

Channel state information estimation for 5G wireless communication systems: Recurrent neural networks approach

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In this study, a deep learning bidirectional long short-term memory (BiLSTM) recurrent neural network-based channel state information estimator is proposed for 5G orthogonal frequency-division multiplexing systems. The proposed estimator is a pilot-dependent estimator and follows the online learning approach in the training phase and the offline approach in the practical implementation phase. The estimator does not deal with complete a priori certainty for channels' statistics and attains superior performance in the presence of a limited number of pilots. A comparative study is conducted using three loss functions, namely, mean absolute error, cross entropy function for k th mutually exclusive classes and sum of squared of the errors. The Adam optimisation algorithm is used to evaluate the performance of the proposed estimator under each loss function. In terms of symbol error rate and accuracy metrics, the proposed estimator outperforms long short-term memory (LSTM) neural network-based channel state information, least squares and minimum mean square error estimators under different simulation conditions. The computational and training time complexities for deep learning BiLSTM- and LSTM-based estimators are provided. Given that the proposed estimator relies on the deep learning neural network approach, where it can analyse massive data, recognise statistical dependencies and characteristics, develop relationships between features and generalise the accrued knowledge for new datasets that it has not seen before, the approach is promising for any 5G and beyond communication system.

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20 Abstract

21 In this study, a deep learning bidirectional long short-term memory (BiLSTM) recurrent neural
22 network-based channel state information estimator is proposed for 5G orthogonal frequency-
23 division multiplexing systems. The proposed estimator is a pilot-dependent estimator and follows
24 the online learning approach in the training phase and the offline approach in the practical
25 implementation phase. The estimator does not deal with complete a priori certainty for channels'
26 statistics and attains superior performance in the presence of a limited number of pilots. A
27 comparative study is conducted using three loss functions, namely, mean absolute error, cross
28 entropy function for k th mutually exclusive classes and sum of squared of the errors. The Adam
29 optimisation algorithm is used to evaluate the performance of the proposed estimator under each
30 loss function. In terms of symbol error rate and accuracy metrics, the proposed estimator
31 outperforms long short-term memory (LSTM) neural network-based channel state information,
32 least squares and minimum mean square error estimators under different simulation conditions.
33 The computational and training time complexities for deep learning BiLSTM- and LSTM-based
34 estimators are provided. Given that the proposed estimator relies on the deep learning neural
35 network approach, where it can analyse massive data, recognise statistical dependencies and
36 characteristics, develop relationships between features and generalise the accrued knowledge for
37 new datasets that it has not seen before, the approach is promising for any 5G and beyond
38 communication system.

39

40 Introduction

41 5G wireless communication is the most active area of technology development and a rapidly
42 growing branch of the wider field of communication systems. Wireless communication has made
43 possible various services ranging from voice to multimedia.

44 The physical characteristics of the wireless communication channel and many unknown
45 surrounding effects result in imperfections in the transmitted signals. The transmitted signals
46 experience reflections, diffractions and scattering, which in turn produce multipath signals with
47 different delays, phase shift, attenuation and distortion arriving at the receiving end; hence, they
48 adversely affect the recovered signals.

49 A priori information on the physical characteristics of the channel provided by pilots is one of
50 the major factors that determine the efficiency of channel state information estimators (CSIEs).
51 For instance, if not a priori information is available (no or insufficient pilots), then channel
52 estimation is useless; finding what you do not know is impossible. When complete information
53 on the transmission channel is available, CSIEs are no longer needed. Thus, a priori uncertainty
54 exists for communication channel statistics. However, the classical theory of detection, recognition
55 and estimation of signals deals with complete a priori certainty for channel statistics, and it is an
56 unreliable and unpractical assumption.

57 In the classic case, uncertainty is related to useful signals. In detection problems, the unknown
58 is the fact of a signal existence. In recognition problems, the unknown is the type of signal being
59 received at the current moment. In estimation problems, the unknown is the amplitude of the
60 measured signal or one of its parameters. The rest of the components of the signal-noise
61 environment in classical theory are regarded as a priori certain (known) as follows: the known is
62 the statistical description of the noise, the known is the values of the unmeasured parameters of
63 the signal and the known is the physical characteristics of the wireless communication channel. In
64 such conditions, the classical theory allows the synthesis of optimal estimation algorithms, but the
65 structure and quality coefficients of the algorithms depend on the values of the parameters of the
66 signal-noise environment. If the values of the parameters describing the signal-noise environment
67 are slightly different from the parameters for which the optimal algorithm is built, then the quality
68 coefficients will become substantially poor, making the algorithm useless in several cases [1], [2].

69 The most frequently used CSIEs are derived from signal and channel statistical models by
70 employing techniques, such as maximum likelihood (ML), least squares (LS) and minimum mean
71 squared error (MMSE) optimisation metrics [3].

72 One of the major concerns in the optimum performance of wireless communication systems is
73 the means of providing accurate channel state information (CSI) at the receiver end of the systems
74 to coherently detect the transmitted signal. If CSI is unavailable at the receiver end, then the
75 transmitted signal can only be demodulated and detected by a noncoherent technique, such as
76 differential demodulation. However, the use of a noncoherent detection method occurs at the
77 expense of a loss of signal-to-noise ratio of about 3–4 dB compared with using a coherent detection
78 technique. To eliminate such losses, researchers have focused on the development of channel
79 estimation techniques to provide perfect detection of transmitted information in wireless
80 communication systems using the OFDM modulation scheme [4].

81 The use of deep learning neural networks (DLNNs) is the state-of-the-art approach in the field
82 of wireless communication. The amazing learning capabilities of DLNNs from training data sets
83 and the tremendous progress of graphical processing units (GPUs), which are considered the most
84 powerful tools for training DLNNs, have motivated its usage for different wireless communication
85 issues, such as modulation recognition [5], [6] and channel state estimation and detection [7-13].
86 According to [4] – [7] and [10], all proposed deep learning-based CSIEs have better performance
87 compared with the examined traditional channel ones, such as LS and MMSE estimators.

88 Recently, numerous long short-term memory (LSTM)- and BiLSTM-based applications have
89 been introduced for prognostic and health management [14], artificial intelligence-based
90 translation systems [15], [16] and other areas.

91 For channel state information estimation in 5G-OFDM wireless communication systems, many
92 deep learning approaches, such as convolutional neural network (CNN), recurrent neural network
93 (RNN) (e.g. LSTM and BiLSTM NNs) and hybrid (CNN and RNN) neural networks have been
94 used.

95 In [17], a deep learning-based CSIE was proposed by using CNN and BiLSTM-NN for the
96 extraction of the feature vectors of the channel response and channel estimation, respectively. The
97 aim was to improve the channel state information estimation performance at the downlink, which
98 is caused by the fast time-varying and varying channel statistical characteristics in high-speed
99 mobility scenarios. In [18], an online-trained CSIE that is an integration of CNN and LSTM-NN
100 was proposed. The authors also developed an offline–online training technique that applies to 5G
101 wireless communication systems. In [7], a joint channel estimator and detector that is based on
102 feedforward DLNNs for frequency selective channel (OFDM) systems was introduced. The
103 proposed algorithm was found to be superior to the traditional MMSE estimation method when
104 unknown surrounding effects of communication systems are considered. In [19], an online
105 estimator was developed by adopting feedforward DLNNs for doubly selective channels. The
106 proposed estimator was considered superior to the traditional LMMSE estimator in all investigated
107 scenarios. In [10], a one-dimensional CNN (1D-CNN) deep learning estimator was proposed.
108 Under various modulation scenarios and in terms of MSE and BER metrics, the authors compared
109 the performance of the proposed estimator with that of feedforward neural networks (FFNN),
110 MMSE and LS estimators. 1D-CNN outperformed LS, MMSE and FFNN estimators. In [11], an
111 online pilot-assisted estimator model for OFDM wireless communication systems was developed
112 by using LSTM NN. The conducted comparative study showed the superior performance of the
113 proposed estimator in comparison with LS and MMSE estimators under limited pilots and a prior
114 uncertainty of channel statistics. The authors in [20] used the genetic algorithm-optimised artificial
115 neural network to build a CSIE. The proposed estimator was dedicated for space–time block-
116 coding MIMO-OFDM communication systems. The proposed estimator outperformed LS and
117 MMSE estimators in terms of BER at high SNRs, but it achieved approximately the same
118 performance as LS and MMSE estimators at low SNRs. The authors in [21] proposed a CSIE for
119 OFDM systems by using ANN under the condition of sparse multipath channels. The proposed
120 estimator achieved a comparable SER performance as matching pursuit- and orthogonal matching
121 pursuit-based estimators at a lower computational complexity than that of the examined
122 estimators.

123 In this study, a BiLSTM DLNN-based CSIE for OFDM wireless communication systems is
124 proposed and implemented. To the best of the authors' knowledge, this work is the first to use the
125 BiLSTM network as a CSIE without integration with CNN. The proposed estimator does not need
126 any prior knowledge of the communication channel statistics and powerfully works at limited
127 pilots (under the condition of less CSI).

128 Although an impressively wide range of configurations can be found for almost every aspect of
129 deep neural networks, one element is underrepresented when addressing communication
130 problems: most studies and applications simply use the 'log' loss function [22].

131 The loss function estimates the loss between the expected and actual outcome. This function can
132 be calculated in many ways. Selecting a loss function is one of the essential and challenging tasks
133 in deep learning. During the learning process, optimisation (learning) algorithms try to minimise
134 the available loss function to the desired error goal by optimising the DLNN weights and biases
135 iteratively at each training epoch. The proposed estimator is trained using the Adam optimisation
136 algorithm and three different loss functions to obtain the most optimal BiLSTM-based estimator
137 for wireless communication systems with low prior information (limited pilots) for signal-noise
138 environments. The obtained results show that the BiLSTM-based estimator attains a comparable
139 performance as the MMSE estimator and outperforms LS and MMSE estimators at large and small
140 numbers of pilots, respectively. In addition, the proposed estimator improves the transmission data
141 rate of OFDM wireless communication systems because it exhibits optimal performance compared
142 with the examined estimators at a small number of pilots.

143 The proposed BiLSTM-based CSIE is a data-driven estimator, so it can analyse, recognise and
144 understand the statistical characteristics of wireless channels suffering from many known and

145 unknown interferences. The performance of the proposed BiLSTM-based estimator is compared
 146 with the performance of the most frequently used LS and MMSE channel state estimators.

147 The rest of this paper is organised as follows. The DLNN-based CSIE is presented in Section
 148 II. The standard OFDM system and the proposed deep learning BiLSTM NN-based CSIE are
 149 presented in Section III. The simulation results are given in Section IV. The conclusions and future
 150 work directions are provided in Section V.

151

152 DLNN-BASED CSIE

153 Add your materials and methods here.

154 In this section, a deep learning BiLSTM NN for channel state information estimation is
 155 presented. The BiLSTM network is another version of LSTM neural networks, which are recurrent
 156 neural networks (RNN) that can learn the long-term dependencies between the time steps of input
 157 data [23] [14, 24].

158 The BiLSTM architecture mainly consists of two separate LSTM-NNs and has two propagation
 159 directions (forward and backward). The LSTM NN structure consists of input, output and forget
 160 gates and a memory cell. The forget and input gates enable the LSTM NN to effectively store long-
 161 term memory. Figure 1 shows the main construction of the LSTM cell. The forget gate enables
 162 LSTM NN to remove the undesired information by currently used input x_t and cell output h_t of the
 163 last process. The input gate finds the information that will be used with the previous LSTM cell
 164 state c_{t-1} to obtain a new cell state c_t based on the current cell input x_t and the previous cell output
 165 h_{t-1} . Using the forget and input gates, LSTM can decide which information is abandoned and which
 166 is retained.

167 The output gate finds current cell output h_t by using the previous cell output h_{t-1} at current cell
 168 state c_t and input x_t . The mathematical model of the LSTMNN structure can be described through
 169 Equations (1)–(6).

$$170 \quad i_t = \sigma_g (w_i x_t + R_i h_{t-1} + b_i), \quad (1)$$

$$171 \quad f_t = \sigma_g (w_f x_t + R_f h_{t-1} + b_f), \quad (2)$$

$$172 \quad g_t = \sigma_c (w_g x_t + R_g h_{t-1} + b_g), \quad (3)$$

$$173 \quad o_t = \sigma_g (w_o x_t + R_o h_{t-1} + b_o), \quad (4)$$

$$174 \quad c_t = f_t \odot c_{t-1} + i_t \odot g_t, \quad (5)$$

$$175 \quad h_t = o_t \odot \sigma_c(c_t), \quad (6)$$

176 where $i, f, g, o, \sigma_c, \sigma_g$ and \odot denote the input gate, forget gate, cell candidate, output gate, state
 177 activation function (hyperbolic tangent function (tanh), gate activation function (sigmoid function)
 178 and Hadamard product (element-wise multiplication of vectors), respectively. $\mathbf{W} = [w_i \ w_f \ w_g \ w_o]^T$
 179 , $\mathbf{R} = [R_i \ R_f \ R_g \ R_o]^T$ and $\mathbf{b} = [b_i \ b_f \ b_g \ b_o]^T$ are input weights, recurrent weights and bias, respectively.

180 The forward and backward propagation directions of BiLSTM are transmitted at the same time
 181 to the output unit. Therefore, old and future information can be captured, as shown in Figure 2. At
 182 any time t , the input is fed to forward LSTM and backward LSTM networks. The final output of
 183 BiLSTM-NN can be expressed as follows:

$$184 \quad h_t = \vec{h}_t \odot \overleftarrow{h}_t, \quad (7)$$

185 where \vec{h}_t and \overleftarrow{h}_t are forward and backward outputs of BiLSTM-NN, respectively.

186 The proposed BiLSTM-based CSIE is built. The weights and biases of the proposed estimator
 187 are optimised (tuned) using the Adam optimization algorithm. Adam trains the proposed estimator
 188 by using three loss functions, namely, mean absolute error (MAE), cross entropy function for k^{th}
 189 mutually exclusive classes (crossentropyex) and sum of squared errors (SSE). The use of these
 190 loss functions aims to obtain the most reliable and robust estimator under unknown channel
 191 statistical characteristics and limited pilot numbers.

192 To build the DL BiLSTM NN-based CSIE, an array is created with the following five layers:
193 sequence input, BiLSTM, fully connected, softmax and output classification. The input size was
194 set to 256. The BiLSTM layer consists of 16 hidden units and shows the sequence's last element.
195 Four classes are specified by considering the size 4 fully connected (FC) layer, followed by a
196 softmax layer and ended by a classification layer. Figure 3(a) illustrates the structure of the
197 proposed estimator. Figure 3(a) can be compacted in one block as in Figure 3(b).

198

199

200 DL BiLSTM NN-BASED CSIE for 5G-OFDM WIRELESS

201 COMMUNICATION SYSTEMS

202 The standard OFDM wireless communication system and an offline DL of the proposed CSIE are
203 presented in the following subsections.

204

205 OFDM SYSTEM MODEL

206 In accordance with [11], Figure 4 clearly illustrates the structure of the traditional OFDM
207 communication system. On the transmitter side, a serial-to-parallel converter is used to convert the
208 transmitted symbols with pilot signals into parallel data streams. Then, inverse discrete Fourier
209 transform is applied to convert the signal into the time domain. A cyclic prefix must be added to
210 alleviate the effects of inter-symbol interference. The length of the cyclic prefix must be longer
211 than the maximum spreading delay of the channel.

212 The multipath channel of a sample space defined by complex random variables $\{h(n)\}_{n=0}^{N-1}$ is
213 considered. Then, the received signal can be evaluated as follows:

$$214 \quad y(n) = x(n) \oplus h(n) + w(n), \quad (8)$$

215 where $x(n)$ is the input signal, \oplus is circular convolution, $w(n)$ is additive white Gaussian noise
216 (AWGN) and $y(n)$ is the output signal.

217 The received signal in the frequency domain can be defined as

$$218 \quad Y(k) = X(k)H(k) + W(k), \quad (9)$$

219 where the discrete Fourier transformations of $x(n)$, $h(n)$, $y(n)$ and $w(n)$ are $X(k)$, $H(k)$, $Y(k)$ and
220 $W(k)$, respectively. These discrete Fourier transformations are estimated after removing CP.

221 The OFDM frame includes the pilot symbols of the 1st OFDM block and the transmitted data of
222 the next OFDM blocks. The channel can be considered stationary during a certain frame, but it
223 can change between different frames. The proposed DL BiLSTM NN-based CSIE receives the
224 arrived data at its input terminal and extracts the transmitted data at its output terminal [11], [7].

225

226 OFFLINE DL OF THE DL BiLSTM NN-BASED CSIE

227 DLNN utilisation is the state-of-the-art approach in the field of wireless communication, but
228 DLNNs have high computational complexity and long training time. GPUs are the most powerful
229 tools used for training DLNNs [25]. Training should be done offline due to the long training time
230 of the proposed CSIE and the large number of BiLSTM-NN's parameters, such as biases and
231 weights, that should be tuned during training. The trained CSIE is then used in online
232 implementation to extract the transmitted data [7], [11].

233 In offline training, the learning dataset is randomly generated for one subcarrier. The
234 transmitting end sends OFDM frames to the receiving end through the adopted (simulated)
235 channel, where each frame consists of single OFDM pilot symbol and a single OFDM data symbol.
236 The received OFDM signal is extracted based on OFDM frames that are subjected to different
237 channel imperfections.

238 All classical estimators rely highly on tractable mathematical channel models, which are
 239 assumed to be linear, stationary and follow Gaussian statistics. However, practical wireless
 240 communication systems have other imperfections and unknown surrounding effects that cannot be
 241 tackled well by accurate channel models; therefore, researchers have developed various channel
 242 models that effectively characterise practical channel statistics. By using these channel models,
 243 reliable and practical training datasets can be obtained by modelling [1], [11], [26].

244 In this study, the 3GPP TR38.901-5G channel model developed by [26] is used to simulate the
 245 behaviour of a practical wireless channel that can degrade the performance of CSIEs and hence,
 246 the overall communication system's performance.

247 The proposed estimator is trained via Adam optimisation, which updates the weights and biases
 248 by minimising a specific loss function. Simply, a loss function is defined as the difference between
 249 the estimator's responses and the original transmitted data. The loss function can be represented
 250 by several functions. MATLAB/software allows the user to choose a loss function amongst its
 251 available list that contains crossentropyex, MSE, sigmoid and softmax. In this study, another two
 252 custom loss functions (MAE and SSE) are created. The performance of the proposed estimator
 253 when using three loss functions (i.e. MAE, crossentropyex and SSE) is investigated. The loss
 254 functions can be expressed as follows:

$$255 \quad \text{crossentropyex} = -\sum_{i=1}^N \sum_{j=1}^c X_{ij}(k) \log(\hat{X}_{ij}(k)), \quad (10)$$

$$256 \quad \text{MAE} = \frac{\sum_{i=1}^N \sum_{j=1}^c |X_{ij}(k) - \hat{X}_{ij}(k)|}{N}, \quad (11)$$

$$257 \quad \text{SSE} = \sum_{i=1}^N \sum_{j=1}^c (X_{ij}(k) - \hat{X}_{ij}(k))^2, \quad (12)$$

258

259 where N is the sample number, c is the class number, X_{ij} is the i^{th} transmitted data sample for the
 260 j^{th} class and $\hat{\cdot}$ is the DL BiLSTM-based CSIE response for sample i for class j .

261 Figure 5 illustrates the processes of generating the training data sets and offline DL to obtain a
 262 learned CSIE based on BiLSTM-NN.

263

264 Simulation Results

265 STUDYING THE PERFORMANCE OF THE PROPOSED, LS AND MMSE 266 ESTIMATORS BY USING DIFFERENT PILOTS AND LOSS FUNCTIONS

267 Several simulation experiments are performed to evaluate the performance of the proposed
 268 estimator. In terms of symbol error rate (SER) performance analysis, the SER performance of the
 269 proposed estimator under various SNRs is compared with that of the LSTM NN-based CSIE [11],
 270 the well-known LS estimator and the MMSE estimator, which is an optimal estimator but requires
 271 channel statistical information. A priori uncertainty of the used channel model statistics is assumed
 272 and considered for all conducted experiments.

273 Moreover, the Adam optimisation algorithm is used to train the proposed estimator whilst using
 274 different loss functions to obtain the most robust version of the proposed CSIE. The proposed model
 275 is implemented in 2019b MATLAB/software.

276 Table 1 lists the parameters of BiLSTM-NN and LSTM-NN architectures and their related training
 277 options. These parameters are identified by a trial-and-error approach. Table 2 lists the parameters
 278 of the OFDM system model and the channel model.

279 The examined estimators' performance is evaluated at different pilot numbers of 4, 8 and 64 as
 280 well as crossentropyex, MAE and SSE loss functions. The Adam optimisation algorithm is used for
 281 all simulation experiments.

282 With a sufficiently large number of pilots (64) and the use of the crossentropyex loss function, the
 283 proposed BiLSTM_{crossentropyex} estimator outperforms LSTM_{crossentropyex}, LS and MMSE estimators
 284 over the entire SNR range, as shown in Figure 6.

285 Figure 7 indicates that at pilot number = 64 and with the MAE loss function, the $\text{BiLSTM}_{\text{MAE}}$
286 estimator outperforms the LS estimator over the SNR range [0–18 dB], but LSTM_{MAE} outperforms
287 it over the SNR range [0–15 dB]. In addition, the $\text{BiLSTM}_{\text{MAE}}$ and LSTM_{MAE} estimators are at par
288 with the MMSE estimator over the SNR ranges [0–10 dB] and [0–4 dB], respectively. Beyond these
289 SNR ranges, the MMSE estimator outperforms $\text{BiLSTM}_{\text{MAE}}$ and LSTM_{MAE} estimators.
290 $\text{BiLSTM}_{\text{MAE}}$ outperforms LSTM_{MAE} starting from 5 dB to 20 dB.

291 At the same number of pilots and with the use of the SSE loss function, Figure 8 shows that the
292 $\text{BiLSTM}_{\text{SSE}}$ and LSTM_{SSE} estimators achieve the same performance as the MMSE estimator over a
293 low SNR range [0–7 dB]. MMSE outperforms the $\text{BiLSTM}_{\text{SSE}}$ and LSTM_{SSE} estimators starting
294 from 8 dB, and the LS estimator outperforms $\text{BiLSTM}_{\text{SSE}}$ starting from 15 dB and LSTM_{SSE} starting
295 from 13 dB. $\text{BiLSTM}_{\text{SSE}}$ outperforms LSTM_{SSE} starting from 9 dB to 20 dB. LS provides poor
296 performance compared with MMSE because it does not use prior information about channel statistics
297 in the estimation process. MMSE exhibits superior performance, especially with sufficient pilot
298 numbers, because it uses second-order channel statistics.

299 Figure 9 summarises the performance of the proposed and the other considered estimators for
300 various loss functions at 64 pilots. MMSE and the proposed $\text{BiLSTM}_{\text{crossentropyex}}$ attain close SER
301 performance with respect to all SNRs. Furthermore, at low SNR (0–7 dB), $\text{BiLSTM}_{\text{(crossentropyex, MAE, and SSE)}}$,
302 $\text{LSTM}_{\text{(crossentropyex, MAE, and SSE)}}$ and MMSE attain approximately the same performance.

303 Figures 10–13 present the performance comparison of LS, MMSE, BiLSTM and LSTM -based
304 estimators using the Adam optimisation algorithm and the different (crossentropyex, MAE and SSE)
305 loss functions at 8 pilots. Figure 13 shows that the proposed $\text{BiLSTM}_{\text{(crossentropyex, or MAE or SSE)}}$
306 estimators outperform the $\text{LSTM}_{\text{(crossentropyex, or MAE or SSE)}}$ estimators and the traditional estimators over
307 the examined SNR range. At a low SNR (0–7 dB), the proposed $\text{BiLSTM}_{\text{(crossentropyex, or MAE or SSE)}}$
308 estimators exhibit identical performance. Furthermore, the proposed $\text{BiLSTM}_{\text{SSE}}$ estimator trained
309 by minimising the SSE loss function outperforms the $\text{BiLSTM}_{\text{crossentropyex}}$ estimator trained by
310 minimising the crossentropyex loss function starting from 8 dB; it outperforms $\text{BiLSTM}_{\text{MAE}}$, which
311 is trained by minimising the MAE loss function starting from 16 dB.

312 Figures 14–17 show the performance comparison of the LS, MMSE, $\text{BiLSTM}_{\text{(crossentropyex, or MAE or SSE)}}$
313 or $\text{LSTM}_{\text{(crossentropyex, or MAE or SSE)}}$ estimators at 4 pilots. Figure 17 shows the superiority of
314 the proposed $\text{BiLSTM}_{\text{(crossentropyex, or MAE or SSE)}}$ estimators in comparison with the traditional
315 estimators, which have lost their workability starting from 0 dB. It also shows the superiority of
316 the proposed estimator $\text{BiLSTM}_{\text{(MAE or SSE)}}$ over $\text{LSTM}_{\text{(MAE or SSE)}}$. $\text{LSTM}_{\text{(crossentropyex)}}$ exhibits a
317 competitive performance as $\text{BiLSTM}_{\text{(crossentropyex)}}$ starting from 0 dB to 12 dB, and
318 $\text{LSTM}_{\text{(crossentropyex)}}$ outperforms $\text{BiLSTM}_{\text{(crossentropyex)}}$ starting from 13 dB.

319 At very low SNRs (0–3 dB), the proposed $\text{BiLSTM}_{\text{(crossentropyex, or MAE or SSE)}}$ estimators have the
320 same performance. The proposed $\text{BiLSTM}_{\text{SSE}}$ estimator outperforms the $\text{BiLSTM}_{\text{crossentropyex}}$
321 estimator starting from 4 dB, and it exhibits an identical performance as the $\text{BiLSTM}_{\text{MAE}}$ estimator
322 until 14 dB and outperforms it in the rest of the SNR examination range.

323 Figures 13, 17 and 18 emphasise the robustness of the BiLSTM -based estimators against the
324 limited number of pilots and under the condition of a priori uncertainty of channel statistics. They
325 demonstrate the importance of testing various loss functions in the deep learning process to obtain
326 the most optimal architecture of any proposed estimator.

327 Figure 18 indicates that the proposed $\text{BiLSTM}_{\text{crossentropyex}}$, $\text{BiLSTM}_{\text{SSE}}$ and $\text{BiLSTM}_{\text{SSE}}$
328 estimators have close SER performance at 64, 8 and 4 pilots, respectively. The performance of
329 $\text{BiLSTM}_{\text{SSE}}$ at 8 pilots coincides with the performance of $\text{BiLSTM}_{\text{crossentropyex}}$ at 64 pilots.
330 Therefore, using the proposed estimators with few pilots is recommended for 5G OFDM wireless
331 communication systems to attain a significant improvement in their transmission data rate. Given
332 that the proposed estimator adopts a training data set-driven approach, it is robust to a priori
333 uncertainty for channel statistics.

334

335 LOSS CURVES

336 The quality of the DLNNs' training process can be monitored efficiently by exploring the
 337 training loss curves. These loss curves provide information on how the training process goes, and
 338 the user can decide whether to let the training process continue or stop.

339 Figures 19–21 show the loss curves of the DLNN-based estimators (BiLSTM and LSTM) at
 340 pilot numbers = 64, 8 and 4 and with the three examined loss functions (crossentropyex, MAE and
 341 SSE). The curves emphasise and verify the obtained results in Figure 6 through Figure 17. For
 342 example, the sub-curves in Figure 19 for BiLSTM_{crossentropyex} and LSTM_{crossentropyex} estimators
 343 emphasise their superiority over the other estimators. This superiority can be seen clearly from
 344 Figures 9. Moreover, the training loss curves in Figures 20 and 21 emphasise the obtained SER
 345 performance in Figures 13 and 17, respectively, of each examined DLNN-based CSIE.

346

347 ACCURACY CALCULATION

348 The accuracy of the proposed and other examined estimators is a measure of how the estimators
 349 recover transmitted data correctly. Accuracy can be defined as the number of correctly received
 350 symbols divided by the total number of transmitted symbols. The proposed estimator is trained in
 351 different conditions as indicated in the previous subsection, and we wish to investigate how well
 352 it performs in a new data set. Tables 3, 4 and 5 present the obtained accuracies for all examined
 353 estimators under all simulation conditions.

354 As illustrated in Tables 3 to 5, the proposed BiLSTM-based estimator attains accuracies from
 355 98.61 to 100 under different pilots and loss functions. The other examined DL LSTM-based
 356 estimator has accuracies from 97.88 to 99.99 under the same examination conditions. The achieved
 357 accuracies indicate that the proposed estimator has robustly learned and emphasises the obtained
 358 SER performance in Figure 18. The obtained results of MMSE and LS in Tables 1, 2 and 3
 359 emphasise the presented SER performance in Figures 9, 13 and 17, respectively, and show that as
 360 the pilot number decreases, the accuracy of the conventional estimators dramatically decreases.

361 The proposed BiLSTM- and LSTM-based estimators rely on DLNN approaches, where they can
 362 analyse huge data sets that may be collected from any plant, recognise the statistical dependencies
 363 and characteristics, devise the relationships between features and generalise the accrued
 364 knowledge for new data sets that they have not seen before. Thus, they are applicable to any 5G
 365 and beyond communication system.

366

367 COMPLEXITY

368 The feed-forward pass and feed-back pass operations dominate the computational complexity
 369 $O(W)$ of all neural networks, such as FFNNs, LSTM and BiLSTM. In a feed-forward pass, the
 370 weighted sum of inputs from previous layers to the next layers is calculated. In feed-back pass, the
 371 errors are evaluated; hence, the weights are modified.

372 The computational complexity of LSTM is

$$373 O(W) = O(KH + KCS + HI + CSI), \quad (13)$$

374 where W is the weight number, K is the output unit number, H is the hidden unit number, I is the
 375 input number, C is the memory cell block number and S is the memory cell block size [23].

376 The BiLSTM architecture has two separate LSTM-NNs and two propagation directions (forward
 377 and backward). Hence, for BiLSTM, $W = 2W$. The computational complexity of BiLSTM is

$$378 O(2W) = O(2(KH + KCS + HI + CSI)). \quad (14)$$

379 The required training time can be used as another a complexity metric. Table 6 lists the
 380 consumed processing time for the examined BiLSTM- and LSTM-based CSIEs. The used
 381 computer is equipped with an Intel(R) Core (TM) i5-2400 CPU running with a 3.10–3.30 GHz
 382 microprocessor and 4 GB of RAM. The LSTM-based estimators consume less processing time
 383 than the BiLSTM-based estimators do. Hence, they have the lowest complexity.

384

385 CONCLUSIONS

386 We summarise the paper by listing the main conclusions in separate points, as follows:

- 387 i. The proposed DL-BiLSTM-based CSIE is an online pilot assisted estimator. It is robust against
388 a limited number of pilots and exhibits superior performance compared with conventional
389 estimators.
- 390 ii. The proposed CSIE is robust under the conditions of a priori uncertainty of communication
391 channel statistics (non-Gaussian/stationary statistical channels) and demonstrates superior
392 performance compared with conventional estimators and DL LSTM NN-based CSIEs.
- 393 iii. The proposed CSIE exhibits a consistent performance at large and small pilot numbers and
394 superior performance at low SNRs, especially at limited pilots, compared with conventional
395 estimators.
- 396 iv. The proposed CSIE achieves the highest accuracy amongst all examined estimators at 64, 8 and
397 4 pilots for all the used loss functions.
- 398 v. The proposed BiLSTM- and LSTM-based estimators have high prediction accuracies of 98.61%
399 to 100% and 97.88% to 99.99%, respectively, when using crossentropyex, MAE and SSE loss
400 functions for 64, 8 and 4 pilots. They are promising for 5G and beyond wireless communication
401 systems.
- 402 vi. Two customised loss functions (MAE and SSE) are introduced.
- 403 vii. The computational and training time complexities are presented to illustrate the complexity of
404 the proposed estimator compared with that of the LSTM-based estimator.
405
406

407 **FUTURE WORK**

- 408 i. Investigating the proposed estimator's performance and accuracy by using other learning
409 algorithms, such as Adadelta, Adagrad, AMSgrad, AdaMax and Nadam.
- 410 ii. Investigating the proposed estimator's performance and accuracy by using different cyclic prefix
411 lengths and types.
- 412 iii. Developing robust loss functions by using robust statistics estimators, such as Tukey, Cauchy,
413 Huber and Welsh.
- 414 iv. Investigating the performance of CNN-, gated recurrent unit (GRU)- and simple recurrent unit
415 (SRU)-based CSIEs whilst using crossentropyex, MAE and SSE loss functions and for 64, 8 and
416 4 pilots.
417

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421

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490

Figure 1

Long short-term memory (LSTM) cell.

II. DLNN-BASED CSIE

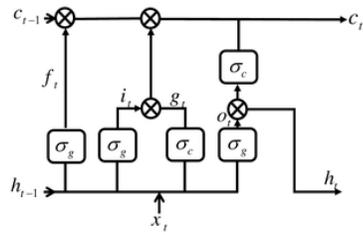


FIGURE 1. Long short-term memory (LSTM) cell.

Figure 2

BiLSTM-NN architecture.

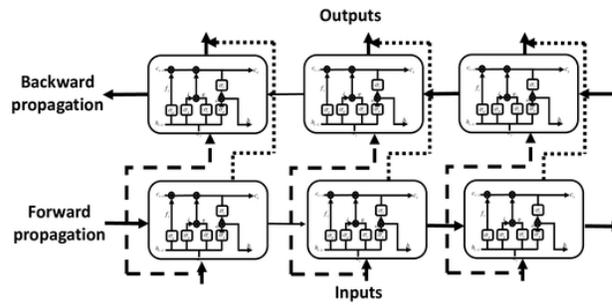


FIGURE 2. BiLSTM-NN architecture.

Figure 3

(a) Structure of the DL BiLSTM NN for the BiLSTM estimator and (b) compacted version of (a).

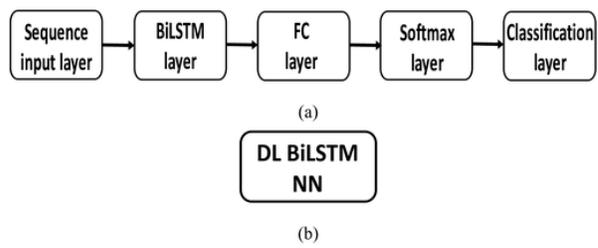


FIGURE 3. (a) Structure of the DL BiLSTM NN for the BiLSTM estimator and (b) compacted version of (a).

Figure 4

Conventional OFDM system

III. DL BiLSTM NN-BASED CSIE for 5G-OFDM WIRELESS COMMUNICATION SYSTEMS

A. OFDM SYSTEM MODEL

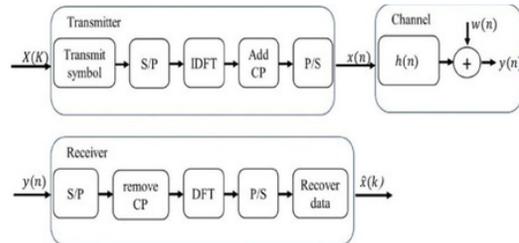


FIGURE 4. Conventional OFDM system [11].

Figure 5

Training data set formation and offline DL process of the BiLSTM-NN-based CSI estimator.

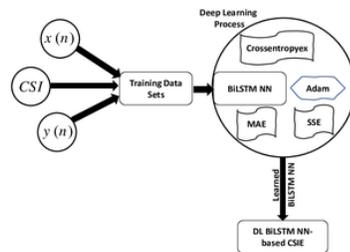


FIGURE 5. Training data set formation and offline DL process of the BiLSTM-NN-based CSI estimator.

Figure 6

SER comparison of the proposed, LSTM and conventional estimators using 64 pilots and the crossentropyex loss function.

IV. SIMULATION RESULTS

A. STUDYING THE PERFORMANCE OF THE PROPOSED, LS AND MMSE ESTIMATORS BY USING DIFFERENT PILOTS AND LOSS FUNCTIONS

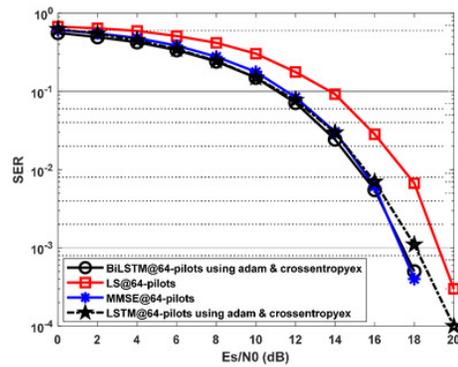


FIGURE 6. SER comparison of the proposed, LSTM and conventional estimators using 64 pilots and the crossentropy loss function.

Figure 7

SER comparison of the proposed, LSTM and traditional estimators using 64 pilots and the MAE loss function.

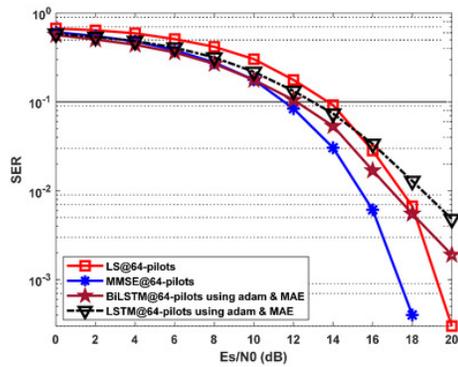


FIGURE 7. SER comparison of the proposed, LSTM and traditional estimators using 64 pilots and the MAE loss function.

Figure 8

SER comparison of the proposed, LSTM and traditional estimators using 64 pilots and the SSE loss function.

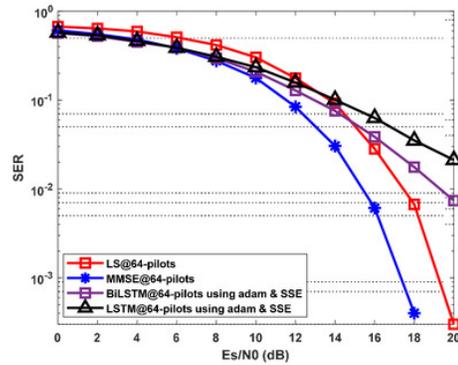


FIGURE 8. SER comparison of the proposed, LSTM and traditional estimators using 64 pilots and the SSE loss function.

Figure 9

SER comparison of LS, MMSE, BiLSTM and LSTM estimators using 64 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

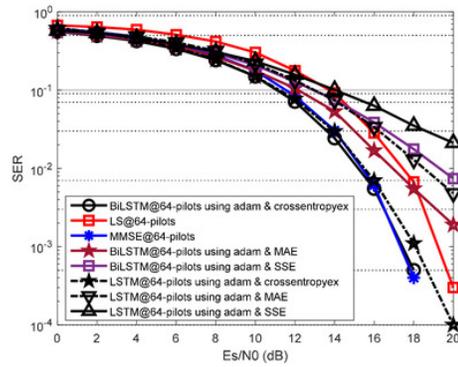


FIGURE 9. SER comparison of LS, MMSE, BiLSTM and LSTM estimators using 64 pilots, the Adam learning algorithm and crossentropy, MAE and SSE loss functions.

Figure 10

SER performance comparison of the proposed, LSTM and conventional estimators using 8 pilots and the crossentropyex loss function.

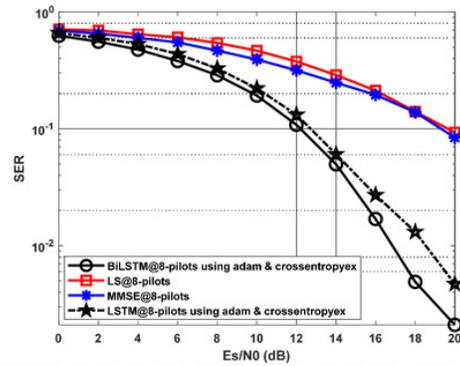


FIGURE 10. SER performance comparison of the proposed, LSTM and conventional estimators using 8 pilots and the crossentropy loss function.

Figure 11

SER performance comparison of the proposed, LSTM and conventional estimators using 8 pilots and the MAE loss function.

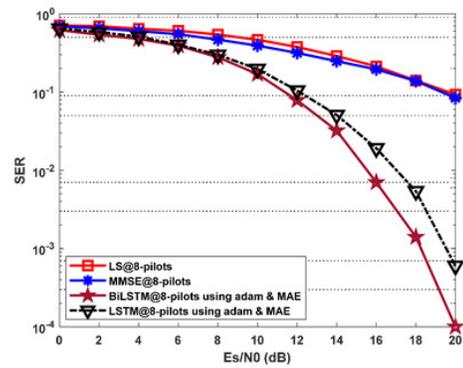


FIGURE 11. SER performance comparison of the proposed, LSTM and conventional estimators using 8 pilots and the MAE loss function.

Figure 12

SER performance comparison of the proposed, LSTM and conventional estimators using 8 pilots and the SSE loss function.

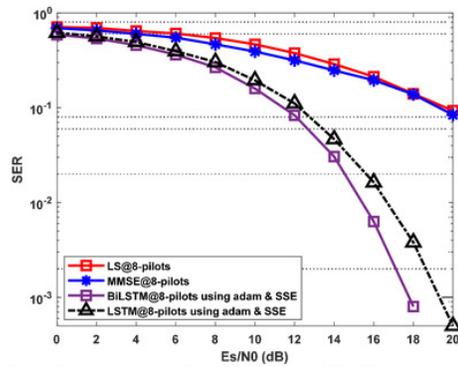


FIGURE 12. SER performance comparison of the proposed, LSTM and conventional estimators using 8 pilots and the SSE loss function.

Figure 13

SER performance comparison of LS, MMSE, LSTM and BiLSTM estimators using 8 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

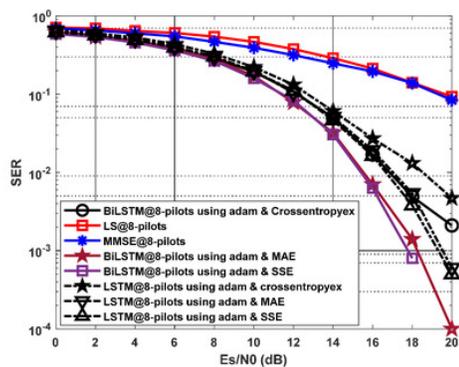


FIGURE 13. SER performance comparison of LS, MMSE, LSTM and BiLSTM estimators using 8 pilots, the Adam learning algorithm and crossentropy, MAE and SSE loss functions.

Figure 14

SER performance comparison of the proposed, LSTM and conventional estimators using 4 pilots and the crossentropyex loss function.

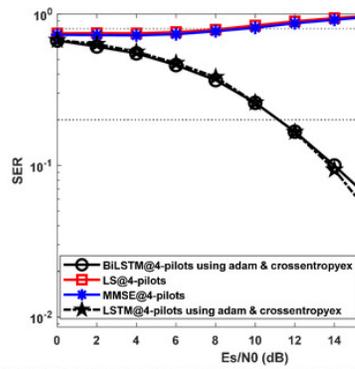


FIGURE 14. SER performance comparison of the proposed, LSTM and conventional estimators using 4 pilots and the crossentropy loss function.

Figure 15

SER performance comparison of the proposed, LSTM and conventional estimators using 4 pilots and the MAE loss function.

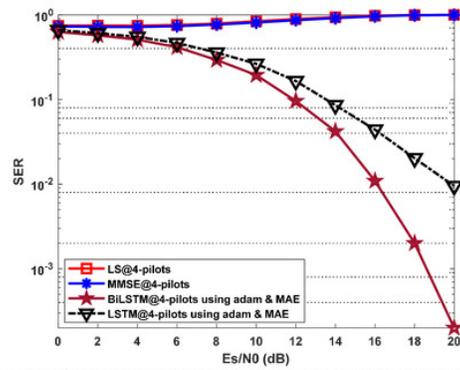


FIGURE 15. SER performance comparison of the proposed, LSTM and conventional estimators using 4 pilots and the MAE loss function.

Figure 16

SER performance comparison of the proposed, LSTM and conventional estimators using 4 pilots and the SSE loss function.

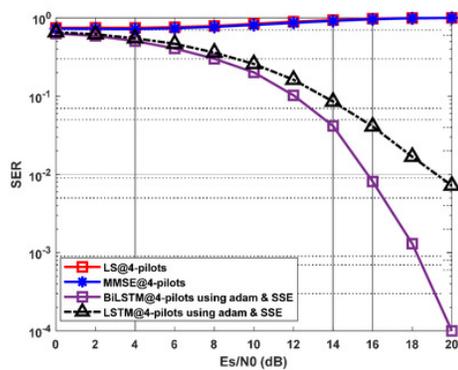


FIGURE 16. SER performance comparison of the proposed, LSTM and conventional estimators using 4 pilots and the SSE loss function.

Figure 17

SER performance comparison of LS, MMSE, LSTM and BiLSTM estimators using 4 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

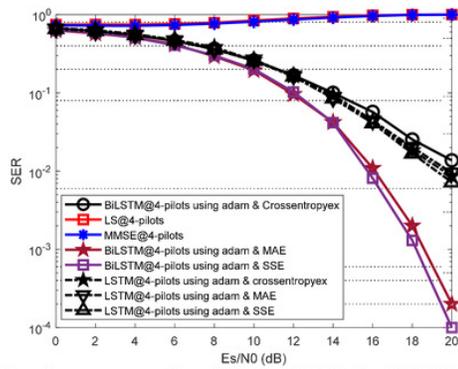


FIGURE 17. SER performance comparison of LS, MMSE, LSTM and BiLSTM estimators using 4 pilots, the Adam learning algorithm and crossentropy, MAE and SSE loss functions.

Figure 18

SER performance comparison of the best DL BiLSTM-based CSIEs using various pilots and loss functions.

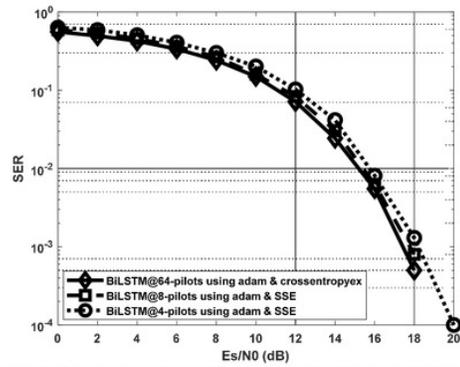


FIGURE 18. SER performance comparison of the best DL BiLSTM-based CSIEs using various pilots and loss functions.

Figure 19

Loss curves comparison of BiLSTM- and LSTM- based estimators using 64 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

B. LOSS CURVES

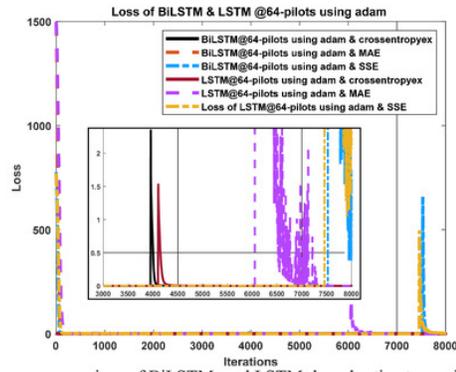


FIGURE 19. Loss curves comparison of BiLSTM- and LSTM- based estimators using 64 pilots, the Adam learning algorithm and crossentropy, MAE and SSE loss functions.

Figure 20

Loss curves comparison of BiLSTM- and LSTM-based estimators using 8 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

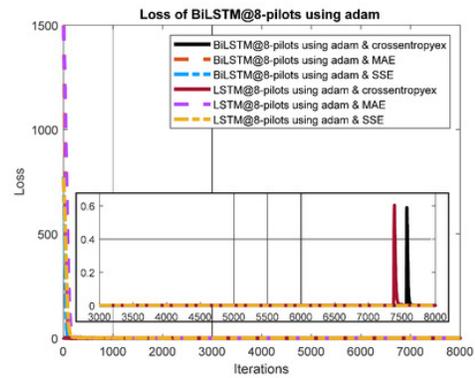


FIGURE 20. Loss curves comparison of BiLSTM- and LSTM-based estimators using 8 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

Figure 21

Loss curves comparison of BiLSTM- and LSTM-based estimators using 4 pilots, the Adam learning algorithm and crossentropyex, MAE and SSE loss functions.

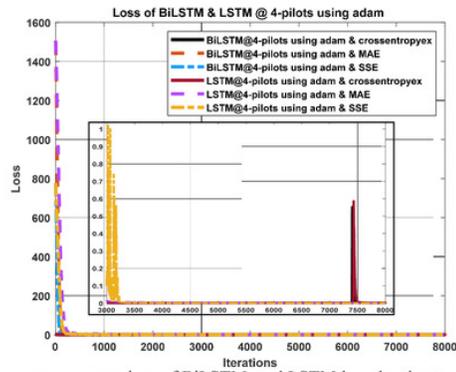


FIGURE 21. Loss curves comparison of BiLSTM- and LSTM-based estimators using 4 pilots, the Adam learning algorithm and crossentropy, MAE and SSE loss functions.

Table 1 (on next page)

BiLSTM- and LSTM-NN structure parameters and training process options

A. *STUDYING THE PERFORMANCE OF THE PROPOSED, LS AND MMSE ESTIMATORS BY USING DIFFERENT PILOTS AND LOSS FUNCTIONS*

TABLE 1
BiLSTM- AND LSTM-NN STRUCTURE PARAMETERS AND TRAINING PROCESS OPTIONS

Parameter	Value
Input Size	256
BiLSTM Layer Size	30 hidden neurons
LSTM Layer Size	30 hidden neurons
FC Layer Size	4
Loss Functions	Crossentropyex, MAE, SSE
Mini Batch Size	1000
Epochs Number	1000
Learning Algorithm	Adam

Table 2 (on next page)

OFDM system and channel parameters

TABLE 2
OFDM SYSTEM AND CHANNEL PARAMETERS

Parameter	Value
Modulation Mode	QPSK
Carrier Frequency	2.6 GHz
Paths Number	24
CP Length	16
Subcarrier Number	64
Pilot Number	64, 8 and 4

Table 3 (on next page)

Accuracy comparison of the examined estimators using 64 pilots

B. ACCURACY CALCULATION

TABLE 3
ACCURACY COMPARISON OF THE EXAMINED ESTIMATORS USING 64 PILOTS

	64 pilots			
	BiLSTM	LSTM	MMSE	LS
Crossentropyex	100	99.99	100	99.94
SSE	99.23	97.88	100	99.96
MAE	99.87	99.52	100	99.97

Table 4 (on next page)

Accuracy comparison of the examined estimators using 8 pilots

TABLE 4
ACCURACY COMPARISON OF THE EXAMINED ESTIMATORS USING 8 PILOTS

	8 pilots			
	BiLSTM	LSTM	MMSE	LS
Crossentropyx	99.84	99.53	91.34	91.62
SSE	100	99.95	91.60	91.49
MAE	100	99.94	91.53	91.50

Table 5 (on next page)

Accuracy comparison of the examined estimators using 4 pilots

TABLE 5
ACCURACY COMPARISON OF THE EXAMINED ESTIMATORS USING 4 PILOTS
4 pilots

	BiLSTM	LSTM	MMSE	LS
Crossentropyex	98.61	97.94	0.24	0.02
SSE	100	99.28	0.24	0.09
MAE	99.97	99.05	0.26	0.04

Table 6 (on next page)

Processing time comparison of the examined DLNN-based CSIEs

TABLE 6
PROCESSING TIME COMPARISON OF THE EXAMINED DLNN-BASED CSIES

	64 pilots		8 pilots		4 pilots	
	Bi-LSTM	LSTM	Bi-LSTM	LSTM	Bi-LSTM	LSTM
Crossentropyex	10:13	8:2	9:14	6:9	8:33	7:53
SSE	10:48	6:57	8:18	7:40	7:43	7:11
MAE	10:43	6:32	9:1	7:24	7:23	7:10