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# The evolution of logic circuits for the purpose of protein contact map prediction

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Predicting protein structure from sequence remains a major open problem in protein biochemistry. One component of predicting complete structures is the prediction of interresidue contact patterns (contact maps). Here, we discuss protein contact map prediction by machine learning. We describe a novel method for contact map prediction that uses the evolution of logic circuits. These logic circuits operate on feature data and output whether or not two amino acids in a protein are in contact or not. We show that such a method is feasible, and in addition that evolution allows the logic circuits to be trained on the dataset in an unbiased manner so that it can be used in both contact map prediction and the selection of relevant features in a dataset.

# The evolution of logic circuits for the purpose of protein contact map prediction

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# 10 ABSTRACT

Predicting protein structure from sequence remains a major open problem in protein biochemistry. One component of predicting complete structures is the prediction of inter-residue contact patterns (contact)

maps). Here, we discuss protein contact map prediction by machine learning. We describe a novel

14 method for contact map prediction that uses the evolution of logic circuits. These logic circuits operate

- 15 on feature data and output whether or not two amino acids in a protein are in contact or not. We show
- that such a method is feasible, and in addition that evolution allows the logic circuits to be trained on the
- dataset in an unbiased manner so that it can be used in both contact map prediction and the selection of

<sup>18</sup> relevant features in a dataset.

<sup>19</sup> Keywords: Protein Structure Prediction, Evolutionary Computation, Machine Learning

# 20 INTRODUCTION

Proteins are important biological molecules that perform many functions in an organism. These molecules 21 are composed of a string of amino acids comprised of a 20-letter "alphabet" of amino acids. The sequence 22 23 of amino acids is referred to as the primary structure of the protein. Beyond this primary structure, proteins are arranged in a higher-order, three-dimensional secondary structure composed of motifs such 24 as alpha-helices and beta sheets. This secondary structure in turn is arranged into a tertiary structure that 25 forms protein domains, which in turn can form a quaternary structure that is composed of multiple protein 26 domains (McNaught and Wilkinson, 1997). To a large extent, the two-dimensional and three-dimensional 27 structure of a protein is determined by its amino acid sequence. For example, two cysteine amino acids 28 can form a disulfide bond even if they are separated by a large distance in terms of the sequence (have 29 a large sequence separation) (Sevier and Kaiser, 2002). Protein structure in turn greatly influences the 30 function of a protein. 31 However, it is still fairly time-consuming and expensive to acquire an accurate structure of a protein. 32 Current experimental methods include crystallizing a protein and performing nuclear magnetic resonance 33 (NMR) imaging (Wuthrich, 1986) or X-ray crystallography (Drenth, 2007). The number of structures 34 that have been determined in these manners is still quite small—on the order of 100,000 as shown in 35 the latest release of the Protein Data Bank (Kouranov et al., 2006) from 2016. This is in contrast to the 36 number of proteins whose primary amino acid sequences have been determined, which is in the tens of 37 millions according to the latest release of RefSeq (Pruitt et al., 2007) from 2016. Thus, it is desirable to 38

<sup>39</sup> find faster and cheaper methods for protein structure determination from sequence. One approach is to use <sup>40</sup> computational and machine learning methods to predict protein structure based on available information.

- <sup>41</sup> These methods are collectively referred to in this paper as protein structure prediction (PSP).
- The benefits of using computational methods in PSP are numerous. In addition to providing a less
- 43 costly and faster method for structural prediction and determination, such methods can also guide and
- <sup>44</sup> confirm experimental research. Furthermore, structural prediction can help in understanding evolutionary
- relationships among organisms (Corbett and Berger, 2004) (Yoshikawa and Ogasawara, 1991); aiding in

the development of new drugs (Gaulton et al., 2012) (Koch and Waldmann, 2005); and the production of
synthetic proteins (Ho et al., 2001).

Computational methods used in protein structure prediction are quite diverse. These include clustering
 methods (Bolten et al., 2001); neural networks (Rost and Sander, 1994); support vector machines (Cheng
 and Baldi, 2007); and template methods (Zhang, 2007). Other examples include those using deep

and Baldi, 2007); and template methods (Zhang, 2007). Other examples include those using deep learning (Lena et al., 2012), which has recently become popular and used in many applications such as

<sup>52</sup> image recognition (Ciresan et al., 2012). Computational metopds also predict different aspects of structure,

including the exact 3D coordinates of the atoms (as in NMR and X-ray crystallography mentioned above),
 the secondary structures of the amino acids (Rost and Sander, 1994), and protein bond angles (Laskowski

et al., 1993). There also exist *de novo* or *ab initio* methods, such as ROSETTA (Simons et al., 1999) and

<sup>56</sup> QUARK (Xu and Zhang, 2012), which use only the amino acid sequence to predict protein structure (Baker <sup>57</sup> and Sali, 2001).

Another type of structural determination is the amino acid "contact map", which we discuss in this paper (Cheng and Baldi, 2007; Lena et al., 2012). A contact map is the list of amino acids that are in proximity to each other below a distance threshold. Computational methods used to elucidate contact maps have included support vector machines (Cheng and Baldi, 2007), deep learning (Lena et al., 2012), integer programming (Wang and Xu, 2013), and cascading neural networks (Ding et al., 2013).

In the standard approach to contact map prediction (CMP) by machine learning, the methods are 63 trained on a set of training examples, and after the training periods are tested on a set of unknown testing 64 examples. The training and testing data can encompass any kind of information and class label. For 65 example, in protein contact map prediction, a typical example would be a particular pair of amino acids 66 in a protein. This pair would have many characteristics associated with it (features such as amino acid 67 identity, protein length, and so on), with an accompanying class label (in contact or not in contact) (Cheng 68 and Baldi, 2007). The scoring need not be based on class label prediction; for example, in cases 69 where atomic coordinates are predicted, scoring can be based on the predicted distance from the true 70 coordinates (Cozzetto et al., 2009). 71

One popular type of machine learning is the use of evolutionary computation (EC), which has also 72 been applied to PSP (Pedersen and Moult, 1996). Broadly speaking, this class of machine learning evolves 73 a population of individuals *in silico* that each represent a candidate solution to the problem at hand. The 74 best-performing individuals (*i.e.*, those with the highest score according to a given *fitness function*) tend to 75 perpetuate in the evolutionary process, improving the performance of the method (Back et al., 1997). This 76 class of methods has been used in many applications and takes many forms, in areas as diverse as medical 77 imaging (Baluja and Simon, 1998), data mining (Alcala-Fdez et al., 2009), signal processing (Fogel, 78 2000), and artificial life (Adami, 1998; Ray and Hart, 1999; Ofria and Wilke, 2004). 79

In an evolutionary computation program, the representation of an individual-that is, the digital encoding of the individual-can be varied. These can include tree structures (Cramer, 1985), strings of digits (Edlund et al., 2011), and even software code itself (Ofria and Wilke, 2004). The encoding of these individuals must then be translated into a solution for the problem at hand; for example, in the work of Ofria *et al.*, the digital organisms composed of computer code are scored based on the complexity of logical operations they perform (Adami, 1998; Ofria and Wilke, 2004).

A particular representation of candidate solutions in evolutionary computation is known as a Markov 86 network (MN). Markov networks are a way of relating mathematical variables to one another. These 87 relations are probabilistic; when the probabilities are either 0.0 or 1.0, they are said to be deterministic. 88 The variables in Markov networks can be arranged such that they are essentially digital logic circuits 89 with deterministic probabilities. That is, they are composed of logic gates that accept binary inputs (0 90 or 1) and produce binary outputs. Markov networks have in recent years become a tool in areas such as 91 the navigational control (Edlund et al., 2011), active categorical perception (Marstaller et al., 2013) and 92 machine learning in image recognitionChapman et al. (2013). 93

This paper examines the use of evolving, deterministic Markov networks toward the problem of contact map prediction. In this work, we evolve Markov networks on a training set comprised of pairs of amino acids, and at the end of the evolution test the best networks on a testing set. The class labels of the examples are whether or not the pairs are in contact or not in contact, and the examples have a mixture of 688 binary and decimal features that describe them. The training and testing data are each comprised of several hundred thousand examples containing both negative and positive contacts. The dataset used is

taken from SVMcon, a paper that uses support vector machines for protein contact map prediction (Cheng

Inputs	Outputs
a b	c d
11	0 1
01	0 0
10	11
0 0	01

**Table 1.** The characteristic logic table for a deterministic gate with two inputs and two outputs.

and Baldi, 2007). In our work, the features are used as inputs to the MNs (logic circuits), and the outputs are the class labels. Our results show that evolving logic circuits to predict protein contact maps is a viable alterinative. To our knowledge, this is the first time that Markov networks have been used in machine learning on a bioinformatics problem. Thus, it is a feasible avenue for study and has the possibility of being quite useful for this problem. Of course, as there is continual improvement in the fields of evolutionary computation and Markov networks, this study should not be seen as representing the "last word" on the capacity of this method to tackle this problem.

Although contact map prediction has improved over the years, there are still a number of challenges remaining. For example, it is unlikely that the entire feature set is useful for classification, a fact mentioned in the SVMcon paper (Cheng and Baldi, 2007). Indeed, it is extremely difficult to know beforehand whether a subset of features performs better on the task, and it may be that the only way to determine this for sure is to manually take out features and re-run the method, an approach that is impractical. In addition, if it is true that a subset of features may be better than a full set, then it follows that it is difficult to know if the addition of more features may help to solve the problem.

115 Evolutionary computation has a number of benefits and addresses some of the concerns outlined above. For example, once the appropriate fitness function has been selected (along with the evolutionary 116 parameters such as mutation rate and number of individuals in the population) the program attempts to 117 evolve a most-fit individual according to the fitness function and fitness landscape. There is no "correct" 118 information that the EC system is told to use, but rather only the information that produces the best 119 outcome through evolution. Thus, when combined with Markov networks, an EC system can discover 120 relevant features in an unbiased manner. This is demonstrated by observing which features the Markov 121 networks evolved to use in their structures-if a feature was used, this indicates that it helped in increasing 122 fitness and was therefore important. 123

## 124 MATERIALS AND METHODS

#### 125 Description of Markov Networks and their Evolution

Markov networks (MNs) are a set of probabilistically interacting state variables (Koller and Friedman, 126 2009). The sets of state variables in a Markov networks are often arranged into input state variables, 127 output state variables, and "hidden state" variables that are "inside" the network and can serve as memory 128 and can be used for processing. This arrangement can be used to represent many processes, such as 129 robotic controllers (Edlund et al., 2011) (e.g. with sensory inputs and movement outputs) or in image 130 classification (Chapman et al., 2013) (e.g. pixels as inputs and image classes as ouptuts). In this work, the 131 tables that determine the network updates are deterministic rather than probabilisitic, so that the Markov 132 networks represent regular logic circuits. 133

An example of a 2-input, 2-output gate is shown in Table 1. Here, a and b represent the binary inputs and c and d represent the binary outputs.

The Markov networks (logic circuits) are created through an evolutionary process. Therefore, the networks themselves must be encoded symbolically into a "genome." This is accomplished by representing the MNs as a string of integers (bytes), the length of which can be arbitrary but is limited to 40,000 integers in our work. The genome of an individual MN is comprised of a set of "genes," which each specify one logic gate. Each gene that represents a logic gate begins with an integer that denotes the start of the gene, and the gene itself specifies where the specific inputs and outputs are located, as well as the logic of the gate. This information is sufficient to describe the entire Markov network. Any other characteristics of the candidate solutions, such as the maximum genome size, the rates of mutation, or the
 number of inputs and outputs to a gate, is specified in a configuration file.

The evolution of the Markov networks in our study follows simple evolutionary operators that act on the genome of an individual. Evolutionary operators that can act upon the genes include point mutation (which change a single byte) or gene duplication and deletion, which duplicate or delete an entire gene, respectively. The rates of each of these are specified in the configuration file. In our work, if two or more genes write into the same output, the the final output is OR'd together. More details of the general makeup

<sup>150</sup> of Markov networks are provided in the Supplementary Information of Edlund *et al.* (Edlund et al., 2011).

#### 151 Dataset Description

Our work centers on protein structure prediction (PSP); specifically, we investigate how protein feature 152 data can be used to predict the amino acid contact map. In order to do this, a dataset of protein sequences 153 and protein sequence features must be prepared. We choose to use the feature dataset provided in Cheng 154 and Baldi (Cheng and Baldi, 2007). That paper described the creation of a contact map predictor based on 155 support vector machines, SVMcon. Their dataset included several hundred proteins divided into a training 156 dataset used to train the SVM (485 proteins) and a testing dataset (48 proteins). Each protein was used 157 158 to provide a large number of amino acid contact examples based on the many possible amino acid pairs. The sequence separation threshold for pairs was six or greater, and the threshold for contact was eight 159 Angstroms or greater. 160

Each pair of amino acids in the training or testing set represented a possible contact pair, *i.e.*, each 161 pair was either in contact or not in contact. The training dataset contained 267,702 contact pairs, reduced 162 from a set of several million. This reduction was done in order to make the dataset more tractable and 163 also to increase the proportion of positive contacts; the final training dataset had 94,110 positive contacts, 164 a proportion of roughly one-third. The reason the proportion of positive contacts was increased in the 165 training dataset was to train the SVM to better recognize these examples. The testing dataset, composed 166 of 377,797 examples, used the full proportion of contact examples and contained 10,498 positive contacts. 167 Each training and testing example had 688 features associated with it. These features included many 168 types of data related to the sequences, such as mutual information, length of sequences, and secondary 169 structure, to name a few. There were 145 binary features (0 or 1) and 543 decimal features (capable 170 of being any number). Many of these features were based on a sequence alignment of the proteins, 171 which allowed all sequences to be compared according to a standardized length. The majority of features 172 were based on sliding windows centered around the amino acids in each pair and a window centered 173 halfway between the amino acids. There were nine window positions each for each amino acid in the pair 174 (including the amino acid in question) and five positions for the central segment. For each of these 23 175 positions, there were 27 features giving the entropy (one feature), secondary structure (three features), 176 solvent accessibility (two features) and the amino acid profiles for those positions (21 features). Thus, 177 the window features comprised 23 \* 27 = 621 out of 688 features. It should be noted that out of the 688 178 features, only those features associated with secondary structure and solvent accessibility could not be 179 calculated precisely from the sequence along. Secondary structure and solvent accessibility were predicted 180 using other software (Cheng et al., 2005). A more-detailed description of the dataset and features used 181 can be found in the SVMcon paper (Cheng and Baldi, 2007). 182

#### 183 Data Encoding

Markov networks take binary input. Since many of the features are continuous, it is necessary to develop
 an input encoding that maps to the features. There are several methods that were tried.

The methods that were tried were based on splitting continuous features into a set number of bins. For each type of encoding, a "split" value was given. Each continuous feature was divided into a split value of bins based on the complete range of that particular feature (in the training set). For example, if using a split of 10, and with a feature with a range from 0.0 to 2.0, the first bin would be from [0.0-0.2) the second from [0.2-0.4), and so on. If the testing set had a range that was out of bounds of the training set, the lowest and/or highest bin was used.

The methods that were tried were based on splitting continuous features into a set number of bins. For each type of encoding, a split number was given (in our case, there were three splits used—4, 10, or 16). Each continuous feature was divided into a split number of bins based on the complete range of that particular feature (in the training set). For example, if using a split of 10, and with a feature with a range from 0.0 to 2.0, the first bin would be from [0.0-0.20] the second from (0.2-0.4], and so on. If the testing set had a range that was out of bounds of the training set, the lowest and/or highest bin from the
training set was used. In order to make all feature representations equal, each binary feature had the same
number of inputs as a continuous feature; for example, if the split was 4, then each binary input used 10
bits, which were either all 0's or all 1's.

Two additional types of encoding were based on the fact that even-numbered splits can be expressed 201 in terms of base 2. For example, a split of 4 bins could be compressed into 2 bits by using the binary 202 values 11, 10, 01, and 00, and a split of 16 bins could be compressed into 4 bits along the same principle. 203 These two binary splits used were: First, a split of 16 across four bits, and a split of four across two bits. 204 We chose these five particular splits for a number of reasons. Based on the general layout of the data, 205 we decided that the lowest split should be 4 as anything less would be too granular on feature data that 206 tended to have at least 4, and often more, distinct values. Second, the highest split of 16 was chosen as a 207 reasonable upper limit, and 10 was chosen as the midpoint between the lowest and highest splits. There is 208 no theory suggesting which split to use, but in practice Markov networks can sometimes have difficulty 209 evolving to find the correct inputs if there are too many of them, which slows down the clock time of the 210 simulation itself (Chapman et al., 2013). The number of inputs for the split of 4 was 4\*688 = 2752, the 211 number for the split of 10 was 10\*688 = 6880, and the number for the split of 16 was 16\*11008. Due to 212 time limitations, it was impossible to perform an exhaustive parameter sweep of all the splits, even from 2 213 to 16. 214

#### 215 Evolution of Markov Networks on the Dataset

The training (evolution) of the Markov networks is achieved by the following steps. We first create an 216 initial population of random networks. We then evolve these networks over a number of updates on a 217 subset of the training dataset. In our case, we ran the evolution over 100,000 updates. For every 25,000 218 updates, we evolved the networks on a different set of 50,000 training examples. The sets of training 219 examples were separate; thus, there used a total of 200,000 training examples. We used different sets of 220 training examples for two reasons. First, it forced the Markov networks to evolve on different examples 221 over time instead of focusing only on one dataset. Second, because of time limitations, it was not possible 222 to evolve the networks on a greater number of examples. 223

During the runs, the networks "learn" (through evolution) to differentiate between positive and 224 negative contacts based on their features. In each update, the networks are tested on the training set and 225 a fitness is assigned to them according to a fitness function. Individuals with the highest fitness tend to 226 survive in the population and reproduce; these "children" undergo mutation, and in the process, may do 227 better than their parents at recognizing contacts. Mutation can affect almost any part of the networks, 228 including the number of features used as input, the number of gates, and the gate logic. In the end, there 229 are two binary outputs provided: an output for a negative contact decision, and one for a positive contact 230 decision. Note that it is possible for a Markov network to give both answers, signifying both a positive 231 and negative contact decision, but in practice, this does not happen very often. 232

In our work, we have tried a number of fitness functions, and so far accuracy has proven to be the 233 best in terms of the final scoring method, described below. Accuracy is defined as TP + TN / P + N, 234 where TP is the number of true positive (correctly-predicted) guesses and TN is the number of true 235 negative (correctly-predicted) guesses in the dataset. Here, accuracy is calculated separately for both 236 positive contacts and negative contacts. Also, a reward for output alone is also included for each accuracy 237 to encourage "empty" networks to evolve to produce outputs. The vector magnitude of these results 238 is combined as shown in Equation (1), and therefore the maximum fitness is the square root of 8.0. 239 Calculating the square root is done in order to "smooth" the resulting fitness values. At each update, 240 every newly-produced individual MN that has not been tested on the training set is tested according to the 241 fitness function. 242

$$f = \sqrt{(\operatorname{acc}_{\operatorname{pos}} + \operatorname{out}_{\operatorname{pos}})^2 + (\operatorname{acc}_{\operatorname{neg}} + \operatorname{out}_{\operatorname{neg}})^2},\tag{1}$$

At the end of an evolutionary run, the best MN in a population is tested on the testing set, which it has not seen before, and performance is assessed according to specificity, sensitivity, and Fmax. Specificity is the number of correctly-predicted positive contacts divided by the number of total predicted positive contacts. Sensitivity is the number of correctly-predicted positive contacts over the total number of positive contacts. Because it is easy to get a specificity of 1.0 by simply giving one very good guess, and

Parameter	Value
Updates	100,000
Population size	500
Starting gates	100
Inputs per gate	4
Outputs per gate	4
Gene duplication rate per update	0.05
Gene deletion rate per update	0.05
Site mutation rate per update	0.001

**Table 2.** Parameters for the evolutionary algorithm.

a sensitivity of 1.0 by simply guessing all contacts to be positive, Fmax is also used, which combines the
 two measures and is shown in Equation (2). The maximum Fmax possible is 0.5.

$$Fmax = \frac{specificity * sensitivity}{specificity + sensitivity},$$
(2)

Note that negative contacts are not considered in the three performance measures (even though they
 are used in the fitness function), since positive contacts are of more interest and more difficult to determine
 in contact map prediction. Finally, even though Fmax is used as the scoring measure, we deermined that
 it was inferior to accuracy as a fitness function.

In order to achieve better performance, committees of MNs are assembled from the highest-fitness individuals from each of the 60 evolutionary runs. These 60 MNs are tested on the testing set, and for each testing example, the sum of all 60 negative contact answers is compared to the sum of all 60 positive contact answers. The final answer is the answer with the highest number of votes (ties are broken randomly).

<sup>259</sup> The list of parameters for the evolutionary runs is given in Table 2.

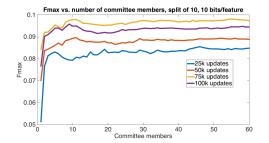
#### 260 **RESULTS**

#### 261 Performance on the Dataset

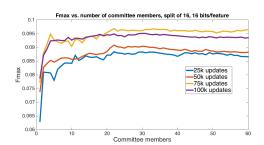
Markov networks were evolved using five different input data encodings (treatments), described in the 262 Methods section. For each encoding, 60 different populations were run and the best individuals from each 263 population (according to the fitness function) were tested on each example from the testing set and their 264 answers combined. The evolution continued for 100k updates, and at intervals of 25k updates, results 265 on the test set for committee sizes up to 60 were recorded. Figures 2, 3, 4, and 5 show the results for 266 the treatments that used splits of 4 with 4 bits per feature, splits of 16 with 16 bits per feature, splits of 4 267 with 2 bits per feature, and splits of 16 with 4 bits per feature, respectively. Even though the treatments 268 ended at 100k updates, the best results for all treatments were from 75k updates; this is probably due 269 to overfitting of the Markov networks to the training set in their evolution. Also, the improvement in 270 performance of each treatment at the four update intervals tended to level out after around 20 committee 271 members and does not tend to improve with more. This is an indication that increasing the number of 272 committee members would not help the performance for this treatment. 273

Figure 6 shows the Fmax results at 75k updates for all treatments. It is interesting to note that the two best treatments were the two that compressed the number of bits per feature according to a base-2 compression: the treatment that used a split of 16 with 4 bits/feature had a final Fmax of 0.103 and the one with a split of 4 with 2 bits/feature had a final Fmax of 0.102. The splits of 10 with 10 bits per feature, 16 with 16 bits per feature, and 4 with 4 bits per feature had Fmax results of 0.098, 0.097, and 0.097, respectively.

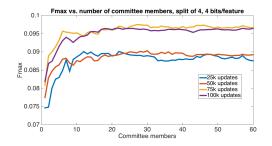
All of the treatments did significantly better than random. Under random guessing that guessed 50 percent of the examples to be positive contacts, the Fmax would be 0.026. Under random guessing that used the proportion of positive contacts from the training set (35.155 percent), the Fmax would also be 0.026.



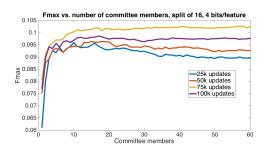
**Figure 1.** Results for the split of 10 with 10 bits per feature (6880 total bits). The highest Fmax at 60 committee members is at 75k, with an Fmax of 0.098.



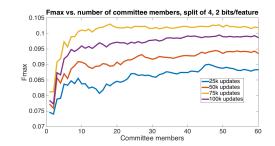
**Figure 2.** Results for the split of 16 with 16 bits per feature (11008 total bits). The highest Fmax at 60 committee members is at 75k, with an Fmax of 0.097.



**Figure 3.** Results for the split of 4 with 4 bits per feature (2752 total bits). The highest Fmax at 60 committee members is at 75k, with an Fmax of 0.097.

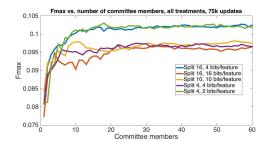


**Figure 4.** Results for the split of 16 with 4 bits per feature (2752 total bits). The highest Fmax at 60 committee members is at 75k, with an Fmax of 0.102.



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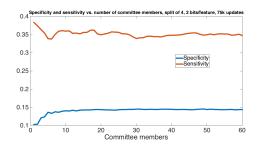
**Figure 5.** Results for the split of 4 with 2 bits per feature (1376 total bits). The highest Fmax at 60 committee members is at 75k, with an Fmax of 0.102.



**Figure 6.** Results at 75k updates for all five split treatments. The highest Fmax is achieved by the split of 16, 4 bits per feature encoding, with an Fmax of 0.103.

We now take a detailed look at the treatment that used a split of 4 with 2 bits/feature. This treatment was chosen for two reasons. First, its Fmax performance is very close to the best (Fmax of 0.102 vs. Fmax of 0.103 obtained by the encoding using a split of 16 with 4 bits/feature); second, it is the simplest type of encoding, using only 2 bits/feature, making it simpler to analyze and describe. Figure 7 shows the specificity and sensitivity values over the committee sizes at 75k updates for the split of 4 with 2 bits per feature treatment. The specificity at 60 committee members was 0.14, and the sensitivity was 0.35. As one can see, even if sensitivity goes down, specificity can go up, leading to a higher Fmax value.

We also comapre our results from the split 4, 2 bits/feature encoding to the results from the SVMcon 291 paper by Cheng et al. (Cheng and Baldi, 2007). Table 3 gives the total specificity and sensitivity values 292 on the testing set for Markov networks and SVMcon across several sequence separations (values under 293 the separation of  $\geq =6$  are for every testing example since that is the smallest separation possible). As 294 one can see, at all sequence separations, SVMcon has a higher specificity, but SVMcon has a higher 295 296 sensitivity. Table 4 shows the Fmax results on the testing set across the six SCOP protein classes covered by the testing set and three sequence separation thresholds. Unfortunately, Markov networks do not do as 297 well as SVMcon. It is clear that this is because SVMcon does better in terms of specificity; therefore, if 298 Markov networks could be made to be more conservative in their guesses, they might achieve a higher 299 overall specificity without sacrificing sensitivity. 300



**Figure 7.** Specificity and sensitivity results at 75k updates for the split of 4 with 2 bits per feature treatment. Specificity at 60 committee members was 0.14, and sensitivity was 0.35.

Method	Separation >=6		<b>Separation</b> >=12		Separation >=24	
	Spec.	Sens.	Spec.	Sens.	Spec.	Sens.
Markov networks	0.144	0.347	0.132	0.280	0.109	0.209
SVMcon	0.37	0.21	0.30	0.20	0.21	0.19

**Table 3.** Average specificity and sensitivity of Markov networks and SVMcon across different sequence separations.

**Table 4.** Fmax comparisons between MN—SVMcon of different SCOP protein classes and sequence separations.

SCOP class	Number	Fmax, separation >=6		Fmax, separation >=12		Fmax, separation >=24	
		MN	SVMcon	MN	SVMcon	MN	SVMcon
alpha	11	0.076	0.12	0.012	0.087	0.009	0.050
beta	10	0.102	0.117	0.093	0.111	0.069	0.096
alpha+beta	15	0.109	0.161	0.094	0.146	0.070	0.110
alpha/beta	7	0.105	0.126	0.103	0.121	0.097	0.117
small	4	0.089	0.120	0.051	0.113	0.021	0.063
coil-coil	1	0.063	0.142	0.023	0.025	N/A	N/A
all	48	0.102	0.134	0.090	0.120	0.072	0.010

#### 301 Network Recognition of Features

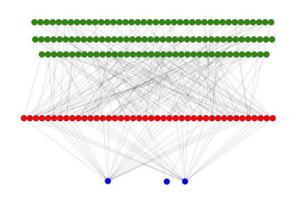
In an evolutionary run, the Markov networks evolve to use certain input bits (and therefore features) to 302 make their decisions; that is, they evolve to recognize the subset of input bits that give them the best 303 answer ("salient" bits). Figure 8 shows a typical network with its output from the treatment that used a 304 split of 4 with 2 bits/feature, at 75,000 updates. Each green circle is an input used by the network, with 305 the red circles representing gates and the blue circles outputs. Because this figure is illustrative, the inputs 306 and gates are unordered. There are several things to notice in this figure. First, even though there are 307 1,376 possible bits that the network could use, it only connects to 118 in this example. Second, in this 308 network it is common for gates to have connections to multiple input nodes and for outputs to have many 309 gate inputs-the networks are quite complex. Third, there are three outputs. Our system allows up to two 310 outputs to evolve for each class label, so that one output in a pair can serve as a "veto" output to prevent 311 too many "yes" outputs. Here, the positive contact label (on the right) evolved two outputs. 312

Because of the nature of the evolutionary process, the networks can select the best features in an unbiased manner. Figure 9 demonstrates how networks focus on some features rather than others. In this histogram, taken from the results from the encoding that uses a split of 4 with 2 bits/feature at 75k updates, we plot the frequency distribution of features used over the networks that use them, by assuming that a feature is "recognized" if there is at least one network that reads from one of the bits for that feature.

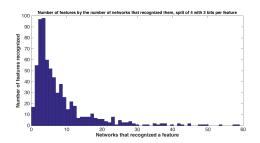
We see that most features are recognized by only a few networks—for example, nearly a hundred features are recognized by only 3 networks, with nearly another hundred recognized by only 4 networks. However, less than 20 features are recognized by no networks. This may be due to networks randomly evolving to recognize a feature before losing that recognition in the evolutionary process, such that it would be very difficult for no networks to recognize a feature. Also, no features are recognized by *all* 60 networks, although there are a few that come close.

Table 5 gives information on the general statistics of the networks according to how many features they recognized. As shown in this table, the average and median tend to be quite similar when examining the number of bits recognized by the networks and the number of features. In addition, even though the maximum number of possible bits used is twice that of the number of features used, this number is not very much higher than the number of features used. In fact, overall, the average number of features used (90.0) is quite small compared to the maximum of 688 and is approximately 13 percent.

It is desirable to examine more closely which features the Markov networks select, because it stands to



**Figure 8.** A sample network diagram taken from the treatment of a split of 4 with 2 bits/feature at 75k updates. Out of a possible 1376 bits, the network has evolved to recognize only 118 of these. Inputs bits are green, gates are red, and outputs are blue. The inputs and gates are unordered. Note that a pair of outputs has evolved to represent a positive contact answer (the maximum is two), but that the negative contact answer evolved only one.



**Figure 9.** A histogram showing how many features are recognized by each number of networks (encoding split of 4 with 2 bits/feature). A network only has to have input from one bit of a feature to recognize it.

**Table 5.** Feature recognition values of the networks from the encoding of split 4 with 2 bits/feature. For a network to recognize a feature, it only has to connect to one bit for that feature.

Statistic	Networks
Average bits recognized	97.6
Median bits recognized	98.0
Average features recognized	90.0
Median features recognized	90.5

Feature	Networks
Contact pair sequence separation $>=50$	59
C-terminus amino acid window position 5,	58
sheet secondary structure	
N-terminus amino acid window position 5,	54
sheet secondary structure	
Amino acid central segment window position	50
4, coil secondary structure	
Amino acid central segment window position	49
4, sheet secondary structure	
Contact pair sequence separation <=49	48
Amino acid central segment window position	45
5, coil secondary structure	
N-terminus amino acid window position 5,	45
exposed solvent accessibility	
Amino acid central segment window position	43
5, sheet secondary structure	
Contact pair sequence separation of 6	42
N-terminus amino acid window position 5,	42
buried solvent accessibility	
C-terminus amino acid window position 5,	40
buried solvent accessibility	

**Table 6.** The features most recognized by the Markov networks.

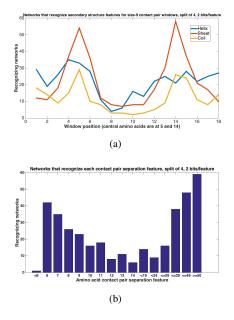
reason that these salient are important in general for the task of contact map determination. Table 6 gives a list of the top 12 features in the treatment according to the number of networks that recognized them. It is clear from this table that secondary structure and solvent accessibility features are very important to the Markov network decisions, and presumably to determination of contact map prediction in general. The importance of contact pair sequence separation to the networks, specifically a separation of 6 and a separation of >=50, seems to suggest that the networks use the extremes of distance as a way to help with classification.

Figure 10(a) demonstrates feature usage related to secondary structure features. Each pair of amino 338 acids in a training or testing sample is situated in a sliding window of size 9, giving a total number of 18 339 positions. There are a number of features at each of these positions, including the secondary structures. At 340 each of these window positions, the figure shows the number of networks (out of the 60) that evolved to 341 recognize the three kinds of secondary structure after 75,000 updates. We also see that the most common 342 type of secondary structure recognized by the MNs is sheet. Further, the MNs focus on recognizing 343 secondary structures that are closer to the central amino acids. Interestingly, even though the number of 344 networks for each kind of secondary structure decreases as the window positions move away from the 345 center, the number of networks for the "outside" positions for each window is greater for both helix and 346 coil. It is also clear that the peaks in the centers and outsides of the windows are high in absolute terms as 347 well; most features in the dataset are not recognized by many networks. 348

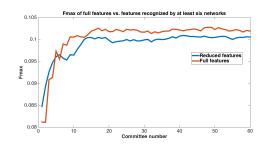
Similarly, Figure 10(b) shows from the same treatment how many networks out of 60 evolve to recognize each feature that describes the sequence separation between the amino acid pair. There is a clear focus on sequence separations that are either very small or very large. One can see that, at least in relation to this dataset, the Markov networks are recognizing that certain pair separations are more useful than others.

It is clear from these figures that a number of secondary structure and sequence separation features are important to the networks. Indeed, 9 out of the top 10 features in terms of networks that recognized them deal with either secondary structure or sequence separation (the tenth deals with solvent accessibility).

As mentioned before, since MNs will tend to evolve to recognize features that benefit them, they will usually only recognize a small subset of the total features. To further demonstrate that the features chosen



**Figure 10.** (a): Number of networks out of the 60 that evolved to recognize each kind of secondary structure along the two size-9 sliding windows. Encoding was split of 4, 2 bits/feature. (b): Number of networks out of the 60 that evolved to recognize the amino acid pair separation features. Encoding was split of 4, 2 bits/feature. Each tick shown is a different contact separation feature.



**Figure 11.** Fmax of the original split-4, 2 bits per feature encoding with all features, and the same kind of run with the reduced feature set that only used features recognized by at least 6 of the networks from the first run.

by the MNs are useful, other evolutionary runs were performed that had as input only the most-used 359 features in the original runs. To this end, the 60 networks from the encoding that used a split of 4 with 2 360 bits per feature were examined after a run of 75,000 updates to see which features they recognized. The 361 training and testing datasets were changed to contain only features that were recognized by at least 6 of 362 the networks, and a new evolutionary run with the same parameters was performed on this reduced-feature 363 dataset. The number of features in this new run was 309, or roughly 45 percent of the original number 364 of features. Figure 11 shows the Fmax results of this new run compared to the original run. Although 365 the Fmax results of the new run are smaller, this difference is quite small, indicating that the Markov 366 networks have discovered what the salient features for solving the problem. Also, it demonstrates that 367 searching for the right features via trial and error is perhaps not necessary; simply picking the features 368 that the most networks recognize is suitable for finding the best features. 369

This figure demonstrates two things. First, many features that were chosen for the dataset were unnecessary to obtain the same level of performance. In addition, the Markov networks successfully evolved to discover which features were useful in contact map prediction.

It is worth noting that many of the 688 features that were not used in the reduced feature set were features that described the amino acid percentages that were based on a sequence alignment of the proteins. Considering the two size 9 windows and the size 5 central segment window, and the fact that

proteins. Considering the two size-9 windows and the size-5 central segment window, and the fact that

the amino acids were the 20 canonical amino acids plus a gap, there were 23\*21 = 483 total features in 376 the dataset based on amino acid percentages alone. Yet only 164 of these (34 percent) were used in the 377 reduced-feature dataset, as opposed to 145 of the remaining 205 features (71 percent of the remaining). 378 Some notable observations included the fact that all but one (22 out of 23) of the gap amino acid features 379 qualified. This could be due to the importance of gap additions in sequence alignments. In addition, most 380 of the central segment window amino acid features were salient-88 out of 104, or 85 percent-and often 381 had a relatively high number of networks that recognized them. 382 The salient features of the size-9 windows around the contact pairs were not as numerous (76 out 383

of 378 features, or 20 percent) and tended to have relatively low numbers of networks that recognized them. An interesting exception was the feature for cysteine in the fifth position (central position) for the C-terminus window. A total of 19 networks recognized this feature. Because cysteine is so important to protein structure, this is not surprising, and the cysteine feature in the center of the N-terminus window was recognized by 8 networks as well.

# 389 **DISCUSSION**

As demonstrated in our results, the performance of the evolution of Markov networks depends mainly on 390 two things: First, the fitness function used, and second, the encoding of the dataset. For example, with 391 respect to encoding, the two treatments that performed the best were the two that used the reduced-bit 392 binary encodings. It is hypothesized that one reason that these two treatments did better than the other 393 three is that there were fewer bits for the MNs to evolve to choose, but also that condensing bits would 394 "force" the MNs to evolve over all bits for a continuous feature due to the nature of the binary encodings. 395 Also, with respect to fitness functions, the best found so far has been accuracy. This is perhaps 396 due to the fact that accuracy is such a simple fitness function-it is simply the proportion of correct 397 guesses (true negative true positive) in the dataset and does not require a complex formula. Furthermore, 398 while other fitness functions such as Fmax measure, specificity/sensitivity, or Matthews correlation 399 coefficient (Matthews, 1975) have been tried and have not performed as well as accuracy, there is 400 the intriguing idea that a "committee of committees" could be used based on a combination of the 401 answers from runs of several fitness functions. Furthermore, it has been noted that a different fitness 402 function/encoding combination might produce better results; in addition, a different type of evolutionary 403 algorithm (such as NSGA2 (Deb et al., 2002)) or different evolutionary parameters, such as the type of 404 population replacement (in our case, we used tournament selection) (Blickle and Thiele, 1996) could 405 possibly foster a more-productive fitness landscape and therefore performance. In particular, Markov 406 networks, at least compared to the SVM con results, were not very conservative in their answers, and thus 407 had a higher sensitivity (and lower specificity). If it could be determined why the networks had trouble in 408 this regard, it might be possible to improve their performance by tuning the factors mentioned above. The 409 open-ended nature of evolutionary computation is both a blessing and a curse. The usage and theory of 410 evolutionary computation is continuously being worked on and improved by many researchers, allowing 411 for the possibility of a great increase in performance of this method. However, it is always unknown 412 which specific fitness function and other parameters to use, and thus there is still an element of trial and 413 error. 414

One of the primary strengths of the evolution of Markov networks is that the evolution proceeds in 415 an unbiased manner. Thus, as demonstrated in the results section, networks evolve to recognize some 416 features more than others. This is useful, since it allows one to differentiate some features as being "better" 417 than others according to how many networks evolve to recognize them. Figure 9 shows that there is quite 418 a bit of diversity in terms of which features are recognized as salient, and Table 6 shows how certain 419 groups of related features (e.g., secondary structure and solvent accessibility) are important to 420 the decisions of the networks. Furthermore, Table 5 shows that the networks are fairly parsimonious in 421 their decisions and need only a relatively small fraction of the total bits to make their decisions. Finally, 422 Figure 11 shows that, when considering only the most-used features, they are capable of performing 423 almost as well when using all the features. This parsimonious behavior that focuses on only a few salient 424 features, and which can also identify groups of related features, shows that Markov networks do not 425 necessarily have to grow to an arbitrary and unwieldy complexity in order to achieve improved results, 426 427 even though they are capable of doing so.

# 428 CONCLUSION

We have shown that the evolution of Markov networks is able to produce MNs that are able to make 429 contact map predictions and recognize relevant features from the SVMcon dataset. As far as we know, 430 this is the first time that such a method has been used on a bioinformatics problem. The results show 431 that the method is promising, and may have wider applications. Naturally, because this is the first time 432 such a method has been used in this manner, there is room for improvement. In particular, the Markov 433 networks we evolved tend to overpredict, sacrificing specificity while increasing sensitivity. There are a 434 number of specific ways in which our method could be improved, including using a different evolutionary 435 algorithm, fitness function, MN structure, encoding, or feature space. We could also use our method in 436 conjunction with other methods; for example, if used with other methods, our method and others could 437 form a committee where each receives a voting weight for a contact pair example. One such additional 438 method could include PsiCOV (Jones et al., 2012), which involves finding correlated mutations between a 439 protein containing the contact pairs and a large database of proteins. Other possible additional methods 440 include the LASSO feature selection method (Tibshirani, 1996), and random forests (Liaw and Wiener, 441 2002; Rainforth and Wood, 2015), among others. 442

Furthermore, we have shown that the evolution of Markov networks can, in an unbiased manner, 443 produce networks that recognize relevant (salient), useful features from a dataset. Choosing these salient 444 features could help to remove extraneous features, a task that would otherwise be computationally 445 intensive. This could be especially relevant to a problem that uses many more features (in the thousands 446 or tens of thousands) than ours. Also, one could use this feature information as a prediction tool to guess 447 which kinds of features are useful or not. For example, if it is demonstrated that all features relating to a 448 particular class of amino acid (e.g. polar amino acids) are used by the Markov networks, then it might be 449 desirable to find more features of this type. Furthermore, this offers the possibility that Markov networks 450 could be used as a general-purpose feature detector in other scientific work. 451

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