

2D hexagonal boron nitride for solar energy conversions

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The optoelectronic properties of free standing monolayer (ML) hexagonal boron nitride (h-BN) is investigated for potential solar energy conversion applications using the Density Functional Theory (DFT) full potential linearized augmented plane wave (FP-LAPW) method. In addition, the bulk optical properties have also been calculated for the sake of comparison. The dielectric functions, optical conductivities and the optical constants are evaluated using the relaxed structures from electronic total energy pseudopotential calculations. The results reinforce previous research on h-BN DUV optoelectronics and demonstrate the suitability of its use as a component in deep ultraviolet (DUV) and energy conversion devices.

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Abstract

The optoelectronic properties of a free standing monolayer (ML) of hexagonal boron nitride (h-BN) is investigated for potential solar energy conversion applications using the Density Functional Theory (DFT) full potential linearized augmented plane wave (FP-LAPW) method. In addition, the bulk optical properties have also been calculated for the sake of comparison. The dielectric functions, optical conductivities and the optical constants are evaluated using the relaxed structures from electronic total energy pseudopotential calculations. The results reinforce previous research on h-BN DUV optoelectronics and demonstrate the suitability of its use as a component in deep ultraviolet (DUV) and energy conversion devices.

Key words: DFT_PAW; DUV; dynamic electrical conductivity; dielectric function, optical constants

Introduction

The last two decades have seen tremendous research on two-dimensional (2D) materials similar to graphene; which was the first 2D material discovered with a honeycomb structure consisting of single layers of carbon atoms and endowed with remarkable electronic, mechanical and optical properties [1-4]. Especially, layered transition metal dichalcogenides (TMDs) are widely investigated due to the rich diversity of properties which can be attributed to the finite and tuneable bandgap in these materials and have seen a multitude of applications [5-8].

In comparison to TMDs a less researched graphene analog is h-BN that is now gaining popularity as the key building block in van der Waal heterostructures [9]. Each B^{3+} atom is bonded in a trigonal planar geometry to three equivalent N^{3-} atoms and vice versa as shown in Figure 1. Similar to graphene, 2D h-BN has a honeycomb structure and consists of alternating B and N atoms that are sp^2 covalently bonded, but, it has an insulating character. Moreover, due to

the difference in electronegativity of the B and N atoms, the bond between B and N shows an ionic character and it is not purely covalent as in graphene. Being the structural analog of graphene h-BN is expected to possess and it does show excellent mechanical properties and high chemical and thermal stabilities [10-12]. The small mismatch in lattice parameter of h-BN with graphene and the absence of dangling bonds and charge traps makes it an ideal substrate for graphene based devices [13, 14]. The indirect to direct bandgap crossover in MLs of TMDs with its efficient light matter coupling is also observed in h-BN [15, 16] and makes it a promising material for optoelectronics and deep ultraviolet (DUV) applications [17-19]. It is now the age of nano electronics and with the increasingly small size of components there is a need to extend optical systems to shorter wavelengths than visible light to improve the image resolution. This has motivated the interest in the short-wave UV region, especially DUV optics. The focus of the present study is to investigate the dynamic electrical conductivity and optical constants in order to better understand and substantiate previous research on h-BN DUV optoelectronics and its possible use as a component in solar energy conversion devices.

Method

The calculations are carried out in two steps. First, DFT calculations using the ABINIT software program [20] with the generalized gradient approximation (GGA) projector augmented wave (PAW) pseudopotentials [21] are performed for structural optimization as in previous works [22, 23]. Convergence criteria of less than 1×10^{-6} Ha for the Self Consistent Field (SCF) iterations and force threshold of less than 1 mRy/a.u. for structural optimizations are used with the optimized k-point grids of $10 \times 10 \times 10$ and $10 \times 10 \times 5$ for h-BN bulk and ML h-BN respectively and a cutoff energy of 20Ha to obtain the lattice constants and relaxed structures. Next, the relaxed geometries that have been obtained are used to perform FP-LAPW calculations with the WIEN2k [24] code employing GGA_PBE to obtain the ground state energies and band structures. The wave functions in interstitial region were expanded in plane waves with a cutoff of $R_{mt} \times K_{max}$ set to 7 for energy eigenvalues convergence; K_{max} gives the magnitude of the largest K vector in the plane-wave expansion and the muffin-tin radii (R_{mt}) are set to 1.37 and 1.36 a.u. for both the atoms in the bulk and ML h-BN respectively. K-point grids of $10 \times 10 \times 10$ and $15 \times 15 \times 2$ are used for the electronic calculations of the bulk and ML respectively. More stringent calculations using denser grids of $19 \times 19 \times 6$ and $50 \times 50 \times 2$ are used for the bulk and ML h-BN respectively to evaluate the optical properties, namely the frequency dependent conductivities, real and imaginary parts of dielectric tensor, index of refraction, reflectivity and the absorption and extinction coefficients.

Results

Structural and electronic

The Simulation of the 2D BN in the hexagonal structure is done by using the supercell technique. The optimized value of the bulk lattice constant is used to set up the super cell that contains a single atomic layer of h-BN separated by sufficient amount of vacuum in the z direction to offset

any interactions between layers. The free standing h-BN ML is relaxed to obtain the ground state. The bulk and ML structures of h-BN are shown in Fig S1. The lattice constant values and band gaps for the optimized bulk and ML are listed in Table 1 and are consistent with those of other experimental and GGA-PBE calculations [16, 25-28]. The band structures of the bulk and ML h-BN are presented in Fig S2. We see an indirect K–M (bulk) to direct K–K band (ML) transition, consistent with recent results showing a direct wide bandgap value of 4.65 eV in the ML. This is also in accordance with other 2D materials like MoS₂ which show an indirect to direct band cross over when going from the bulk to the ML [8, 29]. In the past there was a controversy about the nature of the bandgap of h-BN bulk and ML, but, with the recent experimental evidence using optical spectroscopy of Cassabois et al [15] and the work of Elias et al [16] who used a combination of deep-ultraviolet photoluminescence and reflectance spectroscopy with atomic force microscopy, it is now confirmed that there is an indirect to direct bandgap crossover in h-BN bulk to the ML. The bandgap is much smaller than experiment in this work due to the well known problem of underestimation of GGA-DFT works.

Dynamical optical conductivities and constants

The term “optical conductivity” means the electrical conductivity in the presence of an alternating electric field or dynamic electrical conductivity. The term “optical” here implies the entire frequency range, and is not restricted to just the visible region. The imaginary part of the dielectric constant is related to the real part of the AC conductivity and, therefore, to the optical reflectivity and transmittance [30]. The real part of the dynamic electrical conductivity is connected with the energy absorbed by the electrons. The imaginary part of dielectric function, $\epsilon_2(\omega)$, which represents absorption behavior, can be calculated from the electronic band structure. The real part of dielectric function, $\epsilon_1(\omega)$, can be calculated according to Kramers-Kronig relation [31] which represents the electronic polarization under incident light. The optical conductivity and absorption behaviour of ML h-BN with respect to the photon energies are shown in Figure 2. We see from the figure the maximum conductivity and absorption peaks are at ~ 6, 11 and 13.5eV that is in the mid-UV and DUV regions considering the in-plane xx and perpendicular zz directions. There is also a small shoulder at around 4.5eV. We also note that both the xx and zz directions have almost similar magnitudes for the conductivity and absorption coefficients $\alpha(\omega)$. The absorption coefficient peak value is in good agreement with the experimental work of Li et al [32].

A comparison with the supplementary information Figure S3 and S6 shows that the ML h-BN retains the bulk characteristics for the conductivities and absorption coefficients $\alpha(\omega)$, however, their magnitudes in the bulk are almost three times and two times more than the ML h-BN values respectively.

Figure 3 depicts the real and imaginary parts of the dielectric constant for the ML h-BN. The static values of the real dielectric constant are around 1.6 and 1.2 in the xx and zz directions respectively. Figs. 2(a) and (b) curves show the anisotropic behaviour in the two directions as in the previous conduction and absorption spectra Fig. 2.

However, for bulk h-BN, a look at Figure S4 shows that the static real dielectric constants are almost double in value around 3.6 and 2.3 in the in-plane and perpendicular directions respectively. A comparison of the magnitudes of the first sharp peaks of the imaginary dielectric constants Figs. 3(b) and S4(b) indicate the higher absorption capabilities of bulk as compared to that of ML h-BN.

From the values of $\epsilon_1(\omega)$ and $\epsilon_2(\omega)$ we can obtain the refractive index $n(\omega)$, reflectivity $R(\omega)$ and the extinction and absorption coefficients $k(\omega)$ and $\alpha(\omega)$ respectively from the relevant equations as detailed in the work [33]. The refractive index and extinction coefficients are shown in Fig. 4. Once again we notice the anisotropy in the xx and zz directions. The static refractive index values obtained are 1.3 and 1.1 in the in-plane and out of plane directions respectively and ML h-BN is transparent in the IR and visible region for xx direction and also in mid-DUV for the zz direction as evinced from the flatness of the curves. A direct comparison of the refractive indices of the bulk and ML is depicted in S5 and we see that the bulk values are consistently higher at 1.9 and 1.5 in the xx and zz directions respectively and reflect the higher electron density in the bulk. For the sake of better readability the static values of the refractive indices, the reflectivity and absorption coefficients for the bulk and ML h-BN in both the in-plane xx and out of plane zz directions have been gathered in Table 2. The table also includes the energies at the zero values of $\epsilon_1(\omega)$.

The reflectivity plots for the ML and bulk h-BN are represented in Figure 5. The static values of reflectivity are very low both for ML and bulk h-BN and continues to be low over a wide range of photon energies 0-9eV for the perpendicular component which peaks in DUV region. Whereas, for the in-plane direction the reflectivity values are low in the visible and the first peak is around 6eV.

Discussion

The electronic structure calculations in this work confirms the previous literature results [15, 16, 27, 28] of the bandgap crossover of indirect to direct in h-BN bulk to ML. However, although the band gap values are in fair agreement with other theoretical works it is underestimated in comparison with experimental findings of 6.1eV in ML h-BN [16] due to the shortcomings of the GGA exchange correlation potential. A more accurate calculation using the Modified Becke-Johnson (mBJ) approximation [34, 35] is expected to give a better estimate for the bandgap and is part of future work.

The optical properties are qualitatively consistent with other theoretical and experimental works [16, 32, 36-38] and reinstate the importance of h-BN in DUV optoelectronics. Essentially the h-BN ML mimics the behaviour of the bulk and the shape and peak positions for the optical conductivity and constants are similar but the magnitude is much lower owing to the higher values of the dielectric constants in the bulk. Since, the attractive wide band and optical properties in DUV is maintained in the ML h-BN, with the added advantage of a direct bandgap, ML h-BN is a promising candidate for nano-optoelectronics in the DUV region. Numerous applications as DUV photo detectors/emitters, possible integration with graphene optoelectronics

due its flatness and similarity in structure and close lattice constant values, and in addition, its promise for realizing chip-scale DUV light sources are all waiting to be realized. Moreover, it can be argued that the optical properties of h-BN in the ultraviolet are very useful for the study of peptides and other biomolecules [16, 39, 40].

Conclusions

In conclusion, the study of the optoelectronic properties of ML h-BN using first principles FP-LAPW method with the GGA approximation shows an indirect K–M to direct K–K band transition when going from the bulk to the ML with a wide bandgap value of 4.65 eV, consistent with recent results. The excellent values of conductivity and absorption in the mid UV and DUV uphold the great promise of this material for use in DUV optics and energy conversions. A more accurate calculation using mBJ exchange correlation to reconfirm these very interesting optical properties is highly desirable and is the future direction.

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 280 (2020) 025304
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Table 1 (on next page)

Structural and electronic

Table 1 Structural and electronic properties of the relaxed h-BN

Table 1 Structural and electronic properties of the relaxed h-BN bulk and ML

Compound	Space Group	Lattice constant (Å)		Bandgap (eV)		Inter layer spacing	Other works		
		a	c				a	c	bandgap
h-BN bulk	P63/mmc #194	2.517	6.706	4.23	K–M indirect	3.353	2.505 ^a 2.511 ^b	6.661 ^a 6.688 ^b	5.955 ^c
h-BN ML	P-6 m 2 #187	2.515	15.063	4.65	K–K direct	-			6.1 ^d

^(a)Ref. 25 ^(b)Ref. 26 ^(c)Ref. 16, 27, 28 ^(d)Ref. 16

Table 2 (on next page)

Static values of optical properties

Table 2 The zero ω -values of $\epsilon_1(\omega)$ and the static optical constants (at $\omega=0$): dielectric constant $\epsilon_1(0)$, refractive index $n(0)$, reflectivity $R(0)$ and absorption coefficient $I(0)$ for the bulk and ML h-BN

- 1 **Table 2** The zero y-values of $\epsilon_1(\omega)$ and the static optical constants (at $\omega=0$): dielectric constant $\epsilon_1(0)$, refractive
- 2 index $n(0)$, reflectivity $R(0)$ and absorption coefficient $I(0)$ for the bulk and ML h-BN

Compound	Zeros of $\epsilon_1(\omega)$ [eV]		$\epsilon_1(0)$		$n(0)$		$R(0)$		$I(0)$	
	xx	zz	xx	zz	xx	zz	xx	zz	xx	zz
hBN bulk	5.84; 9.13	11.22; 12.20	3.64	2.32	1.91	1.52	0.097	0.043	0.0055	0.0024
hBN ML	13.51	13.56	1.66	1.22	1.29	1.10	0.016	0.002	0.0021	0.0004

3

Figure 1

h-BN molecule

Figure 1 Illustration of an h-BN molecule

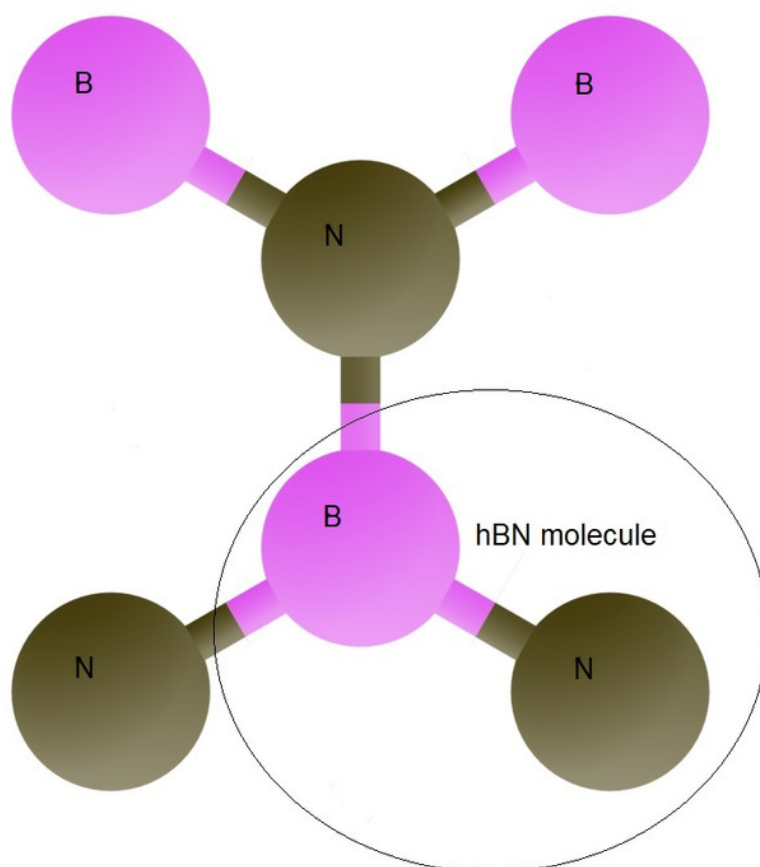


Figure 2

The Optical conductivity

Figure 2 (a). The optical conductivities for ML h-BN in the xx in-plane and zz out of plane directions.

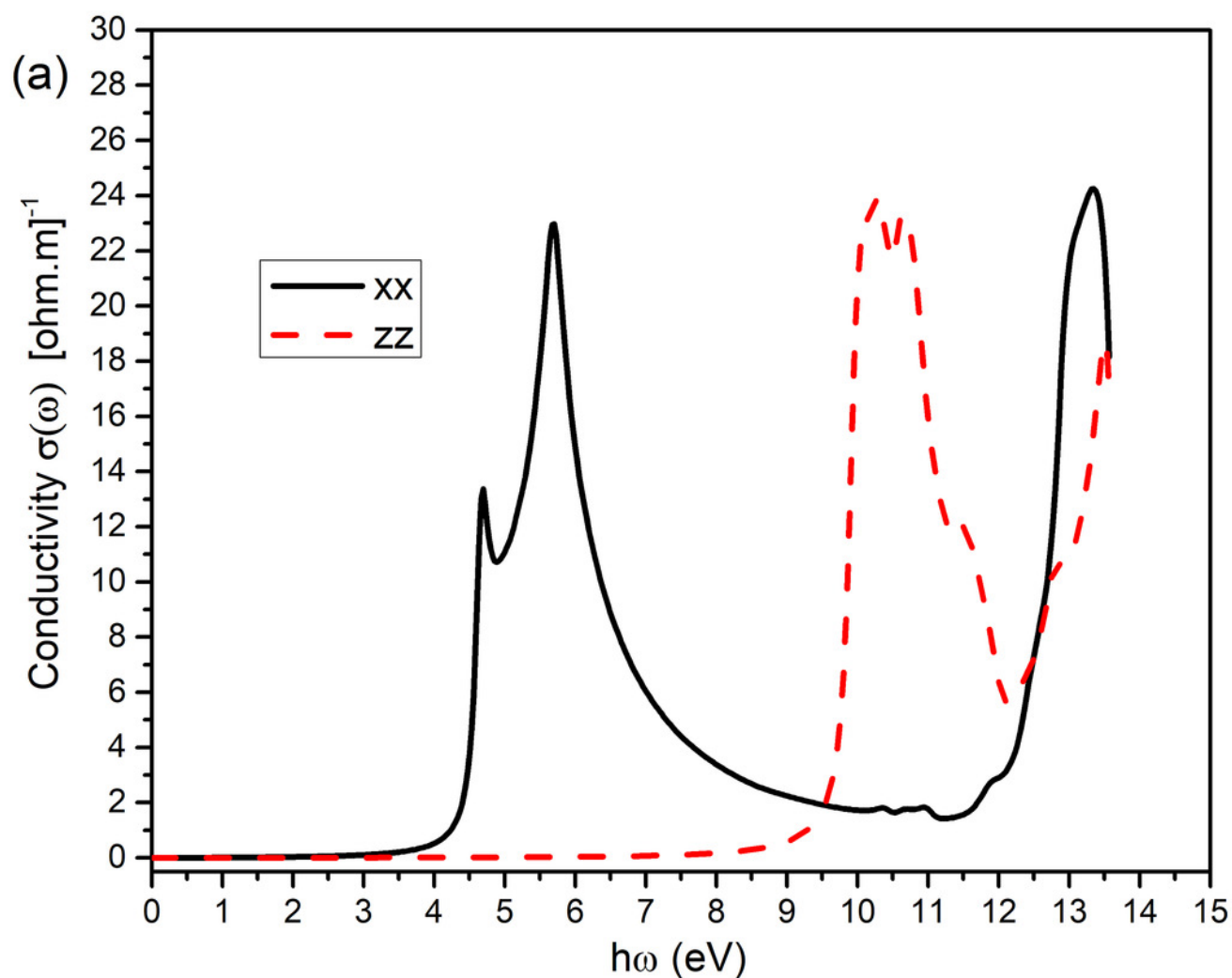


Figure 3

The absorption coefficient

Figure 2 (b). The absorption coefficients for ML h-BN in the xx in-plane and zz out of plane directions.

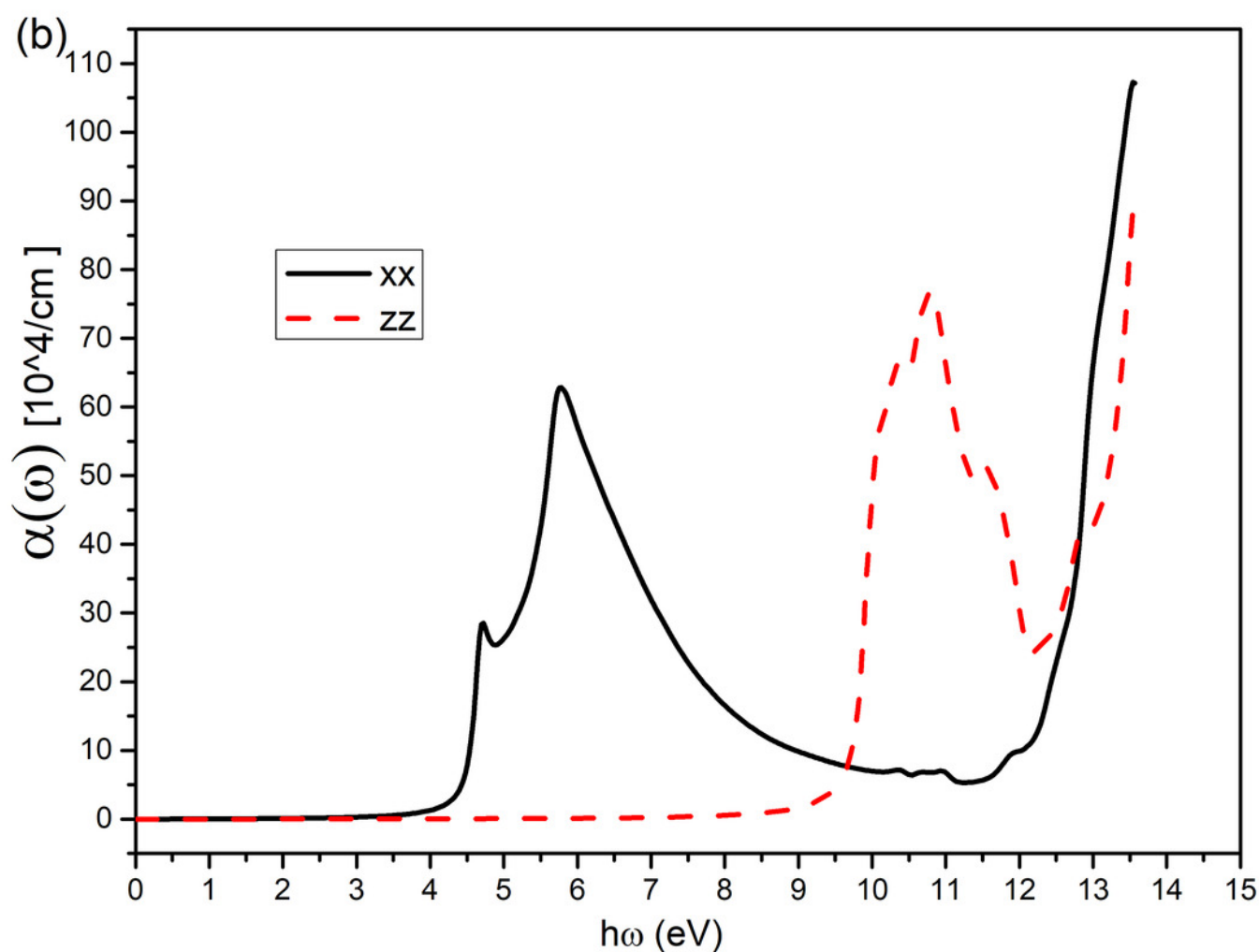


Figure 4

The dielectric function

Figure 3(a). The real parts of the dielectric function in the xx and zz directions for ML h-BN

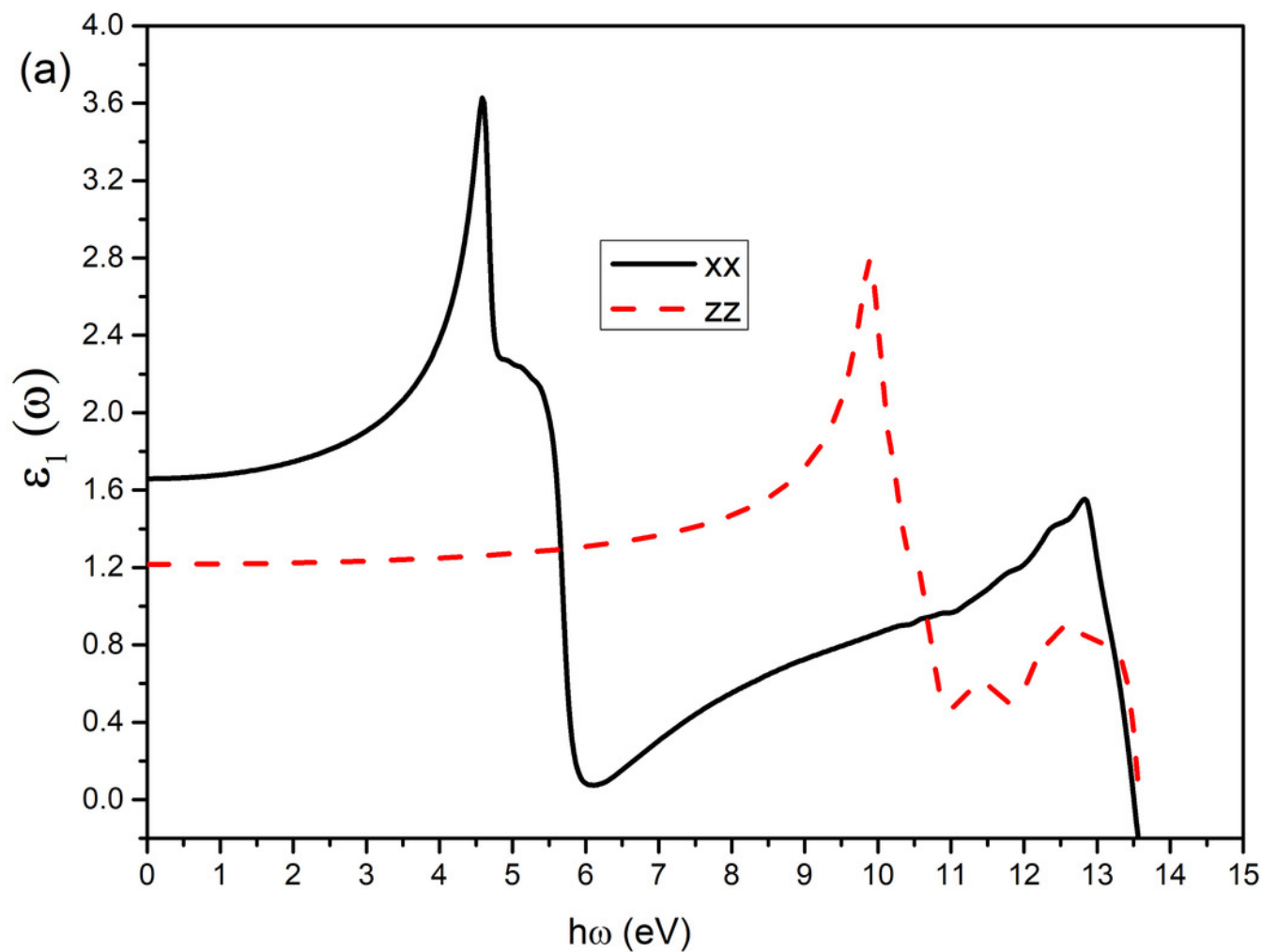


Figure 5

The dielectric function

Figure 3(b). The imaginary parts of the dielectric function in the xx and zz directions for ML h-BN

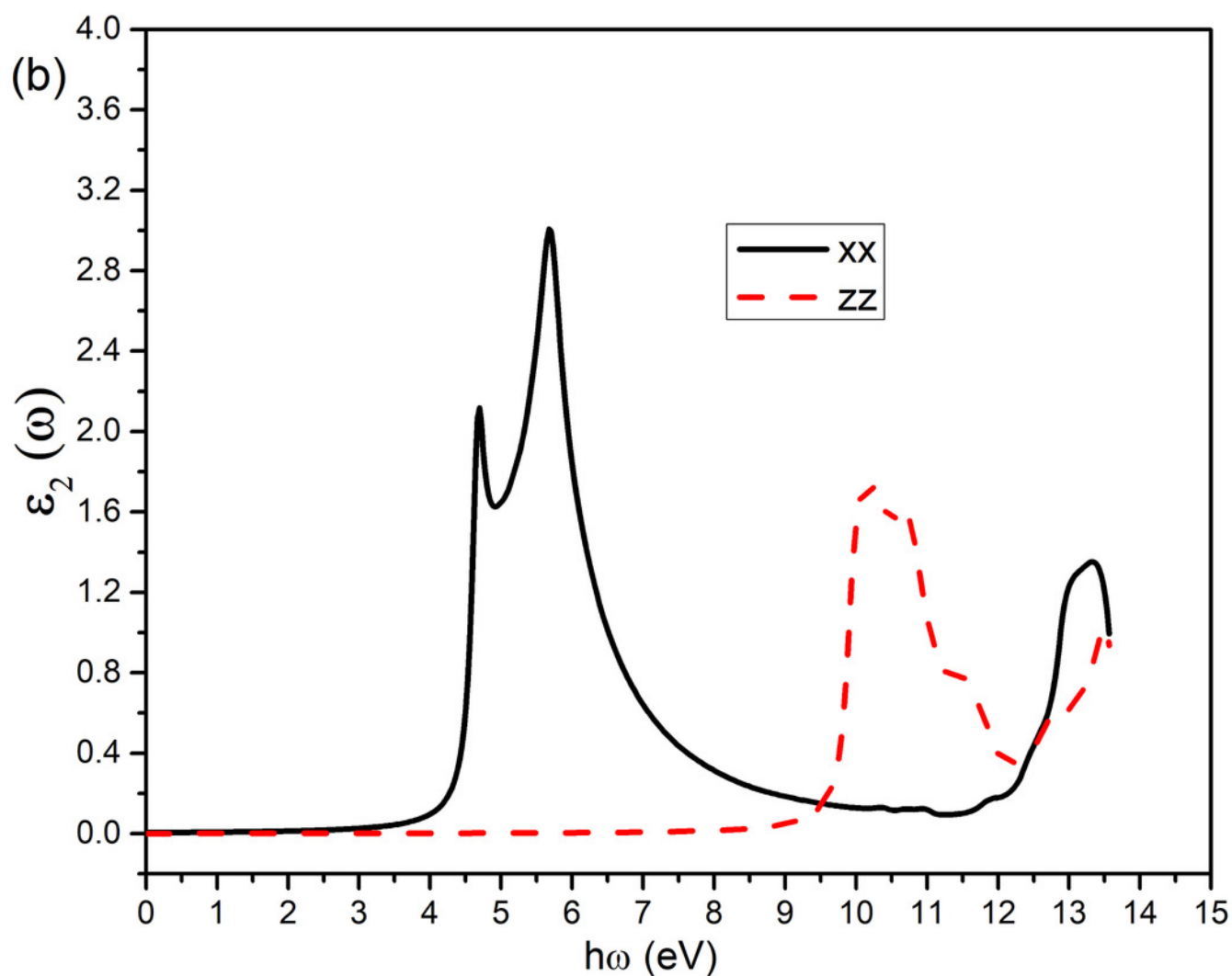


Figure 6

The refractive index

Figure 4(a). The refractive indices in the xx and zz directions for ML h-BN

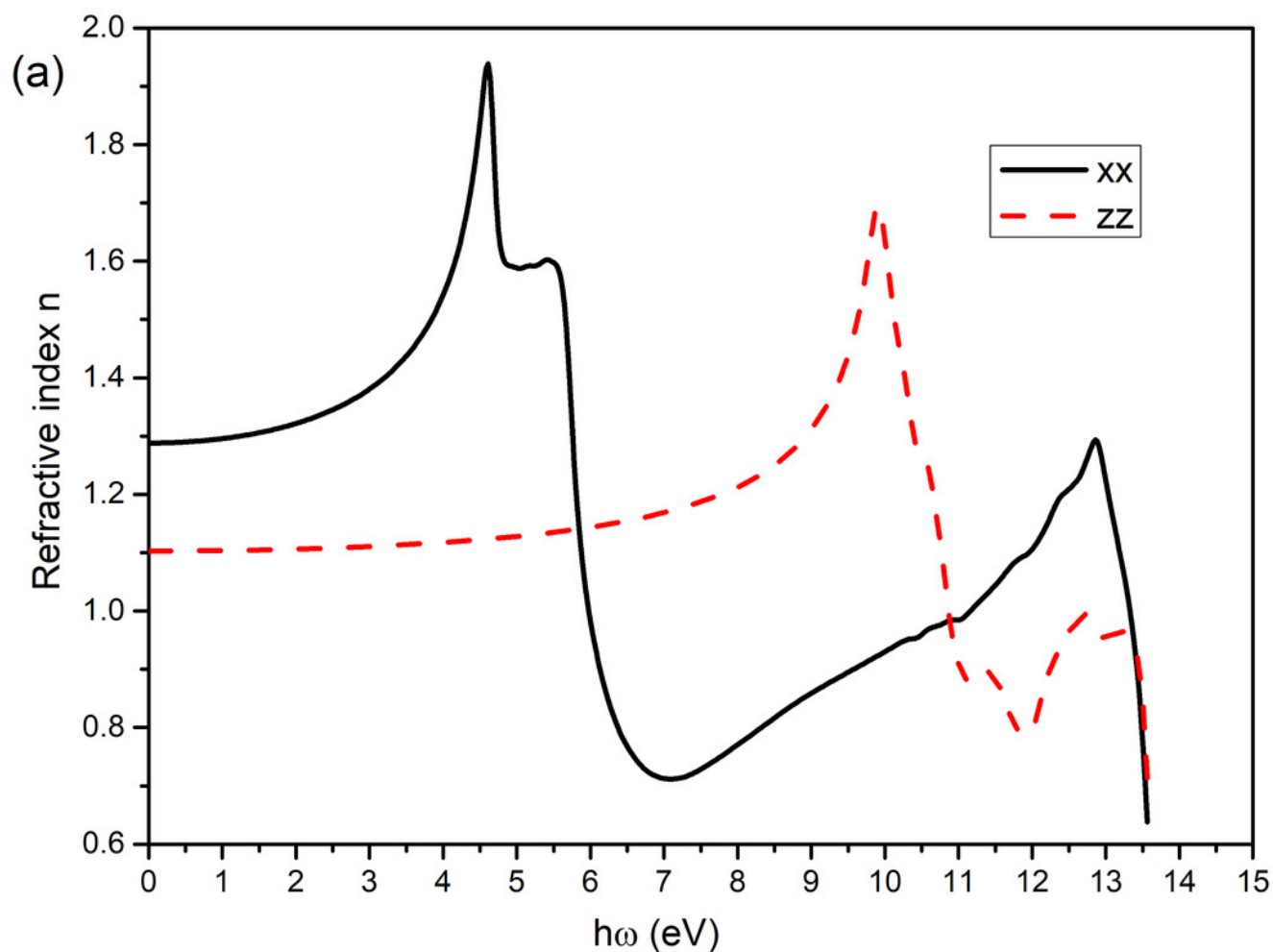


Figure 7

The extinction coefficient

Figure 4(b). The extinction coefficients in the xx and zz directions for ML h-BN

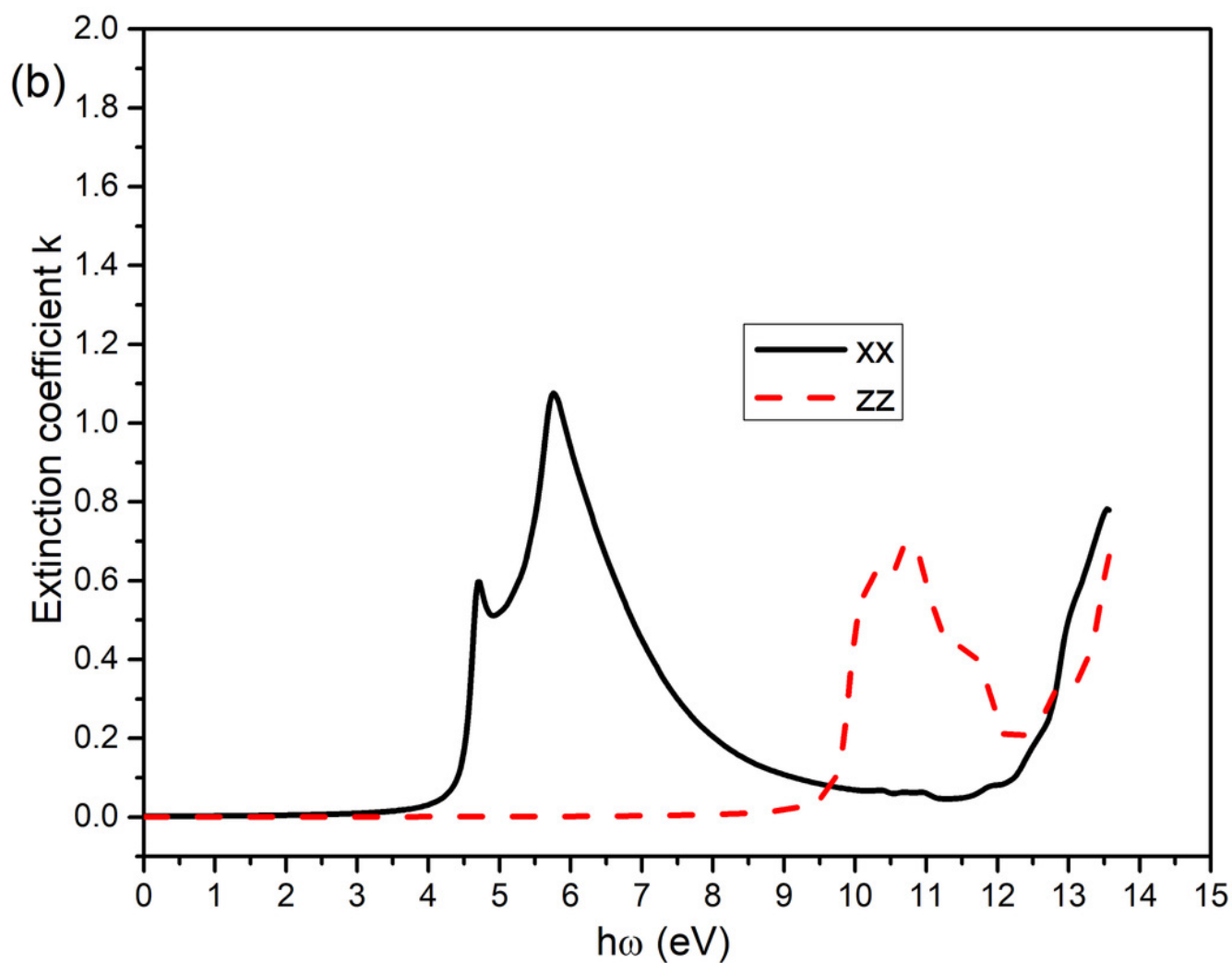


Figure 8

The reflectivity of ML h-BN

Figure 5(a). The reflectivity plots for ML h-BN in the xx and zz directions

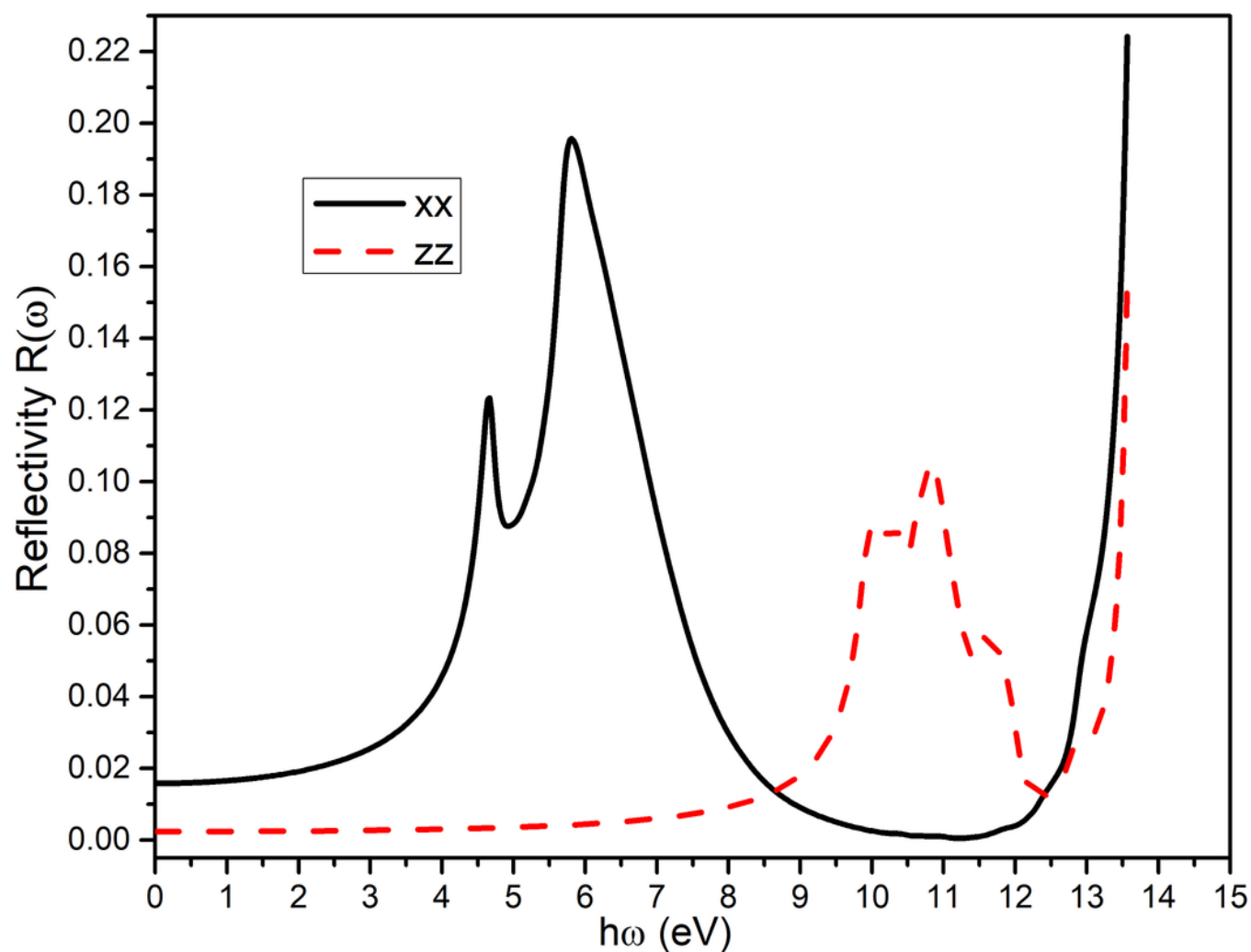


Figure 9

The bulk h-BN reflectivity

Figure 5(b). The reflectivity plots for bulk h-BN in the xx and zz directions

