

1 The stream power variation in a GIS 2 environment as an index to evaluate the 3 most 'sensitive' points of a river

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9 ABSTRACT

10 The note deals with the problem of measurement and variability, along the fluvial reaches of a hydrographic
11 network, of the stream power, understood according to the definition originally provided by Bagnold
12 (1966) "The available power supply, or time rate of energy supply, to unit length of a stream is clearly the
13 time rate of liberation in kinetic form of the liquid's potential energy as it descends the gravity slope S ". In
14 formula: $\Omega = \rho \cdot g \cdot Q \cdot S$

15 where: Ω = stream power per unit of flow length (W/m) $\rho \cdot g$ = density x gravity acceleration = specific
16 weight of the fluid (kg/m^3) Q = liquid discharge (m^3/s) S = slope of the considered reach (m/m)

17 Recent digital elevation models allow the calculation of channel gradient and consequently stream
18 power with a finer spatial resolution, opening promising and novel opportunities to investigate river
19 geomorphological processes and forms. The work carried out consisted in defining and implementing a
20 methodological approach that could be automated within a geographic information system and that meets
21 two requirements: 1) use input data that is easy to find as DEM at a low resolution; 2) estimate, in
22 the best possible way and on the basis of the available data, the stream power and its variability along
23 the considered stream. In particular, the methodological approach has been implemented in the GIS
24 environment (GRASS Gis, Qgis), and it has been applied to a sample basin, highlighting its variability
25 along the streams of a higher order (in practice the main stream and its most important tributaries). The
26 sudden and more substantial variations of stream power were then related to the processes acting in
27 the fluvial system. This approach has made it possible to highlight how the erosion, solid transport and
28 sedimentation phenomena occurring along the fluvial reaches (and the geomorphological and geological-
29 applicative problems that these involve, especially in anthropized areas), are correlated precisely to abrupt
30 variations (increase/decrease) of the "power" available. Hence the idea that automated and standardized
31 screening of stream power variability along a stream can be used as a preliminary diagnostic element to
32 identify the most "sensitive" points of the same, on which to concentrate subsequent investigations (field
33 checks, to verify the causes), aimed at mitigating the risk due to the dynamics of the riverbed.

34 INTRODUCTION

35 The term *Fluvial dynamics* is generally used with reference to water flow, sediment movement, and to
36 bedforms resulting from the interaction between flow and sediment transport in alluvial channels.

37 Stream Power is a very significant quantity in sediment transport studies. Stream Power represents the
38 rate of doing work (in transporting water and sediment). It is commonly expressed either as stream power
39 per unit length (Ω) or power per unit bed area (ω). Bagnold (1966) denotes the stream power as:

$$\Omega = \rho \cdot g \cdot Q \cdot S \quad (1)$$

40 where: Ω = stream power per unit of flow length (W/m) $\rho \cdot g$ = density x gravity acceleration = specific
41 weight of the fluid (kg/m^3) Q = liquid discharge (m^3/s) S = slope of the considered reach (m/m)

42 Stream Power (SP) represents the rate of energy dissipation through friction and work, with the bed and
43 the banks, per unit length of a stream. The SP has been widely used to assess the sediment transport and,

44 in general, the channel pattern evolution in a river (Bagnold, 1977; Nanson and Croke, 1992; Ferguson,
45 2005; Comiti and Mao, 2012; Knighton, 1999). Extensive use of Geographic Information System (GIS)
46 and the geographical data available (frequently provided as open data) allow a local determination of SP
47 in any section of a river. The two parameters most affected by uncertainty in their determinations are
48 flow discharge and slope. The flow discharge is a parameter difficult to calculate as it depends of several
49 aspects as upstream area basin, basin permeability, rainfall, etc.. and by the rainfall-discharge model.
50 Modern digital elevation models (DEMs) allow the quantification of slope channel at high resolution,
51 exploration of SP variability along the full length of a river Barker et al. (2009); Bizzi and Lerner (2015),
52 and offer the opportunity to use SP as a stream assessment tool Vocal Ferencevic and Ashmore (2012).

53 This work uses a GIS approach to define the local value of SP combining the hydrological approach
54 to determine the flow discharge as exposed by Casagrande et al. (2013) and the slope derived from DEM
55 raster. As presented in the equation 1 the transport capacity of a stream is a direct function of flow
56 discharge and local slope and for such reason the correct determination of the slope is crucial for a correct
57 stream assessment.

58 The proposed approach have been applied to the river Topino in Umbria region (central Italy).

59 **Study area**

60 One of the most important river that across the Umbria region in central Italy is the Topino River,
61 a tributary of Tiber River. This river belongs to the hydrographic basin of Topino-Marroggia 1 that
62 incorporate two different basins: the basin of Marroggia-Teverone-Timia and the basin of Topino River
63 s.s. (www.bonificaumbra.it).

64 From a geological point of view (Cencetti, 1993), the River Topino basin is set almost entirely on
65 the Miocene terrigenous deposits of the "Marnoso-Arenacea" Formation (Umbrian-Marchean Series),
66 consisting of an alternation of marls and sandstones in variable proportions. In its middle valley, however,
67 the river receives the contributions of tributaries that, on the right and left hydrographic, are born from the
68 carbonate reliefs of M. Subasio (to the west) and the Foligno Mountains (to the east). The last reach of
69 the Topino forms a wide alluvial fan at its outlet in the Umbrian Valley (Foligno-Spoleto plain) which
70 represents the eastern "branch" of the Ancient Tiberine Lake, filled in the Pliocene and Pleistocene by
71 clastic sediments in lacustrine and fluvio-lacustrine facies (conglomerates, sands and clays).

72 **1 METHODS**

73 The procedure here proposed has the aim to define the value of the SP along any cross section of a river
74 using a GIS procedure as simple and accurate as possible and based on the available data especially for
75 the determination of the local slope.

76 **1.1 Peak flow discharge**

77 The estimated maximum expected peak flow in a particular cross-section of a riverbed, for a given return
78 period, is a problem difficult to solve, due to the great number of involved factors. In Italy, the Basin
79 Authority of River Tiber performed a method in order to evaluate the peak flows in the watersheds
80 within the Tiber Basin di Bacino del Fiume Tevere (1996). This study used data from 165 gauge
81 stations, distributed within the Basin, and It proposed a methodology that combines the results of regional
82 precipitation analysis of duration from 1 to 24 hours with the Curve Number method (Soil Conservation
83 Center, 1972), which allows to quantify the volume of net rainfall. This procedure has been implemented
84 in a GIS system, creating a series of GRASS GIS scripts that, by applying the proposed procedure,
85 determines the peak flow rate for each point of the hydrographic network.

86 **1.2 Slope determination**

87 The slope determination is a crucial aspect for the SP evaluation along a reach. A Digital Elevation Model
88 (DEM) represents the starting point to derive the slope map. In GIS the slope maps are obtained using
89 moving window (3x3 in many cases) following the main method available in GIS software as EVANS
90 (1972) or Zevenbergen and Thorne (1987).

In this work the DEM provided by the European **Copernicus Project** called *European Digital Elevation Model (EU-DEM), version 1.1*. This DEM has a planar resolution of 25 m with a vertical accuracy of 2.9 m as assessed in <https://land.copernicus.eu/pan-european/satellite-derived-products/eu-dem>. Especially when it is necessary to calculate the slope for fluvial stretches, the normal proposed

approaches are no longer valid Hengl and Reuter (2008). In fact, for the given *eu-dem* it appears that the *minimum evaluable slope* is of the order of:

$$\Delta S = \frac{\varepsilon}{cellsize} = \frac{2.9}{25} \approx 0.11$$

91 Where ε is the vertical accuracy.

92 Therefore the minimum evaluable slope is several orders of magnitude bigger then the slope that that
93 the river presents in floodplain that is around 0.001. For such reason in this paper the local slope is not
94 calculated by the mean of the moving window using the classical GIS approach rather calculating the
95 slope as the ration between the elevation drop and the real length of the reach. In particular for any cross
96 section is considered a reach of 20 times the mean-width of riverbed where the cross section is in the
97 middle (10 times upstream and 10 times downstream).

98 2 RESULTS AND DISCUSSION

99 This work envisaged the use of the GRASS GIS for the calculation, first of all, of the precise flow
100 values relating to 72 points identified along the Topino River, from the confluence of Caldognola Creek,
101 approximately near the town of Nocera Umbra (Nocera Scalo), up to the entrance of the river near Foligno,
102 as shown in the figure 2 . These points have been identified in the river hydrographic network of the river
103 under study and are each one of a distance equal to about 20 times the width of the riverbed. Subsequently,
104 we proceeded to determine the slope values (S) of the channel. Therefore the river have been splitted
105 into 71 reaches sections; the relative slope value has been defined for each of them. Once the necessary
106 data (mean flow and relative slope of each section) were collected, the equation1 proposed by Bagnold
107 (1966) was applied. The discharge values corresponding to 72 cross sections are showed in table 1, range
between a minimum value of $304.92 \text{ m}^3/\text{s}$ and a maximum value of $929.7 \text{ m}^3/\text{s}$.

n.punto	Q (m3/s)	n.punto	Q (m3/s)	n.punto	Q (m3/s)	n.punto	Q (m3/s)
0	304,92	21	517,61	43	644,26	64	925,27
1	476,89	22	518,38	44	643,52	65	928,36
2	476,89	23	518,64	45	642,84	66	928,41
3	476,78	24	517,72	46	643,04	67	934,83
4	478,06	26	556,81	47	641,97	68	927,2
5	480,11	27	557,66	48	642,13	69	926,58
6	470,73	28	556,96	49	643,02	70	925,99
7	468,96	29	557,66	50	643,64	71	924,51
8	468,78	30	558,06	51	643,33	72	929,7
9	468,61	31	557,51	52	652,83		
10	474,95	32	557,79	53	653,73		
11	474,66	33	557,7	54	654,08		
12	474,07	34	557,13	55	653,42		
13	473,32	35	561,66	56	652,88		
14	472,85	36	560,95	57	652,29		
15	472,26	37	561,21	58	652,94		
16	471,98	38	560,24	59	652,12		
17	471,1	39	641,56	60	652,9		
18	470,77	40	637,86	61	652,73		
19	485,97	41	644,96	62	651,81		
20	511,94	42	643,86	63	650,98		

Table 1. Values for the peak flow corresponding to the 72 cross sections along the Topino River.

108 As showed in figure 3, by plotting the identification number of the reach with the respective SP value,
109 some evident peaks are observed:
110

- 111 • The first peak have a SP value of $300477.8 \text{ W}/\text{m}^2$, corresponding to the reach number 5. This
112 section is also the one characterized by greater slope (6.4%).
- 113 • The second peak presents a stream power value of $223900.6 \text{ W}/\text{m}^2$, corresponding to the reach
114 number 26.

- 115 • The third peak has a stream power value of $263767 W/m^2$, corresponding to the reach number 37.
- 116 • The fourth peak presents a stream power value of $296577.4 W/m^2$, corresponding to the reach
117 number 43.
- 118 • The fifth peak presents a stream power value of $282906.4 W/m^2$, corresponding to the reach number
119 46.
- 120 • The sixth peak presents a stream power value of $288100.4 W/m^2$, corresponding to the number 52
- 121 • The seventh peak presents a stream power value of $218971.2 W/m^2$, corresponding to reach number
122 67.
- 123 • In reaches ranging from number 6 to number 25 and from 29 to 35, the calculated SP values do not
124 differ much. The image (figure 4) shows the trend of the SP values calculated in each reach.

125 3 DISCUSSION

126 Analyzing the trend of the SP shown in the figure 4, it appears that there are 7 peaks along the studied
127 river.

128 As an example, the reach 5 was taken analyzed near the village Vittiano (Pg), characterized by the
129 maximum value of the SP ($300477.8 W/m$). Even the slope results to have the maximum value compared
130 to all the other reaches (6.4%). This denotes the strong influence that the slope parameter causes on the
131 SP value. The following figure 5 shows the reach studied where appears the strong correlation between
132 the SP and the local channel meandering morphology . The external banks of the riverbed, characterized
133 by a bigger water velocity, shows erosional phenomena; for such reason it is placed a bank defense works.
134

135 Other reaches to analyze are 13 and 21. Both are characterized by very low SP values ($32496.8 W/m$
136 for 13 and $15131.2 W/m$ for 21). The SP values are noticeably lower than the average of the other reaches
137 although they have a discharge values comparable to the previous reaches: this is due to the significantly
138 lower slope values (equal to 0.007 (0.7%) for section 13 and 0,003 for section 21). As shown in Figure
139 XX, the presence of rotational/translational slope close to the riverbed, could justify the strong reduction
140 of the channel slope and consequently of the SP value.

141 4 CONCLUSIONS

142 The paper uses the equation related to the stream power, proposed by Bagnold (1966), was examined,
143 analyzing the variation of its values along a given water course and how they can be related to the geomor-
144 phological structure of the riverbed and river processes. The stream power represents the dissipation of
145 the potential energy per unit of channel length and it is obtained by the product of the flow rate (m^3/s), the
146 slope of the channel (m/m), the density (kg/m^3) and the gravitational acceleration (m/s^2). It is therefore
147 expressed in W/m and can be considered as a measure of the main driving forces acting within a channel,
148 influencing the ability of a waterway to transport sediments.

149 River Topino was chosen as a case study, considering the portion that extends from the confluence
150 with Caldognola Creek, close to the town of Nocera Umbra (Nocera Scalo), until its entrance into the
151 town of Foligno.

152 The variations of SP appeared to be strongly correlated to the shape of the channel and to the processes
153 of erosion/deposition, and how its value can be a cause or consequence of instability phenomena. In some
154 reaches, a strong correlation between the SP values and the channel morphology was observed, especially
155 in correspondence with landslides located close to the riverbed or that involves directly the riverbed
156 (landslide dam). In reaches where the SP value is very high, are present erosion/instability phenomena;
157 the latter, in turn, are often placed upstream or close to reaches characterized by lower SP values (low
158 slopes).

159 The work shows how the determination of the SP values can provide useful indications on river
160 dynamics processes. It is clear that a large-scale analysis within a river basin could indicate, in a
161 preventive and forecasting way, the areas most "sensitive" to changes, as they are potentially subject to
162 instability phenomena caused by the fluvial dynamics.

163 **REFERENCES**

- 164 Bagnold, R. (1977). Bed load transport by natural rivers. *Water resources research*, 13(2):303–312.
- 165 Bagnold, R. A. (1966). *An approach to the sediment transport problem from general physics*. US
166 government printing office.
- 167 Barker, D. M., Lawler, D. M., Knight, D. W., Morris, D. G., Davies, H. N., and Stewart, E. J. (2009).
168 Longitudinal distributions of river flood power: the combined automated flood, elevation and stream
169 power (cafes) methodology. *Earth Surface Processes and Landforms*, 34(2):280–290.
- 170 Bizzi, S. and Lerner, D. (2015). The use of stream power as an indicator of channel sensitivity to erosion
171 and deposition processes. *River Research and Applications*, 31(1):16–27.
- 172 Casagrande, L., Cencetti, C., De Rosa, P., Fredduzzi, A., and Minelli, A. (2013). Procedura web automatica
173 per il calcolo delle portate massime attese nel bacino del f. tevere. *GEOMATICS WORKBOOKS*.
- 174 Cencetti, C. (1993). Morfotettonica ed evoluzione plio/pleistocenica del paesaggio nell'area appenninica
175 compresa tra i monti di foligno e la val nerina (umbria centro-orientale). *Bollettino- Societa Geologica
176 Italiana*, 112(1):235–250.
- 177 Comiti, F. and Mao, L. (2012). Recent advances in the dynamics of steep channels. *Gravel-Bed Rivers:
178 Processes, Tools, Environments*, pages 351–377.
- 179 di Bacino del Fiume Tevere, A. (1996). Quaderno idrologico del fiume tevere. *Suppl. Il Tevere*, 1(2):64.
- 180 EVANS, I. S. (1972). General geomorphometry, derivatives of altitude, and descriptive statistics. *Spatial
181 analysis in geomorphology*, pages 19–70.
- 182 Ferguson, R. (2005). Estimating critical stream power for bedload transport calculations in gravel-bed
183 rivers. *Geomorphology*, 70(1-2):33–41.
- 184 Hengl, T. and Reuter, H., editors (2008). *Geomorphometry: Concepts, Software, Applications*, volume 33.
185 Elsevier, Amsterdam.
- 186 Knighton, A. (1999). Downstream variation in stream power. *Geomorphology*, 29(3):293 – 306.
- 187 Nanson, G. and Croke, J. (1992). A genetic classification of floodplains. *Geomorphology*, 4(6):459–486.
- 188 Vocal Ferencevic, M. and Ashmore, P. (2012). Creating and evaluating digital elevation model-based
189 stream-power map as a stream assessment tool. *River Research and Applications*, 28(9):1394–1416.
- 190 Zevenbergen, L. W. and Thorne, C. R. (1987). Quantitative analysis of land surface topography. *Earth
191 Surface Processes and Landforms*, 12(1):47–56.

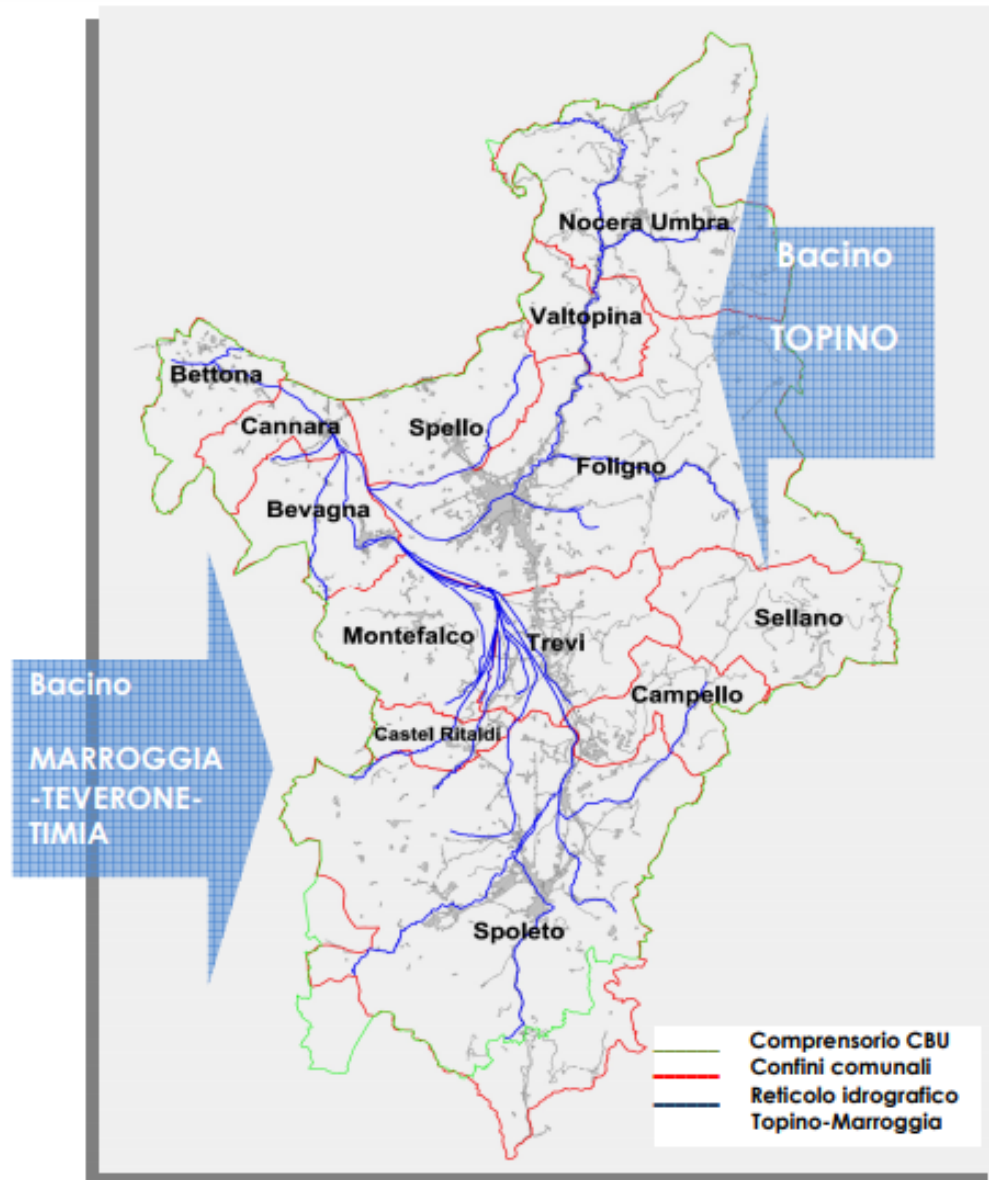


Figure 1. Hydrographic basin of Topino-Marroggia river, divided in Marroggia-Teverone-Timia Basin and Topino basin (source www.bonificaumbra.it).

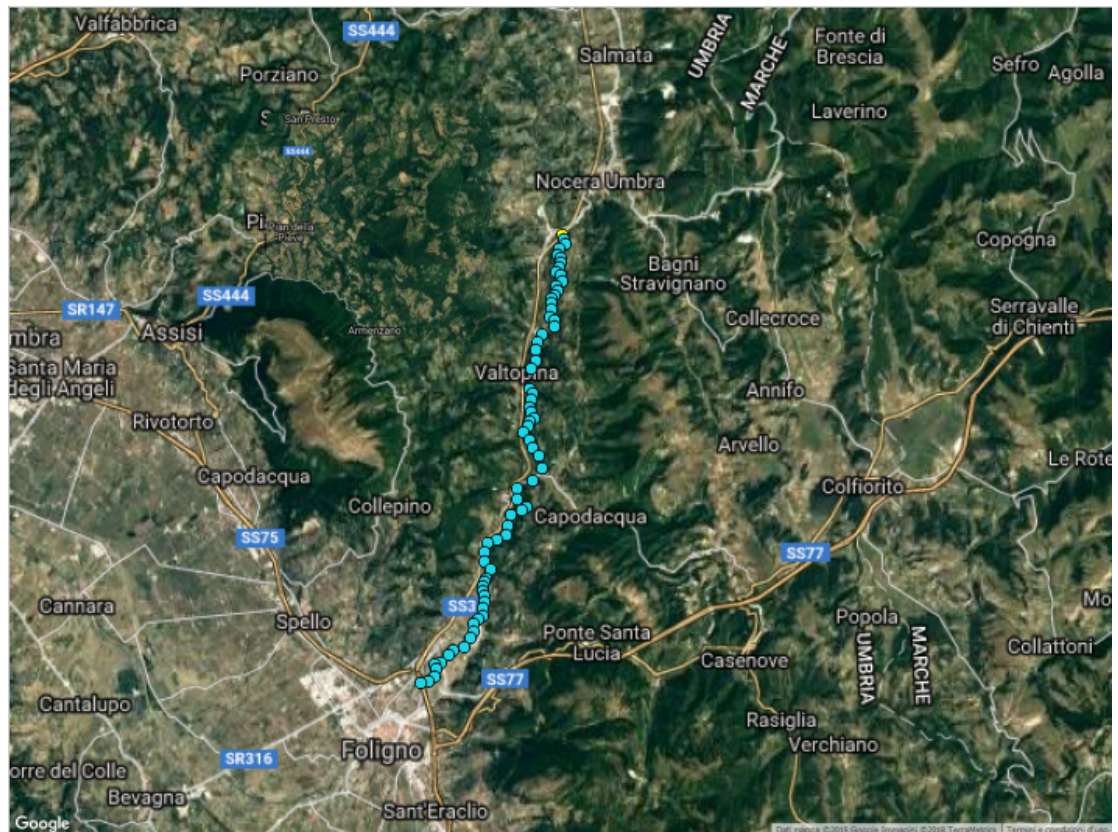


Figure 2. Identification of points along the studied reach of Topino River (from Google Hybrid)

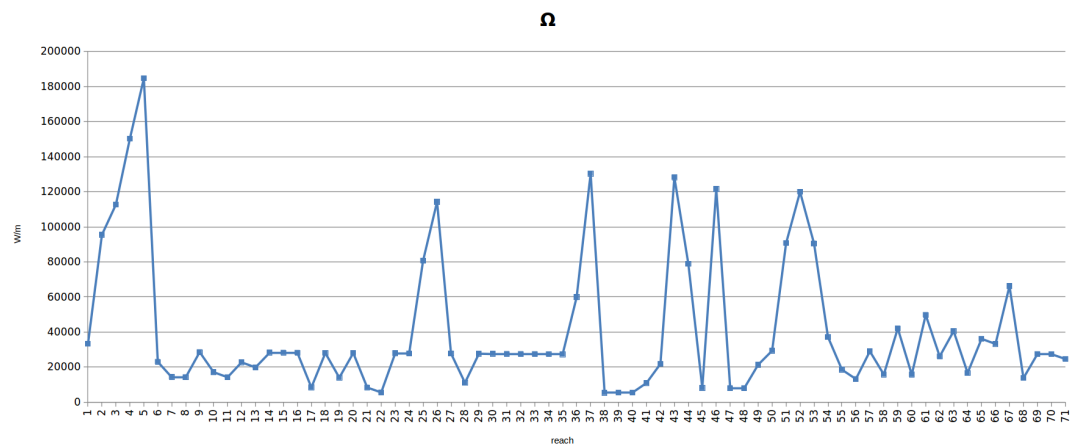


Figure 3. linear representation for the Stream Power values along the reach of the Topino river.

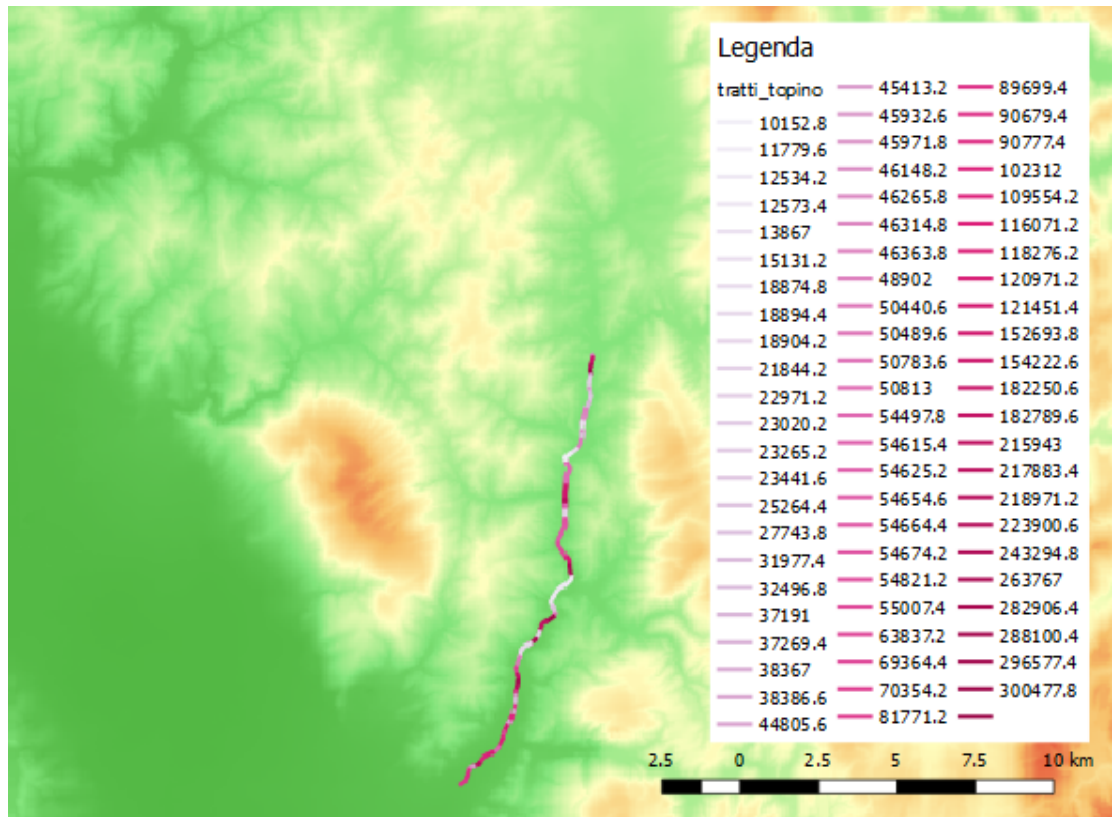


Figure 4. Distribution of the SP values along the reaches of the F. Topino studied. The clearest features are those characterized by a lower SP value, while those characterized by a more intense purple color are those where the SP is higher.



Figure 5. Aerial photo of the reach 5 - Topino River