# The fractal dimension of the tree of life

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#### **Abstract**

The structure pattern of the tree of life clues on key ecological issues; hence knowing the fractal dimension is the fundamental question in understanding the tree of life. Yet the fractal dimension of the tree of life remains unclear since the scale of the tree of life has hypergrown in recent years. Here we show that the tree of life displays a consistent fractal nature for inter- and intra-taxonomic levels, but the fractal dimensions were different among different kingdoms. The fractal dimension of inter-taxonomic levels  $(D_r)$  is 0.873 for the entire tree of life, which smaller than the values of  $D_r$  for Animalia and Plantae but greater than the values of  $D_r$  for Fungi, Chromista, and Protozoa. The hierarchical fractal dimensions values for prokaryotic kingdoms are lower than for other kingdoms. The  $D_r$  value for Viruses was lower than most eukaryotic kingdoms, but greater than prokaryotes. In the entire tree of life, intrataxonomic fractal dimensions  $(D_t)$  for genus are 1.62, for family 1.42, for order 1.56, for class 1.57, and for phylum 1.72. The distribution of taxa size is governed by fractal property but skewed by overdominating taxa with large subtaxa size. The fractal dimensions of accumulating frequency  $(D_{ac})$  could eliminate the skewness effect of taxa with large subtaxa size: for genus  $D_{ac}$  value was 1.41, for family 1.05, for order 1.35, for class 0.67, and for phylum 1.11. The proportion of subtaxa in each taxa with small and large sizes was greater than in taxa with intermediate size. The slope value  $D_a$ -higher proportion of taxa with small subtaxa size when  $D_a > 0$ , and higher proportion of taxa with large subtaxa size when  $D_a$  < 0-related closely to  $D_{ac}$  values, but not  $D_t$  values. This results suggest that the distribution of subtaxa in taxa can be predicted with both fractal dimension and skewness property. Our study determined the fractal dimensions for inter- and intra-taxonomic levels of the present tree of life. These results emphases the need for further theoretical studies, as well as predictive modelling, to interpret the different fractal dimension for different taxonomic groups and skewness of taxa with large subtaxa size.

#### Introduction

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Understanding the pattern of the tree of life has long been a driving force for system biologist. Since the dramatic development in molecular technology, there has been an exponential growth in the number of clades in tree of life each year (Ciccarelli et al., 2006). The end point of the tree of life is the construction of the single phylogenetic tree linking all species living and extinct (Benton and Ayala, 2003). The hierarchical structure of tree of life contains valuable clues on the key issue of realizing the modern diversification of life (Mora et al., 2011; Tittensor et al., 2010), accessing the shape

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of evolution (Doolittle, 2009), determining the threaten of diversity (Mace, Gittleman, and Purvis, 2003), and understanding the underlying mechanisms of constrain ecological complexity (Solow, 2005). Fractal phenomena, which is a mathematical object that has a fractal dimension that usually exceeds its topological dimension and may fall between the integers, are widespread in nature (Brown et al., 2002). The tree of life has long been recognized as a fractal structure, including the diversity of life and taxonomic systems in the tree of life, which have self-similar features that look the same when there is a change in scale (Burlando, 1990, 1993; Chaline, Nottale, and Grou, 1999). Recently released OneZoom visualise the tree of life based on an adaptation of fractal mind (Rosindell and Harmon, 2012).

The fractal property of the tree of life shows a emergent feature that scaling relationship are self-similar

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over a wide range of taxon scales (Rabosky, Slater, and Alfaro, 2012; Lane, 2011; Foote, 2012; Chaline, Nottale, and Grou, 1999; Solow, 2005; Marquet et al., 2005; Burlando, 1990, 1993; Herrada et al., 2008). Powerlaw curve of size-frequency distributions of taxa, derived from a number of checklists and catalogues of species concerning protists, fungi, plants, and animals, pointed out a very large number of taxa with one or few subtaxa and a very small number of taxa with many subtaxa (Mora et al., 2011; Burlando, 1990). The fractal dimension of the taxonomic assemblages represents their diversity characterization, which is viewed as an evolutionary pattern related to scaling evolutionary processes (Villarreal, 2006; Marquet et al., 2005; Bapteste et al., 2009; Foote, 2012). The investigation in the fractal geometry of the taxonomic system from both fossil record and phylogenetic systems indicated that arrangement of life taxonomy generally show fractal properties reflects evolutionary feature (Rabosky, Slater, and Alfaro, 2012). The branching patterns of a large set of phylogenetic tree follow allometric rules conserved across the different levels in the tree of life (Herrada et al., 2008). The universal patterns of phylogenetic differentiation suggests that similar evolutionary forces drive diversification across the broad range of scale, shaping the diversity of life in the planet (Brown et al., 2002).

The fractal dimension of taxonomic systems have 103 been previously estimated based on the size-frequency distributions of taxa with different number of subtaxa (Burlando, 1990). Non-random occurrence of fractal 105 dimension values among groups suggests a relationship with true biologic diversity patterns. The largest checklist used in this study contained 70,000 species, and catalogues of species concerning protists, fungi, plants and animals. At present the number of species in tree of life, however, reach to more than 2,000,000 species, and with different kingdom system (Delsuc, Brinkmann, and Philippe, 2005). Understanding the newly pattern of tree of life require knowing the fractal properties of the tree of life. Here we analyze the hierarchic structure of the global tree of life are obtained, allowing a characterization of the tree of life through the estimation of 116 its fractal dimension. This emphasizes the self-similar relationship for size-frequency distributions of both the 117 hierarchic size among taxon levels and the subtaxa di- 118 versity in each taxon.

## 76 Materials and Methods

77 Data sets

The data sets used in this paper were based on the 124 classification of currently valid species from the Tax- 125

onomy Database of NCBI (http://www.ncbi.nlm. nih.gov/taxonomy) and the Catalogue of Life (www. sp2000.org). The eukaryotic species in the former is largely contained within the latter, whereas the prokaryotic species in the latter is largely contained within the former. These databases were screened for homonyms and the classification of taxa into multiple clades. The combined data sets included five eukaryotic dominations and two prokaryotic dominations, with 126 phylum, 259 class, 4163 order, 14939 family, 214158 genus, and 2031438 species. To describe the fractal property of tree of life, we probe the fractal pattern of intra- and inter-taxonomic level of tree of life.

The inter-taxonomic fractal property of tree of life

We related the logarithmic number of taxa against their numerical rank and estimated the parameters of linear models with least squares regression models:

$$lg(N_r) = -D_r + \mu \tag{1}$$

where  $N_r$  denotes the number of taxon in taxonomic level r,  $\mu = lg(N_1) + r_1D_r$  is the proportionality coefficient, and  $D_r$  is the fractal dimension among taxonomic levels in the tree of life. Since data are not strictly independent across hierarchically organized taxa, we used models based on generalized least squares assuming autocorrelated regression errors.

The intra-taxonomic fractal property of tree of life

For each taxonomic rank from phylum to genus, we represent the frequency distribution of taxa with different subordinate taxa abundance in each taxa as a rankabundance curve. The taxa were arranged in increasing order of the abundance of its subordinate, and taxa frequency were plot as a function of the abundance of subordinate taxa. The probability distribution of the frequency of taxa with different subordinate taxa abundance, P(k), can be represented by a power-law (scale free) with the subordinate taxa abundance:

$$P_k = P_1 k^{-D_t} \tag{2}$$

in which  $P_1$  refer to the number of the taxon with only one subordinate taxa, k to the size rank of the subordinate taxa abundance, and  $D_t$  to the scaling exponent, which also called "fractal dimension" for . We used logarithmic scales for both axes of the rank-abundance curve, so that the power-law abundance distribution is represented as a straight line, and the slope is equal to the power-law exponent. We estimated the scaling exponent of power law using maximum likelihood method

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with BFGS optimization to eliminate the influence of the long tail at low frequency. In order to include the influence of long tail, we converted the taxa abundance curve into the accumulating taxa abundance based on the rank of subordinate taxa:

$$N_k = N_1 k^{-D_{ac}} \tag{3}$$

in which  $N_1$  to the total number of taxa, and  $D_{ac}$  to the fractal dimension for accumulated taxa frequency distribution. Combining equation 2 and 3 yield such a relation:

$$(\frac{P1}{P_{\nu}})^{\frac{1}{D_{t}}} = (\frac{N1}{N_{\nu}})^{\frac{1}{D_{ac}}} \tag{4}$$

In term of equation 4, we have:

$$D_a c = D_t \times \log_{\frac{P_1}{P_k}}(\frac{N1}{N_k}) \tag{5}$$

The distribution of taxonomic abundance is:

$$M_k = k \times P_1 k^{-D_t} = P_1 K^{1-D_t} = P_1 K^{-D_a}$$
 (6)

in which  $M_k$  refer to the taxa abundance at different rank,  $D_a = 1 - D_t$  to the slope of taxa abundance distribution.

#### Results

Fractal property of hierarchical structure in the tree of life

We complied 2 million currently valid species of the tree of life from publicly accessible database. The power-law relation between abundance in each taxa level and the rank of each taxa level indicated the fractal property of hierarchical structure in the tree of life. For the entire tree of life we find fractal dimension of hierarchical structure  $D_r$ =0.873 (Figure 1). Figure 2 shows the power-law property of hierarchical structure for eight kingdoms. It reveal that  $D_r$ =1.004 and 0.889 for Animalia and Plantae, respectively. Among all eukaryotic kingdoms, only the  $D_r$  for Animalia and Plantae were greater than the entire tree of life. The values of  $D_r$  for Fungi, Chromista, and Protozoa were all lower than the entire tree of life, with hierarchical 173 fractal dimension  $D_r$ (fungi)=0.8,  $D_r$ (chromista)=0.586, 174 and  $D_r(\text{protozoa})=0.573$ , respectively. For archaea and bacteria, we find  $D_r$  values were 0.444 and 0.521, respectively. This results indicates that hierarchical fractal 1777 dimensions for prokaryotic kingdoms are significantly 178 lower than for other kingdoms. The Viruses have hierarchical fractal dimension  $D_r$ =0.596, which is lower than

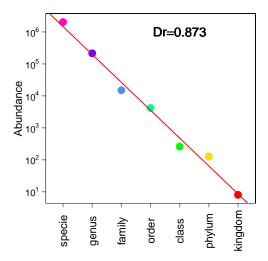


Figure 1: Relationship between the number of taxa and hierarchy of each taxonomic rank for the entire tree of life

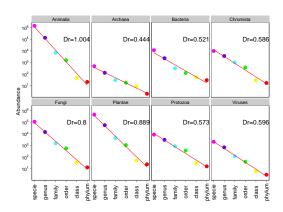


Figure 2: Relationship between the number of taxa and hierarchy of each taxonomic rank for each kingdom

most eukaryotic kingdoms, but greater than prokaryotes.

The value of fractal dimension for hierarchical taxa level indicates the universal scaling between the number of taxa  $(N_t)$  and subordinate taxa  $(N_{st})$ :  $N_{st} = N_t \times 10^{D_r}$ . For the entire tree of life, the number of  $N_{st}$  is approximately 7.5 times of  $N_t$  since  $D_r$  value is 1.133. The  $D_r$  values for bacteria and archaea denote that the the number of  $N_{st}$  is approximately 2.8 times and 3.3 times of  $N_t$ , respectively. The number of  $N_{st}$  is approximately 6.3 times to 10.1 times of  $N_t$  for Animalia, Plantae and Fungi. For Chromista, Protozoa and Viruses, the number of  $N_{st}$  is approximately 3.8 times of  $N_t$ .

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Fractal property of each taxa level in the tree of life

An assessment of the size-frequency distribution of subtaxa in any taxa shows a consistent power-law relation between the number of subordinate taxa in each taxa and the frequency of taxa with same number of subordinate taxa at any taxonomic rank. Figure 3 shows the fractal dimension (power-law exponent  $D_t$ ) for each taxa level of the entire tree of They reveals the existence of self-similarity in each taxa level with fractal dimension  $D_t(genus)=1.62$ ,  $D_t(family)=1.42, D_t(order)=1.56, D_t(class)=1.57, and$  $D_t(phylum)=1.72$ , respectively. The  $D_t$  values were estimated with power law model and can not represent the influence of the long tail of low frequency taxa with very large subtaxa size. We then converted the rank abundance plot into rank accumulating abundance plot in order to reflect the long tail. The fractal dimension (power-law exponent  $D_{ac}$ ) for accumulating frequency plot is related with rank abundance fractal dimension  $D_t$  from Equation 5. The values of  $D_{ac}$  for different taxa level are  $D_{ac}(genus)=1.41$ ,  $D_{ac}(family)=1.05, \ D_{ac}(order)=1.35, \ D_{ac}(class)=0.67,$ and  $D_{ac}(phylum)=1.11$ .

Tendency of  $D_t$  and  $D_{ac}$  values were different among eukaryote, prokaryote, and Viruses. Among eukaryote 232 kingdoms, the variation tendency of fractal dimension 233  $D_t$  and  $D_{ac}$  is similar at same taxa levels.  $D_t$  and  $D_{ac}$  234 values at class and family levels were obviously smaller 235 than at other taxa levels. For Animalia, Plantae and Fun- 236 gi, the fractal dimension values were similar to values 237 for entire tree of life. Except at class level, the  $D_t$  val- 238 ues for Protozoa and Chromista were greater than val- 239 ues for entire tree. The tendency of fractal dimension 240 among prokaryotic taxa levels is different with eukary- 241 otic kingdom. The fractal dimensions  $D_t$  for bacteria 242 and archaea in all taxa levels were all greater than val- 243 ues for entire tree of life.  $D_t$  for genus and family level 244 were smaller than other taxa level, but  $D_{ac}$  for different 245 bacterial taxa levels were all closely to 1.3.  $D_t$  values 246 for archaea were similar to bacteria, but  $D_{ac}$  values for 247 archaea varied in wide range. The fractal dimension  $D_{t}$  248 for viruses were obviously greater than other kingdoms. 249

We also accounted for the distribution of subtaxa 250 abundance in each taxa level (Fig 3). The mathematical 251 description of the proportion distribution (Equation 4) 252 indicated that the relation between abundance of subtaxa a and size of subtaxa in taxa could be also represented 254 by a power-law relationship. For the entire tree of life, 255 the abundance of subtaxa in taxa with small size of subtaxa was greater than in taxa with large size of subtaxa. 257 However, the abundance of subtaxa in taxa with same 258

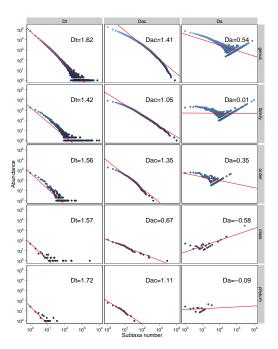


Figure 3: Relationship between the number of taxa and subtaxa number for the entire tree of life

frequency was increase linear with the size of subtaxa. Accordingly, the abundance of subtaxa in taxa with small and large sizes was greater than in taxa with intermediate size. Since  $D_a = 1 - D_t$ , the proportion for taxa with small size of subtaxa number should similar with the proportion for taxa with large size of subtaxa number when  $D_t \approx 1$ . However, the long tail of taxa with large size of subtaxa would skewed the slope of lineage regression for subtaxa abundance distribution. Accordingly,  $D_{ac}$  values could roughly refer  $D_a$  values because  $D_{ac}$  values can reflect the influence of long tail. For genus and order with  $D_{ac} > 1$ , the abundance of species and family in genus and order with small species and family number was greater than in genus and order with great species and family number, respectively. For class with  $D_{ac}$  < 1, the abundance of order in class with small order number was greater than in class with great order number. For family and phylum with  $D_{ac} \approx 1$ , the abundance of genus and class in family and phylum with small genus and class number was greater than in family and phylum with great genus and class number, respectively.

The distribution of subtaxa abundance was also different among eukaryote, prokaryote, and Viruses (Fig S1-S8). The  $D_a$  values of eukaryotic kingdoms were most similar with the entire of tree of life. The  $D_a$  values for genus and order of eukaryotic kingdoms were

all greater than zero, whereas the  $D_a$  values for class  $_{309}$ of eukaryotic kingdoms were all smaller than zero. The 310  $D_a$  values for family of eukaryotic kingdoms were close 311 to zero, except  $D_a$  values of Chromista and Protozoa 312 which were approximately -0.5. The  $D_a$  values for 313 genus, order, and class of archaea were greater than ze- 314 ro, and for family and phylum were less than zero. All  $D_a$  values of bacteria were greater than zero, indicating 316 that the abundance of subtaxa in all bacteria taxa with s- 317 mall subtaxa number was greater than in taxa with great 318 subtaxa number. On the contrary, all  $D_a$  values of Virus- 319 es were greater than zero.

### Discussion

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Knowing the fractal property of tree of life has been a question of great interest motivated in part of our collective curiosity about the evolution of different types of life, and in part by the need to provide a reference point 327 for current and future pattern of biological diversity. In 328 this paper, we describe two type of fractal property in 329 the tree of life, the fractal dimension among different 330 taxa levels  $(D_r)$  and between taxa and subtaxa  $(D_t)$ .

The values of fractal dimension  $D_r$  were different among different kingdoms. The  $D_r$  value represents 333 the scales among different taxa levels, which may pro- 334 mote the discrete evolutionary forces drive diversification across different domination. The evolutionary of 336 organisms is driven with both natural variation and nat- 337 ural selection (Foote, 2012). We now know that the 338 mechanisms of natural variation entailing recombination in its various forms differ starkly between prokary- 340 otes and eukaryotes (Bapteste et al., 2009; Drake, 1999). 341 Among eukaryotes, meiosis ensures reciprocal recom- 342 bination among homologous chromosomes and reassortment of alleles within lineages that recombine within or very near (in the case of hybridization) species 345 boundaries (Ramesh, Malik, and Logsdon Jr, 2005). 346 But for prokaryotes, the mechanisms of natural variation are quantitatively, and many would say fundamen- 348 tally, different from what goes on in sexual eukaryotes 349 (Bapteste et al., 2009; Lake, 2009). These mechanism- 350 s include, gene transfer agents and integrons (Frost 351 et al., 2005). In eukaryotes, the  $D_r$  values for Fungi, 352 Chromista and Protozoa were greater than Animalia and Plantae. The Animalia and Plantae kingdoms were multicellular organisms, but some organisms in the Fungi and Chromista kingdoms and all organisms in Protozoa were single celled organisms (Woese, Kandler, 357 and Wheelis, 1990). It is already known that in singlecelled eukaryotes, endosymbiosis and gene transfer are important processes for evolution (Hotopp et al., 2007;

Moustafa et al., 2009). Increasing knowledge of the genomes of protists may thus in the future expand our conclusion: not only are the tree of life and prokaryotic evolution are two different things, but all microbial evolution (that of prokaryotes and protists) may also be poorly described if addressed in an exclusively tree-like framework (Adl et al., 2007). The fractal dimension for Virus was smaller than prokaryote, was greater than Animalia, Plantae and fungi in eukaryote, and was similar with Chromista and Protozoa in eukaryote. Nevertheless, fractal dimension value did not definitely indicate evolutionary force. The fractal dimension values for Virus was almost equal to the fractal dimension values for Chromista, but the evolutionary force for Virus and Chromista is obviously different (Villarreal, 2006; Drake, 1999).

In each taxa levels, the frequency of taxa with same subtaxa sizes also follow the power-law, which indicated the fractal property of subtaxa numbers in each taxa level. Fractal dimension  $(D_t)$  indicates the distribution of taxa with rare and frequent subordinate taxa. The fractal dimension for genera calculated 30 year ago based on 70 000 species was 1.59 (Burlando, 1990), which is very similar to 1.62 reported in our study based on more than 2 million species. This results might suggests that the fractal pattern of diversity in genera is reliably, although species number increase about 30 times. The  $D_t$  values for each taxa level were similar, whereas the  $D_{ac}$  values for class was extremely lower than for other taxa levels because of the scatting of points at the lower end. Similar fractal dimension at different taxa levels might implies that tree of life is scale free at both the pattern of both macro and micro evolution (Raff, 2000). The long tail in size frequency distribution appears that power law model under estimate the size of large taxa (Burlando, 1990). However, the distinctly difference between  $D_t$  and  $D_{ac}$  might suggests (Burlando, 1993). The skewness of distribution caused by the presence of large size taxa has been regard as an evidence of (Blum and Francoise, 2006). However, the skewness can also be viewed as a scaling cutoff, which shows a transition from fractal to non-fractal diversity (Burlando, 1990). Consequently,  $D_t$  values and scatting points denote frequency distribution of fractal to non-fractal distributing taxa, and  $D_{ac}$  values show the feature of both the fractal to non-fractal diversity. Subtaxa abundance distribution is also influence by both the fractal to non-fractal distributing taxa. Accordingly,  $D_a$ values represents the subtaxa abundance distribution is related to  $D_{ac}$  rather than  $D_t$ .

Fractal dimension of size frequency distribution of subtaxa in each taxa varied with kingdoms. The  $D_t$ 

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values for multiple cellular organisms (e.g. Animali- 413 a, Plantae, and Fungi) were smaller than the  $D_t$  vales 414 for singular cellular organisms (Bacteria, Archaeal, Pro, 415 Protozoa and Chromista). The  $D_t$  values for Virus were 416 greater than all other kingdoms. The  $D_t$  vales yield a 417 diversity measure, since high  $D_t$  values indicates that 418 taxa with one or a few-taxa are more numerous. In other words, the kingdom with high  $D_t$  values has proved with high diversity pattern. The results in present study might suggest that evolutionary scaling is closely relat- 422 ed to the morphologic scaling of organisms (Marquet 423 et al., 2005). The size of an organism affects its al- 424 1 aspects of life, including metabolic, growth, mortal- 425 ity, and other vital rates (Gouws, Gaston, and Chown, 426 2011; Coetzee, le Roux, and Chown, 2013). The body 427 size spectra in natural community are scale-free, which is the product of intra- and interspecies regulation of 429 the relative abundance of organisms of different sizes 430 (Giometto et al., 2013).

We recognize a number of factors that can influence the fractal property. 432

Taxa definitions. Different taxonomic communities use different levels of differentiation to define taxonomic levels (Mora et al., 2011). This difference implies 436 that the numbers of taxa for different taxonomic communities are not directly comparable. For example, the 438 species concept for prokaryotes tolerates a much higher 439 degree of genetic dissimilarity than in most eukaryotes 440 (opez Garcia and Moreira, 2008). Species take longer 441 to isolate in prokaryotes than in eukaryotes due to horizontal gene transfers among phylogenetic (Ochman, Lawrence, and Groisman, 2000). Thus, implication of estimated fractal dimensions are different for different 445 taxonomic communities. Nevertheless, the aim of the 446 present study is describing the hierarchical structure of the Tree of Life but not the topological property. We found that in any taxonomic communities, there is a constantly follows power-law rule for rank-abundance relationship between taxa number and diversity subordinate taxa.

Completeness of the tree of life. It is obviously that the tree of life is still incomplete at present (Benton and Ayala, 2003). The number of eukaryotic species have been estimated to be 8.7 million on earth, but the catalogued species is just 1.2 million at present (Mora et al., 2011). Although the catalogued species number is approximately 10 thousand, it is believe that isolated prokaryotic species is only 1% of entire prokaryotic species at present (Gich et al., 2012). Although the rate of catalogued species varied from 1% (prokaryotes) to 70% (Plantae), there is a constantly follows power-law rule for rank-abundance relationship between taxa

number and diversity subordinate taxa. These results indicated that new discovered species might influence the fractal dimension but not the power-law relationship tendency. Furthermore, increase in the number of higher taxa will distort the shape of the current tree of life. Increasing number of new discovered higher taxa in ongoing for prokaryotes, but the number of catalogued higher taxa is almost reach the entire number of higher taxa for eukaryotes, except Chromista, Protozoa and fungi (Mora et al., 2011). These results suggest that our fractal property analysis for prokaryotes and Chromista, Protozoa and Fungi in eukaryotes should be interpreted with that caution in mind.

Self-similarity of the tree of life. The tree of life is widely accept to be self-similarity. Sub-fractal structure for different taxonomic communities varied in a wide range due to various self-similarity property. However, in this study we do not concern the topological of tree of life, but the diversity number in each taxonomic level. The consistent patterns for entire tree of life imply that the different self-similarity in sub-fractal structure do not obscure the robust underlying relationship for inter- and intra-taxonomic levels.

In summary, the diversity for each level of the Tree of Life display a consistent power-law rules for interand intra-taxonomic levels. The discrepancy of fractal nature indicates different evolutionary force for various kingdoms. The distribution of taxa size is governed by fractal diversity but skewed by overdominating taxa with low frequency. The distribution of subtaxa abundance is influence by both fractal and non-fractal overdominating taxa. The use of fractal geometry provides a unified view of diversity in tree of life and might therefore give clue to the evolutionary of tree of life.

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