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Running head: SPR Supertrees

Supertrees based on the subtree prune-and-regraft distance

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Abstract.

Supertree methods reconcile a set of phylogenetic trees into a single structure that is often interpreted as a branching history of species. A key challenge is combining conflicting evolutionary histories that are due to artifacts of phylogenetic reconstruction and phenomena such as lateral gene transfer (LGT). Although they often work well in practice, existing supertree approaches use optimality criteria that do not reflect underlying processes, have known biases and may be unduly influenced by LGT. We present the first method to construct supertrees by using the subtree prune-and-regraft (SPR) distance as an optimality criterion. Although calculating the rooted SPR distance between a pair of trees is NP-hard, our new maximum agreement forest-based methods can reconcile trees with hundreds of taxa and > 50 transfers in fractions of a second, which enables repeated calculations during the course of an iterative search. Our approach can accommodate trees in which uncertain relationships have been collapsed to multifurcating nodes. Using a series of simulated benchmark datasets, we show that SPR supertrees are more similar to correct species histories under plausible rates of LGT than supertrees based on parsimony or Robinson-Foulds distance criteria. We successfully constructed an SPR supertree from a phylogenomic dataset of 40,631 gene trees that covered 244 genomes representing several major bacterial phyla. Our SPR-based approach also allowed direct inference of highways of gene transfer between bacterial classes and genera; a small number of these highways connect genera in different phyla and can highlight specific genes implicated in long-distance LGT.

Keywords: subtree prune-and-regraft, supertrees, phylogenomics, prokaryotic phylogeny, matrix representation with parsimony, lateral gene transfer, Robinson-Foulds

An organism's genome, typically comprising many thousands of genes, provides a detailed record of its past. While sets of homologous genes from a set of genomes can provide evidence about organismal relationships, individual gene trees covering these genomes may be influenced by processes including paralogy and gene loss, lineage sorting and lateral gene transfer (LGT) (Maddison and Knowles, 2006; Galtier and Daubin, 2008). One approach to reconcile trees that differ due to these processes and to artifacts of phylogenetic inference is to construct a single tree that aims to reflect the relationships in a set of gene trees. Supertree methods generate a single tree, which may serve as a hypothesis of organismal descent or relatedness, by optimizing a similarity criterion. Supertrees have been used to represent large-scale phylogenies including the first phylogeny of nearly all extant mammals (Bininda-Emonds et al. 2007), the first family-level phylogeny of flowering plants (Davies et al. 2004), and the first species-level phylogeny of non-avian dinosaurs (Lloyd et al. 2008). They have also been used to study the extent of LGT in prokaryotes (Beiko et al. 2005) and to disentangle the origin of eukaryotic genomes (Pisani et al. 2007). One key advantage of supertree methods is that they can take as input sets of gene trees sampled from overlapping but non-identical sets of taxa, in contrast with consensus tree approaches, which require that all input trees contain exactly the same set of leaves. Simulations have shown that supertrees are more reliable in the presence of a moderate amount of misleading LGT than the supermatrix approach which is based on concatenated alignments of many gene sequences (Lapierre et al. 2012).

Many optimality criteria have been proposed for supertree construction. Matrix representation with parsimony (MRP) (Ragan 1992; Baum 1992) was among the earliest methods proposed and remains the most commonly used, but detailed work with MRP has raised

several concerns with the approach. MRP converts input trees into a binary character matrix and solves the parsimony problem on this matrix. Although the parsimony problem is NP-hard, fast
25 hill-climbing heuristics in PAUP* or TNT allow MRP to be applied to large datasets (Goloboff 1999; Swofford 2002; Roshan et al. 2004). MRP is very effective in practice, quickly constructing supertrees of competitive quality in every tested metric (Bininda-Emonds et al. 2001; Eulenstein et al. 2004; Chen et al. 2006). However, it is not clear why the MRP approach performs so well and it may generate relationships that do not belong to any of the source trees
30 (Pisani and Wilkinson 2002), has problems resulting from unequal representation of taxa (Bininda-Emonds et al. 2002), and may include relationships contradicted by the majority of source trees (Goloboff 2005). Other developed supertree criteria include consensus supertrees (Adams 1972), majority-rule supertrees (Cotton and Wilkinson 2007), Quartet supertrees (Piaggio-Talice et al. 2004) and Triplet supertrees (Lin et al. 2009). However, like MRP, other
35 supertree building methods that are not based on symmetric tree-to-tree similarity measures may be unduly influenced by the shapes of the input trees (Wilkinson et al. 2005).

Bansal et al. (2010) recently proposed Robinson-Foulds (RF) supertrees, which aim to minimize the total RF distance (Robinson and Foulds 1981) between the supertree and the set of input trees. The RF measure captures the number of bipartitions in one tree that do not exist in
40 another, so the RF supertree approach aims to maintain as much phylogenetic information from the input trees as possible. Fast hill-climbing heuristics make computing rooted RF supertrees feasible from binary input trees and others have begun to extend this to unrooted trees with local search heuristics (Chaudhary et al. 2012). While RF appears to be a good criterion for supertrees, it may not be suitable for datasets with substantial amounts of LGT: a single "long-distance"
45 LGT event between distant taxonomic relatives will result in many discordant bipartitions and a

high RF distance. If many organisms participate in long-distance LGT, then "phylogenetic compromise" trees (Beiko et al. 2008) may emerge which reflect neither the correct species relationships, nor the dominant pathways of gene sharing. The requirement that all input trees be binary is also potentially limiting, as many relationships in trees inferred from sequence data are unsupported by statistics such as the bootstrap, and should be collapsed into multifurcations.

Another well-studied criterion for expressing differences between trees is the subtree prune-and-regraft (SPR) distance (Hein et al. 1996). The SPR operation involves splitting a pendant subtree from the rest of the tree, and reattaching it at a different location, with the rooting of the subtree preserved. Since SPR operations allow the pruned subtree to be reattached anywhere, they can accommodate long-distance transfers in a single step; such a transfer would increase the SPR distance by only 1, whereas the RF distance could be drastically increased. The SPR distance is the minimum number of such operations required to reconcile two trees. The relationship between an SPR operation and the topological consequences of an LGT event (Beiko and Hamilton 2006) makes SPR a natural criterion for assessing a supertree whose constituent trees contain a large number of LGT events. Given its relationship with the RF distance, the SPR criterion may also be suitable for datasets where a phenomenon other than LGT is the principal confounding factor. To date, no SPR-based supertree approach has been developed, in part because computing the SPR distance between two phylogenetic trees is NP-hard (Bordewich and Semple 2005; Hickey et al. 2008).

Combining two recent advances makes SPR supertrees feasible. First, using the equivalence between Maximum Agreement Forests (MAFs) and rooted SPR distance (Hein et al. 1996; Bordewich and Semple 2005), Whidden and Zeh (2009) and Whidden et al. (2010; 2013a) developed an algorithm with running time $O(2.42^k n)$. The resulting implementation was orders

of magnitude faster than any previous algorithm and is able to compute SPR distances of up to
70 46 on trees with 144 prokaryotic taxa, and 99 on synthetic 1000-leaf trees, in less than 5 hours.
We have extended this algorithm with several enhancements that we believe improve the running
time to $O(2^k n)$ for binary input trees, and allow the inclusion of input trees in which uncertain
relationships have been collapsed into multifurcating nodes. Second, Linz and Semple (2011)
developed a cluster reduction technique which can reduce the computation of an MAF into
75 several subproblems, yielding an exponential reduction of the running time in practice. The
approach taken by Linz and Semple is similar to the cluster reduction rule of Baroni et al. (2005)
for computing the hybridization distance but requires more care in choosing which maximum
agreement forest to take for each subproblem to build the complete MAF. We have also reduced
the time required to compute a cluster reduction to linear from the originally published $O(n^3)$.
80 Neither refinement alone is fast enough to compute the thousands of SPR distances required to
build an SPR-based supertree on interesting numbers of taxa. However, by combining the cluster
reduction with our improved MAF-based approach we obtain dramatic improvements in running
time, processing tree pairs that previously required 1-5 hours to reconcile in one second or less,
thus enabling the many SPR distance computations needed to iteratively construct a supertree.

85 Our heuristic approach uses a greedy hill-climbing strategy to build an initial supertree,
then refines this supertree using iterative global SPR rearrangements. We use a bipartition-based
heuristic to identify and ignore proposed rearrangements that violate relationships that are well-
supported in many trees, greatly reducing the number of rearrangements that need to be
evaluated. These algorithms are implemented in the SPR Supertree software version 1.2.0, which
90 is available at <http://kiwi.cs.dal.ca/Software/SPRSupertrees>. The software is freely available,
open source and licensed under the GNU GPL version 3. Here we describe the steps in our

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approach, and demonstrate the speedups achieved using the algorithmic refinements described above. Our experiments using simulated datasets with LGT show that the SPR approach is more accurate than RF and, for some realistic rates and regimes of LGT, MRP as well. Comparisons based on the eukaryotic datasets used by Bansal et al. (2010) for benchmarking show that the SPR approach yields supertrees with lower total SPR distances to the input trees than either RF or MRP, and with slightly higher RF and parsimony scores. To demonstrate the application of the SPR supertree approach on a dataset in which considerable LGT is expected, we also used a phylogenomic data set of 244 bacteria covering 393,876 genes in 40,631 orthologous sets to analyze preferential transfer of genes between bacterial lineages. We were able to reconstruct a highly plausible supertree, and with the SPR approach we identified putative highways of gene sharing. Interestingly, preference for alternative hypotheses of the relatedness between bacterial phyla depended on the choice of gene tree rootings, suggesting that unrooted supertree methods may be ignoring plausible hypotheses.

METHODS

Calculating the Subtree Prune-and-Regraft Distance Between a Pair of Rooted Trees

We can compute the SPR distance between a pair of rooted trees quickly in practice, despite the NP-hardness of the problem (Bordewich and Semple 2005), using our efficient fixed-parameter bounded search tree algorithm in combination with our linear-time formulation of Linz and Semple's cluster reduction (Linz and Semple 2011) to solve the equivalent Maximum Agreement Forest (MAF) problem. The MAF problem is a static version of the SPR distance problem that is easier to manipulate and analyze. An agreement forest of two trees is a forest on the same label set that can be created by cutting (deleting) edges from either tree. Bordewich and

115 Semple (2005) showed that a maximum agreement forest—an agreement forest that requires the fewest edge cuts—requires exactly as many edge cuts as the SPR distance between the trees. Indeed, each edge cut represents a transfer and the proposed series of transfers can be quickly inferred from the MAF (Fig. 1). Our algorithms, like most recent work on the SPR distance, compute such MAFs.

120 Our published MAF algorithm (Whidden et al. 2010; Whidden et al. 2013) operates in a bottom-up fashion in the first tree, denoted T_1 , and reduces the second tree to a forest, denoted F_2 . During the algorithm we identify subtrees that are identical in T_1 and F_2 and, in particular, pairs of such trees that are siblings in T_1 (sibling pairs). If any identical subtree is a component of F_2 we cut its corresponding parent edge in T_1 . If any sibling pair in T_1 is also a sibling pair of F_2 we note that their parent nodes are identical in T_1 and F_2 . If neither of these two situations applies, we identify at most three possible edge cutting scenarios and explore each recursively. We explore each scenario in turn, thus using very little memory, and use our 3-approximation algorithm (which operates similarly but simply cuts all three possible edges so that its running time scales linearly and may return at most 3 times the correct distance) to avoid exploring
125 scenarios that are guaranteed to not return an optimal MAF.
130

We have enhanced our MAF algorithm to prioritize non-branching edge cut scenarios and ignore duplicate search branches through *edge protection*. First, we examine each sibling pair to select a sibling pair with only one edge cutting scenario, if any exist. This limits the exponential explosion of our search when possible. Second, we *protect* edges that have been cut in
135 previously rejected scenarios. If we have two scenarios that cut edges e_1 and e_2 , respectively, and the e_1 scenario fails to find an MAF, then the e_2 scenario will not find an MAF by cutting e_1 so we *protect* e_1 to indicate this and ignore any scenario that would cut e_1 . This prevents us from

exploring duplicate edge sets and increases the chance of finding a non-branching edge cut scenario. When no non-branching sibling pairs remain, we select a sibling pair with a protected member, if possible, to capitalize on this effect. For further details see Appendix I.

We have also extended our MAF algorithm to allow for reconciliation of multifurcating gene trees with the reference supertree (see Appendix I). For such gene trees we define the *soft* SPR distance (Whidden et al. 2013b; Linz and Semple 2008) to be the minimum number of SPR operations required to transform the reference tree into some binary resolution of the gene tree. This definition accounts for the general assumption that multifurcations imply uncertainty rather than simultaneous speciation. Our algorithm proceeds similarly to the binary case (as the reference tree, required to be T_1 , is binary) with modifications to our considered edge scenarios that allow the resolution of multiple siblings and cutting the resulting edge.

The cluster reduction of Linz and Semple (2011) splits the input trees into smaller subproblems that can be solved iteratively (but not independently). As our algorithms' running times scale exponentially with the computed distance, this reduction has an enormous impact in practice. Two subtrees of the input trees on the same leaf sets represent a cluster. A cluster MAF with its root edge removed (representing a transfer prior to the LCA of the leaf set) is guaranteed to be part of some complete MAF of the two trees, if any such cluster MAF exists. Alternatively, if every MAF of the cluster must maintain its root edge, every cluster MAF will be part of a complete MAF. We thus modified our search strategy to prefer MAFs with their root edge removed in order to accommodate this reduction. In addition, we removed the complicated weighting scheme of the original cluster reduction method and improved the time required to compute such a cluster reduction to linear in the size of the trees from the cubic scaling reported by Linz and Semple (see Appendix II).

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165 Recently, Chen and Wang proposed a separate improvement to our previous SPR distance algorithm for binary trees called UltraNet (Chen and Wang 2013). We do not compare our algorithms with UltraNet in detail as UltraNet requires binary trees and failed to find the correct SPR distance in 30 of our tests. However, our improved algorithm for the SPR distance even without the cluster reduction was significantly faster than UltraNet and our previous algorithm with clustering outperformed UltraNet on 65 of our tests.

Supertree Construction

170 We attempt to find the minimal SPR supertree for a given set of gene trees, that is, the binary rooted tree on the union of the label sets of the gene trees with the minimal cumulative SPR distance to the gene trees (hereafter, simply minimal SPR distance). When the leaf set of the (partially constructed) supertree differs from that of a gene tree, we ignore unique taxa when computing this distance. If no starting tree is provided to initiate the search, we construct an initial SPR supertree through stepwise addition of taxa and then use global SPR rearrangements to optimize the tree. To construct the initial tree, we begin with the four most common taxa in the input trees and select the tree shape on these four taxa with minimal SPR distance to the projected input trees. We then successively add taxa to the supertree, in decreasing order according to the frequency of occurrence in the gene trees. Each taxon is added in the location that minimizes the SPR distance. When determining this location, we only compute the SPR distance to gene trees containing the new taxon, as the SPR distance between the supertree and other gene trees is unchanged. Once we have constructed an initial SPR supertree (or, 180 alternatively, are supplied an initial tree by the user) we begin the SPR rearrangement phase. For a prespecified number of iterations, we look at the $O(n^2)$ trees that can be obtained from the

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185 current supertree of n leaves by one SPR operation and select from these the tree with minimal
SPR distance. Many of these SPR rearrangements will be obviously flawed, so we incorporate a
bipartition clustering approach to ignore such rearrangements. Any bipartition of the supertree
that is supported by at least half of the gene trees containing two or more taxa from each of the
two sets induced by the bipartition is considered "fixed", and SPR rearrangements that disrupt it
are disallowed. This greatly decreases the number of considered bipartitions with little effect on
190 the accuracy of the tree search.

Our methods were developed for rooted gene trees, but we provide three options to
accommodate the unrooted gene trees that are typically produced by maximum-likelihood and
Bayesian phylogenetic approaches. Our first method is to compute the minimal SPR distance
between the supertree and any rooting of each gene tree using an exhaustive search of all
195 possible rootings. Second, given a rooted (partial) supertree and unrooted gene tree we use each
bipartition of the gene tree to try and identify the root bipartition of the supertree. We root the
gene tree at the bipartition that best matches the supertree root bipartition according to the
balanced accuracy score, an average of the similarities between each matching side of the
bipartitions. Suppose that the supertree root bipartition splits the taxa into two groups A and B
200 and a gene tree bipartition splits the taxa into two groups C and D. Then the balanced accuracy
of the C|D bipartition as compared to the A|B bipartition is the larger of $((|A| \cap |C|) / 2(|A| + |C|))$
 $+ ((|B| \cap |D|) / 2(|B| + |D|))$ or $((|A| \cap |D|) / 2(|A| + |D|)) + ((|B| \cap |C|) / 2(|B| + |C|))$, depending on
whether A and C or B and D are more closely matched. Third, we can root the gene trees at a set
of outgroup taxa, throwing away trees where this outgroup is not monophyletic. We then build a
205 supertree of this reduced tree set and can then, if desired, root the remainder of the trees using
our balanced accuracy approach to build a final supertree.

Comparative Evaluation and Data Sets

We evaluated the performance of our SPR supertree algorithm against two other
210 approaches: the widely used matrix representation with parsimony (MRP) approach of Baum
(1992) and Ragan (1992) and the recently published Robinson-Foulds (RF) supertree algorithm
(Bansal et al. 2010). Since the RF supertree approach is also based on topological distances
between trees, it is an appropriate comparator for our SPR-based method. To construct MRP
supertrees we used the Clann 3.2.2 (Creevey and McInerney 2005) software package to generate
215 matrices for a PAUP* version 4.0b10 (Swofford 2003) parsimony search using 25 iterations of
SPR rearrangements (to match the SPR and RF approaches). RF supertrees were constructed
using version 1.8.4 of the software described by Bansal et al. (2010) which uses 25 iterations of
SPR rearrangements interleaved with partial data ratchet iterations. The three methods were
compared in terms of their running time on various datasets as well as their accuracy, either
220 against the known phylogeny in the case of simulated data sets or the three supertree criteria
when empirical data sets were used.

We built simulated data sets to evaluate the accuracy of SPR, MRP and RF on gene trees
generated from a completely known species history. EvolSimulator (Beiko and Charlebois 2007)
version 2.2 was used to generate 15 replicated speciation and extinction histories in populations
225 limited to 25 extant genomes. 10,000 simulation iterations were run in all cases. For each of the
15 distinct histories, multiple runs were carried out in which the rate of LGT was varied between
0 (no LGT) and 2.5 events per iteration in increments of 0.1. We also simulated two different
LGT regimes: random, in which transfers between any donor/recipient pair were equally
probable; and divergence-biased, where donor/recipient exchanges were more likely between

230 closely related genomes (i.e., genomes that share a recent common ancestor), with no LGT at all
between genomes that diverged > 5000 generations in the past. The ancestral genome in each
simulation (i.e., iteration 1) had 150 genes, and lineages could gain and lose genes to a minimum
of 100 and a maximum of 200. A full list of parameter settings can be found in the sample
configuration file (see online Supplemental Material). The resulting gene trees were used to infer
235 supertrees under the SPR, MRP and RF criteria: supertree accuracy was evaluated based on
dissimilarity with the known species tree, and the total distance between the supertree and all
gene trees.

We also compared the three methods using published eukaryotic supertree datasets of
marsupials (Cardillo et al. 2006), seabirds (Martyn and Page 2002), placental mammals (Beck et
240 al. 2006) and papilionoid legumes (Wojciechowski et al. 2000) obtained from
<http://www.cs.utexas.edu/~phylo/datasets/supertrees.html>. These datasets cover between 121-
558 taxa in 7-726 trees and were used to compare the supertree methods according to their
respective supertree optimization criteria, as was done by Bansal et al. (2010).

Finally, we constructed a 244-taxon bacterial SPR supertree from a 40,631-tree subset of the
245 159,905 unrooted multifurcating prokaryotic phylogenetic trees from Beiko (2011), compared it
with an MRP supertree and used the SPR supertree to infer “highways of gene sharing”, that is,
frequently implied pathways of LGT among major bacterial lineages. From the 1179 taxa in the
original dataset, we randomly selected 15 Alphaproteobacteria, Betaproteobacteria and
Deltaproteobacteria, 14 Epsilonproteobacteria, 13 Gammaproteobacteria, 40 Bacilli, 34
250 Clostridia, 74 Actinobacteria, 2 Deferribacteres, 11 Thermotogae, 7 Aquificae, 2 Nitrospira and
2 Synergistetes for a total of 244 taxa (listed in online Supplemental Table 1) covering a subset
of well-sampled and sparsely sampled classes of bacteria and restricted the 159,905 trees to this

subset. We then collapsed all branches with a bootstrap support value of less than 0.8 and discarded all star trees and trees with fewer than 4 taxa. After this procedure, 40,631 trees remained. In total, there were 393,876 leaves in the trees for an average of 9.7 taxa per tree. To construct a supertree from the set of unrooted gene trees, we used our rooting method described above with the Aquificae as outgroup. We first constructed an initial guiding supertree from the 40 largest gene trees with a monophyletic Aquificae group (Griffiths and Gupta 2004). This required 13 global rearrangement iterations and 87 CPU hours to converge on a local minimum. The remaining trees were then rooted using our balanced accuracy approach, and we constructed our SPR supertree from this data set using the guiding supertree as a base, which required 16 iterations to converge and 1198 CPU hours.

Once the final supertree was obtained, LGT events were inferred using MAF comparisons between our SPR supertree and the gene trees. We computed a single MAF for each gene tree and determined the equivalent sequence of implied LGT events in less than one minute. Transfers where both the putative donor and recipient were contained within two distinct genera were counted, and the results visualized as a heatmap and LGT affinity graph constructed using Cytoscape 2.8.3 (Smoot et al. 2012). We ignored directionality as it is often possible to identify partners but not the direction of transfer (Beiko and Ragan 2008). Heatmap values were scaled such that each row had a mean of 0 and standard deviation of 1 and relationships with fewer than 5% of the maximum transfer events for a row or only a single transfer event were filtered out. Two genera were connected by an edge if the number of inferred LGT events between them exceeded 5% of the total number of homologous genes common to at least one member of both genera.

275 All supertrees constructed from empirical data, as well as the input bacterial trees we used,
are available online as Supplemental Material.

RESULTS

Bacterial SPR Supertree and Large-Scale Analysis of LGT

280 We first present our supertree of 244 bacterial taxa that was constructed from 40,631
unrooted input gene trees using our two-stage outgroup procedure. The taxa selected for our
bacterial supertree analysis were chosen to examine several interesting phylogenetic questions in
the Bacteria. For example, there are two competing hypotheses for the placement of the
Aquificae. Informational genes such as 16S small subunit ribosomal RNA suggest that the
285 Aquificae are deep-branching and either external to or sister with the Thermotogae but the
majority of other proteins suggest that the Aquificae are sister to the Epsilonproteobacteria (or
other groups such as the Deltaproteobacteria) and not the Thermotogae (Boussau et al. 2008). It
has been suggested that the Aquificae may be closely related to the Epsilonproteobacteria with
either LGT or a thermophilic G+C bias and long-branch attraction responsible for the observed
290 affinity for Thermotogae (Griffiths and Gupta 2004). Informational proteins are thought to be
transferred infrequently, so it has been more recently suggested that there have been large
amounts of lateral gene transfer between the Aquificae and Epsilonproteobacteria (Boussau et al.
2008). Our dataset also includes members of many other groups implicated in LGT, including
the Deltaproteobacteria and Clostridia: both of these groups show evidence of frequent LGT with
295 other lineages (Dagan et al. 2010; He et al. 2010; Beiko 2011). Other genera frequently
associated with high LGT rates including *Pseudomonas* and *Burkholderia* are also included.
Finally, several lineages such as Deferribacteres and Synergistetes with relatively few sequenced

representatives and an uncertain phylogenetic position (Jumas-Bilak et al. 2009) were included to assess their placements in the SPR supertree.

300 Figure 2 shows our SPR supertree of the 244-taxon bacterial dataset. The SPR supertree largely recovered the major bacterial classes as monophyletic groups with several notable exceptions. The Deltaproteobacteria are separated from the other Proteobacteria by the Actinobacteria. The Deltaproteobacteria are also split into a group containing the Myxobacteria and *Candidatus* “Nitrospira defluvii”, and a group containing all other orders of the class.

305 Although assigned to phylum Nitrospirae, *Ca. N. defluvii* has strong affinities to other phylogenetic groups, with deltaproteobacterial genomes constituting seven of the 15 most frequently observed phylogenetic partners. This is an interesting link as *Sorangium cellulosum* has the largest known bacterial genome (Schneiker et al. 2007) and both *Candidatus Nitrospira defluvii* and *Anaeromyxobacter dehalogenans* are gram-negative nitrite reducers. Further, it has

310 been suggested that *Ca. N. defluvii* evolved from microaerophilic or even anaerobic ancestors (Lucker et al. 2010) and *Anaeromyxobacter dehalogenans* exhibits aerobic and anaerobic growth (Sanford et al. 2002). Two other proteobacteria are separated from their classes: *Bdellovibrio bacteriovorus*, a Deltaproteobacterium that parasitizes other gram-negative bacteria (Stolp and Starr) and appears to have acquired genes from the proteobacterial cells it parasitises (Gophna et

315 al. 2006), and *Candidatus Hodgkinia cicadicola*, an alphaproteobacterial cicada symbiont with the smallest known genome (McCutcheon et al. 2009), form a pairing that is sister to the Epsilonproteobacteria.

Among other phylogenetic groups, *Veillonella parvula* and *Acidaminococcus fermentans*, initially assigned to class Clostridia, are sister to the Bacilli. *Veillonellaceae* and

320 *Acidaminococcaceae* have a peculiar cell wall composition which stains Gram-negative, unlike

most Firmicutes, and have been suggested to belong to a class Negativicutes, separate from the Bacilli and Clostridia, by Marchandin et al. (2010). *Coprothermobacter proteolyticus* groups with the Thermotogae rather than the Clostridia. *C. proteolyticus* was assigned to class Clostridia using small subunit ribosomal RNA (Rainey and Stackebrandt 1992) but phylogenomic analysis (Beiko 2011; Yutin et al. 2012) and newer phylogenetic trees built from many more samples of small subunit ribosomal RNA agree with a closer relationship between *C. proteolyticus* and Thermotogae (Munoz et al. 2011). With Aquificae as the outgroup, the next-deepest branches in the bacterial tree are *Thermodesulfovibrio yellowstonii*, the other member of phylum Nitrospirae, and the Deferribacteres, followed by Thermotogae. The Synergistetes are sister to the Firmicutes in this tree.

We then inferred LGT events between these bacteria by computing a single MAF for each gene tree and determining the equivalent sequence of implied LGT events. This entire analysis of the 40,631 gene trees required less than one minute using our refined MAF algorithms. Transfer events with source and endpoints both in a monophyletic subtree of the same genus or different genera were identified to focus on relatively recent transfers. Directionality was ignored as it is often possible to identify partners but not the direction of transfer (Beiko and Ragan 2008). Figure 3a shows the results of this analysis. Clustering based on the strength of their LGT affinities still groups most genera by class and phylum, and the majority of inferred LGT events occur within clusters of taxonomically related genera. However, there are also many linkages between genera of distinct phyla and clusters of genera with distinct classes and phyla. Online Supplemental Figure 1 shows a heatmap of the relative LGT trends between classes.

A genus-level LGT affinity graph (Fig. 3b) between genera was used to further explore these relationships and identify paths of gene sharing between distinct lineages. Genera were

connected by edges representing transfer events exceeding 5% of their total number of shared
345 homologous genes. As in Figure 3a, the majority of inferred LGT events connect members of the
same class or phylum. Yet many linkages connect different classes and phyla such that all of the
genera but two, *Ehrlichia* and *Wolbachia*, are connected. The large and diverse genus
Clostridium, in particular, connects Actinobacteria, Thermotogae, four of the five classes of
Proteobacteria, *Thermoanaerovibrio* (phylum Synergistetes), and has many strong connections
350 with Bacilli and other Clostridia (online Supp. Fig. 2). Family Coriobacteriaceae, comprising
Slackia, *Eggerthella*, and *Cryptobacterium*, had linkages with the other Actinobacterial genera
Corynebacterium and *Bifidobacterium* but was also connected to the Firmicute genera
Clostridium, *Eubacterium*, and *Streptococcus*. There are numerous pathways of gene sharing
between actinobacterial genera such as *Acidimicrobium*, *Corynebacterium* and *Mycobacterium*
355 on the one hand, and proteobacterial genera such as *Helicobacter*, *Sorangium*, *Xanthomonas* and
Mesorhizobium on the other. A single path between *Nitratiruptor* and *Persephonella* connects
the Epsilonproteobacteria with the Aquificae. Many connections are observed between the
different classes of Proteobacteria, highlighting the numerous LGT events that occur between
distinct lineages of phylum Proteobacteria. The connectedness of higher taxonomic groups is
360 supported by the class-level affinity graph (online Supp. Fig. 3), in which each class is connected
to 3.92 other classes on average, with the Actinobacteria connected to a total of ten.

Validation of Efficiency and Accuracy

We next demonstrate the improved performance of our MAF algorithms with a single SPR
365 distance analysis of our 244-taxon bacterial supertree as compared to each of the 40,631 gene
trees. Figure 4 shows the mean running time for tree comparisons with a given SPR distance on a

log scale. Our improved algorithms reduced the time required for individual calculations from 5 hours to a maximum of 0.8 seconds on the initial set of binary gene trees. Both the cluster reduction and our improved algorithms are necessary to achieve these running times. Our
370 algorithm requires slightly more time to compare the supertree with multifurcating trees for a given SPR distance but this is balanced by the reduction in SPR distance caused by collapsing unsupported bipartitions; clustered comparisons required at most 0.76 seconds. As mentioned previously, a full LGT analysis now requires just 34 seconds on a single CPU. Without our new algorithms, such an analysis would be limited to binary trees and require more than 65 hours.

375 *Validation with Simulated Datasets*

We next compared the ability of SPR, RF, and MRP based supertrees to recover the species tree in a series of simulated datasets. EvolSimulator (Beiko and Charlebois 2007) was used to evolve sets of genomes under a model of lineage duplication and extinction, with each
380 lineage capable of gene duplication, gene loss, and LGT. Varying the rate of LGT in different sets of replicated simulations allowed us to explore the effectiveness of SPR, RF and MRP at relatively low or high levels of LGT. We also simulated two regimes of LGT: random LGT, which can interfere with the recovery of correct branching patterns, and divergence-biased LGT, which can actually reinforce the true tree due to preferential sharing between close relatives
385 (Beiko et al. 2008).

Simulated LGT rates varied between 0 (no LGT) and 2.5 events per iteration (see Methods for details). To give context to our LGT rate simulation parameter, we computed the mean ratio of SPR distance to number of leaves in the simulated trees, to similar values inferred for the 244-taxon SPR supertree (Fig. 5). The inferred frequency of LGT in our empirical data equated to a

390 simulated random LGT rate between 0.1 and 0.2 and a simulated divergence-biased LGT rate
between 0.3 and 0.4. Since the bacterial supertree has 244 leaves rather than 25, we also
restricted our bacterial supertree and gene trees to 25 randomly sampled subsets of 25 leaves and
computed this ratio. We found these subsampled supertrees corresponded to lower simulated
rates of LGT. This suggests that our simulations with lower rates of LGT are biologically
395 plausible; also, since the distribution of LGT events is non-uniform across bacterial lineages
(Kunin et al. 2005; Beiko et al. 2005; Thiergart et al. 2012) the higher rates are likely to be
relevant to the inference of some relationships in the supertree.

Having established the relevance of our simulated rates of LGT, we then assessed the
ability of different supertree algorithms to recover the correct organismal history based on
400 analysis of the gene trees. Figure 6 shows the mean SPR difference between the simulated
species histories and the RF supertree, SPR supertree, SPR supertree seeded with an MRP
starting tree, and SPR supertree seeded with the correct species tree. SPR supertrees were
significantly more similar to the simulated species tree than RF supertrees for the LGT rates seen
in our bacterial dataset and higher ($p < 0.05$ for random LGT rates of 0.2-1.4 and divergence-
405 biased LGT rates of 0.7,0.8 and 1.0 with a 2-tailed paired student's t-test; $p < 0.01$ for random
LGT rates of 0.2-0.7, 0.9, 1.3, 1.4; the overall results were significant with $p < 10^{-5}$ for both
types of LGT). Seeding the SPR supertree search with an MRP tree did not substantially change
these results. Seeding the SPR supertree search with the correct tree does not substantially
change the results for divergence-biased LGT or plausible rates of random LGT. We see that the
410 SPR supertree and the simulated species tree diverge as the random LGT rate increases, even
when seeded with the species tree. These results suggest that datasets with substantially higher

rates of LGT than our bacterial data would require a better search strategy or a network-based analysis rather than a supertree.

Figure 7 compares the accuracy of SPR and MRP supertrees. As MRP constructs unrooted
415 supertrees, the error is measured here as the minimum SPR distance between the simulated
species history and any rooting of the inferred supertrees. The upper panels of Figure 7 show the
mean supertree error between the simulated species histories and the MRP supertree, SPR
supertree, SPR supertree seeded with an MRP starting tree, and SPR supertree seeded with the
correct species tree. The SPR supertrees were significantly more similar to the simulated species
420 history than the MRP trees under biologically plausible rates of LGT ($p < 0.01$ for random LGT
rates of 0.3-0.5 with a two-tailed paired student's t-test; the divergence-biased results were not
significantly different for individual rates other than 0.6 and 1.0 due to the small supertree error
but were significantly better overall with $p < 0.001$). At higher simulated rates of LGT the
accuracy of SPR supertrees matches that of the MRP trees. We observed that this occurs when
425 the accuracy of the SPR supertree and the SPR supertree seeded with the correct tree diverge,
suggesting that a better search strategy may improve these results. We also examined the
accuracy of RF supertrees with this unrooted measure and found similar results to the unrooted
comparison, that is, SPR supertrees and MRP supertrees were both significantly more similar to
the simulated species tree than the RF supertrees (online Supp. Fig. 4). The lower panels of
430 Figure 7 show the mean supertree error between the simulated species histories and the MRP
supertree and SPR supertrees using our balanced accuracy based simple unrooted comparison
without and with an MRP seed tree. The accuracy of our SPR supertrees when the gene tree roots
are unknown matches that of the MRP trees for plausible rates of LGT but the performance of
our SPR supertrees declines with increasing rates. Using an MRP seed tree prevented this decline

435 which suggests that our initial tree construction step is not well suited to gene trees with
unknown roots. Developing an improved method for building starting trees from unrooted gene
trees could improve these results.

Comparison with MRP and RF Supertrees on Eukaryotic Datasets

440 Bansal et al. (2010) validated their RF supertree approach on a series of eukaryotic datasets
that varied substantially in the number of input trees and total number of taxa. We compared the
accuracy of each supertree method on these datasets as measured by their ability to minimize the
three supertree criteria of SPR distance, RF distance, and parsimony score to the gene trees. In
addition to the three basic methods, we tested a variant of SPR supertrees that uses the RF
445 distance as a secondary optimization criterion to break ties when multiple supertrees have the
same SPR distance, and tested the SPR and RF supertree methods when the MRP supertree was
used as the initial tree. As MRP supertrees are unrooted, we computed the RF and SPR distances
for each rooting of the MRP supertree and show the minimum value. For these tests each
supertree method was run with its default parameters to match the comparisons of Bansal et al
450 (2010) so we used the SPR and RF methods with 25 iterations of SPR rearrangements and the
MRP method with 10 iterations of TBR rearrangements. Due to excessive running times (> 3
days) for the MRP method on the marsupial and legume datasets we disabled the 'multrees'
option on these runs which would otherwise retain multiple trees per iteration.

The performance of each approach according to all optimality criteria is shown in Table 1.
455 Each supertree method was best at minimizing its respective optimization measure, suggesting
that each method has merit and a well-balanced analysis should either include a justification for
the choice of method (e.g. the presence of LGT for the SPR distance) or consider multiple

optimization criteria. The MRP method required the least amount of time and the SPR method the most. However, the SPR method converged rapidly in 3, 1, 5 and 3 iterations on the
460 marsupial, seabird, placental mammal, and legume datasets respectively and thus produced an optimal result in only a fraction of the reported time. Seeding the search with the MRP tree greatly reduced the time required by the SPR method and reduced the resulting parsimony scores at the expense of increasing the SPR distance. Starting with the MRP tree reduced the time required by the RF method and found supertrees with better RF and MRP scores on the
465 marsupial and placental mammal datasets but increased RF and MRP scores on the legume dataset. Using the RF distance as a tie-breaker with the SPR method found lower SPR distances, RF distances and parsimony scores in a shorter period of time over the basic method and avoided an issue with the seabird dataset where many supertrees have the same SPR distance but poor RF distances and parsimony scores. These results suggest that blended methods have merit even
470 when only considering a single optimization criterion. In particular, the SPR distance with RF distance as a tie-breaker should be used when nontrivial amounts of lateral gene transfer are expected.

Comparison of SPR and MRP Supertrees of 244 Bacterial Genomes

475 To contrast with the SPR supertree described above and examine the influence of tree rootings, we constructed an MRP supertree from the 244-taxon bacterial dataset using 25 iterations of an SPR rearrangement search and compared it to our SPR supertree (Fig. 8). The MRP supertree does not recover the same arrangement of hyperthermophiles as the SPR supertree; notably, it places the Epsilonproteobacteria in close proximity to the Aquificae. If we
480 place the root somewhat arbitrarily between the Firmicutes and all other Bacteria, the MRP

485 supertree like the SPR supertree places the Thermotogae and *C. proteolyticus* as sisters, although this pairing is sister to the Synergistetes and not the Deferribacteres in the MRP supertree. The two Nitrospirae are again split, with *Nitrospira* sister to the Deltaproteobacteria and *Thermodesulfovibrio* with the Aquificae and Deferribacteres. As with the SPR supertree, the Deltaproteobacteria are separated from the other Proteobacteria.

490 The rooted nature of MAFs allowed the evaluation of our chosen rooting and alternative rootings on inferring phylogenetic relationships from this dataset. We have already described the MRP supertree rooted to separate the Firmicutes from the other taxa (MRP), the SPR supertree constructed from the 40 largest trees with a monophyletic Aquificae group (40-Aquificae) and the SPR supertree constructed using the SPR-Aquificae supertree (SPR-Aquificae). Three more supertrees were constructed to test the influence of starting topology and rooting. The first was an SPR supertree seeded with the MRP supertree (SPR-MRP). We then rooted the gene trees with both the MRP supertree and SPR-Aquificae tree using our balanced accuracy measure and constructed an SPR supertree from these two sets of rooted gene trees (SPR-MRP-Rooting and 495 SPR-Aquificae-Rooting, respectively).

500 These six supertrees were compared to the two sets of rooted gene trees (see Table 2). The three MRP-rooted supertrees had a much smaller aggregate SPR distance (nearly 11% smaller) to the MRP-rooted gene trees than the Aquificae-rooted supertrees but the three Aquificae-rooted supertrees had a much smaller SPR distance (more than 8% smaller) to the Aquificae-rooted gene trees than the three MRP-rooted supertrees. Thus, it is impossible to determine which supertree is more similar to the gene trees without choosing a specific rooting of the gene trees.

The four SPR supertrees constructed from the full bacterial dataset were compared by measuring their pairwise SPR distances (see Table 3). The two Aquificae-rooted supertrees

505 differed by only 10 SPRs, despite the fact that one was constructed from the 40-Aquificae tree
and the other was constructed with our usual greedy addition procedure and no *a priori*
information other than the gene tree roots. Even more telling, the two MRP-rooted supertrees
were essentially identical, differing by only 2 SPRs. The SPR-MRP-Rooting supertree also
differed from the MRP supertree by only 2 SPRs, so we were able to essentially recover the
MRP supertree just by biasing the gene tree roots. This suggests that MRP infers relationships
510 that are consistent with certain gene tree roots despite not implicitly assuming any rooting. As
these relationships are also inconsistent with plausible alternative roots, it may be that unrooted
supertree methods such as MRP are insufficient to distinguish between controversial
evolutionary hypotheses such as the placement of the Aquificae.

515 DISCUSSION

Large phylogenies are being built from multiple sequence datasets to reconstruct the
histories of many groups of living organisms, and supertrees offer the means to carry this out in a
rigorous fashion. The known limitations of widely used approaches such as MRP have motivated
the development of new strategies, such as the use of Robinson-Foulds distance as an alternative
520 optimality criterion. Although RF is frequently used to assess the dissimilarity of phylogenetic
trees, it is not based on a specific phylogenetic process and can be heavily influenced by shifts in
the position of single taxa. A single LGT event will influence the RF distance (and parsimony
score) in proportion to the number of branches in the path between the donor and recipient
lineages, and many LGT events are likely to confound RF-based supertree inference. The SPR
525 distance is an alternative optimality criterion that is particularly well-suited to analyzing
phylogenomic data where LGT or other reticulate evolutionary processes are expected to play an

important role in generating phylogenetic discordance. Each SPR operation is equivalent to an LGT event, and the degree of separation between donor and recipient in the tree does not influence the SPR score. The SPR distance may thus avoid some of the “phylogenetic compromises” of other supertree methods.

Using simulations, we verified that SPR supertrees were significantly more similar to the known species history than RF supertrees given biologically plausible rates of simulated LGT. The effect was more pronounced for random LGT, which produces more "long-distance" transfers, than for divergence-biased LGT. The improved performance of SPR with random LGT events suggests that penalizing phylogenetic discordance in a manner that is insensitive to the number of impacted bipartitions may be preferable to the alternative RF criterion. However, in the future this assertion should be tested under a wider range of scenarios, with larger trees and different types of phylogenetic discordance modelled. SPR also outperformed MRP in a narrower, but still biologically relevant, range of LGT rates. However, the advantage of SPR disappeared when the gene tree roots were unknown, demonstrating that the obligately rooted SPR approach is influenced by alternative rootings of the reference and gene trees. We also verified that each of the three supertree methods excel at minimizing their respective supertree criteria on a eukaryotic dataset. Combining multiple supertree criteria, such as using the RF distance to break ties in an SPR supertree approach, yielded better results than any method did alone. This finding suggests that combinations of criteria that consider different types of phylogenetic discordance may provide even greater accuracy.

Although the history of bacteria may be better represented with a phylogenetic network than a single tree, the supertree we inferred offers a useful backdrop for the inference of highways of gene sharing. As shown in Figures 2 and 8, both SPR and MRP recovered a

550 majority of bacterial classes as monophyletic groups, regardless of the choice of rooting. Many
of the topological differences between the SPR and MRP supertrees are minor, including subtle
shifts in the position of taxa such as *Nitrospira defluvii* and the Negativicutes. One point of
substantial difference between the two trees related to the controversial placement of Aquificae
and the Epsilonproteobacteria: MRP, being unrooted, placed these two groups adjacent to one
555 another, corresponding to a sister relationship under the reasonable assumption that the root of
the supertree is placed somewhere outside of this pairing. When the SPR supertree was rooted to
reflect the MRP tree topology in the manner described above, the two supertrees were nearly
identical; however, if Aquificae were treated as the outgroup then the SPR supertree produced a
topology that placed other groups with many thermophiles, such as Thermotogae, as early
560 branches. These results suggest that unrooted supertree criteria such as MRP provide hypotheses
that are consistent with certain rootings despite not implicitly assuming any rooting.
Furthermore, the Aquificae SPR supertree was much more similar to the Aquificae rooted gene
trees than the MRP supertree, but the MRP supertree was much more similar to the MRP-rooted
trees. It was thus impossible to distinguish between these two hypotheses of Aquificae
565 placement; either could be plausible given knowledge of the correct gene tree roots. This is a
practical example of the fundamental limits of unrooted supertree methods identified by Steel et
al. (2000).

Using the tree in Figure 2 as a basis for LGT inference, we searched for highways of LGT
between classes and genera. Not surprisingly, connections were more frequently associated with
570 specific lineages such as *Clostridium* and interactions between the Proteobacteria and other phyla
varied considerably. In addition, larger gene trees (those shared by many taxa) required
proportionately more transfers to explain, including ribosomal proteins. Such biased LGT could

muddy or completely obscure the vertical evolutionary signal. Our improved SPR algorithm allowed the entire set of >40,000 trees to be reconciled with the supertree in less than one
575 minute: a similar analysis could have been carried out using any rooted reference tree, regardless of what method was used to construct this tree. The rapid inference of LGT highways raises the possibility of using information about lateral connections to construct phylogenetic networks with reticulations explicitly based on major directions of LGT (MacLeod et al. 2005; Nakhleh et al. 2005; Beiko and Hamilton 2006).

580 The scaling of runtimes with the number and size of trees is a central concern in phylogenomics. The analysis of Beiko et al. (2005) required over 20,000 CPU hours to reconcile 22,432 gene trees with a 144-taxon supertree, and the largest trees could not be reconciled at all due to limitations of the breadth-first search of EEEP (Beiko and Hamilton, 2006). Alternative methods of inferring highways of LGT have been proposed based on quartets (Bansal et al.
585 2013), but such methods are limited to finding the most obvious highways and required on the order of two days to analyze the same dataset of 22,432 gene trees. Repeated applications of SPR distances in large phylogenomic data sets were heretofore not feasible due to the complexity of the algorithm, but our efficient new methods for computing the SPR distance made the computation of these supertrees feasible even for hundreds of taxa and tens of thousands of gene
590 trees. Of particular importance is the adaptation of the clustering strategy of Linz and Semple (2011) to subdivide the construction of a MAF for a given pair of trees. Clustering yields no improvement in theoretical runtime, because there is no guarantee that >1 cluster will be identified between a pair of trees. However, our results clearly demonstrate that clustering is effective in practice, because LGT connections are not random and consistent partitioning can
595 usually be identified and used as the basis for subdivision. We are optimistic that our approach

will be applicable to much larger phylogenomic data sets with thousands of taxa, for two reasons: first, our fixed-parameter algorithm scales exponentially with the *distance* between a pair of trees and not their *size*; and second, as the timing results of Figure 5 suggest, clustering increases the speed of the algorithm and reduces the rate of increase of running times with increasing SPR distance. With only a small number of exceptions, all trees with SPR distance < 60 were resolved in less than one second, with the time of MAF construction dominated by the single cluster with the largest distance. We expect that most large trees will have a cluster size distribution similar to that of the trees we tested here; consequently the size of the largest cluster and the corresponding computational burden may increase only slightly. This hypothesis remains to be tested on larger phylogenomic data sets.

Our methods could be expanded and refined in several ways. As we identified in our results, our current supertree search method could potentially be improved with a better strategy for constructing the initial guide tree such as SuperFine (Swenson et al. 2012), methods for avoiding local optima such as ratchet searches, or using prior knowledge to constrain the supertree search (Wehe et al. 2012). An RF supertree method has been recently proposed for multi-labelled gene trees (Chaudhary et al. 2013); extending our SPR distance algorithms to accept such trees would enable their inclusion in SPR supertrees. The rooting problem remains to be resolved. While in many cases rooting can be performed using an appropriate outgroup taxon, the bacterial case considered here lacks an obvious outgroup: the Archaea could be used to root the Bacteria and vice versa, but many gene trees have shown evidence of interdomain LGT and rooting between domains may be invalid or even impossible. Finally, our approach considers only the history of observed genes, and does not attempt to account for processes such as gene duplication and loss. Methods of reconciling multiple evolutionary processes such as

620 duplications, losses, transfers and incompatible lineage sorting (ILS) show a great deal of
promise (Bansal et al. 2012; Szölloosi et al. 2012), but are currently limited to smaller datasets
(Stolzer et al. 2012).

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Table 1: Experimental results comparing the performance of the SPR supertree method to RF and MRP supertree methods. Six analyses are shown: The SPR supertree method starting from an SPR greedy addition tree (SPR) or MRP supertree (SPR-MRP), the SPR supertree method breaking ties with the RF distance using a greedy addition tree (SPR-RF-TIES), the RF supertree method starting from random addition sequence trees (RF-Ratchet) or MRP supertree (RF-MRP), and MRP with TBR global rearrangements (MRP-TBR). The best optimization criteria or running times for a dataset are shown in bold.

Data Set	Supertree Method	SPR Distance	RF-Distance	Parsimony Score	Time (s)
Marsupial (267 taxa; 158 trees)	SPR	382	1604	2203	1097.79
	SPR-RF-TIES	373	1536	2149	767.01
	SPR-MRP	380	1534	2126	219.64
	RF-Ratchet	394	1520	2145	2150.30
	RF-MRP	379	1502	2116	2044.07
	MRP-TBR	379	1514	2112	20.52
Sea Birds (121 taxa; 7 trees)	SPR	17	109	235	31.15
	SPR-RF-TIES	17	63	208	29.44
	SPR-MRP	17	61	208	2.04
	RF-Ratchet	17	61	208	10.43
	RF-MRP	17	61	208	9.16
	MRP-TBR	17	61	208	1.03
Placental Mammals (116 taxa; 726 trees)	SPR	1715	5908	8946	5561.84
	SPR-RF-TIES	1713	5902	8934	5040.03
	SPR-MRP	1713	5876	8921	1819.08
	RF-Ratchet	1790	5738	8827	801.92
	RF-MRP	1780	5692	8810	659.32
	MRP-TBR	1783	5702	8809	34.27
Legumes	SPR	108	651	1175	21130.08

(558 taxa; 19 trees)	SPR-RF-TIES	92	471	1037	12376.00
	SPR-MRP	110	511	903	276.49
	RF-Ratchet	117	401	1102	1349.56
	RF-MRP	130	429	1068	1558.60
	MRP-TBR	140	519	891	579.76

Table 2: Aggregate SPR distance to supertrees constructed from different rootings of the bacterial protein trees. Six different construction methods were compared: The MRP supertree (MRP), the SPR supertree constructed from the 40 largest trees with a monophyletic Aquificae group (40-Aquificae), the SPR supertrees constructed using the MRP supertree (SPR-MRP) or SPR-Aquificae supertree (SPR-Aquificae), and the SPR supertrees constructed by only rooting the gene trees using the MRP supertree (SPR-MRP-Rooting) or SPR-Aquificae tree (SPR-Aquificae-Rooting) and building a greedy addition supertree. Each supertree was compared to the MRP rooted gene trees or SPR-Aquificae rooted gene trees with the SPR distance.

MRP rooted gene trees		SPR-Aquificae rooted gene trees	
	SPR Distance		SPR Distance
SPR-MRP-Rooting	52867	SPR-Aquificae-Rooting	53534
SPR-MRP	52896	SPR-Aquificae	54488
MRP	52896	40-Aquificae	55570
SPR-Aquificae-Rooting	58539	SPR-MRP-Rooting	58023
SPR-Aquificae	59561	SPR-MRP	58057
40-Aquificae	60611	MRP	58057

Table 3: Dissimilarity of supertrees constructed from the same rooting of bacterial protein trees. We compared the minimal SPR distance between any rooting of the SPR supertree constructed from the 40 largest trees with a monophyletic Aquificae group (40-Aquificae), the SPR supertrees constructed using the MRP supertree (SPR-MRP) or SPR-Aquificae supertree (SPR-Aquificae), and the SPR supertrees constructed by only rooting the gene trees using the MRP supertree (SPR-MRP-Rooting) or SPR-Aquificae tree (SPR-Aquificae-Rooting) and building a greedy addition supertree.

	SPR-Aquificae	SPR-Aquificae-Rooting	SPR-MRP	SPR-MRP-Rooting
SPR-Aquificae	0	10	34	33
SPR-Aquificae-Rooting	10	0	27	25
SPR-MRP	34	27	0	2
SPR-MRP-Rooting	33	25	2	0

FIGURE LEGENDS

Figure 1: The equivalence between the SPR distance and MAF size. (a) The species tree S and gene tree G differ only in the placement of the grey subtree. The roots of these trees are denoted by ρ . (b) The MAF of S and G is produced by cutting the dotted edge in both trees. (c) Each component of an MAF other than the component containing ρ represents an SPR move. A single SPR move transforms S into G by moving the grey subtree in S to its position in G . (d) Each SPR move models an LGT event in the reverse direction. From the MAF of S and G we infer that a transfer of gene G has occurred from an ancestor of taxon 1 to an ancestor of taxon 4.

Figure 2. SPR supertree constructed using Aquificae as outgroup. Genera such as *Mycobacterium* with multiple representatives are shown as collapsed subtrees for brevity. Colours indicate the classes of bacteria.

Figure 3. Inferred LGT events between 135 distinct bacterial genera. (a) An LGT heatmap. The coloured side bars indicate class using the colour mapping of Figure 2. The row and column genus order is the same. The number of transfers is shown in a white-yellow-red colour scale with darker colours indicating a higher proportion of transfer events. Colour intensity is relative to the largest number of transfers in a row. Relationships with fewer than 5% of the maximum transfer events for a row or only a single transfer event were filtered out. (b) Each node of the LGT affinity graph represents a bacterial genus, colored by class and scaled relative to the number of genomes representing that genus (1-15). Two genera are connected by an edge if the number of inferred LGT events between them exceeds 5% of the number of homologous genes

common to both genomes. The shade of an edge is proportional to this ratio of LGT events to common genome size; black edges indicate relationships with at least as many LGT events as the size of their common genome. The thickness of an edge scales relative to the actual number of inferred transfers (between 2 and 370) with thicker edges indicating more transfers. The graph is shown with a spring-loaded layout.

Figure 4: Mean time required to compare gene trees with a given SPR distance from an SPR supertree of a 244-genome dataset. The time axis is on a log scale as the time required increases exponentially with the SPR distance. The left panel compares our previous ($2.42^k n$) and new ($2^k n$) algorithms, with (C) and without clustering, on the set of binary trees. The right panel compares our new algorithm with and without clustering on the set of trees with unsupported bipartitions collapsed. Note that collapsing bipartitions reduces the SPR distance.

Figure 5: A comparison of our LGT rate simulation parameter to the bacterial dataset. Supertrees of empirical data have the same mean SPR distance to leaf ratio (within 95% confidence intervals) as our simulations with a random LGT rate less than 0.2 and a divergence-biased LGT rate less than 0.4.

Figure 6: A comparison of the mean supertree error (as measured by the SPR distance) of RF supertrees (RF) to SPR supertrees using the default parameters (SPR), seeded with an MRP starting tree (SPR-MRP), or seeded with the correct tree (SPR-C).

Figure 7: A comparison of the accuracy of SPR and MRP supertrees with known or unknown gene tree roots. The upper panels compare the mean supertree error (as measured by the minimal SPR distance to any rooting of a supertree) when the gene trees are correctly rooted. We compared MRP supertrees (MRP) to SPR supertrees using the default parameters (SPR), seeded with an MRP starting tree (SPR-MRP), or seeded with the correct tree (SPR-C). The lower panels compare the mean error of the MRP supertree to SPR supertrees when the gene tree roots are unknown, using our balanced accuracy based simple unrooted comparison without and with an MRP seed tree (SPR-SU and SPR-MRP-SU, respectively).

Figure 8: Comparison of SPR and MRP supertrees of 244 bacterial genomes. The SPR supertree on the left was constructed with the Aquificae as outgroup while the MRP supertree on the right is unrooted and places the Aquificae as neighbours of the Epsilonproteobacteria. Both figures show the largest monophyletic group of each class as a collapsed subtree and all members of a given class with the same color.

Supplemental Figure 1. Inferred LGT events between 13 bacterial classes. (a) LGT heatmap. The colour side bars indicate class. The row and column order is the same. The number of transfers is shown in a white-yellow-red colour scale with darker colours indicating a higher proportion of transfer events. Colour intensity is relative to the largest number of transfers in a row.

Relationships with fewer than 5% of the maximum transfer events for a row or only a single transfer event were filtered out. (b) LGT affinity graph of the bacterial classes. Each node of the graph represents a bacterial class scaled relative to the number of represented taxa (2-75). Two genera are connected by an edge if the number of inferred LGT events between them exceeds 5%

of their shared genes. The shade of an edge is proportional to this ratio of LGT events to shared genes; black edges indicate relationships with at least as many LGT events as shared genes. The thickness of an edge scales relative to the actual number of inferred transfers (30-1414) with thicker edges indicating more transfers.

Supplemental Figure 2: The LGT affinity neighbourhood of genus *Clostridium*. Each node of the graph represents a bacterial genus coloured by class and scaled relative to the number of represented taxa (1-13). Two genera are connected by an edge if the number of inferred LGT events between them exceeds 5% of their shared genes. The shade of an edge is proportional to this ratio of LGT events to shared genes; black edges indicate relationships with at least as many LGT events as shared genes. The thickness of an edge scales relative to the actual number of inferred transfers (2-125) with thicker edges indicating more transfers.

Supplemental Figure 3: A comparison of the accuracy of SPR, RF and MPR supertrees as measured by the minimal SPR distance between simulated species histories and any rooting of the supertree under varying rates of random or divergence-biased simulated LGT events.

APPENDIX 1: FAST MAF ALGORITHM

In this appendix we discuss the efficiency and practicality improvements of our new MAF algorithm. We first introduce our previous algorithm (Whidden et al. 2010; Whidden et al. 2013a) whose running time is bounded by $O(2.42^k n)$ for two binary trees with n leaves and an SPR distance of k . We then introduce our novel concept of “protecting” edges during the search for an MAF. This “edge protection” scheme allows us to avoid exploring the same edge cutting scenarios multiple times and greatly speeds up the search for an MAF, as we demonstrated in Figure 5. In a forthcoming paper (Whidden and Zeh 2013) we give the full details of this algorithm and prove that its running time is bounded by $O(2^k n)$. Finally, we explain how we extended our algorithm to compute MAFs of a binary and multifurcating tree and thereby account for uncertainty in the gene trees input to our supertree method. In a recently submitted manuscript (Whidden et al. 2013b) we gave the full details of this algorithm as applied to two multifurcating trees and proved that its running time remains bounded by $O(2.42^k n)$. However, by requiring that one tree be binary and applying edge protection our new MAF algorithm requires roughly the same time in practice to compute an MAF regardless of whether the other tree is multifurcating, as we demonstrated in Figure 5.

Previous MAF Algorithm.—Our previous MAF algorithm (Whidden et al. 2010; Whidden et al. 2013a) takes two binary trees T_1 and T_2 as input along with a parameter k and returns an agreement forest with at most $k+1$ components (and thus k edge cuts) if and only if such an agreement forest exists. To find an MAF, we run this algorithm with increasing values of k from 0 until an agreement forest is found. Since the running time of the algorithm scales exponentially with k , this entire procedure only takes a small constant factor more time than the invocation that

finds the MAF. Our algorithm proceeds in a bottom-up fashion from the leaves of T_1 . T_1 remains a tree through this procedure but T_2 may become a forest, denoted F_2 . We maintain a set of
 835 *sibling pairs*, sibling subtrees (a,c) in T_1 such that identical subtrees a and c exist in F_2 . The algorithm examines each such sibling pair in turn and applies one of three cases:

- (1) If a and c are also siblings in F_2 , then the subtree rooted at their parent is identical in T_1 and F_2 and so becomes a candidate for membership in a sibling pair,
- 840 (2) If a or c is a component of F_2 then it must be cut off in T_1 ,
- (3) We identify at most 3 sets of edges in F_2 such that cutting one of these edge sets will lead to an MAF and try each edge set recursively in turn.

Case (3), which defines multiple edge sets to consider for cutting, requires detailed
 845 explanation. Assume that a is the deeper subtree of F_2 , if a and c are in the same component, and let b be the sibling of a in F_2 . If a and c are in separate components of F_2 then cutting off a or c will lead to an MAF. If a and c are in the same component but only one subtree, b , is on the path between them then cutting off b will always lead to an MAF. Otherwise, cutting off a , c , or simultaneously cutting off all of the subtrees between a and c in F_2 will lead to an MAF. Note
 850 that this last case is the worst case of our algorithm as it splits our computation into three branches cutting one, one, or at least two edges respectively. We previously showed in Whidden et al. (2010) that this last case bounds our running time of $O(2.42^k n)$ with a recurrence relation analysis.

New MAF Algorithm.—Our improved algorithm introduces the concept of *edge protection*
 855 to alleviate the bottleneck of the 3-way branching case of our previous MAF algorithm. Observe that if some MAF can be found by a recursive invocation of this case that cuts off subtree a in F_2 then an MAF will be found by this invocation. Thus, we can assume that cutting off subtree a does not lead to an MAF in the recursive invocation that cuts off subtree c , or we would have

860 already found it. We *protect* edge a in this search branch to denote this and ignore any recursive
invocations that cut a protected edge. By ignoring these search paths we reduce the running time
of the algorithm to $O(2^k n)$. The proof of this bound is highly technical, as it relies on showing
that this edge protection either forces our best case, cutting subtree b without branching, or
avoids enough search branches to achieve this bound and requires some additional boundary
cases. In a forthcoming paper (Whidden and Zeh 2013) we will provide the full details of our
algorithm and prove this bound.

870 We have also developed a theory for MAFs of multifurcating trees to incorporate
uncertainty in gene trees. In a recently submitted manuscript (Whidden et al. 2013b) we
developed a general MAF algorithm for two multifurcating trees. This algorithm is based on our
 $O(2.42^k n)$ algorithm for binary trees and achieves the same running time but is significantly
more complicated and requires many more cases. For the purposes of constructing SPR
supertrees, however, we only need to allow that the gene trees be multifurcating; the supertree is
binary. By requiring that T_1 be binary in our MAF algorithm these extra cases disappear and we
can use the same overall algorithm structure but with the ability to resolve multifurcations as
well as cut edges. Our MAF algorithm when T_2 is multifurcating still examines each sibling pair
in turn and applies one of three cases:

- 880 (1) if a and c are also siblings in F_2 , then either the subtree rooted at their parent is
identical in T_1 and F_2 and so becomes a candidate for membership in a sibling
pair or we resolve the multifurcation of their parent in F_2 to separate them so
that this occurs.
- (2) If a or c is a component of F_2 then it must be cut off in T_1 .
- (3) We identify at most 3 sets of edges in F_2 such that cutting one of these edge
sets will lead to an MAF and try each edge set recursively in turn.

885 We again assume that a is the deeper subtree of F_2 , if a and c are in the same component. Since F_2 is multifurcating, a may now have multiple siblings and we represent them collectively by B which we call a pendant subtree. If a and c are in separate components of F_2 then cutting off a or c will again lead to an MAF. If a and c are in the same component separated only by B then either cutting off c or resolving B separately from a and cutting the introduced edge will lead to
890 an MAF. Otherwise, cutting off a , c , or resolving and cutting off all pendant subtrees of the path from a to c in F_2 will lead to an MAF. We further apply edge protection to this last case as in our improved binary algorithm. Note that this procedure is essentially identical to our prior binary algorithm with the exception that our previous best case, where we could bring a and c together in F_2 with a single cut now requires us to branch into two possibilities. Fortunately, cutting off c
895 is never necessary when a 's parent is binary, that is, B is a single node b , so this has a negligible running time impact in practice, as we demonstrated in Figure 5. This does, however, preclude the argument we used to prove that edge protection reduces the running time of the binary MAF algorithm to $O(2^k n)$ so the running time of our MAF algorithm when one tree is multifurcating remains $O(2.42^k n)$ in the worst case.

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APPENDIX 2: LINEAR-TIME CLUSTER REDUCTION

In this appendix we explain how to accelerate the computation of MAFs (and, thus, the SPR distance) using the Cluster Reduction of Linz and Semple (2011). This reduction partitions the input trees into pairs of subtrees, or clusters, that can be solved iteratively and reassembled
905 into a full solution. The time required to solve these clusters with our MAF algorithms scales exponentially with the maximum number of components in an MAF of any cluster rather than the full MAF of the trees so this strategy greatly accelerates the recovery of MAFs in practice.

The Cluster Reduction as originally formulated is only suitable to compute an MAF variant, weighted MAFs, that cannot be computed with our algorithms. We first extend the Cluster
 910 Reduction to apply to ordinary MAFs and then show how to identify clusters in linear time, greatly improving on the previous cubic time algorithm.

Linz and Semple defined a *cluster* of two trees T_1 and T_2 to be a pair of subtrees T_1^e and T_2^f , for appropriate edges e in T_1 and f in T_2 such that both trees have the same set of labelled
 915 (T_1^t, T_2^t) , (T_1^ρ, T_2^ρ) defined inductively as follows: if $t = 0$, then $T_1^\rho = T_1$ and $T_2^\rho = T_2$. If $t > 0$ then (T_1^1, T_2^1) is a cluster of T_1 and T_2 with at least two taxa, the roots of T_1^1 and T_2^1 are labelled with a new label ρ_1 , and $(T_1^2, T_2^2), \dots, (T_1^t, T_2^t), (T_1^\rho, T_2^\rho)$ is a cluster sequence of the two trees obtained from T_1 and T_2 by replacing the subtrees T_1^1 and T_2^2 with a single labelled leaf a_1 . This is illustrated in Figure A1. Clearly, ρ is the root of T_1^ρ and T_2^ρ . An agreement forest F of T is the
 920 disjoint union of forests $F = F_1 \cup F_2 \cup \dots \cup F_t \cup F_\rho$, where F_i is an agreement forest of T_1^i and T_2^i , for all i in $\{1, 2, \dots, t, \rho\}$. The weight of F is defined to be $w(F) = |F| - |\{(p_i, a_i): p_i \text{ and } a_i \text{ are singletons in } F\}| - t$, where $|F|$ denotes the number of trees in F . We say that F is an MAF of T if it has minimum weight among all agreement forests of T . The key result proved by Linz and Semple is that the weight of an MAF of any cluster sequence is exactly the number of
 925 components in an MAF of the original trees. They also provided a divide-and-conquer approach for computing an MAF of T : Process the clusters in order, for each i computing an agreement forest F_i of T^i and T_2^i . If $F = F_1 \cup F_2 \cup \dots \cup F_{i-1}$ is the union of forests computed so far (for $i=\rho$, let $i-1=t$), then F_i is computed to be an agreement forest of T^i and T^i that minimizes $w(F_i) = |F_i| - |\{(p_j, a_j): p_j \text{ is a singleton in } F \text{ and } a_j \text{ is a singleton in } F_i\}|$. This weight corrects for the fact that
 930 we have cut the same edge twice; p_j and a_j are nodes introduced by the cluster reduction to

represent the intersection of two clusters so the edge below ρ_j and above a_j are the same edge.

Thus, for $i \neq p$, we choose F_i to be an agreement forest of T_1^i and T_2^i that minimizes this weight and such that p_i is a singleton, if possible, to capitalize on this correction. The final forest defined in this way is an MAF of T .

935 We used the key observation of the cluster reduction, that it is best to cut the root edge of each cluster when possible, to modify this procedure to compute unweighted MAFs. We first compute the cluster sequence as above. We then apply a modification (described below) of our MAF algorithm that returns an MAF of the current cluster such that it has the root edge cut if and only if any MAF of the current cluster i has an isolated ρ_i . If the root edge, below ρ_i , was cut in this MAF then we separate the two clusters by simply cutting the edge above a_i in its
940 corresponding cluster and then removing a_i and ρ_i completely to avoid counting this double cut. If the root edge is not cut then we reattach the two clusters by cutting this root edge, removing ρ_i , and then replacing a_i with the subtree formerly rooted by ρ_i (thereby removing this subtree from the agreement forest of the current cluster). We apply this procedure iteratively to the
945 cluster sequence and then take the union of these forests as our MAF. We have removed each ρ_i and a_i so this is an unweighted MAF. To see that this is indeed an MAF, observe that we apply the same procedure as Linz and Semple for each cluster other than our treatment of ρ_i and a_i . If ρ_i is not isolated in a given cluster, then we remove one component from our forest by replacing a_i , whereas the weighted algorithm applies a weight of -1 (from the $-t$ factor) to compensate. If ρ_i is
950 isolated in a given cluster then we remove ρ_i (equivalent to the -1 weight) and remove a_i (equivalent to the singleton portion of the weight calculation, this reduces the weight by 1 if p_i and a_i are singletons in some weighted MAF). Thus, our computed forest has exactly as many components as the weight of some weighted MAF and is indeed an MAF.

We now explain how we modified our MAF algorithm to prefer MAFs with isolated roots.

955 Recall that each recursive step of our algorithm identifies at most three edge sets to cut from the intermediate forests and tries each edge set in turn. If more than one of these edge set choices lead to an MAF then our algorithm arbitrarily chooses one of them. We simply modified our algorithm to instead select between these at most three MAFs by preferring MAFs with their root edge cut. Since our algorithm does not find all MAFs of the two trees, it is not immediately
960 obvious that this change is sufficient to find one MAF where the root edge is cut if such an MAF exists. However, the correctness proof of our previous MAF algorithm (Whidden et al. 2013a) and our forthcoming correctness proofs start with an arbitrary agreement forest F and construct an agreement forest F' from F that has no more components than F and such that our algorithms find F' . If we choose F to be an agreement forest where ρ_i is a singleton, then this construction
965 ensures that F' also contain ρ_i as a singleton. In other words, if there exists an MAF that has ρ_i as a singleton, our algorithms find one such MAF.

Finally, we developed a linear-time algorithm for computing a cluster sequence, greatly improving on the naïve cubic algorithm. Let n be the number of leaves in T_1 and T_2 . The cubic algorithm compares each of the subtrees of T_1 , starting at the leaves, to each subtree of T_2 and
970 appends each found cluster to the cluster sequence. There are $O(n)$ subtrees in each tree and it takes $O(n)$ time to compare two leaf sets so this procedure requires $O(n^3)$ time. We improve on this by using least common ancestors (LCAs). The LCA of two or more nodes in a tree is their common ancestor furthest from the root. Let s_1 be a subtree of T_1 with leaf set L_1 and s_2 be a subtree of T_2 with leaf set L_2 . Observe that these subtrees have the same leaf set if and only if the
975 LCA of L_1 in T_2 is s_2 and the LCA of L_2 in T_1 is s_1 . Efficient least common ancestor (LCA) query structures exist (e.g., Bender and Farach-Colton 2000) that can be built in $O(n)$ time and

that allow for constant time LCA queries of two nodes. We use such a structure to compute a mapping M of T_1 subtrees to the LCAs of their leaf sets in T_2 . First, for each leaf x in T_1 , we set $M(x)$ to the corresponding leaf x of T_2 . Then, for any node n of T_1 with children c_1 and c_2 such
980 that the mapping $M(c_1)$ and $M(c_2)$ have been defined, we compute $M(n) = \text{LCA}(M(c_1), M(c_2))$. We apply this procedure again with T_1 and T_2 reversed to compute the mapping M^{-1} of T_2 subtrees to the LCAs of their leaf sets in T_1 . Finally, for each subtree s_1 of T_1 in a bottom-up postorder traversal we check if s_1 is a cluster by checking if $M^{-1}(M(s_1)) = s_1$ and, if so, appending s_1 and $M(s_1)$ to the cluster sequence.

Supplemental Table 1: List of 244 bacterial genomes included in this work.

Class	Taxon
Actinobacteria	<i>Acidimicrobium ferrooxidans</i> DSM 10331
	<i>Acidothermus cellulolyticus</i> 11B
	<i>Amycolatopsis mediterranei</i> U32
	<i>Arcanobacterium haemolyticum</i> DSM 20595
	<i>Arthrobacter aurescens</i> TC1
	<i>Arthrobacter</i> sp. FB24
	<i>Beutenbergia cavernae</i> DSM 12333
	<i>Bifidobacterium adolescentis</i> ATCC 15703
	<i>Bifidobacterium animalis</i> subsp. lactis AD011
	<i>Bifidobacterium animalis</i> subsp. lactis BI-04
	<i>Bifidobacterium longum</i> NCC2705
	<i>Bifidobacterium longum</i> subsp. infantis ATCC 15697
	<i>Bifidobacterium longum</i> subsp. longum JDM301
	<i>Catenulispora acidiphila</i> DSM 44928
	<i>Cellulomonas flavigena</i> DSM 20109
	<i>Clavibacter michiganensis</i> subsp. michiganensis NCPPB 382
	<i>Corynebacterium aurimucosum</i> ATCC 700975
	<i>Corynebacterium efficiens</i> YS-314
	<i>Corynebacterium glutamicum</i> ATCC 13032 DSM 20300
	<i>Corynebacterium glutamicum</i> R
	<i>Corynebacterium jeikeium</i> K411
	<i>Corynebacterium kroppenstedtii</i> DSM 44385
	<i>Corynebacterium pseudotuberculosis</i> FRC41
	<i>Corynebacterium urealyticum</i> DSM 7109
<i>Cryptobacterium curtum</i> DSM 15641	
<i>Eggerthella lenta</i> DSM 2243	
<i>Frankia alni</i> ACN14a	
<i>Gardnerella vaginalis</i> 409-05	
<i>Geodermatophilus obscurus</i> DSM 43160	
<i>Gordonia bronchialis</i> DSM 43247	
<i>Jonesia denitrificans</i> DSM 20603	
<i>Kribbella flavida</i> DSM 17836	

Kytococcus sedentarius DSM 20547
Leifsonia xyli subsp. *xyli* str. CTCB07
Mobiluncus curtisii ATCC 43063
Mycobacterium avium 104
Mycobacterium avium subsp. *paratuberculosis* K-10
Mycobacterium bovis AF2122/97
Mycobacterium bovis BCG str. Pasteur 1173P2
Mycobacterium bovis BCG str. Tokyo 172
Mycobacterium gilvum PYR-GCK
Mycobacterium leprae Br4923
Mycobacterium leprae TN
Mycobacterium marinum M
Mycobacterium smegmatis str. MC2 155
Mycobacterium sp. KMS
Mycobacterium tuberculosis F11
Mycobacterium tuberculosis H37Ra
Mycobacterium tuberculosis H37Rv
Mycobacterium vanbaalenii PYR-1
Nakamurella multipartita DSM 44233
Nocardia farcinica IFM 10152
Nocardioides sp. JS614
Propionibacterium acnes KPA171202
Propionibacterium freudenreichii subsp. *shermanii* CIRM-BIA1
Rhodococcus erythropolis PR4
Rhodococcus jostii RHA1
Rothia mucilaginosa DY-18
Salinispora arenicola CNS-205
Salinispora tropica CNB-440
Sanguibacter keddieii DSM 10542
Segniliparus rotundus DSM 44985
Slackia heliotrinireducens DSM 20476
Stackebrandtia nassauensis DSM 44728
Streptomyces avermitilis MA-4680
Streptomyces griseus subsp. *griseus* NBRC 13350
Streptomyces scabiei 87.22

Streptosporangium roseum DSM 43021
Thermobifida fusca YX
Thermobispora bispora DSM 43833
Thermomonospora curvata DSM 43183
Tropheryma whipplei TW08/27
Tsukamurella paurometabola DSM 20162
Xylanimonas cellulosilytica DSM 15894

Alphaproteobacteria

Bradyrhizobium sp. BTAi1
Candidatus Hodgkinia cicadicola Dsem
Candidatus Pelagibacter ubique HTCC1062
Ehrlichia canis str. Jake
Ehrlichia chaffeensis str. Arkansas
Erythrobacter litoralis HTCC2594
Gluconacetobacter diazotrophicus PAI 5
Mesorhizobium loti MAFF303099
Ochrobactrum anthropi ATCC 49188
Parvularcula bermudensis HTCC2503
Rickettsia akari str. Hartford
Rickettsia canadensis str. McKiel
Rickettsia peacockii str. Rustic
Rickettsia rickettsii str. Sheila Smith
Wolbachia endosymbiont of *Culex quinquefasciatus* Pel

Aquificae

Aquifex aeolicus VF5
Hydrogenobacter thermophilus TK-6
Hydrogenobaculum sp. Y04AAS1
Persephonella marina EX-H1
Sulfurihydrogenibium azorense Az-Fu1
Sulfurihydrogenibium sp. YO3AOP1
Thermocrinis albus DSM 14484

Bacilli

Bacillus anthracis str. Sterne
Bacillus cereus 03BB102
Bacillus cereus AH187
Bacillus cereus ATCC 10987
Bacillus cereus G9842
Bacillus cereus Q1

Bacillus clausii KSM-K16
Bacillus thuringiensis BMB171
Bacillus thuringiensis str. Al Hakam
Enterococcus faecalis V583
Exiguobacterium sibiricum 255-15
Exiguobacterium sp. AT1b
Geobacillus sp. WCH70
Lactobacillus acidophilus NCFM
Lactobacillus casei ATCC 334
Lactobacillus casei str. Zhang
Lactobacillus crispatus ST1
Lactobacillus reuteri JCM 1112
Lactobacillus rhamnosus Lc 705
Lactobacillus salivarius UCC118
Lactococcus lactis subsp. cremoris MG1363
Leuconostoc kimchii IMSNU 11154
Listeria monocytogenes HCC23
Listeria monocytogenes serotype 4b str. CLIP 80459
Listeria monocytogenes serotype 4b str. F2365
Staphylococcus aureus RF122
Staphylococcus carnosus subsp. carnosus TM300
Staphylococcus lugdunensis HKU09-01
Streptococcus gordonii str. Challis substr. CH1
Streptococcus mitis B6
Streptococcus mutans NN2025
Streptococcus pneumoniae 670-6B
Streptococcus pneumoniae JJA
Streptococcus pyogenes MGAS10270
Streptococcus pyogenes MGAS10394
Streptococcus pyogenes MGAS10750
Streptococcus pyogenes NZ131
Streptococcus pyogenes str. Manfredo
Streptococcus suis 98HAH33
Streptococcus thermophilus LMD-9

Betaproteobacteria

Azoarcus sp. BH72

Bordetella parapertussis 12822
Burkholderia ambifaria MC40-6
Burkholderia sp. 383
Burkholderia vietnamiensis G4
Candidatus *Accumulibacter phosphatis* clade IIA str. UW-1
Gallionella capsiferriformans ES-2
Methylibium petroleiphilum PM1
Methylobacillus flagellatus KT
Methylotenera mobilis JLW8
Methylotenera sp. 301
Nitrosomonas europaea ATCC 19718
Ralstonia pickettii 12D
Ralstonia solanacearum CFBP2957
Thiobacillus denitrificans ATCC 25259

Clostridia

Acetohalobium arabaticum DSM 5501
Acidaminococcus fermentans DSM 20731
Ammonifex degensii KC4
Caldicellulosiruptor obsidiansis OB47
Caldicellulosiruptor saccharolyticus DSM 8903
Caldicellulosiruptor becscii DSM 6725
Clostridiales genomsp. BVAB3 str. UPII9-5
Clostridium acetobutylicum ATCC 824
Clostridium botulinum A str. ATCC 19397
Clostridium botulinum B str. Eklund 17B
Clostridium botulinum Ba4 str. 657
Clostridium botulinum E3 str. Alaska E43
Clostridium cellulovorans 743B
Clostridium difficile CD196
Clostridium kluveri DSM 555
Clostridium kluveri NBRC 12016
Clostridium perfringens ATCC 13124
Clostridium perfringens SM101
Clostridium tetani E88
Clostridium thermocellum ATCC 27405
Coprothermobacter proteolyticus DSM 5265

Desulfotomaculum acetoxidans DSM 771
Eubacterium rectale ATCC 33656
Finegoldia magna ATCC 29328
Halothermothrix orenii H 168
Heliobacterium modesticaldum Ice1
Natranaerobius thermophilus JW/NM-WN-LF
Pelotomaculum thermopropionicum SI
Syntrophothermus lipocalidus DSM 12680
Thermincola potens JR
Thermoanaerobacter mathranii subsp. mathranii str. A3
Thermoanaerobacter tengcongensis MB4
Thermosediminibacter oceani DSM 16646
Veillonella parvula DSM 2008

Deferribacteres

Deferribacter desulfuricans SSM1
Denitrovibrio acetiphilus DSM 12809

Deltaproteobacteria

Anaeromyxobacter dehalogenans 2CP-1
Anaeromyxobacter sp. Fw109-5
Bdellovibrio bacteriovorus HD100
Desulfotalea psychrophila LSv54
Desulfovibrio desulfuricans subsp. desulfuricans str. G20
Desulfovibrio salexigens DSM 2638
Desulfovibrio vulgaris str. Miyazaki F
Desulfurivibrio alkaliphilus AHT2
Geobacter bemidjensis Bem
Geobacter lovleyi SZ
Geobacter uraniireducens Rf4
Lawsonia intracellularis PHE/MN1-00
Pelobacter carbinolicus DSM 2380
Pelobacter propionicus DSM 2379
Sorangium cellulosum So ce 56

Epsilonproteobacteria

Arcobacter nitrofigilis DSM 7299
Campylobacter concisus 13826
Campylobacter jejuni subsp. doylei 269.97
Campylobacter jejuni subsp. jejuni 81116
Campylobacter jejuni subsp. jejuni NCTC 11168

Helicobacter acinonychis str. Sheeba
Helicobacter hepaticus ATCC 51449
Helicobacter mustelae 12198
Helicobacter pylori B38
Helicobacter pylori HPAG1
Helicobacter pylori J99
Helicobacter pylori Shi470
Nautilia profundicola AmH
Nitratiruptor sp. SB155-2

Gammaproteobacteria

Acinetobacter baumannii AB0057
Acinetobacter baumannii ATCC 17978
Actinobacillus pleuropneumoniae serovar 3 str. JL03
Escherichia coli BW2952
Escherichia coli HS
Francisella tularensis subsp. tularensis FSC198
Pseudomonas fluorescens Pf-5
Shewanella halifaxensis HAW-EB4
Shigella flexneri 2a str. 2457T
Xanthomonas albilineans
Xenorhabdus bovienii SS-2004
Yersinia pestis Antiqua
Yersinia pestis CO92

Nitrospirae

Candidatus Nitrospira defluvii
Thermodesulfobivrio yellowstonii DSM 11347

Synergistetes

Aminobacterium colombiense DSM 12261
Thermanaerovibrio acidaminovorans DSM 6589

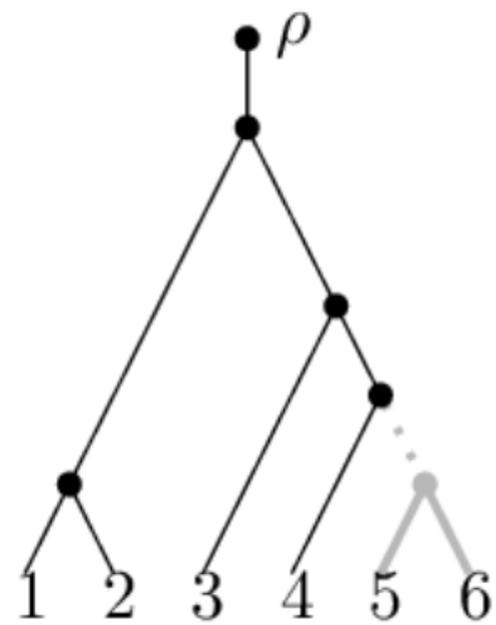
Thermotogae

Fervidobacterium nodosum Rt17-B1
Kosmotoga olearia TBF 19.5.1
Petrotoga mobilis SJ95
Thermosipho africanus TCF52B
Thermosipho melanesiensis BI429
Thermotoga lettingae TMO
Thermotoga maritima MSB8
Thermotoga naphthophila RKU-10
Thermotoga neapolitana DSM 4359

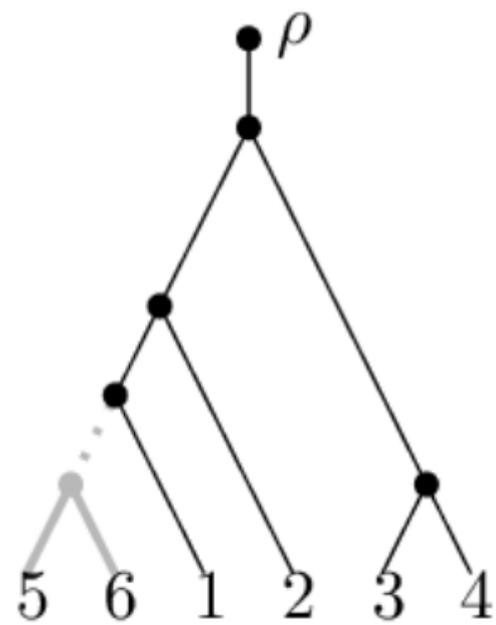
Thermotoga petrophila RKU-1

Thermotoga sp. RQ2

(a)

 S

(b)

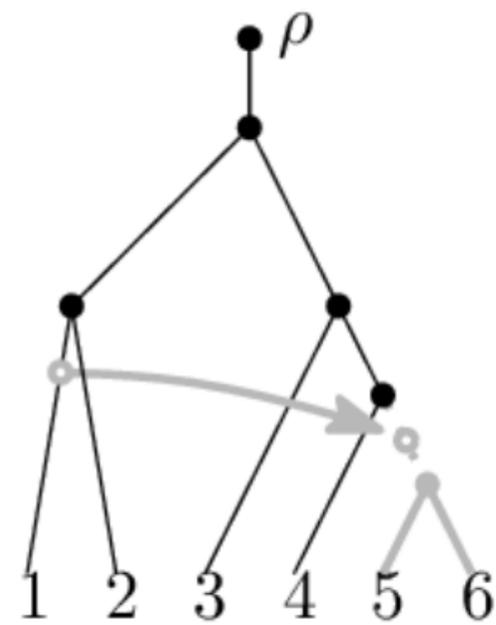
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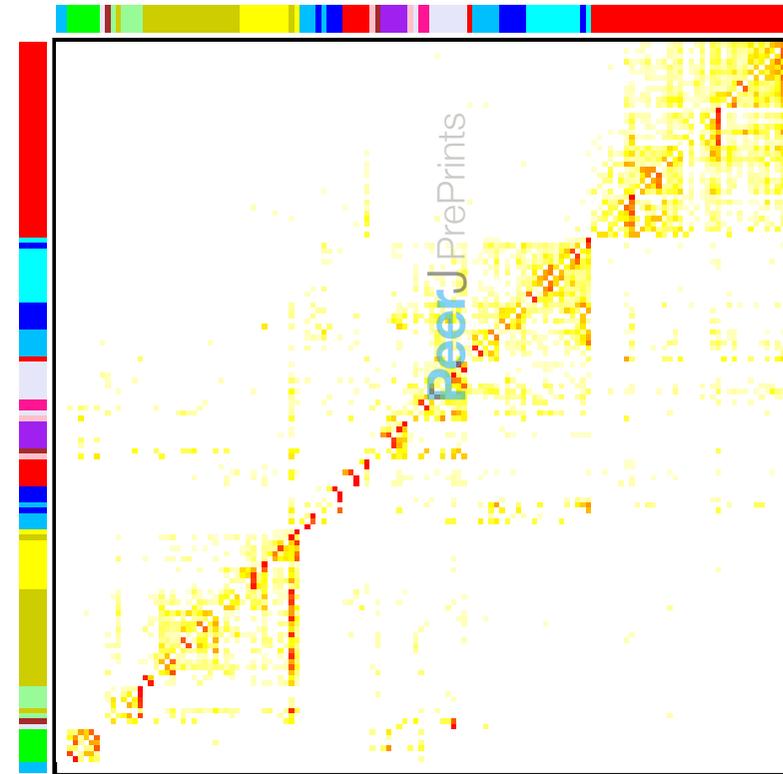
(c)

 SPR

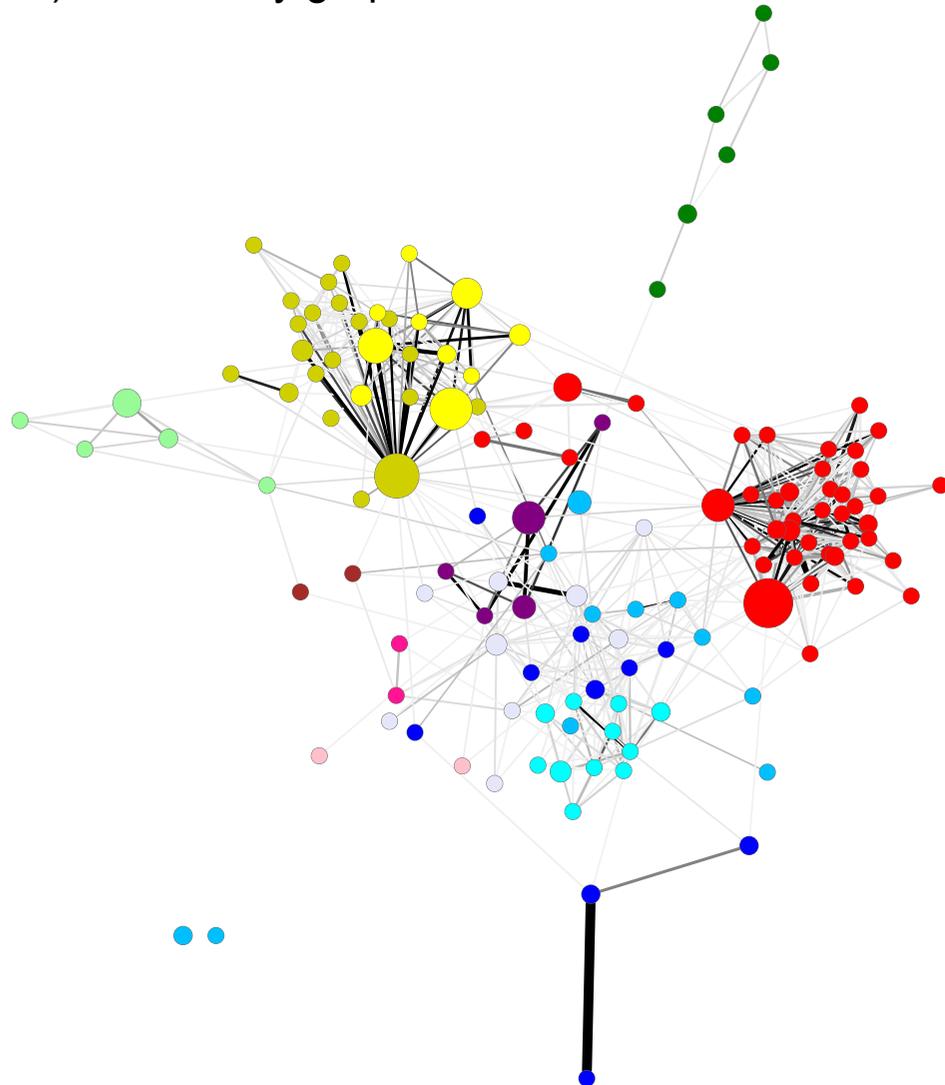
(d)

 LGT MAF

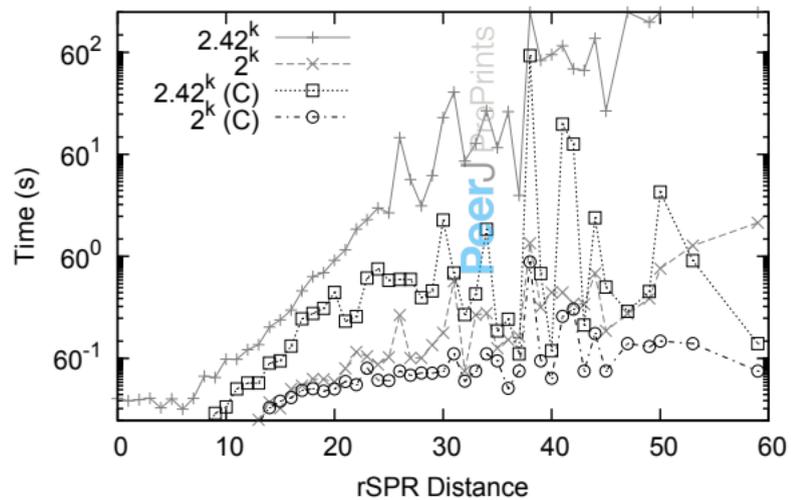
a) LGT heatmap



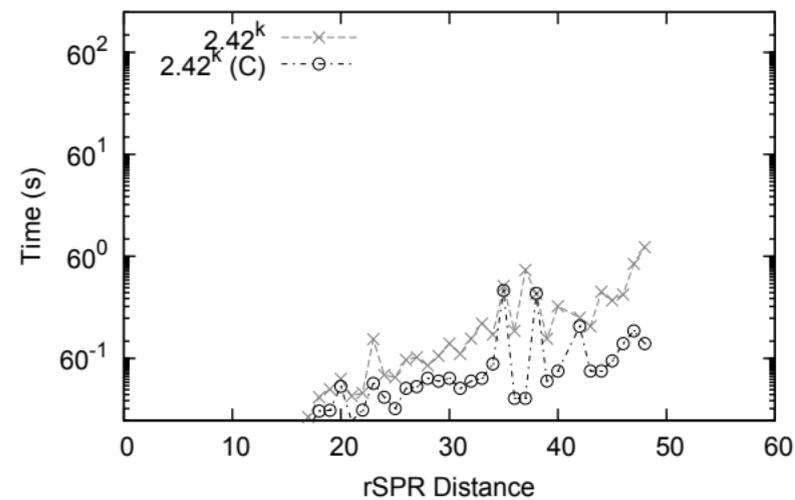
b) LGT affinity graph

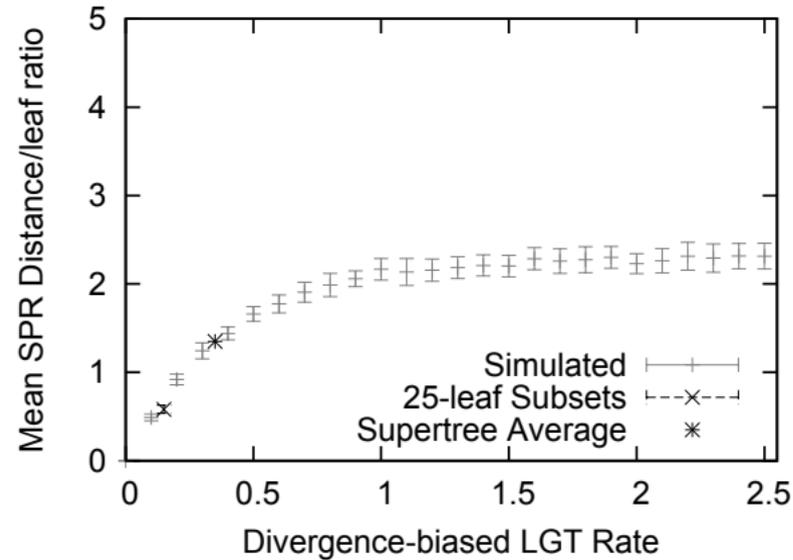
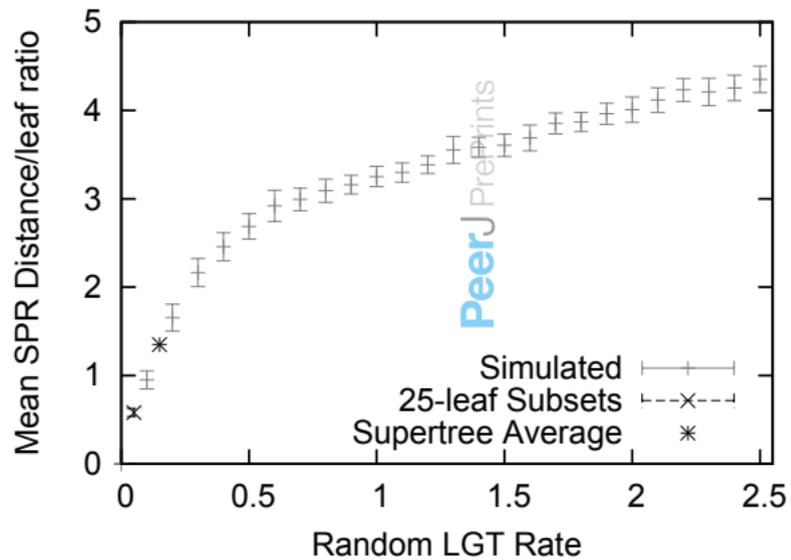


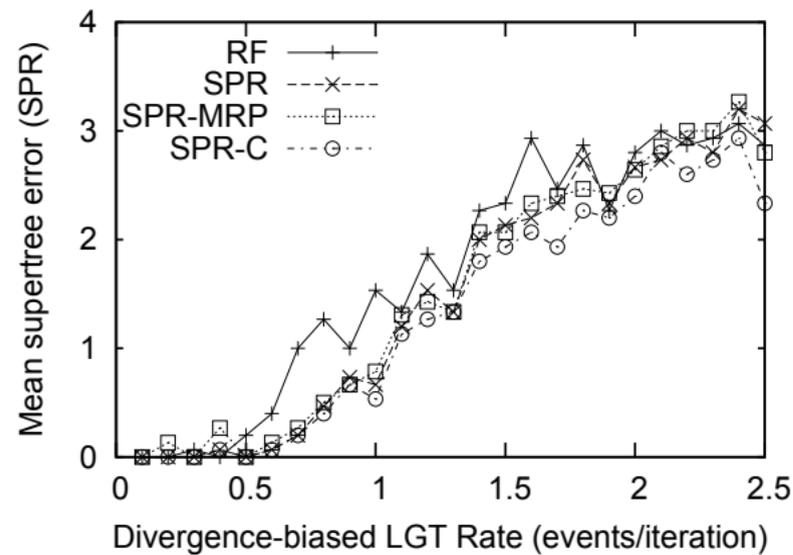
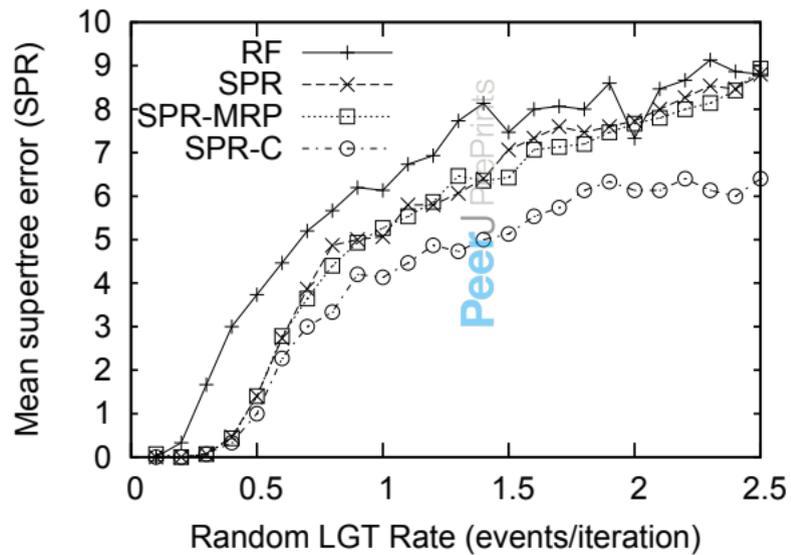
Running Time Comparison (Binary Trees)

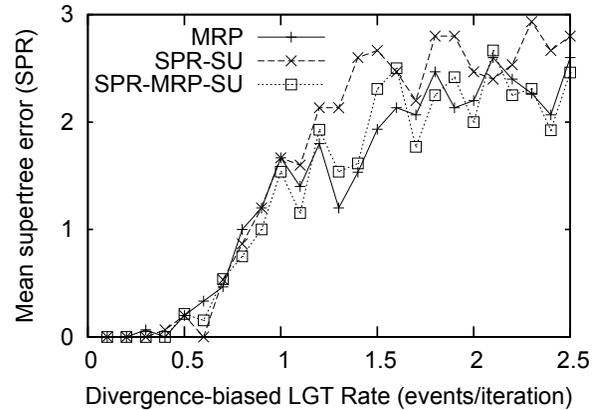
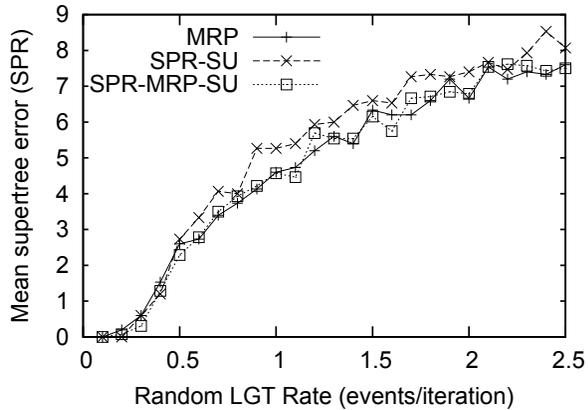
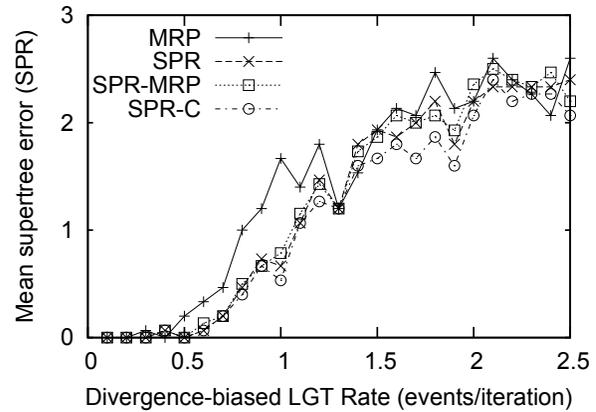
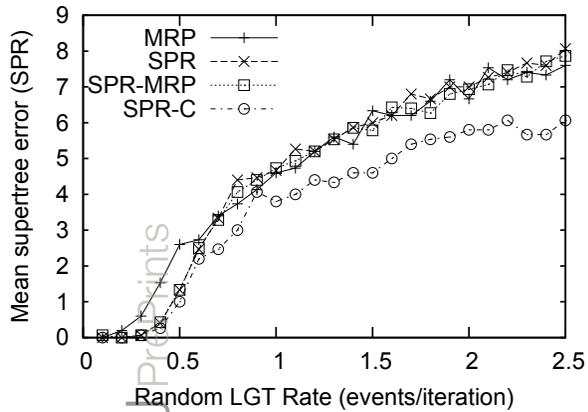


Running Time Comparison (Multifurcating Trees)

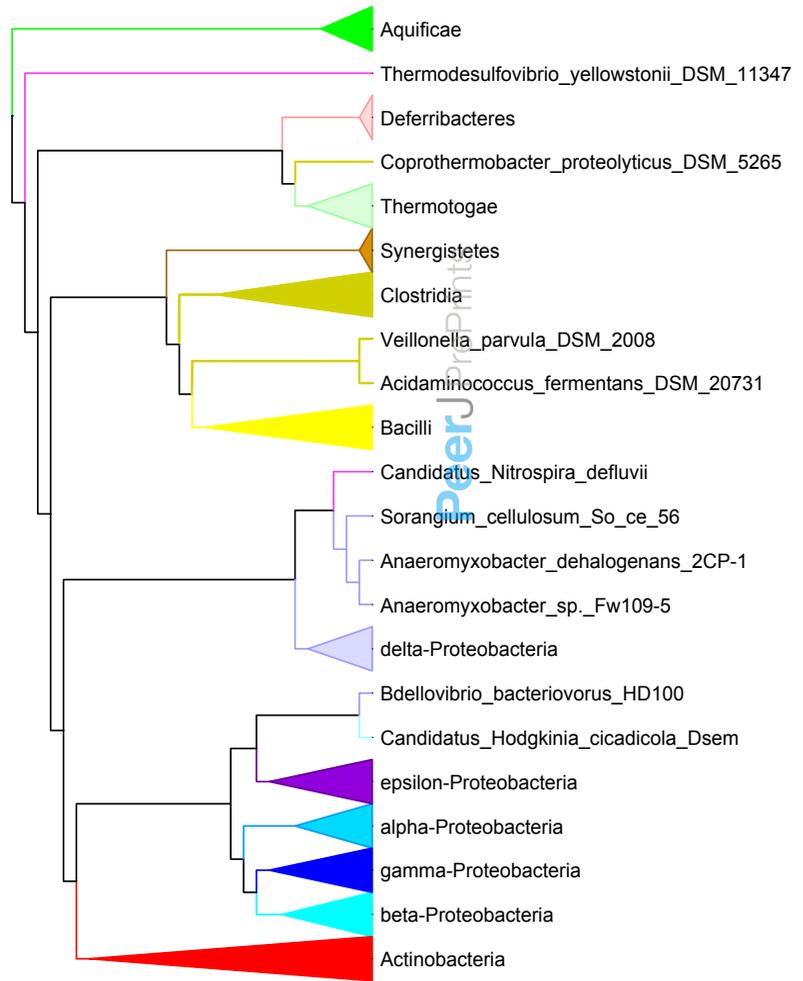








a) SPR Supertree



b) MRP Supertree

