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Architecture of the sperm whale forehead facilitates ramming combat

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Herman Melville’s novel Moby Dick was inspired by historical instances in which large sperm whales (Physeter macrocephalus L.) sank 19th century whaling ships by ramming them with their foreheads. The immense forehead of sperm whales is possibly the largest, and one of the strangest, anatomical structures in the animal kingdom. It contains two large oil-filled compartments, known as the “spermaceti organ” and “junk”, that constitute up to one-quarter of body mass and extend one-third of the total length of the whale. Recognized as playing an important role in echolocation, previous studies have also attributed the complex structural configuration of the spermaceti organ and junk to acoustic sexual selection, acoustic prey debilitation, buoyancy control, and aggressive ramming. Of these additional suggested functions, ramming remains the most controversial, and the potential mechanical roles of the structural components of the spermaceti organ and junk in ramming remain untested. Here we explore the aggressive ramming hypothesis using a novel combination of structural engineering principles and probabilistic simulation to determine if the unique structure of the junk significantly reduces stress in the skull during quasi-static impact. Our analyses indicate that the connective tissue partitions within the junk reduce stress across the skull during impact; stress reduction is greatest in the anterior aspect of the skull; and removal of the connective tissue partitions increases stress concentrations on the tip of the skull, possibly making it prone to fracture. Although the unique structure of the junk certainly serves multiple functions, our results are consistent with the hypothesis that the structure also evolved to function as a massive battering ram during male-male competition.
Title: Architecture of the sperm whale forehead facilitates ramming combat

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Abstract

Herman Melville’s novel *Moby Dick* was inspired by historical instances in which large sperm whales (*Physeter macrocephalus* L.) sank 19th century whaling ships by ramming them with their foreheads. The immense forehead of sperm whales is possibly the largest, and one of the strangest, anatomical structures in the animal kingdom. It contains two large oil-filled compartments, known as the “spermaceti organ” and “junk”, that constitute up to one-quarter of body mass and extend one-third of the total length of the whale. Recognized as playing an important role in echolocation, previous studies have also attributed the complex structural configuration of the spermaceti organ and junk to acoustic sexual selection, acoustic prey debilitation, buoyancy control, and aggressive ramming. Of these additional suggested functions, ramming remains the most controversial, and the potential mechanical roles of the structural components of the spermaceti organ and junk in ramming remain untested. Here we explore the aggressive ramming hypothesis using a novel combination of structural engineering principles and probabilistic simulation to determine if the unique structure of the junk significantly reduces stress in the skull during quasi-static impact. Our analyses indicate that the connective tissue partitions within the junk reduce stress across the skull during impact; stress reduction is greatest in the anterior aspect of the skull; and removal of the connective tissue partitions increases stress concentrations on the tip of the skull, possibly making it prone to fracture. Although the unique structure of the junk certainly serves multiple functions, our results are consistent with the hypothesis that the structure also evolved to function as a massive battering ram during male-male competition.
Introduction

The sperm whale (*Physeter macrocephalus* L.) is unique in having a massively expanded forehead that is highly sexually dimorphic, being much larger and extending up to a meter and a half beyond the anterior tip of the jaws in mature males (Benzin, 1972; Cranford, 1999). Internally the forehead is composed of two large oil-filled sacs, stacked one on top of the other, known as the spermaceti organ and junk (Fig. 1). These sacs extend for one-third of the total length of the whale and can constitute more than one-quarter of the whale’s mass (Benzin, 1972; Clarke, 1978). The oil contained in the upper sac (spermaceti organ) was a primary target of the whaling industry of the early 19th century. At the same time, the forehead of sperm whales was considered by whalers to be a battering ram that the whales sometimes used to attack and sink oak whaling ships of up to 238 tons (Chase, 1821; Starbuck, 1878; Philbrick, 2000).

The lower sac (junk) is derived from the ondocete melon (Heyning & Mead, 1990) and is organized into sections by transverse partitions of connective tissue that contain waxy oil (Clarke, 1978) (Fig. 1). The connective tissue partitions are widest about 10-25% of the length from the anterior end and the sections are narrow ventrally and broad dorsally (Clarke, 1978). The partitions become thinner progressively towards the posterior aspect of the junk until they are totally replaced by a mixture of oil and wax. The oil and connective tissue partitions of the junk are enclosed in a fibrous connective tissue case which sits in a trough formed by the upper jaw (Clarke, 1978).

The function of the spermaceti organ and junk in adding directionality and amplitude to sonar clicks is relatively well studied and accepted (Møhl et al., 2000; Møhl, 2001; Møhl et al., 2003a; Møhl et al., 2003b; Huggenberger, André & Oelschläger, 2014). Previous studies have also suggested that the unique structural configuration of the sperm whale forehead is functionally related to, acoustic sexual selection (Cranford, 1999), acoustic prey debilitation (Norris & Møhl, 1972), communication (Madsen, Wahlberg & Møhl, 2002) and buoyancy control (Clarke, 1970). Although all of these functional hypotheses are plausible, they cannot explain how the forehead of sperm whales can function as a battering ram capable of sinking ships that are four to five times the mass of the whale.

The ramming hypothesis was originally proposed by whalers following the sinking of at least 2 whaling ships, the *Essex* in 1821 and the *Ann Alexander* in 1851 (Chase, 1821; Starbuck,
Based on these incidents, researchers have recently suggested that the forehead of a swimming sperm whale possess sufficient momentum to injure an opponent when used as a battering ram, and may at the same time absorb energy to protect the brain and skull of the attacking whale allowing mature males to use their foreheads as battering rams in male-male contests over harems of females (Carrier, Deban & Otterstrom, 2002).

The ramming hypothesis remains highly controversial because (1) the structures that generate sound, the distal sac and monkey lips of the right nasal passage, are located at the rostral end of spermaceti organ (Fig. 1) and are therefore assumed to be in harm’s way in a ramming event (Huggenberger, André & Oelschläger, 2014), and (2) ramming episodes have not been observed by scientists who study the behavior of sperm whales. Although the monkey lips do reside at the front end of the spermaceti organ, these structures are located well above and to the right of the rostral end of the junk (Huggenberger, André & Oelschläger, 2014), and it is the junk, not the spermaceti organ, that has been suggested to function as a battering ram during aggressive encounters (Chase, 1821; Carrier, Deban & Otterstrom, 2002). As far as we know, the scientific literature does not include observations of sperm whale ramming behavior, yet there is one documented observation of male-male ramming that we report here (Supplementary Material). On January 30, 1997, a reputable marine biologist, while flying over the Gulf of California, watched two mature males swim directly toward each other, from an initial observed distance of approximately 6.4 kilometers, at an estimated average swimming speed of 17 km/h and collide forehead-to-forehead. Shortly before impact both whales, which had been swimming at the surface, “shallow dove” so that the impact occurred below the surface of the water. This ramming event occurred a few miles north of a group of approximately of 50 females. This observation plus reports of ramming attacks on 19th century whaling ships suggest that sperm whales do sometimes engage in ramming contests. If these ramming contests generally occur at a shallow depth, they may be much more common than whale biologists realize because a human observer would have to be located well above the surface of the water to watch it happen.

Another reason to consider the ramming hypothesis is the extreme body size sexual dimorphism of sperm whales. This species is the most sexually dimorphic of all cetaceans, with mature males being 3-times bigger than mature females (Whitehead, 2003). Among mammals, body size sexual dimorphism is generally greatest in polygynous species in which males compete through fighting and the threat of fighting (Clutton-Brock & Harvey, 1977; Parker, 1983;
Andersson, 1994). Additionally, because sexual dimorphism is often greatest in those characters
that enhance a male’s capacity to dominate other males (Clutton-Brock & Harvey, 1977;
Hamilton, 1979; Clutton-Brock, Albon & Harvey, 1980; Parker, 1983; Jarman, 1983; Andersson,
1994), the observation that the part of the body that is most dimorphic in sperm whales is the
length of the head (Nishiwaki, Ohsumi & Maeda 1963) is consistent with the head being a
weapon important to male-male competition.

This paper addresses the battering-ram hypothesis using finite element analysis and
probabilistic simulation. Our main objective was to determine if the connective tissue partitions
of the spermaceti junk have potential to reduce stress in the bones of the skull during ramming
impact. We predict that the vertically oriented connective tissue partitions within the junk can
dissipate load through tension during posteriorly directed compressive loading of the forehead.
Bone stress reduction would be particular important on the anterior aspect of the skull (i.e., upper
jaw) that would otherwise be most vulnerable to potential tissue damage.

Materials and Methods

Finite element analysis (FEA) is a numerical technique well entrenched in comparative
biomechanics as a tool to assess the mechanical architecture of anatomical tissues and to better
comprehend the complex interaction of their form–function relationships. Nevertheless, FEA
accuracy is dependent on a variety of factors and its reproducibility is often obscured in scientific
publications due to both public unavailability of the underlying models and the lack of standard
reporting guidelines (Erdemir et al., 2012). To mitigate these problems we here describe our
methods in accordance with biomechanical FEA reporting guidelines (Erdemir et al., 2012) and
we also make all raw data and FE models available for public use (Panagiotopoulou et al. 2015).

Model Identification. Our study utilized three FE models to study the effect of the connective
tissue partitions on the reduction of bone stresses in quasi-static loading of the sperm whale head
(Fig. 2).

Model name. Sperm Whale Head Model A (Generic Base) consisted of twelve connective tissue
partitions embedded in the spermaceti tissue of junk.
Sperm Whale Head Model B (Half Partitions) had reduced number (six) of connective tissue
partitions.
Sperm Whale Head Model C (No Partitions) had no connective tissue partitions.
Model keywords. Sperm whale skull, quasi-static impact.


Physiological domain. No segmental motion, evenly distributed anterior surface loading, small deformations of hard and soft tissue.

Mechanical domain. All models were static and linear elastic.

Structure of interest. The biological structure under investigation was the sperm whale upper jaw (skull).

Demographics. Adult male sperm whale (Physeter macrocephalus L.).


Disease state. Healthy.

Spatial scale. Within a volume of (length 5.3 m x height 1.6 m x width 0.1 m).

Time scale. Not applicable (quasi-static analysis).

Primary utility. To provide mechanical insight into a physiologic process.

Secondary utility. First model of sperm whale skull mechanics.

Primary highlight. To elucidate the likely mechanically protective role of the vertical connective tissue partitions within the sperm whale skull.

Secondary highlight. Not applicable.

Primary limitation. Linear isotropic and homogeneous materials.

Due to lack of experimental data on the elasticity of the sperm whale head tissues, anisotropy and heterogeneity, as well as environmental and time dependencies could not be modeled in this study. Thus, isotropy, homogeneity and linear elasticity were assumed and the material properties assigned to each tissue were the closest estimations based on published values of tissues similar to those of interest (Rho, Ashman & Turner 1993; Shahar et al., 2007).

A biologically unrealistic consequence of this assumption was that the dorsal horizontal components of connective tissue partitions provided resistance to compression in the model. To this end we assigned a Young’s modulus (E) value of 14.8 GPa and Poisson (v) value of 0.1 for the skull; E = 2 GPa and v = 0.2 for the connective tissue partitions; and E = 1 GPa and v = 0.49 for the oil/wax mixture enclosed within the spermaceti organ and junk (Fig.2) (Rho, Ashman & Turner 1993; Shahar et al., 2007). Nevertheless, our study was comparative and such an assumption likely created a constant error across all models. Additionally, uncertainties due to material variations had been handled through numerical statistic elaboration of the models.
Lastly, the basic mechanism of skull-stress reduction we described was independent of model realism.

Secondary limitation. Simplifications in the model geometry (see below), static simulation.

Reference to publications. Clarke (1970, 1978); no explicit mechanical model described.

Model Structure

Loading and boundary conditions. We used a static force of 764 kN (Fig. 3) distributed evenly over the most anterior aspect of the head as a simplified model of ramming force. We calculated the applied force by assuming that each of the two colliding whales were traveling at an intermediate speed of 6.26 ms\(^{-1}\) (Aoki et al., 2007) had masses of 39,000 kg, and decelerated over a distance of 1 meter upon impact. The deceleration distance was based on the length of the spermaceti junk that extended beyond the tip of the skull. Boundary conditions included no-displacement constraints on all external nodes on the posterior surface of the skull.

Primary output variables. von Mises Stress.

Source of anatomy. To test our hypothesis, we developed FE models based partially on previously published structural properties and schematic configurations of male sperm whale adult cadavers. Due to the inaccessibility of sperm whale cadaveric species the report by Clarke 1978 was the most detailed hitherto available and encompassed skeletal and soft tissues such as the connective tissue partitions, and the oil cases of the spermaceti case and junk. To calculate the dimensions of the various structural components of the model, we scaled the anatomical elements shown in Figure 1 of Clark (1978) to a total spermaceti organ length of 5m (Clarke 1970). For modelling purposes and due to the unclear description of the individual connective tissue partitions thickness, we assumed a universal thickness of 0.05m and 0.150m for all connective tissue partitions and the spermaceti junk compartments between the connective tissue partitions respectively (Fig. 2).

Model A, representative of the sperm whale head, consisted of the upper sack or spermaceti organ; the lower sack or spermaceti junk; the connective tissue partitions and their subsequent connective tissue case enclosed in the spermaceti junk and the upper jaw (Fig. 2).

We compared Model A against two modified models (Models B and C) to assess the mechanical function of the spermaceti organ (Fig. 2). Model B had fewer connective tissue partitions than Model A. Model C lacked the connective tissue partitions altogether (Fig. 2).
The skin and the blubber were discarded from the modeling process due to their negligible thickness and stiffness.

The FE mesh assembly of all models consisted of solid continuum linear tetrahedral elements (type “C3D4” in the Abaqus Library, Simulia-Dassault Systemes, Waltham, USA). Each model contained approximately 42,000 to 48,000 nodes and 220,000 to 260,000 elements. Model A had 257,542 elements in total (28,009 for the upper jaw; 65,588 for the spermaceti case; 91,272 for the spermaceti junk; and 72,673 for the connective tissue partitions). Model B had 242,509 elements in total (278,96 for the upper jaw; 654,67 for the spermaceti case; 93,482 for the spermaceti junk; and 55,664 for the connective tissue partitions). Model C had 227,925 elements in total (281,37 for the upper jaw; 65,519 for the spermaceti case; 134,269 for the spermaceti junk. The nominal element size was 50 mm (0.05 m), and the actual elements sizes across the model varied from 15 to 85 mm approximately.

**Reference configuration.** The Abaqus default x (cranial-caudal), y (medial-lateral), z (vertical) coordinate system was used.

**Simulation structure**

**Name of simulation software.** Abaqus/CAE (Simulia-Dassault Systemes).

**Version of simulation software.** 6.12

**Solution strategy.** Abaqus/Standard implicit direct static solver. Minimum and maximum increments set to 1.000E-05 and 1 respectively.

**Numerical algorithms.** Full Newton default iterations.

**Convergence criteria.** Default convergence tolerances of the simulation software were used. We interpreted stress differences amongst our models using a Monte Carlo simulation. A total of 1000 Monte Carlo iterations were run for each of the three models, varying the three materials’ stiffness values randomly with a standard deviation of 10%, and von Mises stress distributions were stored for each iteration (Supplementary Materials Code). This resulted in a population of 1000 random individuals which represented the population of interest, under an assumption of 10% error in each of the material parameters. The latter is an essential approach in cases when the assigned material properties are based on generalized published values and not on experimental analysis of the tissues of interest.
For each population pair (i.e. Model B vs. Model A, Model C vs. Model B and Model C vs. Model A), the following statistic was calculated for each element:

\[
z_i = \frac{(\overline{s}_i)_B - (\overline{s}_i)_A}{\frac{1}{2}[(\sigma_i)_A + (\sigma_i)_B]}.
\]

where \(i\) indexes the elements, A and B represent models, \(\overline{s}_i\) represents mean elemental von Mises stress and \(\sigma_i\) represents elemental standard deviation. Since the input variance nonlinearly maps to elemental variance, the \(z\) distribution is a non-trivial function of mean group differences.

Next, the “significance” of the \(z\) distribution was assessed using paired non-parametric permutation tests (one for each model pair). A total of 10,000 label permutations were applied to each model pair, yielding a non-parametric distribution of the \(z\) statistic at each element. The 99\(^{th}\) percentile of that distribution was taken as the “significance” threshold. In other words, if an element’s \(z\) value survived that threshold, it would suggest that 99\% of all randomly labelled individuals would yield a \(z\) value less than that observed in the original labellings, and thus that threshold-surviving elements represented true population differences at alpha=0.01 under the assumption of 10\% true population material parameter variance.

**Validation.** Validation of the FE models against experimental *ex vivo* data was not feasible due to size and accessibility constraints. Nevertheless our study is comparative and conclusions are fundamentally mechanical rather than empirical.

**Availability.** Not yet public.

**Results**

In all our FE models the highest concentration of von Mises stresses occurred in the most anterior aspect of the skull (Figs. 4, 5 and Table 1). The anterior connective tissue partitions within the junk were subjected to higher tensile loading than the posterior portions (Fig. 6). Tension in the connective tissue partitions redistributed compressive stresses across the skull (Models A and B) and the absence of the partitions (Model C) raised anterior skull stresses (Fig. 4, 5 and Table 1).

A reduced number of partitions (Model B) did reduce stresses in the anterior skull, but stress...
reduction was not as effective as Model A (Fig. 4, 5 and Table 1). The skull stress difference distributions resulting from Monte Carlo simulations suggest that our main finding regarding the load-redistribution functionality of the connective tissue is insensitive to relatively large changes in both material parameters (Fig. 7) and, indirectly, load magnitudes.

Discussion

Our findings suggest that the connective tissue partitions of the junk may be able to reduce impact stresses and thus potentially function as a protective mechanism during ramming. The mechanism of skull stress reduction appears to be connective partition tension; as the spermaceti junk is compressed upon impact, the oil between the partitions is displayed vertically and laterally, placing the connective tissue partitions into tension (Fig. 6). This connective tissue tension allows the total compressive bone load to be shared over a greater volume (Figs. 4-7). While our static simulations do not quantify dynamic effects of the connective partitions including energy dissipation, our results suggest that connective partition tension would in fact dissipate energy in dynamic impacts because dynamic loading, like the current quasi-static loading, would be distributed over a broader region of the skull. Additionally, during a dynamic impact soft tissues within the skull would displace, and the connective tissue partitions would limit this displacement. The connective tissue might therefore protect both bone and soft tissue from injury. Absence of the partitions increased stresses by 45%, concentrated on the most anterior aspect of the skull, making the skull more prone to tissue failure (Table 1, Figs.4-7).

Our findings appear to provide an explanation for previous observations that, in real whales, the partitions become progressively thinner posteriorly until they are replaced by a mixture of oil and wax (Clark, 1978). The anterior thicker partitions are subjected to the greatest tensile loading (Fig. 6) and, if the battering ram hypothesis is correct, they likely play the biggest role in skull stress reduction in the face of posteriorly-directed impact forces.

The connective tissue partitions of the junk are acquired traits that likely facilitate a variety of functions. In addition to acoustic signals between groups (Madsen, Wahlberg & Møhl 2002), the partitions may play an important role in the dissipation of stresses during ramming combat to protect the skull and brain. This “mechanical advantage” is a trait that is likely related to selection on male-male aggressive behavior. Such developmental non-independent morphological features of the junk are an example of how a derived structure, such as the
connective tissue partitions, facilitates evolutionary modifications while maintaining functional integrity (Wagner & Altenberg 1996).

Our results are not directly relevant to the behavioral strategies behind ramming impacts; however, our findings are consistent with the hypothesis proposed in 1821 by Owen Chase (Chase, 1821). Following the sinking of the Essex whaling ship, Owen Chase hypothesized that sperm whales not only use their immense and elaborately complex foreheads as battering rams when fighting, but also that "the whale's head is admirably designed for this mode of attack". The prevalence of head-butting in sperm whales is not well documented. However, ramming is a basal behavior for bovidae (Farke, 2008; Alvaraez, 1990) and cetacean (Carrier, Deban & Otterstrom, 2002), including humpback whales (Baker & Herman 1984), bottle-nosed whales (Gowans & Rendell 1999), narwhales (Silverman & Dunbar 1980), long-finned pilot whales (Reilly & Shane, 1986) and killer whales (Goley & Straley, 1994). Based on these reports, it has previously been hypothesized that the spermaceti organ of male sperm whales may function as a weapon and is more developed in males due to sexual selection (Carrier, Deban & Otterstrom, 2002). If this is true then males may be exposed to increased stresses during head-butting ramming and as such necessitate additional support via a dramatically increased and more structurally robust melon.

Our study illustrates how structural engineering principles and probabilistic simulation can be used to address hypotheses of mechanical function in biological systems that are too big or inaccessible to be studied directly. We anticipate our study will stimulate future research aimed at unraveling the mechanical function of the head during aggressive head-butting and ramming in other species such as the Hippopotamus (Kingdon, 1979) which head-butting aggressive behavior is common but remains unsimulated.

Acknowledgments:
We thank Sandra Lanham for sharing with us her report on the sperm whale ramming incident that occurred near Mildriff Island at the Gulf of California, on the 30th of January 1997. We are also grateful to Dr. Ali Nabavizadeh (University of Chicago) for creating Figure 1. The authors declare no conflicts of interest.
References:


**Figure legends**

**Fig. 1.** Schematic representation of sperm whale head structure.

**Fig. 2.** Finite element models. Young’s moduli for the connective tissue partitions (blue), spermaceti organ (yellow) and skull (red) were 14.8 GPa, 1 GPa and 2 GPa, respectively. Models A, B and C have twelve, six and zero connective tissue partitions, respectively.

**Fig. 3.** Loads and constraints assigned to all FE models. A force of 764 kN was applied to the anterior surface of the head (1). Motion was constrained at the posterior surface (2) in all directions.

**Fig. 4.** Von Mises stress distribution results.

**Fig. 5.** Region definitions (blue vertical bars).

**Fig. 6.** Maximum principal stress distributions across the connective tissue partitions. Positive and negative stresses indicate areas of tension and compression respectively.

**Fig. 7.** Z statistic distributions depicting mean elemental von Mises stress differences divided by elemental standard deviation under an assumed population material stiffness variance of 10%. Data are thresholded at alpha=0.01.
Table 1 (on next page)

Maximum (Max.), mean and minimum (Min.) percentage increase of the regional (Fig. 5) von Mises stress values (Pa) between Models A and C and Models B and C.
Table 1.
Maximum (Max.), mean and minimum (Min.) percentage increase of the regional (Fig. 5) von Mises stress values (Pa) between Models A and C and Models B and C.

<table>
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<td>35.7</td>
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Schematic representation of sperm whale head structure.
Finite element models.

Young’s moduli for the connective tissue partitions (blue), spermaceti organ (yellow) and skull (red) were 14.8 GPa, 1 GPa and 2 GPa, respectively. Models A, B and C have twelve, six and zero connective tissue partitions, respectively.
3

Loads and constraints assigned to all FE models.

A force of 764 kN was applied to the anterior surface of the head (1). Motion was constrained at the posterior surface (2) in all directions.
Von Mises stress distribution results.

Model A

Model B

Model C

von Mises stress (Pa)

1E+6  1.5E+6  2E+6  2.5E+6  3E+6  3.5E+6  4E+6  4.5E+6  5E+6  6E+6  7E+6  1E+7
5

Region definitions (blue vertical bars).

Model A

Model B

Model C
Maximum principal stress distributions across the connective tissue partitions.

Positive and negative stresses indicate areas of tension and compression respectively.

Model A

Model B

Model C

Maximum Principal Stress (Pa)

5E+6  4E+6  3.5E+6  3E+6  2.5E+6  2E+6  1.5E+6  1E+6  8E+5  2E+5  -4E+5  -1E+6
Probabilistic FEA simulation.

Z statistic distributions depicting mean elemental von Mises stress differences divided by elemental standard deviation under an assumed population material stiffness variance of 10%. Data are thresholded at alpha=0.01.