

1 What should mobile app developers do 2 about machine learning and energy?

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9 ABSTRACT

10 Machine learning is a popular method of learning functions from data to represent and to classify sensor
11 inputs, multimedia, emails, and calendar events. Smartphone applications have been integrating more
12 and more intelligence in the form of machine learning. Machine learning functionality now appears
13 on most smartphones as voice recognition, spell checking, word disambiguation, face recognition,
14 translation, spatial reasoning, and even natural language summarization. Excited app developers who
15 want to use machine learning on mobile devices face one serious constraint that they did not face on
16 desktop computers or cloud virtual machines: the end-user's mobile device has limited battery life, thus
17 computationally intensive tasks can harm end-user's phone availability by draining batteries of their
18 stored energy. How can developers use machine learning and respect the limited battery life of mobile
19 devices? Currently there are few guidelines for developers who want to employ machine learning on
20 mobile devices yet are concerned about software energy consumption of their applications. In this paper
21 we combine empirical measurements of many different machine learning algorithms with complexity
22 theory to provide concrete and theoretically grounded recommendations to developers who want to
23 employ machine learning on smartphones.

24 1 INTRODUCTION

25 Imagine we are in a hot new start-up and your app, which will be deployed to millions of phones, needs
26 to take advantage of machine learning. Which machine learning algorithms should we employ to avoid
27 sapping the energy of your customers' phones? Should we use neural networks since they are so popular,
28 or should we stick to simpler models to save energy? In this work we address the questions of "how
29 energy efficient are these machine learning algorithms?" and "which algorithms should we use on a
30 mobile device?"

31 Machine learning is growing in popularity. Google in particular has made the results of machine
32 learning available to the general public in terms of speech recognition (1), translation (2), computer vision,
33 and search. Many machine learning implementations have been deployed to servers in the cloud, or data
34 centers. But the popularity of mobile devices such as smartphones and tablets are causing a push toward
35 mobile-apps that employ machine learning. One of the issues that mobile platforms face that servers
36 and desktop computers do not, is that mobile platforms tend to rely on batteries for power and when the
37 batteries are out of energy the mobile device is no longer available for use. This is different from data-
38 centres that have machines on racks that face power limits and need constant cooling. Machine learning
39 on mobile platforms is often out-sourced to the cloud, but the bandwidth to the cloud is quite limited so a
40 lot of machine learning is pushed back to the mobile device itself. Some apps engage in computer vision,
41 others learn from the textual and event based data on the phone to schedule appointments (3), and others
42 link and organize documents (4).

43 If machine learning is pushed to mobile devices what should practitioners do about the software
44 energy consumption of machine learning on their mobile devices? Surveys of developers and users have
45 found that poor software energy consumption performance can lead to negative app-store reviews and
46 poor user satisfaction (5; 6; 7). In this work we will empirically test, measure, and detail the costs and

47 trade-offs between machine learning performance and software energy consumption. We will show that
48 there is no best algorithm but there are a wide range of trade-offs that one can make depending on the
49 context that one is operating within. Furthermore not all energy consumption is CPU bound as some
50 algorithms cost more in terms of memory-use than others that in a memory constrained environment can
51 induce more energy consumption.

52 The contributions of this paper are:

- 53 • an empirical evaluation of the tradeoffs that machine learning algorithms make between accuracy
54 and software energy consumption;
- 55 • concrete recommendations for choosing machine learning algorithms for use on mobile platforms;
- 56 • empirical testing and measurement of multiple machine learning contexts that demonstrate “one
57 size does not fit all”.

58 2 PRIOR WORK

59 Prior work relevant to this paper include machine learning, mobile devices, and software energy consump-
60 tion research.

61 2.1 Software Energy Measurement

62 Software energy consumption is an up and coming field in software engineering and computer engineering.
63 With the popularity of mobile devices and apps, more and more software engineering research is targeted
64 to energy constrained platforms.

65 Energy consumption recommendations and guidelines for developers are popular avenues of research.
66 Hasan *et al.* (8) and Pereira *et al.* (9) investigated the energy profiles of Java collections to help developers
67 manually choose the right collection. Linares-Vásquez *et al.* (10) produced a methodology of finding
68 energy consuming libraries and APIs in Android applications. Li *et al.* (11) discussed causes of energy
69 consumption on Android.

70 Many researchers have investigated what developers know about software energy, which motivates this
71 paper because most of the works conclude that developers are woefully ill-equipped to address software
72 energy consumption concerns. Pinto *et al.* (12) and Malik *et al.* (13) sought questions developers were
73 already asking. Pang *et al.* (5) surveyed developers to see what they understood about software energy
74 consumption. Manotas *et al.* (14) went further and surveyed numerous industrial developers.

75 Recommenders quickly turn into optimizers that apply search techniques and find solutions to software
76 energy consumption concerns. SEEDS from Manotas *et al.* (15) attempts to find the most energy efficient
77 Java collections to use in a program for a particular context. GUI optimizations have also been approached
78 using a search-based approach by Linares-Vásquez *et al.* (16). Bruce *et al.* (17) explicitly applied
79 search-based software engineering techniques to mutate existing source code. Saborido *et al.* (18) use
80 multi-objective heuristics to find optimal apps where energy is one dimension.

81 Measuring software energy consumption is another avenue of research. We used the GreenMiner (19)
82 in this paper to measure software energy, but other researchers such as Banerjee *et al.* (20) have made
83 their own measurement frameworks.

84 Numerous empirical studies exist about different aspects of software development juxtaposed against
85 software energy consumption. Researchers such as Rasmussen *et al.* (21) and Gui *et al.* (22) have
86 investigated the cost of advertisement on energy consumption. Chowdhury *et al.* (23) and Li *et al.* (24)
87 benchmarked HTTP related energy concerns. Many researchers have suggested ranking and measuring
88 apps by energy consumption (25; 26; 18).

89 A very popular area of research is the modelling of software energy consumption. Pathak *et al.* (27; 28)
90 and Aggarwal *et al.* (29) used system-call based models. Chowdhury *et al.* (30) used count based models.
91 Some tools attempt to diagnose the actual cause of software energy consumption in terms of the code (31).

92 2.2 Machine Learning on Mobile Platforms

93 Multiple frameworks exist that enable machine learning within mobile applications. As Android uses
94 Java, any Java-based machine learning framework can easily be integrated into an Android application.
95 For our tests, we used the Weka (32) and Neuroph (33) frameworks. Google Brain’s TensorFlow machine
96 learning library (1) is also intended to be portable to mobile and embedded devices.

97 As a demo for an Android application, TensorFlow provides example code for an application that can
98 classify what is being viewed in the phone's camera frame in real time. Similarly, the Google Translate
99 mobile application can translate words being viewed through a phone's camera offline and in real-time
100 using a trained convolutional neural net (2).

101 There are numerous cases of machine learning being used in apps. "Smart calendar" apps use machine
102 learning to enhance calendar applications. Google Calendar Goals automatically schedules time for
103 user-set personal goals, such as exercising three times a week, re-schedules these goals if a conflicting
104 appointment is added, and learns the best times to schedule goals based on when the user completes or
105 defers a goal (3). The Tempo app could pull and bundle data related to calendar events from the user's
106 accounts — such as participant contact information, directions to the location, associated documents —
107 and present them together in one organized entry (4).

108 Triposo is an app that provides travel recommendations and booking options to users. It uses machine
109 learning to process websites and reviews, and combines the results with user preferences to make
110 personalized recommendations (34). Weotta is an app that uses machine learning and natural language
111 processing to provide event and activity recommendations to user queries (35).

112 2.3 Algorithms Used

113 We tested eight machine learning algorithms: *Naïve Bayes* (NB), *J48* (Weka's implementation of C4.5),
114 *Sequential Minimal Optimization* (SMO) which is a support vector machine, *Logistic Regression* (LogReg),
115 *Random Forest* (RF), *k-Nearest Neighbour* (IBk), *ZeroR*, and *MultiLayer Perceptron* (MLP) which is a
116 neural network. All algorithm implementations except for MLP were from the Weka Java codebase. The
117 MLP implementation, a neural network, is from the Neuroph framework.

118 *ZeroR* is a very simple classifier, that disregards any attribute information and always predicts the
119 majority class of the training set. As such, *ZeroR* can provide the baseline accuracy for a dataset (36). For
120 a dataset with n training instances, *ZeroR* will take $O(n)$ time to build a classifier as it needs to check the
121 class value of each instance in order to find the most frequent class. However, it takes virtually no time,
122 constant time $O(1)$, to classify.

123 *Naïve Bayes* is a type of Bayesian network that uses the simplifying assumptions that the predictive
124 attributes are conditionally independent, and that there are no hidden attributes that influence predictions.
125 With these simplifying assumptions, given a dataset with d attributes, n testing instances and m training
126 instances, the *Naïve Bayes* classifier can perform training and testing in $O(dn)$ and $O(dm)$ time respec-
127 tively (37). The Weka *Naïve Bayes* algorithm used for these tests is not updateable, although Weka also
128 has an updateable implementation of *Naïve Bayes*.

129 *J48* is Weka's implementation of the C4.5 decision tree algorithm (38). For a dataset with d attributes
130 and n testing instances, C4.5 training has an algorithmic time complexity of $O(nd^2)$ (39).

131 *SMO* is an algorithm for training a Support Vector Machine (SVM) classifier, that breaks down the
132 SVM quadratic programming optimization to simplify implementation, speed up computation, and save
133 memory (40) (41). Platt found empirically that the training time of *SMO* ranges from $O(n)$ up to $O(n^{2.2})$
134 for n training instances (40). In Weka's implementation, datasets are automatically processed to replace
135 missing values, normalize all attributes, and convert nominal attributes to binary ones.

136 *Logistic Regression* is a statistical machine learning algorithm. Using logistic regression with the
137 Quasi-Newton method, a dataset with d attributes and n instances takes $O(d^2n + nd)$ time per iteration (42).
138 For our tests logistic regression was set to iterate until convergence. Weka's implementation of the
139 algorithm is slightly modified from the original *Logistic Regression* to handle instance weights.

140 *Random Forest* is an advanced tree classifier that grows multiple trees and allows them to vote for
141 the best class (43). For a forest with L trees, n instances, and d attributes, theoretically the random
142 forest will be constructed in $O(Ln^2d \cdot \log(n))$ time, although practically the complexity is often closer to
143 $O(Lnd \cdot \log(n))$ (44).

144 *IBk* is an instance-based learner algorithm, that is similar to the k -nearest neighbour algorithm (45).
145 For our tests, we classified instances based on the nearest three neighbours ($k = 3$). *IBk* is lazy when
146 training, taking almost no time to create a model (46). However, for a dataset with d attributes and n
147 instances, it takes $O(nd)$ to classify an instance (45).

148 *MLP* is a neural network implementation. For our tests, *MLP* used back-propagation learning and
149 had only one hidden layer of neurons. The number of hidden neurons was fixed at 15 and the number of
150 training epochs was fixed at 100. In general, for a dataset with n instances and a neural network with a

Table 1. Size and type of datasets used in energy tests

Dataset	Description	Number of Attributes	Number of Instances	Number of Classes
MNIST	Image classifier – Integer attributes	785	5000	10
PGSQL	Text classification – Binary categorical attributes	2000	400	2
Mushroom	Classification – Categorical attributes	23	8124	2
Adult	Classification – Categorical, integer attributes	15	32561	2
Spambase	Text classification – Integer, real attributes	58	4601	2
Waveform	Numeric classification – Real attributes	22	5000	3
Pendigits	Image classifier – Integer attributes	17	10992	10

151 input neurons, b hidden neurons, and c output neurons, the network will take $O(nabc)$ time to train per
 152 epoch (47).

153 2.4 Datasets Used

154 We used seven existing datasets to test the machine-learning algorithms. The datasets chosen were
 155 of different sizes and datatypes, and represented different classification problems. We used our own
 156 text classification dataset (PGSQL) from our prior work (48; 49), the MNIST number classification
 157 dataset (50), and five datasets from the UCI archive (51) (Mushroom, Adult, Waveform, Spambase, and
 158 Pendigits). MNIST and Pendigits are image classification problems; PGSQL and Spambase are text
 159 classification problems; Adult and Waveform are numeric classification problems; and Mushroom is
 160 categorical classification.

161 Weka is designed to work with the ARFF file format. A version of the MNIST dataset already
 162 converted to the ARFF format was obtained (52) and used for the tests. The other datasets were converted
 163 to ARFF files using the Weka Explorer's conversion capabilities. For our tests, the size of the MNIST
 164 dataset was reduced to 5000 randomly selected instances. The size of the PGSQL dataset was also reduced
 165 from 640 instances with 23008 attributes to 400 instances with 2000 attributes, one of which was the class.
 166 The datasets are summarized in Table 1.

167 The MLP implementation we used from the Neuroph framework required datasets in CSV format.
 168 It also requires that numeric attributes be normalized to values between 0 and 1, nominal attributes and
 169 classes be represented as one-hot binary inputs, and instances with missing attribute or class values be
 170 removed beforehand. This processing and conversion to CSV was done using the Weka Explorer. As a
 171 result of converting categorical attributes to one-hot binary attributes, the number of input neurons for the
 172 Mushroom dataset became 111, and 104 for the Adult dataset.

173 A mirror of our datasets can be found at this url: [https://archive.org/details/mnist_](https://archive.org/details/mnist_test_reduced_5k)
 174 [test_reduced_5k](https://archive.org/details/mnist_test_reduced_5k).

175 3 METHODOLOGY AND MEASUREMENTS

176 In this section we describe how we setup benchmarks for the machine learning algorithms and datasets.
 177 We also describe how we measured the energy consumption of the machine learning benchmarks.

178 3.1 Energy Measurement with GreenMiner

179 Energy and power measurements were collected using the GreenMiner energy-measurement framework.
 180 This framework uses hardware-instrumented Android smartphones to physically measure the energy
 181 consumption and power use of apps running on the phones (19). It automatically runs submitted tests
 182 and uploads the results to a central webservice. Before each test is run, the application APK (Android
 183 package) is installed on the phone, required data is uploaded onto the SD card, and phone settings such as
 184 screen brightness, and screen timeout are set as required. After each test the application is uninstalled,
 185 the data is deleted from the SD card, settings are restored to previous values, and data generated during
 186 the tests such as log-files are pulled from the phones to be uploaded to the web service and then deleted
 187 from the phone, so that the next test can begin with a clean environment. Tests run for a set duration, and
 188 testers can split the test's energy measurements into partitions of varying duration to capture the energy
 189 and power use of different phases of app execution. Such a phase could be reading the data or training the

190 model. The GreenMiner measures and reports information about the test run including energy use, power
191 use, and runtimes for both the entire test duration and over each tester-specified partition. An example
192 of an energy profile for a cross-validated Naïve Bayes test displayed on GreenMiner's web interface is
193 shown in Figure 1.

194 3.2 Measurement Process

195 To test machine learning algorithms on the GreenMiner phones, two Android apps were created. An app
196 was created to run Weka machine learning algorithms, based on an existing modification of the Weka
197 codebase that can run on Android.¹A second app was created to test a MultiLayer Perceptron neural net
198 algorithm, using the Neuroph framework. Both apps ran the same datasets.

199 Tests of the different algorithms and datasets were written as Android `InstrumentationTestCases`,
200 with the phases of evaluating an algorithm (reading data, training the model, validating the model) written
201 as separate tests. The different tests were initiated by pressing buttons, and data was transferred between
202 different test methods via a singleton object. To keep the screen energy consumption of the apps constant,
203 the screens were almost completely black, with some small grey text on the buttons for debugging
204 purposes. Both the Weka and the Neuroph apps had exactly the same user interface.

205 Tests were created for eight different machine learning algorithms to evaluate seven different datasets.
206 Separate tests methods were written to perform two different types of evaluation. For each algorithm two
207 tests were written to train on 50% of the data and then test on the other 50%. Two more tests were written
208 to train and test on the whole dataset using 10-fold cross validation. Each train/test evaluation pair was
209 run separately on the GreenMiner.

210 Each test method was invoked in turn by pressing a button on the app's interface once the previous
211 method had completed. The GreenMiner framework cannot automatically detect when a test method has
212 completed, because it runs uninstrumented, so in order to invoke the next method initial timing test runs
213 were performed to determine appropriate delays to add to the GreenMiner scripts. Each algorithm-dataset-
214 validation combination was run at least 10 times on the GreenMiner so that their results could be averaged
215 and to allow for enough statistical power to determine an effect. Some combinations, such as random
216 forest on the MNIST dataset with cross validation, ran out of memory when evaluating on the phones, and
217 so are not included in our results.

218 The GreenMiner collects the energy consumption measurements and power measurements of each test
219 method. The results of all successful test runs were compiled and compared. For comparisons, the training
220 and testing phases of 50% split evaluation are combined, and are compared against the energy for cross-
221 validating with 10-folds, that includes training and testing each fold. Energy consumption measurements
222 are compared to determine which algorithms will require the most or least energy to evaluate on each
223 dataset. Power usages are compared to determine if some algorithms are more energy-hungry, independent
224 of how long it takes them to evaluate.

225 The correctness of the Weka algorithms was gathered from the Weka 3.8 desktop application, based on
226 performing 10-fold cross validation. The total root-mean-squared errors (RMSE) of the MLP algorithm
227 were gathered from NeurophStudio. The average accuracies of an algorithm over all datasets were
228 compared to determine which algorithms were generally the most or least accurate. The accuracy for
229 Logistic Regression could not be calculated for the Adult dataset because the desktop Weka application
230 ran out of memory.

231 Statistical significance testing was executed using a Student's *t*-test as energy measurement data
232 typically is normally distributed. Anders-Darling tests confirmed normality in most cases. We addressed
233 multiple hypotheses and comparisons by applying Bonferroni correction with an initial alpha (α) of 0.05.

234 4 ENERGY PROFILING RESULTS

235 We profiled the energy and power use of eight machine learning algorithms, and compared how they
236 varied with datasets of different sizes. We compared how eight machine-learning algorithms used power
237 and energy when applied to datasets of different sizes. We asked four research questions:

238 RQ1: Can we identify the best performing algorithm in terms of energy?

239 RQ2: Can we identify the best performing algorithm in terms of power?

240 RQ3: Can we identify the best performing algorithm in terms of accuracy?

241 RQ4: Can we identify the best performing algorithm for training/testing in terms of energy?

¹Weka for Android <https://github.com/rjmarsan/Weka-for-Android>

Table 2. Average ranking of each algorithm from lowest to highest energy consumption

Sorted Algorithm	Rank – 50%	Sorted Algorithm	Rank – 10-CV
ZeroR	1	ZeroR	1
NB	2.57	NB	2
J48	3.57	J48	3.86
SMO	3.86	SMO	4.43
LogReg	5.43	LogReg	5
MLP	6.29	IBk	5.29
IBk	6.57	RF	7.14
RF	6.71	MLP	7.29

4.1 RQ1: Can we identify the best performing algorithm in terms of energy?

Which algorithms are more energy efficient? Figure 2 shows the energy used to train and test the algorithms on a 50% split of each dataset. Figure 3 shows the energy used to perform 10-fold cross validation on the algorithms for each dataset. Note that some algorithms could not be evaluated on some datasets, and so not all algorithm-dataset combinations are shown in the figures.

Generally, energy consumption increases with increasing dataset size, however these increases typically do not strictly follow a clear trend. One reason for deviations could be related to memory cache; spikes in energy consumption could be due to the memory cache exhaustion for that particular dataset.

Figure 2 shows that other than ZeroR, Naïve Bayes and J48 tend to have the lowest energy consumption for 50%-split. SMO also has good energy performance for most datasets except for the Adult dataset. Figure 3 shows that Naïve Bayes is consistently consumes the nearly the least energy for cross validation, and J48 is one of the highest energy users for smaller dataset sizes, but one of the lower energy consumers for larger datasets.

The overall rankings of the algorithms' energy use were determined by assigning a rank value to each algorithm for each dataset, with 1 using the least energy and 8 using the most. The rankings for each dataset were then summed, and divided by the number of datasets. Table 2 shows that ZeroR always uses the least amount of energy, followed by Naïve Bayes and J48. There were some deviations in the rankings of each algorithm on a dataset between cross-validation and 50% split. The order of average rankings for each evaluation method had high correlation of 0.93.

The energy use of the algorithms were compared using a pairwise t-test to determine if the energy differences are statistically significant for an alpha of 0.05. For the combined training and testing energies of 50% split, all algorithms had significantly different energy consumptions except for NB vs J48, J48 vs LogReg, J48 vs RF, SMO vs IBk, SMO vs MLP, and IBk vs MLP. For cross validation, all algorithms had significantly different energy consumptions except for J48 vs LogReg, J48 vs IBk, LogReg vs IBk, LogReg vs RF, IBk vs RF, and MLP vs RF.

4.2 RQ2: Can we identify the best performing algorithm in terms of power?

Figure 4 shows the average power use to train and test the algorithms on a 50% split of each dataset. Figure 5 shows the average power use of each algorithm to perform 10-fold cross validation. Note that some algorithms could not be evaluated on some datasets, and so not all algorithm-dataset combinations are shown in the figures.

Figures 4 and 5 show that the power use of all algorithms are similar. Table 3 shows the average rankings for the algorithms are less evenly-spread between 1 and 8, indicating that the rank of an algorithm's power use varies more from dataset to dataset. Additionally, the rankings of algorithms between 50% split and cross validation are not as well-correlated as the energy rankings, with a Spearman's rank correlation rho value of 0.62. However, overall the algorithms' power rankings are similar to the energy rankings, with ZeroR and Naïve Bayes consistently having the lowest power consumption.

The power use of the algorithms were compared using a pairwise t-test to determine if the power use differences are statistically significant for an alpha of 0.05. For the combined training and testing energies of 50% split, all algorithms had significantly different power consumptions except for J48 vs MLP, SMO vs LogReg, SMO vs RF, SMO vs IBk, LogReg vs IBk, and RF vs IBk. For cross validation, all algorithms

Table 3. Average ranking of each algorithm from lowest to highest power use

Sorted Algorithm	Rank – 50%	Sorted Algorithm	Rank – 10-CV
ZeroR	1.43	ZeroR	1.14
NB	3.14	NB	2.86
MLP	3.57	LogReg	3.71
J48	4.43	J48	4.29
SMO	4.71	MLP	5
IBk	5.86	IBk	5.71
RF	6.14	SMO	6.29
LogReg	6.71	RF	7

Table 4. Average algorithmic accuracies ordered based on percentage of correctly classified instances, kappa statistic, and Root Mean Squared Error

Accuracy	Algorithm	% Correct	Algorithm	Kappa	Algorithm	RMSE
Most	MLP	95.66%	MLP	0.9293	MLP	0.08
	Random Forest	90.32%	SMO	0.7488	Random Forest	0.21
	SMO	90.13%	Random Forest	0.7211	IBk	0.21
	IBk	88.32%	IBk	0.7194	LogReg	0.25
	LogReg	87.08%	LogReg	0.7087	J48	0.25
	J48	85.73%	J48	0.6911	SMO	0.29
	Naïve Bayes	81.97%	Naïve Bayes	0.6332	Naïve Bayes	0.32
Least	ZeroR	46.36%	ZeroR	0.0000	ZeroR	0.41

283 had significantly different power consumptions except for NB vs LogReg, NB vs MLP, NB vs RF, J48 vs
 284 IBk, SMO vs IBk, LogReg vs MLP, LogReg vs RF, and MLP vs RF.

285 4.3 RQ3: Can we identify the best performing algorithm in terms of accuracy?

286 Algorithmic accuracy is determined based on the percentage of correctly classified instances and on
 287 the kappa statistic. Kappa measures agreement between the predicted and the true class. As different
 288 algorithms sometimes had the same accuracy for a dataset, rather than ranking algorithmic accuracy for
 289 each dataset — which would result in ties — the average accuracy of each dataset was calculated. As the
 290 accuracy for Logistic Regression could not be calculated for the Adult dataset, the average for Logistic
 291 Regression was taken over only 6 values, while the other algorithms were calculated over 7. Table 4
 292 shows the algorithms ordered in terms of both measures of accuracy.

293 Weka outputs predicted classes, and also provided a calculation of the root mean squared error (RMSE)
 294 of the predictions. Neuroph outputs the probabilities of each class. The outputs of the five datasets that
 295 could run on GreenMiner with cross validation (PGSQL, Mushroom, Waveform, Spam, and Pen) were
 296 normalized using softmax, and the highest normalized probability was taken as the predicted class. From
 297 this, the accuracies and kappa statistics for MLP on each dataset were computed in R. The total RMSE of
 298 MLP on each dataset was obtained from NeurophStudio. The average RMSE of each algorithm over all
 299 datasets is included in Table 4.

300 Table 4 shows the most accurate Weka algorithms are Random Forest and SMO; their percentage of
 301 correctly classified instances are very close, with Random Forest being about 0.2% higher. Yet SMO had
 302 a slightly better kappa statistic implying its classifications are more balanced. Overall, MLP is clearly the
 303 most accurate algorithm. It has significantly higher average classification accuracy and kappa statistic
 304 than the next-best algorithms, and the lowest RMSE.

305 4.4 RQ4: Can we identify the best performing algorithm for training/testing in terms of 306 energy?

307 Figure 6 compares the average energy to train and test each algorithm over all datasets with 50%
 308 split. Lazy algorithms such as IBk were the most efficient for training, followed by Naïve Bayes. For

Table 5. Spearman rank correlation rho value for 50% split energy use and CPU use between algorithms classifying a dataset

Dataset	User Time	System Time	Idle Time	IO Wait Time	Number of Interrupts	Context Switches	Processes
Adult	1.00	0.57	1.00	0.07	0.96	0.79	0.85
MNIST	1.00	0.61	1.00	0.04	0.96	0.82	0.93
Mushroom	1.00	0.76	0.90	0.52	0.95	0.86	0.64
Pendigits	0.98	0.36	1.00	0.57	0.95	0.74	0.83
PGSQL	1.00	0.19	0.98	0.17	0.76	0.12	0.81
Spambase	1.00	0.00	0.98	0.45	0.79	0.07	0.50
Waveform	1.00	0.14	0.93	0.19	0.67	0.33	0.95

Table 6. Spearman rank correlation rho value for CV energy use and CPU use between algorithms classifying a dataset

Dataset	User Time	System Time	Idle Time	IO Wait Time	Number of Interrupts	Number of Context Switches	Number of Processes
Adult	1.00	0.90	1.00	0.30	1.00	0.90	1.00
MNIST	1.00	1.00	1.00	0.50	1.00	1.00	1.00
Mushroom	1.00	0.88	1.00	0.71	0.95	0.83	0.93
Pendigits	1.00	0.76	1.00	0.33	0.98	0.81	0.98
PGSQL	1.00	0.57	1.00	0.21	0.96	0.75	0.93
Spambase	1.00	0.21	1.00	0.25	0.86	0.57	0.93
Waveform	1.00	0.36	1.00	0.18	0.86	0.57	0.96

309 evaluation/classification other than ZeroR, J48 was quite efficient to classify data in terms of energy. For
 310 both training and test combined Naïve Bayes performed well.

311 5 CAUSES OF ENERGY DIFFERENCES

312 5.1 Is energy use related to the CPU usage of an algorithm?

313 Before and after running a test, the phone's `/proc/stat` file is collected to gather information about
 314 the phone's CPU time and processes. The difference between the two measurements is used to determine
 315 the CPU time and resource usage of a test. These results are compared to determine how an algorithm's
 316 CPU usage is related to its energy usage.

317 When comparing the results from 50%-split tests, energy use was strongly correlated to user time and
 318 idle time for all datasets. Table 5 shows that energy consumption was not strongly correlated to system
 319 time usage or IO wait time for most datasets. Energy was strongly correlated to the number of interrupts
 320 for most datasets, except for PGSQL and Waveform, where it was only moderately correlated. For other
 321 CPU use measurements, the strength of correlation to energy usage varied widely between datasets. The
 322 results were similar for cross-validation.

323 In general, the correlations between energy use and CPU use were stronger for cross validation. It
 324 should be noted that the Adult and MNIST could not be evaluated by many algorithms on the phones
 325 because they ran out of memory. Thus, there are fewer energy results to compare for these datasets.

326 For the 10-fold results, energy use was strongly correlated to user time, idle time, and number of
 327 processes. The number of interrupts was also well-correlated to energy use for all datasets. IO wait time
 328 was not strongly correlated to energy use, and, excluding the Adult and MNIST values, system time was
 329 generally not strongly correlated to energy use for any dataset.

330 The number of processes did not significantly increase between 50% split evaluation compared to
 331 cross validation. On average, over all datasets and algorithms, only 1.2 times as many processes were
 332 created for cross validation as compared to 50% split. In contrast, on average, 10-fold evaluation used 7.0
 333 times more idle time, and 10.5 times as much user time.

Table 7. Average memory usage of each algorithm over all datasets

Algorithm	Number of Concurrent GC	GC Concurrent Time (ms)	Number of GC for Alloc	GC for Alloc Time (ms)	Times Grown	Used (Bytes)	Allocated (Bytes)
IBk	148	4853	79	3449	34	12647	21148
J48	332	22650	27	1268	9	13853	18139
LogReg	942	69496	1592	86693	121	31019	35258
MLP	698	24260	286	16671	1	6966	12022
NB	668	32272	16	573	4	9818	12914
RF	957	122458	244	18323	74	28504	50757
SMO	328	13448	381	15336	226	28189	37138
ZeroR	135	3674	6	189	1	8989	11348

334 5.2 Is energy use related to the memory use of an algorithm?

335 Android's Dalvik VM automatically logs information about heap use and garbage collection (GC). These
 336 logs were collected for the algorithms and datasets using Android's logcat tool. These logs have the
 337 number of kilobytes allocated for and used on the heap, the number of times the app's heap size was
 338 grown, the number of concurrent GCs performed when the heap grows too large, the number of GCs
 339 performed when the heap is too full to allocate required memory, and the total time taken to perform these
 340 GCs, could be parsed and compared. The average results for each algorithm performing 10-fold cross
 341 validation over all datasets are shown in Table 7.

342 Logistic Regression and Random Forest used the most memory on the heap and performed the most
 343 concurrent garbage collections. Overall, they are the most inefficient in terms of memory use. It should
 344 also be noted that Random Forest's performance was most affected by memory, as five datasets could
 345 not be evaluated with 10-fold cross validation on the phones as they ran out of memory or had a stack
 346 overflow occur. Excluding both MLP and ZeroR, Naïve Bayes, J48, and IBk performed the fewest garbage
 347 collections to make space for allocations, grew their heap the fewest number of times, and used the least
 348 amount of heap space. Random Forest and Logistic Regression were both large energy users, while Naïve
 349 Bayes and J48 were the lowest energy users, so for these algorithms their memory use seems related to
 350 their energy use. However, IBk was one of the most memory-efficient, but the second-highest energy
 351 consumer, so memory use alone cannot account for memory efficiency. Additionally, MLP, which was
 352 implemented with the Neuroph framework rather than Weka, was very memory efficient despite being the
 353 highest energy user with cross validation. Excluding ZeroR, MLP used and allocated the least amount of
 354 heap space, and grew its heap the fewest number of times. However, it performed the third-most GCs, so
 355 it is may be reducing its memory requirements by performing more frequent memory clean-ups.

356 The memory use of the Weka-implemented algorithms, not MLP, was compared to energy use, and
 357 the Spearman's correlation rho estimates are shown in Table 8. Table 8 shows that energy use is not
 358 consistently well-correlated to memory use. Generally energy use was most strongly correlated to the
 359 maximum heap space used in a test and the maximum heap space allocated in a test. Spambase and
 360 Waveform datasets generally showed weak correlations between their energy and memory use.

361 When the MLP memory usage data is added to the comparison most of the correlations were unchanged
 362 or became weaker as, exhibited by Table 9, although some correlations — particularly for the Waveform
 363 dataset — became stronger.

364 5.3 Is energy use related to the methods called by an algorithm?

365 Method traces for algorithms with different datasets were generated using Android's Dalvik Debug
 366 Monitor Server (DDMS) and dmtracedump tools. The method traces were generated by sampling every
 367 millisecond. The methods called by each algorithm are compared, and the total number of CPU cycles
 368 and total number of method calls made are correlated to energy use.

369 The total number of method calls is strongly correlated to the energy use of each algorithm on a
 370 dataset, with algorithms making more method calls using more energy. All datasets had rho estimates of
 371 0.9 or better. Similarly, the number of CPU cycles elapsed during execution also had a rho estimate of 0.9
 372 or better for all datasets when correlated to energy use.

373 Additionally, algorithms that used more energy, such as MLP or Random Forest, called costly methods

Table 8. Spearman's rank correlation rho value for 10-fold energy use and memory use between Weka-implemented algorithms classifying a dataset

Dataset	GC Concurrent	GC Concurrent (ms)	GC for Alloc	GC for Alloc (ms)	Grow	Used	Allocated
Adult	0.40	0.70	0.90	0.90	0.87	0.70	0.90
MNIST	0.50	0.50	1.00	1.00	1.00	1.00	1.00
Mush	0.75	0.75	0.64	0.64	0.26	0.96	0.96
Pen	0.68	0.68	0.79	0.82	0.71	0.86	0.86
PGSQL	0.71	0.71	0.77	0.83	0.06	0.66	0.66
Spam	0.49	0.49	0.49	0.60	0.60	0.60	0.60
Wave	0.14	0.31	0.60	0.60	0.60	0.60	0.66

Table 9. Spearman's rank correlation rho value for CV energy use and memory use between all algorithms classifying a dataset

Dataset	GC Concurrent	GC Concurrent (ms)	GC for Alloc	GC for Alloc (ms)	Grow	Used	Allocated
Adult	0.4	0.7	0.9	0.9	0.87	0.7	0.9
MNIST	0.5	0.5	1	1	1	1	1
Mush	0.69	0.69	0.42	0.42	0.19	0.74	0.74
Pen	0.79	0.76	0.69	0.74	0.34	0.67	0.67
PGSQL	0.36	0.57	0.86	0.86	-0.19	0.5	0.5
Spam	0.65	0.65	0.47	0.47	0.44	0.76	0.68
Wave	0.54	0.65	0.68	0.68	0.72	0.68	0.94

374 many times. For the applicable datasets Random Forest was able to perform cross validation to completion
 375 on, the method invoked the most number of times by the algorithm was Weka's QuickSort. Naïve
 376 Bayes and J48 also invoked QuickSort, but significantly fewer times per dataset: Random Forest called
 377 QuickSort 9 to 41 times as often as often as J48 did, and 69 to 83 times as often as Naïve Bayes. QuickSort
 378 was never used on the Mushroom dataset with any algorithm as it only has categorical attributes. MLP
 379 called methods to update weights with backpropagation calculations the most. Logistic regression,
 380 another high energy-user, frequently calls methods to evaluate the model's gradient vector and to perform
 381 exponentiation.

382 5.4 Is energy use related to algorithmic complexity?

383 To determine the correlation between algorithmic complexity and energy usage, the relevant statistics of
 384 each dataset, including number of attributes, and number of instances, were substituted into the algorithmic
 385 time complexity formulas for training each learner. For IBk, which has a constant time complexity, the
 386 cost was set to the constant 100000 for each dataset. For SMO, which was empirically determined to have
 387 a time complexity between $O(n)$ up to $O(n^{2.2})$ for n training instances (40), a time complexity of $O(n^2)$
 388 was used. The rho values for the Spearman correlations between these computed numeric complexities
 389 and the energy required to train each algorithm on a dataset are shown in Table 10.

390 The curves of these complexity functions were then tuned by a single coefficient for a better fit. J48
 391 was multiplied by a factor of 5, Logistic Regression by 75, Random Forest by 10, and MLP by 100. The
 392 new rho estimates from these tuned curves are shown in Table 11.

Table 10. Spearman correlation rho estimates between algorithmic complexity and energy consumption when training model

	PGSQL	MNIST	Mush	Adult	Wave	Spam	Pen
50%	0.81	0.82	0.83	1.00	0.81	0.76	0.90
10-CV	0.86	1.00	0.83	1.00	0.75	0.64	0.93

Table 11. Spearman correlation rho estimates between algorithmic complexity tuned with constant factors and energy consumption when training model

	PGSQL	MNIST	Mush	Adult	Wave	Spam	Pen
50%	0.81	0.96	0.83	0.96	0.90	0.93	0.93
10-CV	0.86	1.00	0.83	1.00	0.89	0.89	0.98

393 5.5 Analysis

394 Hasan *et al.* (8) found that the power use of different collection classes was similar, and that energy
395 consumption seemed to increase at the same rate as program runtimes, indicating that programs that use
396 more energy do so because they do more work in the extra time it takes them to run. Our results agree
397 with this.

398 While the energy consumptions of different algorithms could differ significantly, the algorithms tended
399 to have similar power use. This is likely because the processes are primarily CPU bound. We found that
400 energy use was positively correlated to both runtime complexity, and the user and idle CPU time taken
401 by an algorithm. Further, energy use was positively correlated to the number of methods called by an
402 algorithm during execution, indicating that algorithms that use more energy to evaluate a dataset both
403 take longer and call more methods, thus doing more work. Algorithms and datasets that invoked garbage
404 collection more typically took longer and consumed more energy.

405 6 EVALUATING MACHINE LEARNING CHOICES ON MOBILE DEVICES

406 In this section we provide guidance to app developers who seek to use machine learning within their
407 mobile-apps. Developers should decide if they need to train machine learners or if they can simply
408 share a trained model with their mobile-app. Developers should also consider the effect that the number
409 of attributes have on energy consumption. Furthermore developers should consider how much energy
410 consumption they are willing to allow for versus the accuracy or agreement they want to achieve.

411 6.1 What are the best algorithms to use for models that do not need updating?

412 The Google Translate application uses a convolutional neural net that was trained on a carefully selected
413 dataset, and then deployed in the application (2).

414 J48, SMO, Logistic Regression, and MLP all have significantly higher training costs than classifying
415 costs. Thus, these algorithms would be ideal for implementations where the model could be trained ahead
416 of time, and not updated after release for classification in the application. J48, Logistic Regression and
417 SMO are Pareto optimal choices based on our limited evaluation, depicted in Figure 7.

418 6.2 What are the best algorithms to use for models that need updating?

419 If the model must be trained or re-trained on the phone, Naïve Bayes is the best algorithm to use to limit
420 energy use, as it has the lowest energy use overall and has the same time complexity for training as for
421 classifying [8]. The IBk classifier is trivial to update, making updating fast and low-energy, but it is slow
422 and energy-intensive to classify and it is one of the worst energy consumers for classification.

423 6.3 What are the best algorithms to use to minimize energy consumption?

424 Excluding ZeroR, Naïve Bayes used the least amount of energy on average for training and testing. J48
425 was also energy efficient, being the next-lowest energy user on average, after Naïve Bayes. Thus, Naïve
426 Bayes and J48 are the best algorithms to use for applications trying to reduce energy use. For 50% split
427 training and testing Naïve Bayes was the lowest energy consumer on average, but was the second-lowest
428 energy consumer for some datasets. For cross-validation, Naïve Bayes was the lowest energy consumer
429 across all datasets. This suggests that Naïve Bayes' energy performance will scale well over time.

430 Naïve Bayes is recommended over J48 in terms of energy use if the model must be trained as well
431 as evaluated by the app. If the model can be pre-trained, J48 will likely use less energy and be faster to
432 validate than Naïve Bayes, but Naïve Bayes can train models faster and with less energy than J48.

433 6.4 What are the best algorithms to use to maximize accuracy?

434 Of the Weka algorithms, Random Forest and SMO were the best classifiers overall, with Random Forest
435 having the highest average accuracy and SMO having the highest average kappa statistic, making these

436 the best algorithms to use to obtain correct results. Random Forest was also the highest average energy
437 user on 50% split datasets, and the second highest for 10-fold evaluation. SMO was less energy-hungry
438 overall and dominated RF.

439 MLP had the highest average accuracy overall, with an average classification accuracy of over 95%
440 and an average kappa of over 0.92. On some datasets it was able to achieve RMSEs smaller than 0.0001,
441 suggesting potential overfitting. MLP could likely achieve even higher accuracies if optimized. To
442 standardize the tests, all our MLP networks had the same number of hidden neurons (15), learning rate
443 (0.2), and fixed number of training epochs (100) regardless of input size or type. Tuning these parameters
444 for each dataset could likely improve prediction accuracies. For example, the Spambase dataset had the
445 highest error, with a classification total mean square error of 0.37 with the test parameters, but using
446 a learning rate of 0.1 and 1000 training epochs, the total mean square error could be reduced to 0.31.
447 However, tuning these parameters would likely also affect energy consumption of the network.

448 **6.5 What are the best algorithms for datasets with many attributes?**

449 Energy consumption is strongly-correlated to algorithmic time complexity. Thus, it is not surprising that
450 the algorithms with the lowest energy use on datasets with large numbers of attributes (PGSQL, MNIST,
451 Spambase) also have algorithmic complexities that have a low dependence on the number of attributes.
452 SMO had low energy use on the PGSQL and Spambase datasets, especially with 50% split evaluation.
453 Naïve Bayes, which has a linear dependence on the number of attributes, also performs well on these
454 datasets.

455 **6.6 What algorithms dominate in terms of energy versus accuracy?**

456 Figure 7 shows a clear dominating Pareto front of machine learners that are “optimal” for energy
457 consumption or accuracy measured in Kappa score. Clear dominators in order of Kappa score versus
458 energy are ZeroR, J48, Logistic Regression and support vector machines (SMO). These candidates make
459 sense because they are effectively small functions (logistic regression and SMO) or conditions (J48) that
460 are quick to evaluate. For training, ZeroR, IBk and SMO dominate as IBk’s lazy training beats Naïve
461 Bayes. Ignoring IBk, the training dominators are in order of Kappa are: ZeroR, Naïve Bayes, J48, logistic
462 regression, RF, and SMO.

463 **7 THREATS TO VALIDITY**

464 Construct validity is threatened by our choice of experiments, machine learning algorithms, and data sets.
465 We tried to control for attribution errors by having a constrained environment that was very similar for
466 every run.

467 Internal validity is threatened by selection bias of datasets and algorithms, as well the use of two
468 machine learning frameworks. The consistency of the measuring framework could affect internal validity.

469 External validity is threatened by the limited number of machine learning algorithms evaluated. We
470 could apply more and furthermore we are limiting ourselves to only two machine learning frameworks.
471 Some frameworks could have better energy efficiency or run-times. We hope that a lot of the external
472 validity can be addressed with the theoretical run-time estimates provided by complexity estimates.

473 **8 CONCLUSIONS**

474 We conclude that machine learning can be used in an energy efficient manner on mobile devices such
475 as smartphones. Currently we would not recommend training neural nets on mobile devices, however
476 evaluation with neural networks on mobile devices is quite successful (1; 2).

477 We observed that many machine learning algorithms cost more to train them to evaluate. Many of the
478 issues with applying these machine-learning algorithms can be addressed by offloading the training to the
479 cloud — which we recommend for logistic regression, support vector machines, and neural networks.

480 Depending on the context and the need for updates, a lazy trainer, such as nearest neighbours, with
481 expensive evaluation could make more sense than an algorithm with relatively good performance balance
482 between training and evaluation. One needs to balance how much evaluation versus how much training
483 one needs to do. Constant evaluation implies one needs a cheap evaluator whereas constant updates and
484 changing signals implies one need an algorithm that is cheap to train, such as Naïve Bayes or nearest
485 neighbours.

486 Dominating algorithms for only evaluation include Support Vector Machine, Logistic Regression
487 and J48. Support Vector Machines, Random Forest, and Neural Nets (MLP) performed the best in terms
488 of accuracy but with poor energy efficiency for training. Naïve Bayes was balanced and offered good
489 accuracy compared with its training energy efficiency but suffers from high evaluation energy costs. Some
490 algorithms did not fare very well for training such as logistic regression that requires lots of memory and
491 CPU and had middle-ground accuracy without the ability to update easily.

492 Thus mobile app developers need to be aware of the trade-offs between different machine learning
493 algorithms. We conclude that neural networks have good performance but suffer from poor energy
494 efficiency in terms of both training and evaluation. Perhaps fixed-point or binarized neural networks as
495 suggested by Courbariaux et al. (53) will enable the training of neural networks and deep learning on
496 mobile devices.

497 Future work would be to integrate smart search techniques to emulate the SEEDS approach (15) of
498 choosing machine learning algorithms given domain context and constraints. Thus, recommender systems
499 could be built that could analyze the problem and make the best suggestion based upon empirical and
500 theoretical constraints and measurements. Future work can also include accounting for more neural-net
501 architectures, more learners, and more data-sets.

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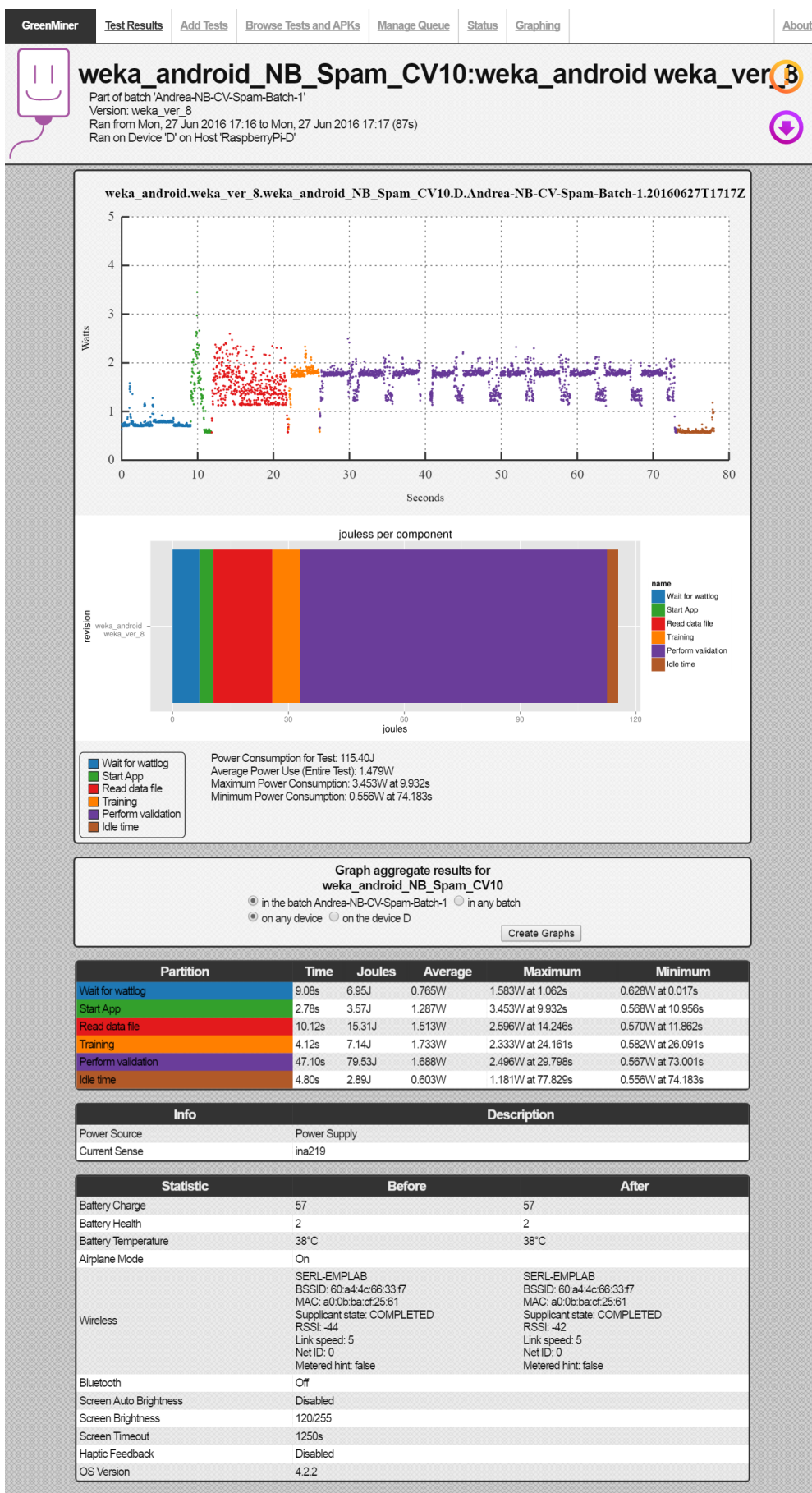


Figure 1. Example of a GreenMiner profile for a test run of 10-fold cross validation on Naïve Bayes 17/23

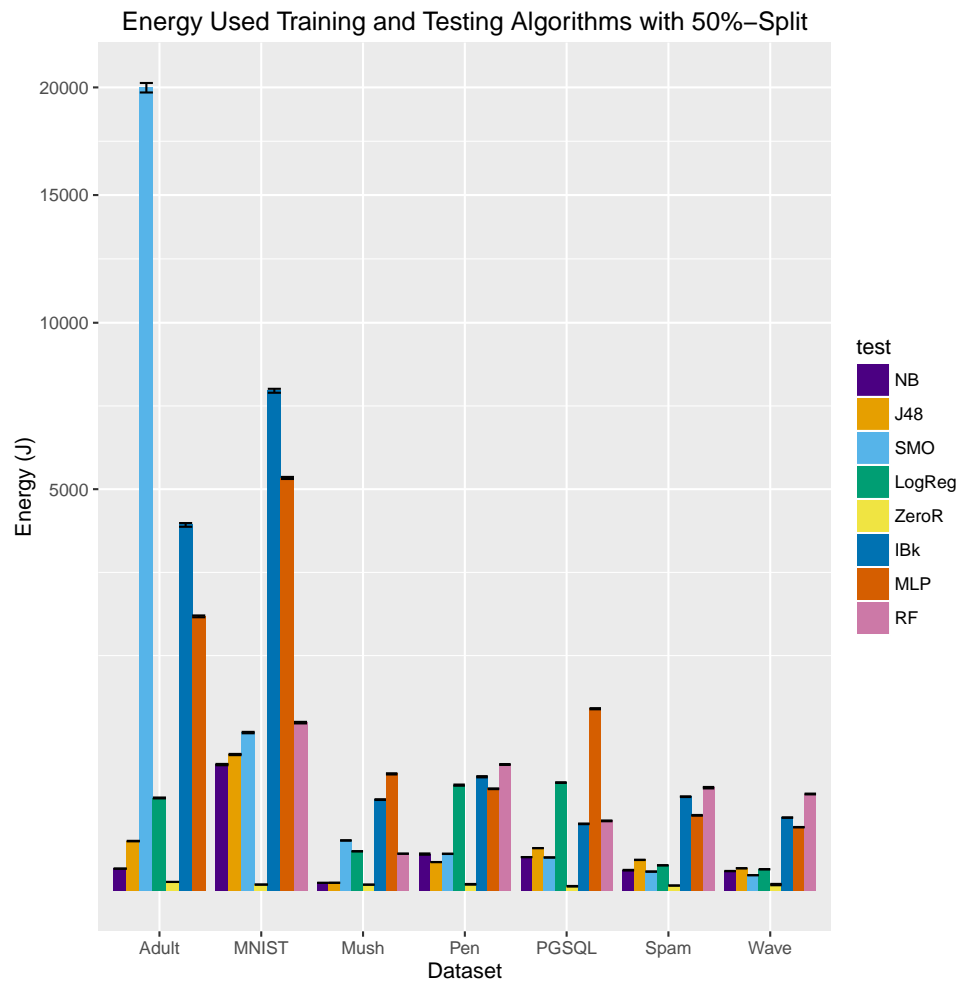


Figure 2. Energy consumption to train and test on 50% split

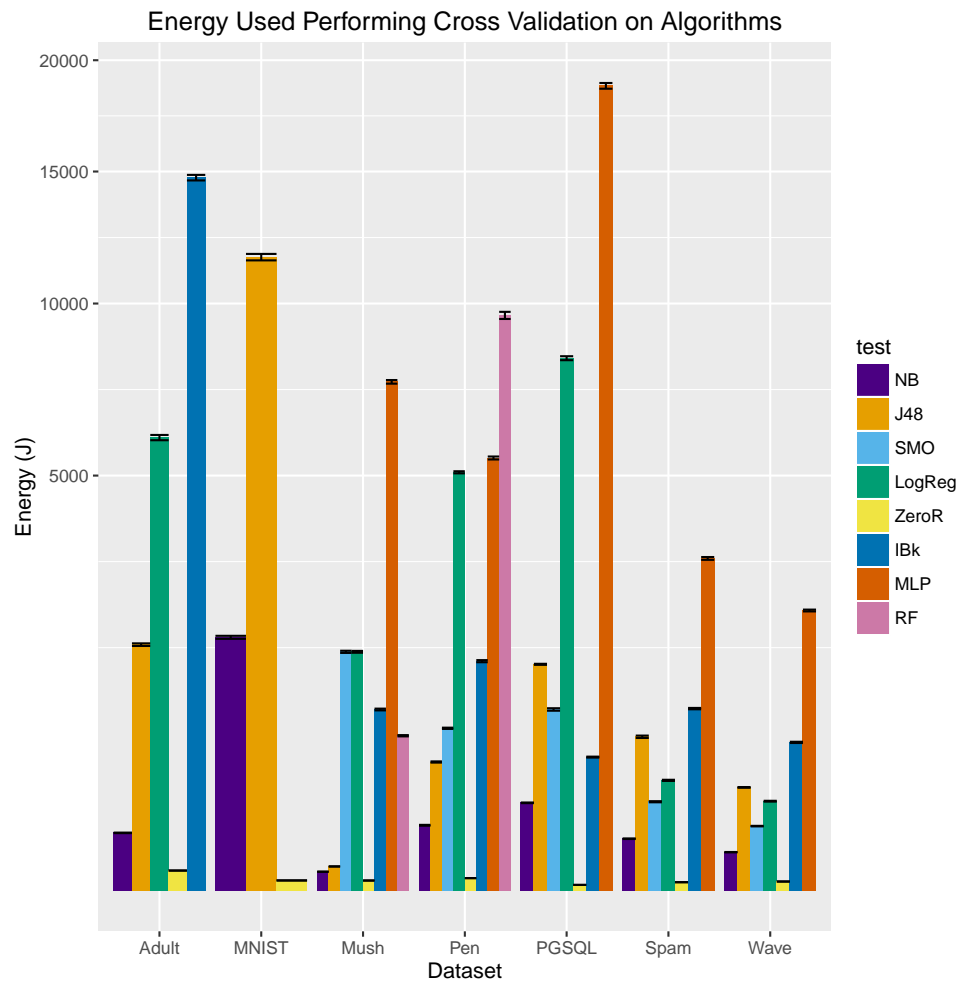


Figure 3. Energy consumption to perform 10-fold cross validation

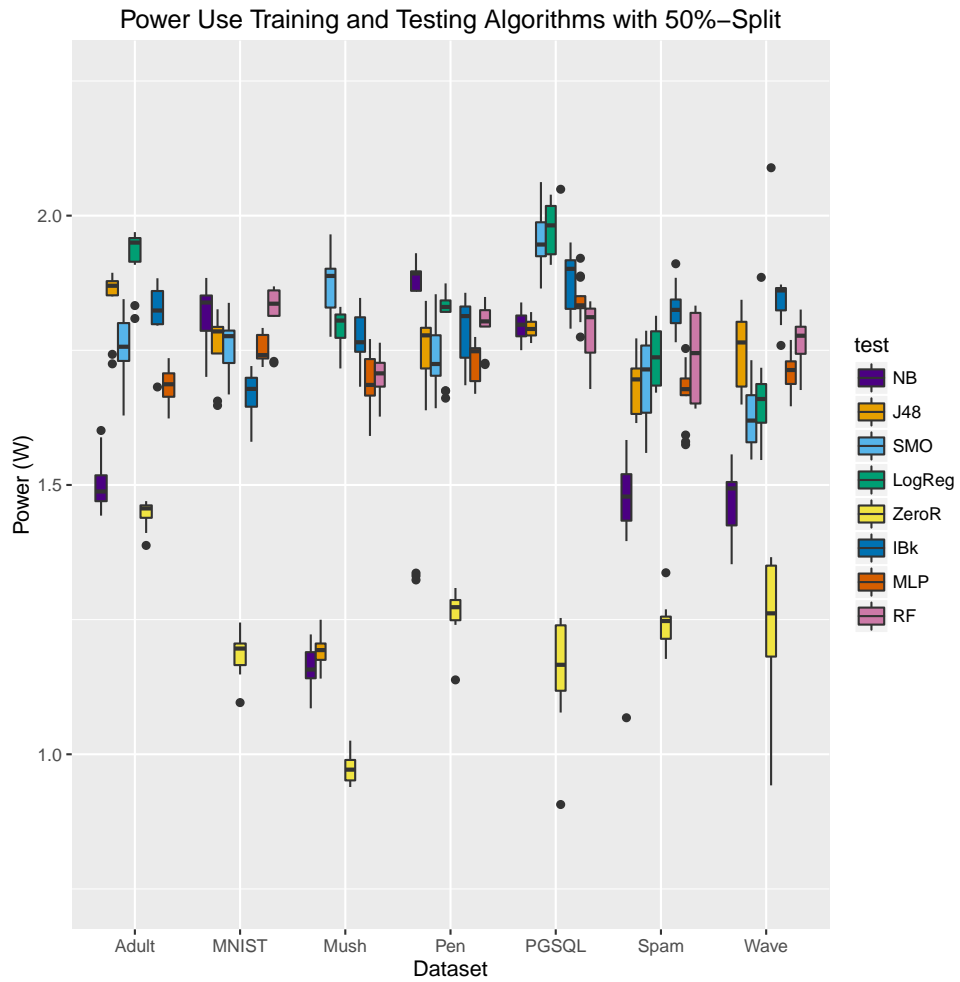


Figure 4. Power consumption to train and test with 50% split

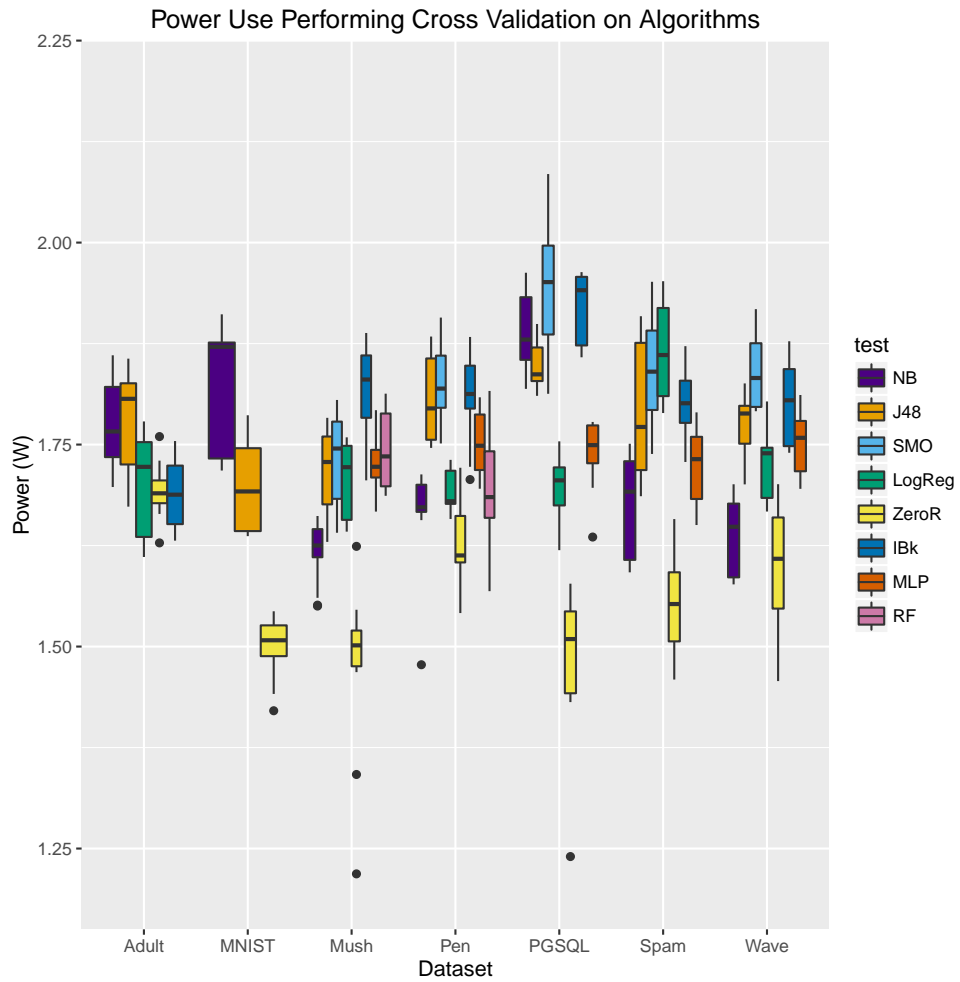


Figure 5. Power consumption to perform 10-fold cross validation

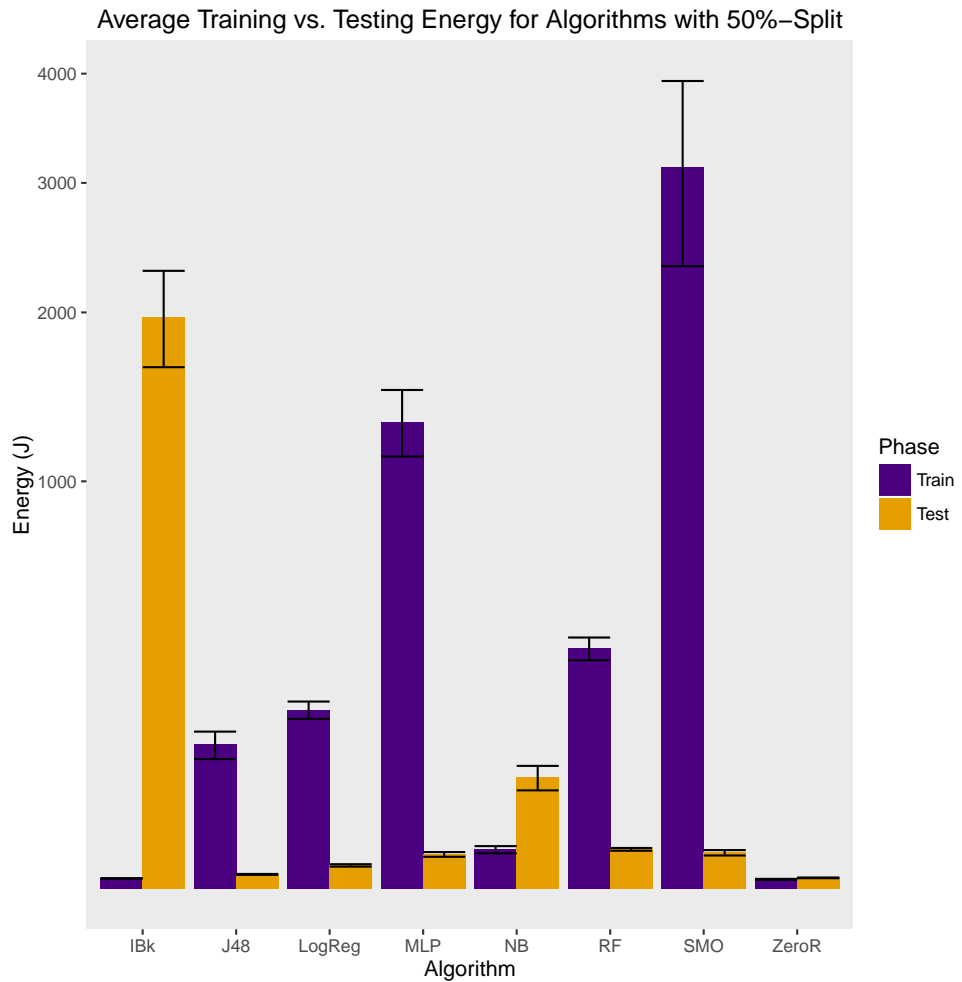


Figure 6. Comparison of average energy use training and testing algorithms with 50% split

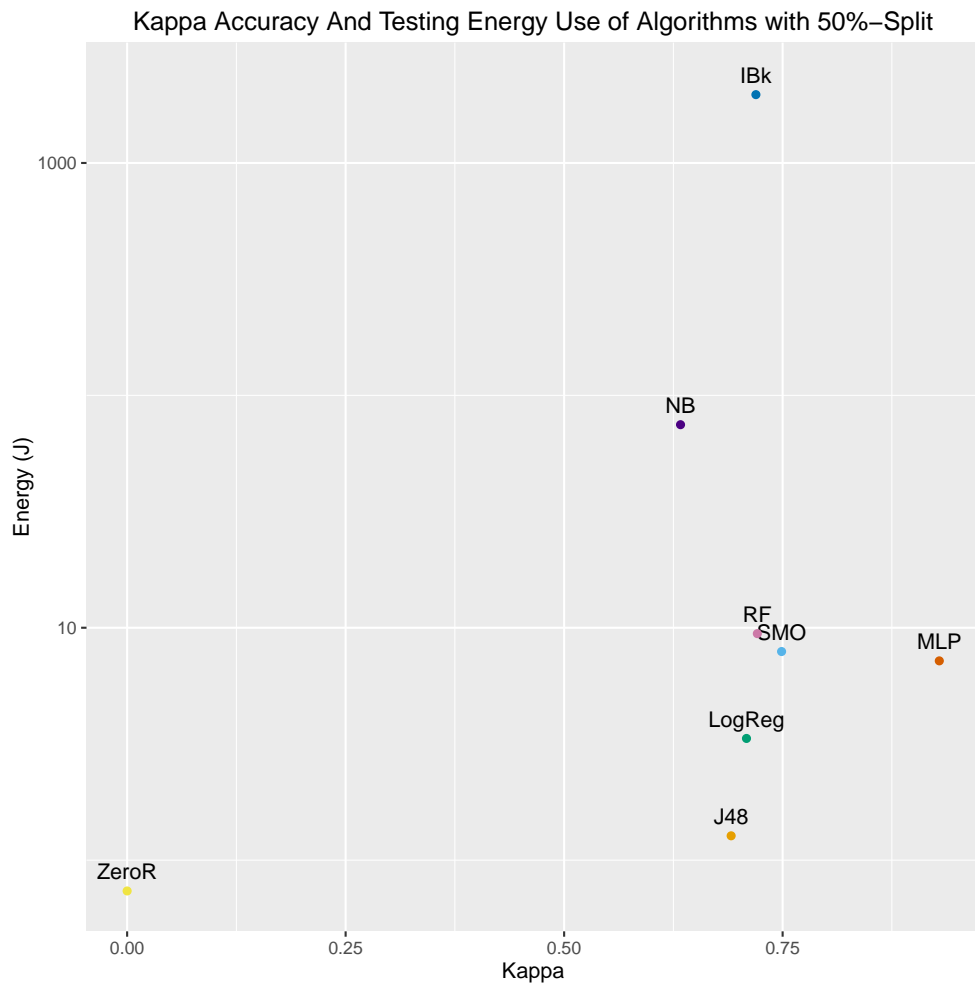


Figure 7. Scatterplot of energy consumption during classification (not training) versus Kappa.