

1 **Models for biomass prediction of *Cunninghamia lanceolata*** 2 **tree and stands in Southeastern China**

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7 **Abstract**

8 Large uncertainties still remain when using existing biomass equations to estimate total
9 tree and forest stand scale. In this paper, we develop individual-tree biomass models for
10 Chinese fir (*Cunninghamia lanceolata* (Lamb.) Hook.) stands in Fujian Province,
11 southeast of China. For this, we used 74 previously established models that are most
12 commonly used to estimate tree biomass, and selected the best fit models and modified
13 it. The results showed the published model with $\ln(B)$ (biomass), $\ln(D)$ (diameter at
14 breast height), $(\ln(H))^2$, (total height) $(\ln(H))^3$ and $\ln(WD)$ (wood density) to be the
15 best fitting model for estimating the tree biomass of Chinese fir. Furthermore, we
16 observed that variables D, H (height), WD significantly correlated with the total tree
17 biomass estimation model, as a result of it portraying the natural logarithm structure to
18 be the best tree biomass structure. Finally, when a multi-step improvement on tree
19 biomass model was performed, the analytic model with TV (tree volume), WD and
20 BECF (biomass wood density conversion factor), achieved the highest accuracy
21 simulation. Therefore, when combined with TV, WD and BECF to tree biomass volume
22 coefficient b_i for Chinese fir, the optimal model is the forest stand biomass (SB)
23 estimation model, model with variables of stand volume (SV) and coefficient b_i .
24 **Key words:** *Cunninghamia lanceolata*, stand, generic models, total tree biomass.

25 1Introduction

26 Forest managers are constantly facing new problems and challenges including climate
 27 change, mitigation and adaptation. To meet a variety of ecological demands created by
 28 social valuations (Taerøe et al. 2015). In the future, different business deal in forestry,
 29 scientific measurements of the value of forest ecological services need to have high
 30 precision and forest biomass prediction model is indisputable(Hounzandji et al. 2015,
 31 Zeng 2015). In addition to climate change, the development of a regional biomass
 32 energy industry, carbon distribution and artificial forests the energy management
 33 problems still exist, so the high accuracy of forest stand biomass models is
 34 important(Temesgen et al. 2015, Qiu et al. 2015).

35 The current biomass equations mainly use the following methods, biomass factor
 36 method, the outlier growth equation method and the volume source biomass method
 37 (R.Ostadhashemi et al 2014). At present many forest biomass estimation models mainly
 38 use diameter at breast height (D) to estimate biomass (Jenkins 2003). This method lacks
 39 specificity for different tree species and site features and the accuracy of the area
 40 measurement is always poor, resulting in high precision on only a small scale
 41 (Hailemariam et al 2015).

42 In different allometric equation methods, Jenkins et al. (2003) have incorporated data
 43 from published studies into new biomass estimation equations. In order to adapt to
 44 different research purposes, many researchers have performed many trials and modified
 45 different models in recent years (Ostadhashemi et al. 2014). In previous researches, Li
 46 et al. (2010) and Dimitris et al. (2005) summarized the biomass models with diameter
 47 at breast height (D), tree height (H), D^2H and DH as the independent variables. They
 48 used a combination of the commonly used power function model, exponential model
 49 and the polynomial model to simulate a part of or the whole plant wood biomass.
 50 Similarly, Liu et al. (2015) established a relevant analysis of the biomass of the shrub
 51 using a new biomass model. Almeida et al. (2014) included the D^2 related to the

52 analysis of biomass

53 With the progress of biomass research and utilization, Jos é established the site index
54 (SI) and forest biomass variable model of stand basal area(Jos é 2015). The study
55 showed that as the objective changed the reliability of the D indicator does not meet the
56 needs of practical forestry estimates (Zheng et al. 2015). Wood density (WD) and stand
57 basal area (G) have become more and more popular. For example, Gurdak et al. (2014)
58 and Sabina et al. (2011) used a combination of D and H and WD, respectively, to
59 establish a logarithmic and an exponential biomass model in combination with these
60 indicators. Timothy et al. (2004) used a fusion variable and established a logarithmic
61 model to estimate the biomass of the Amazon forest. To study the structural
62 relationships between form factor, wood density, and biomass in African savanna
63 woodlands, Matthew et al. (2014) established a variable containing the D, H, WD and
64 G logarithmic combined biomass model

65 Several studies (Timothy et al. 2004, Matthew et al. 2014, Zou et al. 2015), assert that,
66 within the small area, an increase in the stem biomass, increases the independent
67 variable and the goodness of fit of the model. This results in large-scale forest biomass
68 estimations that consider the use of binary and tertiary biomass models. This is
69 necessary in order to obtain a higher accuracy of the estimates (Zou et al., 2015).
70 Therefore, in view of the different purposes and the actual demand, an increase in the
71 independent variable parameter of the biomass model is meaningful (Zuo et al. 2015).
72 In many cases, however, when the model was used to assess the biomass, the evaluation
73 accuracy of large-scale or small-scale areas was not high, or there was uncertainty or
74 restrictions (Jenkins 2003). For instance, the definition of a forest stand is uncertain at
75 large and small scales. So the selection of either scale leads to uncertainty when
76 selecting a model (Malhi et al., 2006). In order to solve this problem, Zuo et al. (2014)
77 used different biomass estimation parameters to analyze the biomass estimation model
78 of fir forests. Gomez - Garcia et al. (2014) used using D and H as the independent
79 variables to determine 8 parameters in a forest stand biomass model.

Chinese fir (*Cunninghamia lanceolata* (Lamb.) Hook.) is one of the most popular plantation timber species in China due to its good timber quality, fast growth, straight stem and high resistance of bending (Guan et al. 2015, Zhao et al. 2009). To evaluate stand biomass for Chinese fir forests at large scale, the model must be extended to the entire stand or planted region for accurate biomass estimation (Pasalodos-Tato et al. 2015). Because the selection of an established forest biomass model may not suit the Chinese fir stand the use of a more reasonable stand variable also needs to be researched (Gomez-Garcia et al. 2015). In few studies for Chinese fir stand biomass it was found that the models based on a large sample of forest biomass had a relatively high accuracy and being able to be applied in large area, whereas the regional models with small sample were limited to small area (Li et al. 2010).

This paper aims at: (1) base on the published biomass models, accurately fitting the total tree biomass (TB) for *Cunninghamia lanceolata* (Lamb.) Hook. (2) Selected and modified the best tree biomass (TB) model published before for the tree biomass (TB) of *Cunninghamia lanceolata* (Lamb.) Hook. (3) Base on the best (modified) tree biomass model, calculate the tree biomass (TB) volume coefficient (bi) for *Cunninghamia lanceolata* (Lamb.) Hook. (4) Model for biomass prediction of *Cunninghamia lanceolata* (Lamb.) Hook. stands (SB) by tree biomass volume coefficient (bi) and stand volume (SV).

2Materials and methods

2.1Materials

The study area is in Jiangle state-owned forest farm located between 117°05'-117°40'E and 26°26'-27° 04' N, Fujian province, China. The main species of the forest farm are *Cunninghamia lanceolata* (Lamb.) Hook., *Pinus massoniana* Lamb, *Phyllostachys heterocycla* (Carr.) Mitford cv. *Pubescens*. The region is characterized by ferromagnesian (red) soils and has mean annual precipitation of approximately 1699

106 mm, a mean annual frost-free season of 287 days, and a mean annual temperature of
 107 18.7 °C. We sampled four regions, which were divided into 35 plots of *Cunninghamia*
 108 *lanceolata* trees and are represented by I, II, III and IV, respectively (**Fig 1**). Established
 109 between 2010 and 2014, the plots vary in size from 400 to 600 m².
 110 In the plots, we measured the diameters at breast height (DBHs) over the bark (at 1.3 m
 111 above ground) of fresh trees (height > 1.3 m) and the total tree height of 35 trees that
 112 were felled for stem analysis. Before felling each tree, we measured two attributes:
 113 diameter at breast height (1.3 m above ground) and total tree height (H). After felling,
 114 we measured the diameter at intervals of 1 meter above the breast height depending on
 115 the total tree height by diameter tape. These diameters were measured along the largest
 116 axis and smallest axis. Base diameters of all sections were measured at intervals of 1
 117 meter. (1)The fresh masses of stem wood, stem bark, branch, and foliage were measured,
 118 and subsamples were selected and weighed in the field. (2)Fresh mass of stem bark was
 119 equal to fresh mass of stem or trunk multiplied by bark percent from subsamples. (3)
 120 The whole roots were excavated out, and fresh weights of stump (below ground level),
 121 coarse roots (more than 10 mm), middle roots(2–10 mm) and small roots (0-2 mm)
 122 were measured, respectively, and subsamples were selected (Zeng, 2015).Taking of
 123 subsamples for determination of fresh to dry weight ratios (65 °C). Based on the ratio
 124 of dry biomass to fresh biomass, the biomass of stem, bark, foliage and root was
 125 calculated and then summed to obtain the total biomass of each tree (TB). Table 1
 126 summarizes the characteristics of the selected trees (Xu et al. 2014).

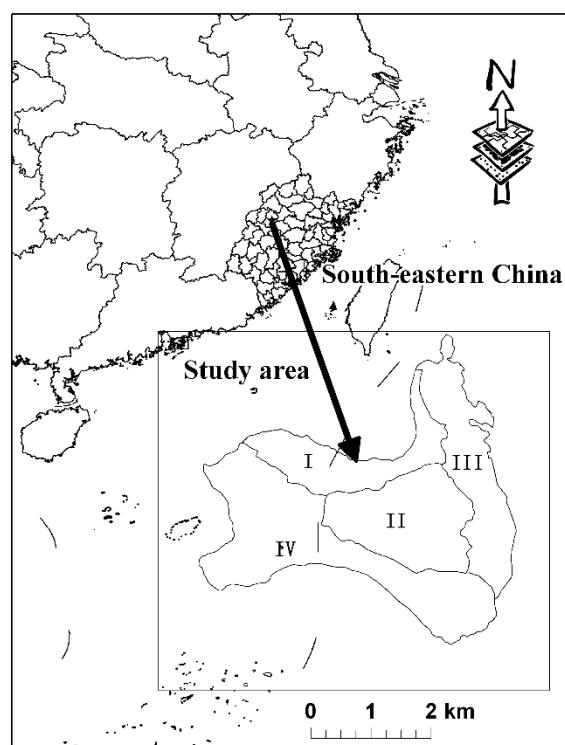


Figure 1: Four sites in Fujian province, Southeast China, where 35 trees were sampled.

Table 1: Mean diameter at breast height (1.3) (D), total height (H), age, BECF (BECF = BEF * WD, BEF is biomass expansion factor), volume(V), wood density (WD), total tree biomass (TB) for sampled biomass trees.

	D(cm)	H(m)	Age	BECF	V (m ³)	WD	B (kg)
Mean	17.0	15.8	24.4	391.8	0.2655	304.2	107.8
SD	7.3	6.7	9.5	81.4	0.31	59.7	101.3
Minimum	5.1	4.1	6	236.3	0.0060	117.0	4.6
Maximum	38.4	31.8	38	613.8	1.7091	427.1	482.4

2.2 Model fitting and evaluation

74 biomass models were selected (Dimitris et al. 2005; Dimitris et al., 2004; Dimitris et al., 2011). The nls (non-linear least squares regression) function was used to fit the equations with R project. Different starting values were used for the parameters to ensure that a global minimum was achieved.

The best function was selected on the basis of four statistical criteria: mean absolute

139 bias (MAB), root mean square error (RMSE), average relative error (ARE) and the
140 adjusted coefficient of determination (R^2) (Zhang 2011). The formulae of these
141 statistics are as follows:

$$142 \quad MAB = \frac{\sum_{i=1}^n |B_i - \hat{B}_i|}{n} \quad (1)$$

$$143 \quad RMSE = \sqrt{\frac{\sum_{i=1}^n (B_i - \hat{B}_i)^2}{n-1}} \quad (2)$$

$$144 \quad ARE = \sum \left| (B_i - \hat{B}_i) / B_i \right| / n * 100 \% \quad (3)$$

$$145 \quad R^2 = 1 - \frac{\sum_{i=1}^n (B_i - \hat{B}_i)^2}{\sum_{i=1}^n (B_i - \bar{B})^2} \quad (4)$$

146 Where B_i and \hat{B}_i are the biomass measurements and predictions, respectively; \bar{B} is
147 the average of measurements; n is the data size.

148 2.3 Variable computed

149 (1)V (volume): Based on taper model, formula (5) was used to calculate the volume of trees
150 (Mei et al. 2015).

$$151 \quad V = \frac{\pi}{40000} \int_0^H D^2 \left(\frac{(H-h)}{(H-1.3)} \right)^{(3.482321-2.153699h^{0.007})} dh \quad (5)$$

152 where H is the total height, D is the diameter at breast height, h is the height above ground level.

153 Add all the tree volume together as the stand volume, tree-level and stand-level biomass
154 prediction expanded by the stand volume.

155 (2)BEF (biomass expansion factor): BEF= Aboveground biomass / Trunk biomass (Luo 2014).

156 (3)WD (wood density): WD=Aboveground biomass/ Stem dry weight (kg*m-3).

157 (4)BECF (biomass wood density conversion factor): BCEF = BEF * WD (Enes et al., 2014).

158 (5)Accuracy (%) = (predict value/ measure value)*100%.

3Results

3.1Total tree biomass model

The best method to calculate total tree biomass (include both aboveground and belowground) can be seen from the fitting results (Table 2). Based on the models accuracy evaluation variable analysis, the MAB in model No.1 is the lowest among the candidate models (Fig 2). From the perspective of total statistics, the average relative error (ARE) is of great importance. When comparing the ARE, the ARE of model No.1 is 7.037, model No.2 is 12.623, and model No.3 is 15.931, so the simulation effect of model No.1 is the best.

Table 2. 74 Commonly used biomass models that have been previously published.

No	Model	a	b	c	d	e	MAB	RMSE	R ²
1	$\ln(B) \sim a + b \ln(D) + c * (\ln(H))^2 + d * (\ln(H))^3 + e * \ln(WD)$	-5.744	2.480	-0.217	-0.278	0.60	7.675	13.656	0.982
2	$B \sim \exp(a) * (D + 1)^b * H^c * \exp(d * D) * \exp(e * H)$	-6.104	5.162	-1.340	-0.138	0.10	8.017	11.750	0.987
3	$B \sim \exp(a) * (D + 1)^b * H^c * \exp(d * D)$	-6.250	3.389	0.704	-0.064		8.601	12.602	0.985
4	$B \sim a + b * D + c * D^2 + d * H + e * D * H$	-2.878	4.827	-0.124	-7.493	0.60	9.892	13.796	0.981
5	$\ln(B) \sim a + b * \ln(D^2 * H) + c * \ln(WD)$	-4.720	0.831	0.370			10.007	18.936	0.967
6	$\ln(B) \sim a + b * \ln(D) + c * \ln(WD)$	-5.702	2.546	0.504			10.025	19.425	0.965
7	$\ln(B) \sim a + b * \ln(D) + c * \ln(H) + d * \ln(WD)$	-5.723	2.567	-0.020	0.507		10.095	19.895	0.965
8	$B \sim a + b * D + c * D^2 + d * (D^3 / H)$	-9.452	-0.808	0.572	-0.171		10.961	14.627	0.979
9	$B \sim a + b * D^2 + c * D + d * D * H$	-10.924	-0.696	0.198	0.200		11.029	14.847	0.979
10	$B \sim a + D^2 * b + D * H * c$	-16.477	0.195	0.183			11.130	14.894	0.978
11	$\ln(B) \sim a + (D / (D + 10))^b$	-2.411	10.864				11.440	15.666	0.976
12	$\ln(B) \sim a + b * (D / (D + 7)) + c * H + d * \ln(H)$	-2.785	10.899	0.005	-0.046		11.558	21.683	0.954
13	$\ln(B) \sim a + (D / (D + 11))^b + c * \ln(H)$	-2.121	10.451	0.071			11.628	16.219	0.974
14	$B \sim \exp(a + b * \ln(D^2 * H))$	-1.823	0.748				11.809	16.116	0.975

15	$B \sim a \cdot (D^2 \cdot H)^b$	0.162	0.748			11.809	16.116	0.975
16	$B \sim a \cdot D^b \cdot H^c$	0.171	1.574	0.650		11.943	15.834	0.976
17	$\ln(B) \sim a + b \cdot (D / (D + 1))$	-2.111	10.757			11.970	16.732	0.973
18	$B \sim \exp(a) \cdot (D + 1)^b \cdot H^c$	-2.050	1.617	0.674		12.316	16.148	0.975
19	$B \sim \exp(a + b \cdot \ln(D^2 \cdot H \cdot G))$	-1.543	0.436			12.455	16.285	0.975
20	$B \sim a + b \cdot H + c \cdot D^2$	-24.870	1.493	0.319		12.669	16.118	0.975
21	$\ln(B) \sim a + b \cdot D / (D + 13) + c \cdot H + d \cdot \ln(H)$	-1.582	10.205	0.005	0.040	12.796	21.425	0.955
22	$B \sim a + b \cdot D^2$	-11.692	0.349			12.853	16.582	0.973
23	$B \sim a + b \cdot D^2 \cdot H + c \cdot D^2$	-13.130	0.001	0.363		12.940	16.810	0.973
24	$B \sim a + b \cdot D + c \cdot D^2 \cdot H$	-48.700	6.542	0.006		12.968	16.736	0.974
25	$B \sim a + b \cdot D^c$	-20.336	0.559	1.869		13.007	16.442	0.974
26	$\ln(B) \sim a + (D / (D + 14))^b + c \cdot \ln(H)$	-1.499	10.211	0.106		13.028	21.937	0.953
27	$\ln(B) \sim a + (D / (D + 13))^b$	-1.643	10.667			13.037	20.706	0.958
28	$B \sim a + b \cdot D + c \cdot D^2$	-23.013	1.314	0.317		13.118	16.628	0.974
29	$\ln(B) \sim a + (D / (D + 14))^b$	-1.456	10.666			13.578	23.191	0.948
30	$\ln(B) \sim a + b \cdot D / (D + 18) + c \cdot H + d \cdot \ln(H)$	-1.338	10.419	-0.020	0.360	13.790	23.329	0.947
31	$B \sim a \cdot D^b$	0.245	2.090			14.713	18.004	0.969
32	$B \sim \exp(a + b \cdot \ln(D))$	-1.407	2.090			14.713	18.004	0.969
33	$\ln(B) \sim a + b \cdot \ln(D) + c \cdot \ln(H \cdot D^2)$	-2.821	2.117	0.143		14.812	29.533	0.915
34	$\ln(B) \sim a + (D / (D + 5))^b$	-5.560	13.001			14.864	24.769	0.940
35	$\ln(B) \sim a + b \cdot \ln(D) + c \cdot H + d \cdot \ln(H \cdot D^2)$	-2.794	2.139	0.001	0.130	14.879	30.159	0.911
36	$\ln(B) \sim a + b \cdot \ln(D) + c \cdot H$	-2.676	2.441	0.008		15.654	34.441	0.884
37	$\ln(B) \sim a + b \cdot \ln(D)$	-2.843	2.550			15.682	32.304	0.901
38	$\ln(B) \sim a + b \cdot \ln(\pi \cdot D)$	-5.762	2.550			15.682	31.826	0.901
39	$\ln(B) \sim a + b \cdot (D / (D + 30)) + c \cdot H + d \cdot \ln(H)$	-1.261	11.587	-0.005	0.074	15.714	28.420	0.921
40	$\ln(B) \sim a + (D / (D + 18))^b$	-0.901	10.841			15.877	34.020	0.887
41	$B \sim a \cdot (WD \cdot D^2 \cdot H) / 1000$	0.054				15.900	35.951	0.878
42	$B \sim a + b \cdot H + c \cdot D^2 \cdot H$	-24.710	4.595	0.008		15.983	20.399	0.961

43	$B \sim a + b * D^2 * H + c * H^2$	1.586	0.007	0.197	15.996	20.989	0.958
44	$B \sim a + b * D + c * (D^2 * H)^2$	-85.590	10.830	0.000	16.618	21.062	0.958
45	$B \sim a + b * H^2 + c * H^3$	0.373	0.155	0.010	20.297	27.868	0.924
46	$B \sim a * H^b$	0.061	2.595		20.318	28.225	0.925
47	$B \sim a + b * D + c * H^2$	-81.275	7.637	0.200	20.367	26.335	0.934
48	$B = aV + b$	312.470	24.740		20.502	26.497	0.934
49	$B \sim a + b * D^2 * H$	27.464	0.011		20.986	27.187	0.930
50	$B \sim a + b * D$	-118.191	13.264		22.249	29.696	0.917
51	$B \sim a + b * D + c * H$	-115.504	15.366	-2.428	22.285	29.212	0.919
52	$B \sim a * H * D^2$	0.013			23.777	34.283	0.886
53	$B \sim a + b * H + c * (D^2 * H)^2$	-64.280	9.985	0.000	25.411	30.737	0.911
54	$B \sim a + b * (1/D^2 * H) * D^2 * H$	-23.380	0.445		25.779	31.257	0.905
55	$\ln(B) \sim a + b * \ln(D)^2$	0.405	0.484		26.178	81.410	0.355
56	$B \sim a * \exp(H * b)$	14.665	0.112		26.306	32.099	0.900
57	$B \sim a * \exp(b * D)$	23.845	0.081		28.721	32.615	0.899
58	$B \sim a * B A^b * S I^c$	1.067	0.604	1.206	30.605	61.748	0.640
59	$\ln(B) \sim \ln(a) + b * H$	4.070	0.172		34.697	90.892	0.219
60	$B \sim a + b * H$	-105.634	13.467		36.505	47.096	0.790
61	$B \sim a + b * \ln(D)$	-387.080	180.950		37.662	53.784	0.727
62	$B \sim a * \ln(H * D^2) + b$	58.273	-		38.751	55.563	0.699
			365.449				
63	$B \sim a + b * \ln(D^2 * H)$	-365.451	58.274		38.751	56.399	0.699
64	$B \sim a + b * \ln(H)$	-295.080	151.940		45.808	64.782	0.603
65	$\ln(B) \sim \ln(a) + b * D$						
66	$\ln(B) \sim \ln(a) + b * D^2 * H$						
67	$B \sim (WD/a) * \exp(b * \ln(D) + c * (\ln(D))^2 + d * (\ln(D)^3) + e)$						
68	$B \sim (WD/a) * \exp(b * \ln(D) + c)$						

Misconvergence

$$B \sim \exp(a + b \ln(D) + c (\ln(D))^2 + d \ln(H) + e) \ln(G)$$

$$n(G))$$

$$B \sim a * H^b * (D+1)^{(c+d \ln(D))}$$

$$B \sim a * D^2 + (D^2 - b) * c$$

$$\ln(B) \sim a + b \ln(D) + c \ln(D^2) + d \ln(H)$$

$$B \sim \exp(a + b \ln(D)) + \exp(c + d \ln(D))$$

$$B \sim a + (b * (1/D^2) + c * (1/D^2)) * D^2$$

Where a, b, c, d, e, f is the model parameters; RMSE, MAD and R² is model evaluation index; V is stem volume (m³); B is the whole tree biomass (kg); D is the diameter at breast height (cm); H is the tree total height (m); G is a basal area (m²); BCEF is biomass wood density conversion factor, that is, the ratio of aboveground biomass over buck volume (kg*m⁻³); BEF is biomass expansion factor, that is, the ratio of aboveground biomass over trunk biomass, dimensionless; BCEF = BEF * WD (Enes, Fonseca, 2014); WD is wood density, the dry weight per unit volume of wood (kg*m⁻³); Ln is the natural logarithm (Zuo et al. 2014).

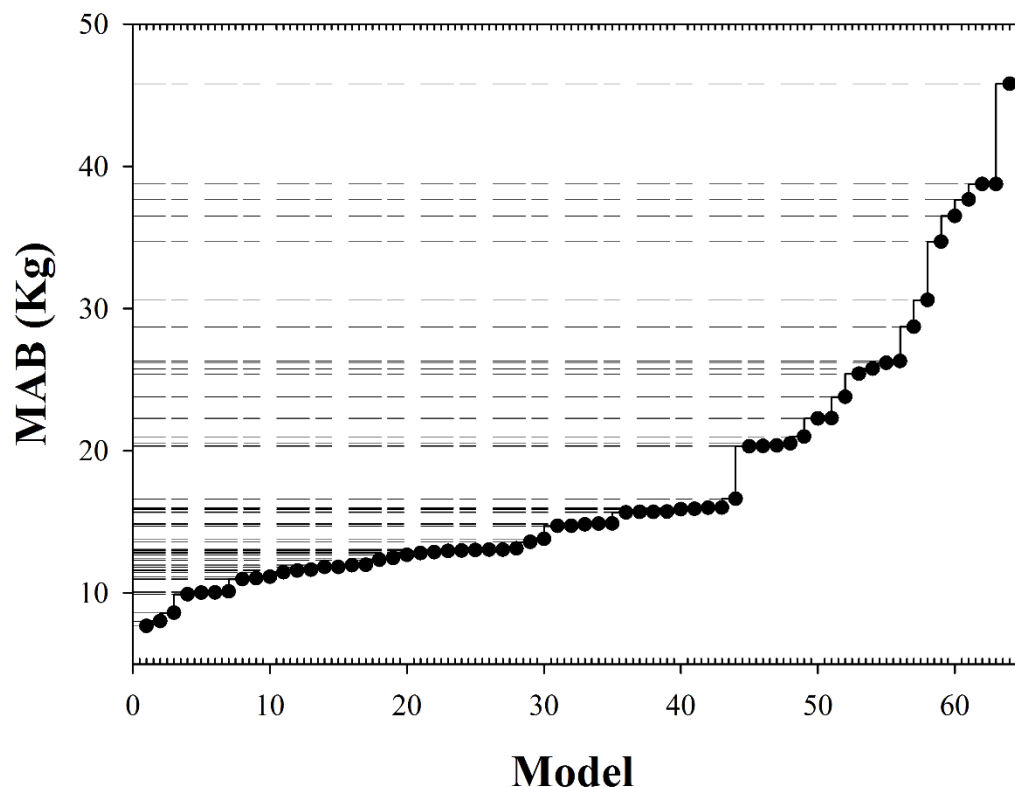


Figure 2: The MAB of 64 convergence biomass models in table 2.

3.2 Stand biomass model

(1) Based on the above analysis, the model can be used for the natural logarithms of the mathematical model structure.

(2) The parameters of the model can consider the 3 indices of D, H and WD (Gomez-Garica Esteban et al. 2014, Gurdak et al. 2013).

(3) The size of the trees can be described by the forest measurements D and H, and the D and H are comprehensive statistics for the volume (TV) (André et al. 2015).

(4) According to the (1), (2), and (3) analyses, the improved expression can be written as:

$$\ln(TB) = a + b \cdot \ln(TV) + c \cdot \ln(WD) \quad (75)$$

After an analysis of the fit: $a = 3.5743$, $b = 0.8887$, $c = 0.4106$, $MAB = 9.051$, $RMSE = 16.424$, $R^2 = 0.975$.

A comprehensive comparison of model 5 (with 3 variables) and model 75, under the conditions of the 3 variables model, the evaluation indicates of RMSE and R^2 are similar but the mean absolute bias of model 75 is smaller than model 5 at 0.956. Compared to other model, model 75 has easy measure stand variable and can better explain the biomass, which has an obvious relationship between tree volume and wood density. At this step, the accuracy is less than model 1, model 75 not the best biomass model. So we need keep on modifying model 75.

(5) In analysis (4), model 75 used an expression of V performed very well, as in the Fang's study (Fang 2001), which signifies that a certain type of biomass is closely associated with timber volume ratio (BEF) (Taeroe et al. 2015). The equation $BCEF = BEF \cdot WD$ is combined with model No.75 in accumulation variable BECF (Zuo et al. 2014), thus introducing BECF parameters. That is, model 75 can be further written as:

$$\ln(TB) = a + b \cdot \ln(TV) + c \cdot \ln(WD) + d \cdot \ln(BECF) \quad (76)$$

which is defined as model 76.

After fitting model 76, $a = 0.3766$, $b = 0.9685$, $c = 0.9365$, $d = 0.1538$, $MAB = 4.8483$,

206 RMSE = 9.3294, $R^2 = 0.992$.

207 (6) The comparative analysis of model 1 and model 76 showed that, after inserting the
208 biomass conversion factor BECF, the MAB dropped to 4.8483, less than model No.1
209 by 2.8267, the RMSE decreased to 7.09, less than model 1 by 6.566 and R^2 increased
210 by 0.017. Model including the variable of BECF, increasing the accuracy significantly.

211 (7) Through the above analysis, we can conclude that model 76 is the optimal tree
212 biomass model for Chinese fir, namely:

$$213 \quad \ln(TB) = 0.3766 + 0.9685 \cdot \ln(TV) + 0.9365 \cdot \ln(WD) + 0.1538 \cdot \ln(BECF) \quad (77)$$

214 The wood density and conversion coefficient, in combination with a different volume
215 size, can estimate the biomass of a species. From the definition of a forest stand, which
216 can be determined for a tree species, the WD and BECF are consistent (Timothy et al.
217 2004). Therefore, the unit stand biomass model (bi) can be:

$$218 \quad bi = \exp(0.3766 + 0.9685 \cdot \ln(TV) + 0.9365 \cdot \ln(WD) + 0.1538 \cdot \ln(BECF)) \quad (78)$$

219 This paper defined bi as the stand biomass coefficient (Sabina et al. 2011). The stand
220 biomass model can be written as:

$$221 \quad SB = bi \cdot SV/TV \quad (79)$$

222 where SV is the stand volume (m^3), SB is stand biomass (kg), TV is the sample tree
223 volume (m^3).

224 n is defined as $n = SV/TV$, which can be used to obtain:

$$225 \quad SB = bi \cdot n \quad (80)$$

226 In this new model, the parameter is less than model No.1, making it highly significant
227 in forestry and biology, like a universal biomass model.

228 4Discussion

229 In this paper, we used previous research to reconstruct a stand biomass estimation
230 model for Chinese fir. Compared with the best previous biomass model the precision of
231 our model is higher and the absolute bias in the mean is nearly 3 times lower for Chinese
232 fir (Fig 3).

233 The buck volume, wood density, and biomass wood density conversion coefficient
 234 BECF indices are included in the new model. The variable D and H are included in the
 235 stock volume estimation variable V, so the model explains the key elements that
 236 influence the biomass. At the same time the forest tree total biomass model contains the
 237 aboveground and belowground biomass. With the total tree biomass as the dependent
 238 variable, the model estimates all biomass components of a tree, which gives the model
 239 the advantage of compatibility, it is better than estimate the biomass model using one
 240 parts of one tree (Menéndez-Miguélez et al. 2013). In case of Chinese fir biomass
 241 estimation model to estimate forest biomass directly the model needs the biomass of all
 242 the tree organs or the total diameter at breast height, tree height and basal area. However,
 243 this type of estimation not only is incompatible but also has too much variance in the
 244 estimations. Based on the single tree volume calculate the tree biomass and stand
 245 biomass is a good way.

246 Over the 35 types of trees, the precision is stable, and the highest accuracy is found in
 247 the BECF from 300 to 350, WD from 350 to 400, the accuracy up to 90% (Fig 4). The
 248 BECF smaller than 363.49, the estimate value is small the measure value, or it will
 249 bigger than measure value (Crecente-Campo 2010). The parameters are easy to obtain,
 250 so this method is highly feasible.

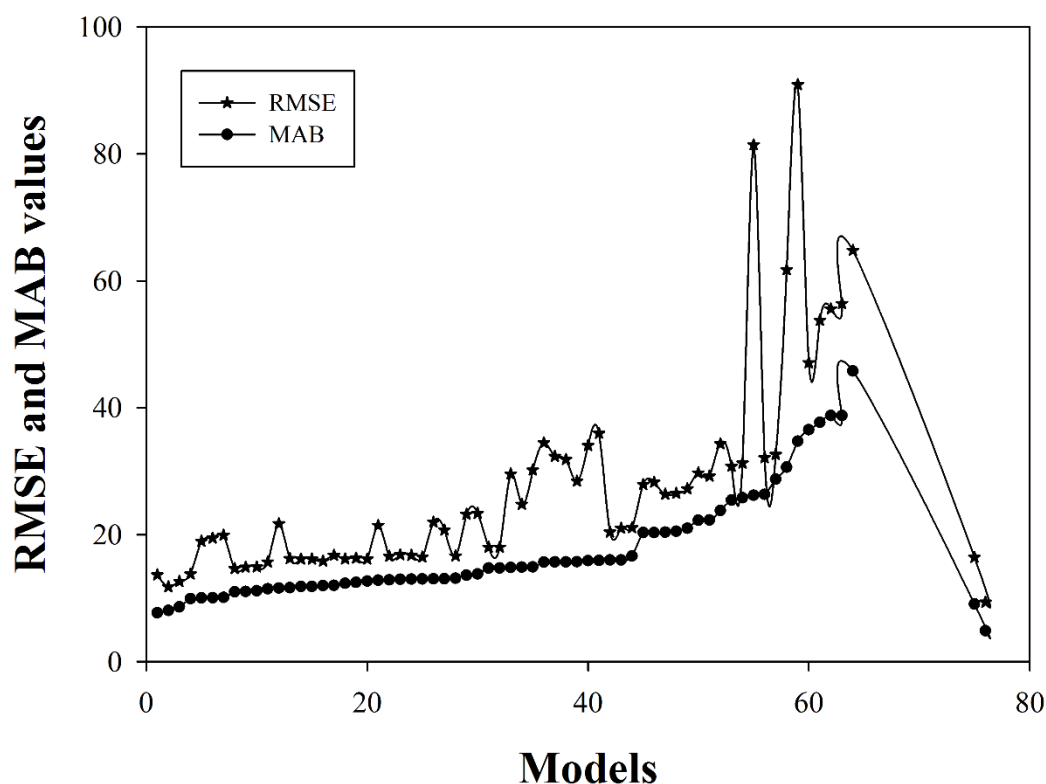


Figure 3: MAB and RMSE values of different biomass estimation models.

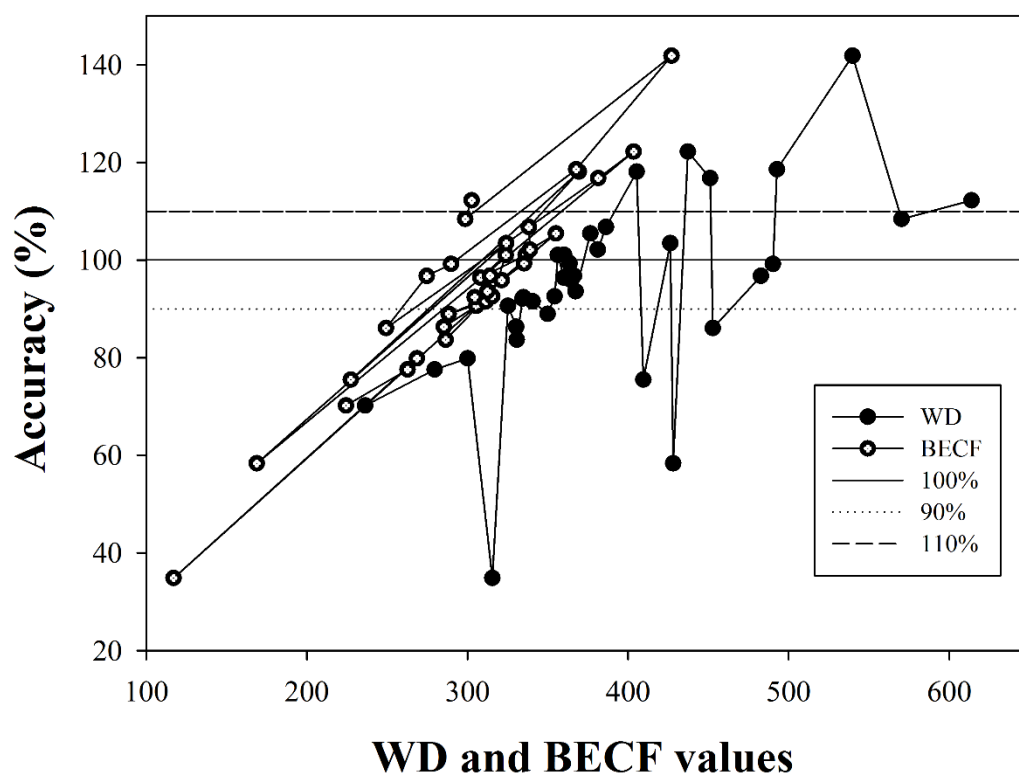


Figure 4: Changes of model accuracy with parameters WD and BECF.

In a different analysis strategy for a different age structure coefficient of Chinese fir plantations that provides the stand biomass b_i , this series of parameters can be used to estimate forest stand biomass for different sized stands. The dynamic stand volume can be combined with the site index and age estimates of growth, and the calculation formula for the stand volume (SV) forecast can be used to perfect the forest biomass estimation model using easy stand measurement variables (Návar, 2015).

Compared to the model Fang published in the journal of Science in which they applied a biomass conversion factor (BEF) for large-scale biomass estimation (Fang, 2001), but in this paper we used the biomass wood density and conversion factor BCEF ($BCEF = BEF * WD$) to estimate the stand biomass. Because our model also considered density of the wood as variable, our model has the same biological meaning. Using this better estimation variable, the new model established in this paper for small-scale stands can also have a high prediction precision, better scale adaptability, and the ability to use the tree volume of forest management data to calculate the b_i of different species.

In this paper, we propose a new forest biomass model: $B = b_i * n$, where b_i is the first proposed variable for different tree species. As a new variable parameter, the relationship between b_i and stand indicators still needs further in-depth study (Litton et al, 2008).

5Conclusions

Depending on the degree of accuracy pursued, the buck volume (TV), diameter at breast height (D), tree total height (H), biomass wood density conversion factor (BCEF), wood density (WD), and the natural logarithm \ln combined together produce the best tree biomass model $\ln(TB) = a + b * \ln(TV) + c * \ln(WD) + d * \ln(BECF)$.

We provided the first available models for stand biomass. For different species, it is necessary to calculate the stand biomass coefficient b_i first, and then the stand biomass can be estimated easily using the formula $SB = b_i * n$. The model has high precision, and the parameter is less than in model No.1, which makes the model highly significant for

forestry and tree biology. Higher efficiency of the models, for bi, the BECF from 300 to 350, WD from 350 to 400 trees has high precision in stand biomass estimation, the parameters are easy to obtain, and it is highly feasibly. The model is very useful in evaluating the ecological benefit of forest planning, and can be useful for carbon stock age and sequestration assessments in those fast-growing plantations.

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