0 - \eta(t - t_i), & t \geq t_i \end{cases}\end{aligned}$$

A simulation of this outcome is shown in Figure 5.





**Figure 5.** A simulation of the migration model with additional factors showing how the density of infected people ( $I$ , in red) rises, then decreases and then increases again. The density of susceptible people ( $S$ , in black) declines throughout this process. The density of people who recover ( $R$ , in blue) increases and then decreases again due to the decline in the rate of recovery due to breakdown in infrastructure.

Migration has a significant effect on infectious diseases during and even after conflicts: it may make more people susceptible to diseases or isolate people from diseases in regions with poor connectivity. In future work, we will look at spatial models of migration, disease and conflicts.

## 5. Scenario with multiple factors

We acknowledge the complexity of the problem of looking at conflict, disease and socio-economics as a coupled system. Many of the factors that we outlined above may co-occur with each other. As an example, we present one such integrated model below. The model below incorporates an increase in the susceptible population ( $S(t)$ ). It also simulates a breakdown of critical infrastructure that causes a decline in the recovery rate ( $\nu$ ).

$$\frac{dS}{dt} = -\beta IS + \alpha X$$

$$\frac{dI}{dt} = \beta IS - \nu I$$

$$\frac{dR}{dt} = \nu I$$

$$\nu = \begin{cases} \nu_0, & t < t_i \\ \nu_0 - \eta(t - t_i), & t \geq t_i \end{cases}$$

$$X = \begin{cases} 0, & t < t_i \\ \delta(t - t_i), & t \geq t_i \end{cases}$$

## 6. Modelling interventions

If there is available data, future modellers can even try to estimate the increase in recovery rate ( $\nu$ ) required to reduce epidemics to a certain threshold. This assumes that the intervention can only effect  $\nu$ . Other interventions can affect the susceptible ( $S$ ) and infected ( $I$ ) populations by targeted vaccinations.

We present such a model below. We note that currently we do not have data to calibrate these models. We hope that emerging technologies like smartphones in developing nations and remote sensing by satellites can enable modellers to get some approximate estimates of model parameters like populations of infected and susceptible people (World Health Organization Report, 2019). This may enable forecasts of amount of humanitarian aid required to reduce an infection below a threshold. We model an intervention as an increase (piecewise linear) in the rate of recovery of infected individuals ( $\nu$ ).

$$\frac{dS}{dt} = -\beta IS + \alpha X$$

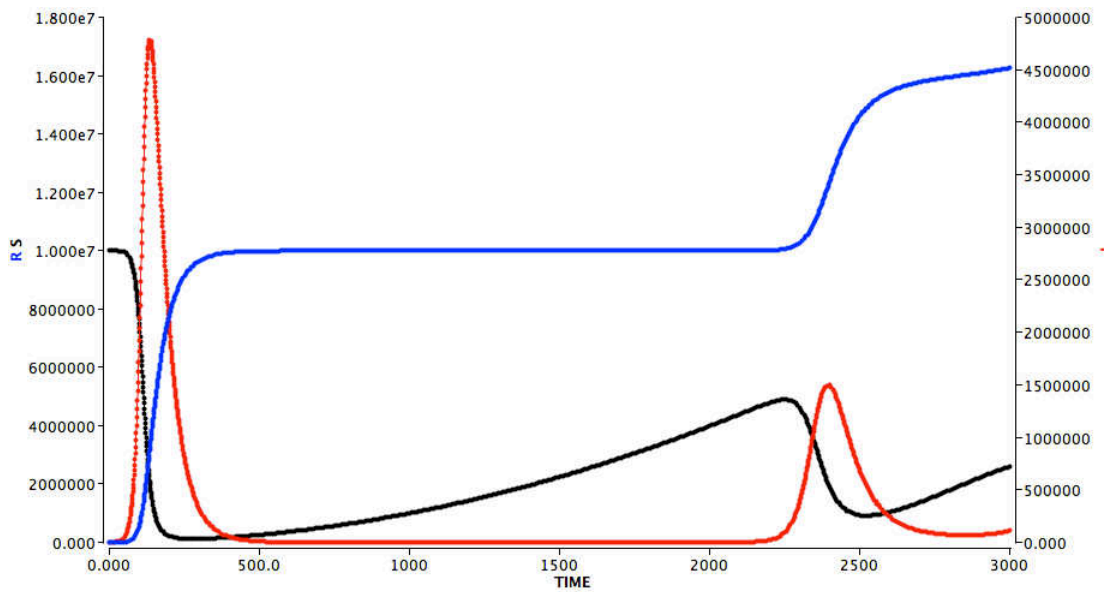
$$\frac{dI}{dt} = \beta IS - \nu I$$

$$\frac{dR}{dt} = \nu I$$

$$\nu = \begin{cases} \nu_0, & t < t_i \\ \nu_0 + \eta(t - t_i), & t \geq t_i \end{cases}$$

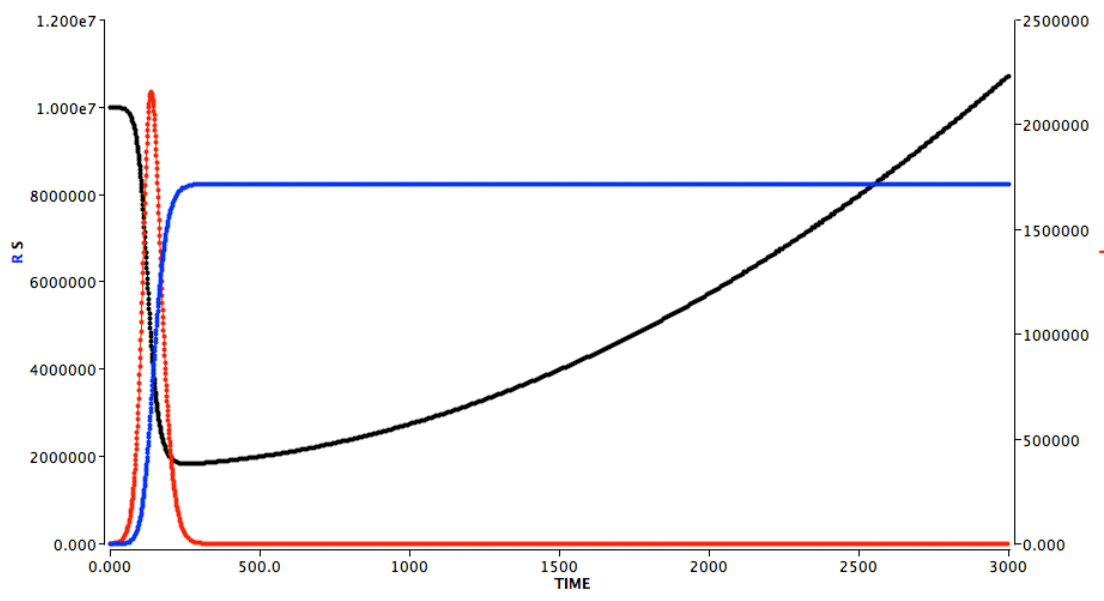
$$X = \begin{cases} 0, & t < t_i \\ \delta(t - t_i), & t \geq t_i \end{cases}$$

First, we show the simulations from a model without the intervention (Fig. 6).



**Figure 6.** A simulation of the migration model showing how the density of infected people ( $I$ , in red) rises, then decreases and then increases again (due to migration). The density of susceptible people ( $S$ , in black) declines and then increases due to migration.

We then show the effect of an intervention of increasing the rate of recovery ( $\nu$ ) by improved access to health services and vaccination (Fig. 7). The intervention, initiated after some time, has the effect of checking the rebound in infections seen in the model without interventions.



**Figure 7.** A simulation of the migration model with an intervention of increasing the rate of recovery after some time ( $\nu$ ). This has the effect of checking the increase in infected people seen in the model without intervention. The density of infected people ( $I$ , in red) rises and then decreases.

## 7. Effect of poverty on diseases

We can simulate the effect of poverty on disease propagation by coupled models of socio-economics and diseases. The gross domestic product (GDP) of a country may affect the rate at which infected patients recover (parameter  $\nu$ ). Poorer nations may have a lower value of  $\nu$  thereby compromising their chances of recovering from epidemics after a conflict. We parameterize  $\nu$  as a function of GDP.

We present a simple model of this effect below

$$\begin{aligned}\frac{dS}{dt} &= -\beta IS \\ \frac{dI}{dt} &= \beta IS - \nu I \\ \frac{dR}{dt} &= \nu I \\ \nu &= \begin{cases} f(GDP), & t < t_i \\ f(GDP) - \eta(GDP)(t - t_i), & t \geq t_i \end{cases}\end{aligned}$$

## 8. Socio-economics of disease spread

Conflicts can contribute to and also may be caused by diseases (Altman, 2010). Here we consider the socio-economics of infectious disease spread.

Diseases can breakdown resources, reduce GDP, and deplete resources. This may in some instances compel these nations to initiate conflicts for acquiring resources externally (Altman, 2010).

We look at coupled models of socio-economics and disease spread. We assume that the rate of recovery ( $\nu$ ) from infections is related to the GDP.

The model is shown below. We assume there are two countries that are competing with each other economically. Their GDPs are denoted by  $x$  and  $y$ . They each have epidemics where the rate of recovery ( $\nu$ ) is dependent on GDP.

$$\frac{dx}{dt} = \alpha x - \sigma xy$$

$$\frac{dy}{dt} = -\delta y + \gamma xy$$

$$\frac{dS_1}{dt} = -\beta I_1 S_1$$

$$\frac{dI_1}{dt} = \beta I_1 S_1 - \nu_1 I_1$$

$$\frac{dR_1}{dt} = \nu_1 I_1$$

$$\nu_1 = \begin{cases} f(y), & t < t_i \\ f(y) - \eta(t - t_i), & t \geq t_i \end{cases}$$

$$\frac{dS_2}{dt} = -\beta I_2 S_2$$

$$\frac{dI_2}{dt} = \beta I_2 S_2 - \nu_2 I_2$$

$$\frac{dR_2}{dt} = \nu_2 I_2$$

$$\nu_2 = \begin{cases} f(x), & t < t_i \\ f(x) - \eta(t - t_i), & t \geq t_i \end{cases}$$

Our models demonstrate the vicious cycle of poverty, disease and conflicts especially in some developing nations. This also suggests that aid organizations should take an integrated public health approach that is combined with efforts to aid socio-economic development.

## 9. A scenario of a complex interaction of disease spread in a predator-prey system

Our models are general enough to capture conflict-disease dynamics in other species. We consider a final scenario which may occur in other species. Consider two species, one of which preys on the other (predator-prey system). Assume that there is an infectious disease that infects only one species (say, the prey).

The model is shown below

$$\frac{dx}{dt} = \alpha x - \sigma xy$$

$$\frac{dy}{dt} = -\delta y + \gamma xy$$

$$y = S + I + R$$

$$\frac{dS}{dt} = -\beta IS$$

$$\frac{dI}{dt} = \beta IS - \nu I$$

$$\frac{dR}{dt} = \nu I$$

Here we have a predatory-prey Lotka-Volterra model coupled to an SIR model. Whenever the density of predator ( $x$ ) goes down, the prey ( $y$ ) goes up. The total population of the prey ( $y$ ) is composed of  $S + I + R$ . Some fraction of  $S$  is going to increase whenever the population of prey increases.

From the discussion in the previous sections, when we increase the susceptible population, we can get oscillations of infections going up and down. We hypothesize that in certain cases the pathogen may evolve to reproduce around the peaks of the prey population.

## Discussion

The effects of conflict on infectious diseases are multi-faceted and complex: there have been observations of both increase and decrease in disease outbreaks during conflicts. For example, epidemics have been observed to be both initiated and extinguished by conflicts (McInnes, 2009). However there is no unified mathematical model that explains all these counter-intuitive observations.

The recent appearance of emerging pathogens like Zika and Ebola virus in conflict-prone regions highlights the need for a quantitative framework that integrates both diseases and conflicts.

Such models can be a first step towards policy, spreading public awareness and may also be a tool for public health professionals in conflict zones. Quantitative techniques like these may also help us predict possible emerging hotspots for emerging diseases (Banerjee et al., 2016, 2017).

In this work, we introduce a set of mathematical models to understand the role of conflicts in epidemics. Our mathematical framework has the potential to explain counter-intuitive observations and the complex role of human conflicts in epidemics.

### **The role of non-linear models in understanding complex systems**

We suggest that non-linear mathematical models can help us understand why conflicts may both increase and decrease epidemics. We outline a few situations which explain the previously counter-intuitive observations. We develop coupled non-linear models of conflict, socio-economics and disease spread.

We show representative plots to demonstrate the role of dynamical systems in this field. We note that the models are not specific to any disease nor do we estimate model parameters specific to any pathogen. Our objective is only to demonstrate that such a situation is indeed feasible. It would be possible to fit similar mathematical models to data, once such data becomes available.

Our work raises further concern for use of biological agents during warfare which could be more devastating than currently thought to be the case.

We note that the type of disease also matters, e.g. a vector-borne disease will have different characteristics compared to sexually transmitted diseases. Hence diseases may have different effects on conflicts based on their type.

Conflicts also cause a higher incidence of stress and trauma related diseases like diabetes and strokes (Maxmen, 2017).

Conflicts can also help introduce new pathogens. Invading armies can introduce new diseases to a population that has no immunity (the English and the American armies introduced smallpox to Native Americans) or the invading army itself may be exposed to a novel pathogen (Napoleon's army suffered from typhus during the Russian invasion) (Roy and Ray, 2018).

## Policy Implications

At the end of conflicts, epidemics could go away or reappear due to migration of aid workers, displaced populace, etc. Timely humanitarian intervention is key to reducing the spread of diseases.

The policy implications are that public health officials will need to work closely with peacekeeping missions and humanitarian aid workers to manage crises both during and after conflicts.

Migration has a significant effect on infectious diseases during and after conflicts. This suggests that steps taken to manage refugee crises during and after conflicts are critical in preventing outbreaks of infectious diseases.

Our models demonstrate the vicious cycle of poverty, disease and conflicts especially in some developing nations. Diseases can cause more poverty due to the increased public health burden. Ultimately this may also lead to conditions that encourage conflicts for resources.

This suggests that aid and peacekeeping organizations should take an integrated approach that combines:

- 1) public health measures
- 2) efforts to aid socio-economic development
- 3) peacekeeping in the region

We also suggest that managing public health crises and ameliorating poverty can have significant knock-on effects including, we hope optimistically, reduction of conflicts. It is intriguing to speculate that perhaps an integrated approach where public health intervention is coupled with nation-building efforts, for example to build technological infrastructure and international scientific collaboration networks, may help these countries recover in the long term (Banerjee, 2015).

## Conclusion

We view our work as a step towards a quantitative model of disease spread in conflicts. Our model explains apparently inconsistent observations on disease spread during conflicts. A multitude of possibilities are explained in a quantitative framework.

Our work also highlights the importance of simple mathematical models and the perils of applying linear thinking to non-linear complex systems. Non-linear models produce counter-intuitive results; disease spread is a non-linear phenomenon which produces counter-intuitive results. Such mathematical models have been used in the past to model diverse complex systems ranging from socio-economic to biological systems (Banerjee et



al., 2016, 2017). We note that similar mathematical models have been also used to explain crime and violence in human societies (Banerjee, 2017).

Our work raises the hope for a predictive model that may be of use to first responders and public health officials in conflict hotspots. Mathematical models of joint epidemic and conflict risk would be of considerable interest to future humanitarian and peacekeeping missions.

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