

Decomposition aided attention-based recurrent neural networks for multistep ahead time-series forecasting of renewable power generation

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Renewable energy plays an increasingly important role in our future. As fossil fuels become more difficult to extract and effectively process, renewables offer a solution to the ever-increasing energy demands of the world. However, the shift toward renewable energy is not without challenges. While fossil fuels offer a more reliable means of energy storage that can be converted into usable energy, renewables are more dependent on external factors used for generation. Efficient storage of renewables is more difficult often relying on batteries that have a limited number of charge cycles. A robust and efficient system for forecasting power generation from renewable sources can help alleviate some of the difficulties associated with the transition toward renewable energy. Therefore, this study proposes an attention-based recurrent neural network approach for forecasting power generated from renewable sources. To help networks make more accurate forecasts, decomposition techniques utilized applied the time series, and a modified metaheuristic is introduced to optimized hyperparameter values of the utilized networks. This approach has been tested on two real-world renewable energy datasets covering both solar and wind farms. The models generated by the introduced metaheuristics were compared with those produced by other state-of-the-art optimizers in terms of standard regression metrics and statistical analysis. Finally, the best-performing model was interpreted using SHapley Additive exPlanations.

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ABSTRACT

Renewable energy plays an increasingly important role in our future. As fossil fuels become more difficult to extract and effectively process, renewables offer a solution to the ever-increasing energy demands of the world. However, the shift toward renewable energy is not without challenges. While fossil fuels offer a more reliable means of energy storage that can be converted into usable energy, renewables are more dependent on external factors used for generation. Efficient storage of renewables is more difficult often relying on batteries that have a limited number of charge cycles. A robust and efficient system for forecasting power generation from renewable sources can help alleviate some of the difficulties associated with the transition toward renewable energy. Therefore, this study proposes an attention-based recurrent neural network approach for forecasting power generated from renewable sources. To help networks make more accurate forecasts, decomposition techniques utilized applied the time series, and a modified metaheuristic is introduced to optimized hyperparameter values of the utilized networks. This approach has been tested on two real-world renewable energy datasets covering both solar and wind farms. The models generated by the introduced metaheuristics were compared with those produced by other state-of-the-art optimizers in terms of standard regression metrics and statistical analysis. Finally, the best-performing model was interpreted using SHapley Additive exPlanations.

1 INTRODUCTION

The role of renewable energy is a paramount factor in sustainability of the society. Traditional energy systems based on fossil fuels are not efficient and require more complicated processes of extraction. The demands of human civilization are always growing, which exposes the difficulties for eco-friendly energetic growth. As renewable energy source (RES) become more available the distribution of new resources in the network result in stochasticity, intermittency, and uncertainty. Consequentially, the traditional energy systems are dominant in the share of energy used amounting to 81% of the global share (Loe, 2022).

For RES to become more widely utilized, the previously mentioned challenges need to be overcome. Additionally, energy storage on a smaller scale remains difficult when working with RES, in comparison to fossil fuel storage which is still considered more reliable. The storage of electricity is mostly achieved by batteries which are a limited resource on their own due to the limited number of life cycles for each one of them (Zhang and Zhao, 2023). All things considered, a possible solution is a mechanism that can provide accurate forecasts of the amount of resources being generated from RES. Such a solution would have to be able to analyze short-term time series and provide a robust mechanism as it affects electricity

45 load and its price. Electricity traders and system operators are most affected by these changes.

46 Traditional methods for regression have previously been applied to forecasting RES power produc-
47 tion (Foley et al., 2012; Abuella and Chowdhury, 2015) However, as the world's need for energy increases
48 further improvements are needed in order to make forecasting methods viable. A major challenge when
49 tackling RES production forecasting comes from the noisy nature of the data. Since renewable resources
50 rely on natural phenomena such as wind or solar exposure, many chaotic factors play a role in the amount
51 of power that can be produced. Nevertheless, patterns in this data are still present, though often difficult
52 to initially observe.

53 By applying advanced signal processing techniques, such as decomposition techniques, strong signals
54 can be separated from the noise, allowing prediction methods to focus on determining correlations between
55 signals with strong patterns rather than those heavily affected by the noise. This concept has often been
56 applied to systems that require precise moments in noise environments such as electroencephalogra-
57 phy (Murariu et al., 2023) demonstrating great potential. Several decomposition techniques have been
58 developed in recently such as empirical mode decomposition (EMD) (Boudraa and Cexus, 2007) and
59 ensemble empirical mode decomposition (EEMD) (Wu and Huang, 2009). While efficient, the lack of
60 a strong mathematical background in these methods has led to the development of variational mode
61 decomposition (VMD) (Dragomiretskiy and Zosso, 2013) that has shown great potential for tackling
62 signal decomposition with a strong mathematical basis (Liu et al., 2022; Zhang et al., 2022; Gao et al.,
63 2022).

64 One additional approach that has shown great potential when working with data catheterized by
65 complex nonlinear relations is the application of artificial intelligence (AI). Powerful AI algorithms are
66 capable of improving their performance through an iterative data-driven process. By observing data
67 AI algorithms can determine correlations without explicit programming. This makes AI a promising
68 approach for tackling this pressing issue. Nevertheless, the modern algorithms' performance is reliant on
69 proper hyperparameter selection. With increasing numbers of hyperparameters, traditional methods such
70 as trial and error have become insufficient to optimize algorithm performance. The use of metaheuristic
71 optimization algorithms provides a potential solution for efficient hyperparameter selection.

72 Forecasting power generation is regarded as a time series forecasting challenge. By doing so,
73 algorithms capable of responding to data sequences can be leveraged in order to make more accurate
74 forecasts. One promising approach, that extensive literature review suggests has not yet sufficiently been
75 explored when applied to renewable forecasting, is the use of recurrent neural networks (RNN) (Medsker
76 and Jain, 1999). These networks represent a variety of artificial neural networks (ANN) that allow
77 previous inputs to affect future outputs, making them highly suitable for time series forecasting. A
78 recent improvement incorporates attention mechanisms (Olah and Carter, 2016) into RNN allowing
79 networks to focus their attention on specific features improving accuracy. Additionally, the literature
80 review suggests that attention-based RNNs (RNN-ATT) have not yet been applied to renewable power
81 forecasting, indicating a gap in research that this work hopes to address. Exploring the potential of these
82 networks is essential as a robust forecasting method could help make RES more viable and lower the
83 world's dependence on fossil fuels.

84 This research proposes an approach that applies a neural network model based on attention for that
85 purpose. Moreover, the proposed model was applied to two different problems including the Spain
86 wind and solar energy predictions and the wind farms in China predictions. Datasets for both countries'
87 surveys have been used with the RNN model and the attention-based recurrent neural network RNN-ATT.
88 However, these networks require fine-tuning of a large number of hyperparameters, that can result in non-
89 deterministic polynomial time complexity (NP-hard). Hyperparameter optimization is done through the
90 use of metaheuristics, and a modified version of the well-known Harris hawk optimization (HHO) (Heidari
91 et al., 2019) algorithm is introduced. Two sets of experiments have been carried out both with RNN and
92 RNN-ATT networks, applied to each real-world dataset.

93 This research is an extension of previous researches in this domain (Bacanin et al., 2023c; Stoean
94 et al., 2023; Bacanin et al., 2023b), where the long short-term (LSTM), bidirectional LSTM (BiLSTM) and
95 gated recurrent unit (GRU) were applied for RES forecasting challenges. However, the goal of this work
96 is to test lighter models (classical RNNs) for problems of RES with the application of fewer neurons over
97 layers while providing satisfactory performance. Additionally, conversely to previous experimentation,
98 current research also investigates the potential of RNNs with attention mechanism and it was validated
99 against different RES time-series datasets. Also, the classical RNNs (without attention mechanism) were

100 also validated in order to establish the influence of attention layer to overall network performance.

101 The primary contributions of this work can be summarized as the following:

- 102 • The RNN-ATT-based method for forecasting RES power generation.
- 103 • A modified version of a metaheuristic tasked with selecting network parameters.
- 104 • The application of the introduced approach to two real-world datasets to determine their potential
105 for real-world use.
- 106 • The interpretation of the best generated RNN models that can be used as a valuable tools for renew-
107 able energy specialists to determine which factor has the most influence on the RES performance.

108 The structure of the paper includes Section 2 for providing the technological fundamentals for the
109 performed experiments. Section 3 explains the original version of the applied metaheuristic as well as
110 the modified version. Section 4 explains the utilized datasets in detail and gives information on the test
111 setup. The outcomes are presented in Section 5, followed by a discussion. statistical validation and model
112 interpretation presented in Section 6. Finally, Section 7 concluded the work and presents potential future
113 research.

114 2 BACKGROUND AND PRELIMINARIES

115 This section introduces techniques required for the reader to have a full and insightful understanding of
116 experiments conducted in this research.

117 2.1 Time-Series Decomposition and Integration

118 Time-series decomposition is a technique used to break down a time-series data into its constituent
119 components, such as trend, seasonality, and residual (noise). By decomposing a time-series, we can
120 better understand the underlying patterns and relationships within the data, which can, in turn result in
121 improvements of reliability and accuracy of the time-series forecasting, models like the Luong attention-
122 based RNN model.

123 2.1.1 Decomposition Techniques

124 Various decomposition techniques can be applied to time-series data, including:

125 **1. Classical Decomposition:** This method decomposes a time-series into its trend, seasonal, and
126 residual components using moving averages and seasonal adjustments. There are two primary approaches
127 in classical decomposition: additive and multiplicative. In the additive decomposition, the time-series
128 is expressed as the sum of its components, while in the multiplicative decomposition, the time-series is
129 expressed as the product of its components.

130 **2. Seasonal and Trend decomposition using Loess (STL):** STL is a flexible and robust decomposi-
131 tion method that uses locally weighted regression (Loess) to estimate the trend and seasonal components
132 of a time-series. It can handle both constant and time-varying seasonality, as well as arbitrary patterns of
133 missing data. The STL method also allows for user-defined control over the smoothness and periodicity
134 of the seasonal and trend components.

135 **3. Seasonal Decomposition of Time Series (SDTS):** SDTS is an extension of the classical decompo-
136 sition method that incorporates a seasonal adjustment factor for each observation in the time-series. This
137 factor is obtained by dividing the observed value by the corresponding seasonal component. The seasonal
138 adjustment factors can be used to deseasonalize the time-series, which can then be analyzed for trend and
139 residual components.

140 **4. Wavelet Transform:** Wavelet transform is a mathematical technique used to decompose a time-
141 series into a set of wavelet coefficients, which represent the time-series at different scales and resolutions.
142 Wavelet transform can capture both the low-frequency (trend) and high-frequency (seasonal and noise)
143 components of a time-series, making it a powerful tool for time-series decomposition and analysis.

144 **5. Empirical Mode Decomposition:** EMD is a powerful and flexible technique for analyzing non-
145 stationary and non-linear time series data. Introduced by Huang et al. (Huang et al., 1998), EMD is
146 designed to adaptively decompose a time series into a finite set of intrinsic mode functions (IMFs) that
147 capture the local oscillatory behavior of the signal at various scales. The primary goal of EMD is to
148 provide a data-driven decomposition that does not rely on any predefined basis functions or assumptions

149 about the underlying signal characteristics (Abayomi-Alli et al., 2020). By incorporating EMD into the
 150 renewable power generation forecasting process, we can potentially enhance the accuracy, reliability, and
 151 interpretability of the forecasting models, ultimately aiding in the efficient management and planning of
 152 renewable energy resources.

153 **2.1.2 Variational mode decomposition**

154 The VMD (Dragomiretskiy and Zosso, 2013) technique used for signal decomposition builds upon the
 155 solid foundation established but other methods. However, VMD does so with a strong mathematical
 156 foundation compared to empirical techniques. Signal modes of varying frequencies are extracted from the
 157 original signal original signals by finding modes that are orthogonal to each other with localized frequency
 158 content. The decomposition is achieved through progressive optimization according to Eq. (1).

$$E(V) = \int \left(\frac{1}{2} \|V'(t)\|_2^2 + \mu U(V(t)) \right) dt \quad (1)$$

159 in which $V(t)$ are signal modes, $V'(t)$ denotes the derivative of $V(t)$ with respect to time. Additionally
 160 the regularization parameter μ balances between extracted mode smoothness and sparsity. Accordingly,
 161 function $U(V(t))$ promotes sparsity.

162 The decomposition process is handled by an algorithm that switches between solving modes and
 163 determines the penalty. Minimizing the energy function modes can be determined with respect to $V(t)$. A
 164 Lagrange multiplier $\alpha(t)$ is also introduced giving Eq. (2).

$$E(V) = \int \left(\frac{1}{2} \|V'(t)\|_2^2 + \mu U(V(t)) + \alpha(t) \sum_{k=1}^K V_k(t)^2 \right) dt \quad (2)$$

165 where the k -th mode of a signal is represented by $V_k(t)$. In order to revise the penalty function, the energy
 166 function is minimized with respect to $\alpha(t)$. To accomplish this, the derivative of $E(V)$ with respect to
 167 $\alpha(t)$ is set to zero. The resulting function is shown in Eq. (3)

$$\frac{d}{dt} \alpha(t) = \mu \sum_{k=1}^K V_k(t)^2 - \lambda \quad (3)$$

168 with the λ constraint defining the overall mode energy.

169 **2.1.3 Integration of Decomposed Components**

170 Once the time-series has been decomposed into its constituent components, the next step is to integrate
 171 these components into the forecasting model. There are several ways to incorporate the decomposed
 172 components into the Luong attention-based RNN model:

173 **1. Component-wise Modeling:** Train separate RNN models for each of the decomposed components
 174 (trend, seasonal, and residual), and then combine the forecasts from these models to obtain the final forecast
 175 for the original time-series. This approach can help in capturing the unique patterns and dependencies
 176 within each component more effectively.

177 **2. Feature Augmentation:** Use the decomposed components as additional input features to the
 178 RNN model, along with the original time-series. This approach can help the model in learning the
 179 relationships between the decomposed components and the target variable, potentially improving the
 180 model's forecasting performance.

181 **3. Preprocessing:** Deseasonalize the time-series by removing the seasonal component before training
 182 the RNN model, and then add back the seasonal component to the model's forecasts to obtain the final
 183 forecast for the original time-series. This approach can help in reducing the complexity of the time-series
 184 and make it easier for the model to capture the underlying trend and residual patterns.

185 **4. Postprocessing:** Train the RNN model on the original time-series, and then adjust the model's
 186 forecasts using the decomposed components (e.g., by adding the seasonal component to the model's
 187 forecasts). This approach can help in correcting the model's forecasts for any systematic errors or biases
 188 related to the seasonal component.

189 2.2 Recurrent neural network

190 Time series prediction is the motivation for the improvements in artificial neural networks (ANN) (Pascanu
191 et al., 2013). The difference from the multilayer perceptron is that the hidden unit links are enabled with a
192 delay. The results of such modifications allow the model to be sensitive toward temporal data occurrences
193 of greater length.

194 RNNs are considered as a high-performing solution but further improvements were applied to achieve
195 even greater performance. The main issues are the exploding and vanishing gradient. The solution was
196 provided with LSTM model. The reason for not using the latest solution is that sometimes RNNs tend
197 to outperform LSTMs as they introduce a large number of hyperparameters that can sometimes hinder
198 performance (Bas et al., 2021).

199 The advantage of the RNN as well is that it does not have to take inputs of fixed vector length, in
200 which case the output has to be fixed as well. While working with rich structures and sequences this
201 advantage can be exploited. In other words, the model works with input vectors and is able to generate
202 sequences on the output. The RNN processes the data of the sequence while the hidden state is held.

203 2.3 Luong attention-based model

204 The attention phenomenon is not defined by mathematics and its application in the Luong attention-
205 based model should be considered as a mechanism (Luong et al., 2015; Raffel et al., 2017; Harvat and
206 Martín-Guerrero, 2022). Some examples of different mathematical expression applications of the attention
207 mechanism are the sliding window methods, saliency detection, local image features, etc. Regarding the
208 attention mechanism application in the case of an RNN, the definition is precise.

209 The networks that can work with the attention mechanism and possess RNN characteristics are
210 considered attention-based. The purpose of such a mechanism is to work with different weights for the
211 sequence in input. The data can be captured as a result and input-output relations are usable. The basic
212 solution of such architecture is the application of a second RNN.

213 The authors chose the Luong attention-based model for that purpose. Weight represented as w_t is
214 calculated for the source for every timestep t for the decoding of attention-based encoder-decoder as
215 $\sum_s w_t(s) = 1$ and $\forall s w_t(s) \geq 0$. The hidden state h_t has a function that is the related timestep's predicted
216 token, while the $\sum_s w_t(s) * \hat{h}_s$.

217 Different mathematical applications of the attention mechanism differ in the way they compute
218 weights. In the case of the Luong model, it is the softmax function on the scaled scores of each token.
219 Matrix W_a linearly transforms the decoder's h_t dot product and the encoder \hat{h}_s to calculate the score.

220 2.4 Hyperparameters of Luong-attention based RNN

221 The Luong attention-based RNN model is an extension of the basic RNN model with the addition of
222 an attention mechanism allows for selective focus on particular parts of the input sequence upon output
223 generation. The following hyperparameters are typically involved in the configuration of the Luong
224 attention-based RNN model:

225 **1. Number of hidden layers (n_{hid}):** The number of hidden layers in the RNN architecture, which
226 determines the depth of the model. More hidden layers can enable the model to capture patterns of higher
227 complexity and data dependencies but with the risk of overfitting and requiring more computational
228 resources.

229 **2. Number of hidden units per layer (n_{unit}):** The number of hidden units (neurons) in each hidden
230 layer of the RNN. A larger number of hidden units can increase the model's capacity to learn complex
231 patterns, but it may also increase the risk of overfitting and require more computational resources.

232 **3. Type of RNN cell:** The choice of RNN cell used in the model, such as LSTM or GRU. These
233 cells are designed to better handle long-range dependencies and mitigate the vanishing gradient problem
234 compared to the traditional RNN cells.

235 **4. Attention mechanism:** The specific attention mechanism used in the model. In the case of the
236 Luong attention-based RNN model, the attention mechanism can be of two types: global or local attention.
237 Global attention attends to all the source positions, while attention is focused locally only on a small
238 window of source positions around the current target position.

239 **5. Attention scoring function:** The scoring function computes the alignment scores between the
240 source and target sequences in the attention mechanism. Luong et al. proposed three different scoring
241 functions: dot product, general (multiplicative), and concatenation (additive). The choice of scoring
242 function can affect the model's performance and interpretability.

243 **6. Learning rate (α):** The learning rate is a critical hyperparameter in control of the size of updates
244 to the model's weights during the training process. A smaller learning rate might lead to more precise
245 convergence but require more training iterations, while a larger learning rate may speed up the training
246 process but risk overshooting the optimal solution.

247 **7. Dropout rate (p_{drop}):** The dropout rate is a technique of regularization used to prevent overfitting
248 in neural networks. During training, a fraction of the neurons in the network is randomly "dropped out"
249 or deactivated, with the specified dropout rate determining the proportion of neurons deactivated at each
250 training iteration.

251 **8. Batch size:** The number of training samples used in a single update of the model's weights. A
252 larger batch size can lead to more accurate gradient estimates and faster training but may require more
253 memory and computational resources.

254 **9. Sequence length:** The length of input and output sequences used in the model. Longer se-
255 quences may allow the model to capture more extensive temporal dependencies but can also increase the
256 computational complexity and risk of overfitting.

257 These hyperparameters play a paramount role in performance determination of the Luong attention-
258 based RNN model for renewable power generation forecasting. Selecting optimal values for these
259 hyperparameters requires careful experimentation, and metaheuristic optimization techniques like the
260 HHO algorithm can be helpful in this process, as shown by different authors recently (Tayebi and
261 El Kafhali, 2022; Bacanin et al., 2022a; Nematzadeh et al., 2022; Drewil and Al-Bahadili, 2022; Akay
262 et al., 2022; Bacanin et al., 2022c; Jovanovic et al., 2023a).

263 2.5 Metaheuristic Optimization

264 In recent years model optimization has become a popular topic in computer science. Increasing model
265 complexity, as well as growing numbers of hyperparameters of modern algorithms, has made it necessary
266 to develop techniques to automate this process, which was traditionally handled through trial and error.
267 However, this is a challenging task, as selecting optimal parameters is often a mixed NP-hard problem,
268 with both discrete and continuous values having a role to play in defining model performance. A powerful
269 group of algorithms capable of addressing NP-hard problems within reasonable time constraints and
270 with realistic computational demands are metaheuristic optimization algorithms. By formulating the
271 process of parameter selection as an optimization task, metaheuristics can be employed to efficiently
272 improve performance. A notably popular group of metaheuristics is swarm intelligence that models
273 observed behaviors of cooperating groups to perform optimizations. Some notable algorithms that have
274 become popular for tackling optimization tasks among researchers include the HHO (Heidari et al., 2019),
275 genetic algorithm (GA) (Mirjalili and Mirjalili, 2019), particle swarm optimizer (PSO) (Kennedy and
276 Eberhart, 1995), artificial bee colony (ABC) (Karaboga, 2010) algorithm, firefly algorithm (FA) (Yang and
277 Slowik, 2020). Additionally the LSHADE for Constrained Optimization with Levy Flights (COLSHADE)
278 algorithm (Gurrola-Ramos et al., 2020) and Self-Adapting Spherical Search (SASS) (Zhao et al., 2022)
279 are notable recent examples of optimizers. These algorithms, and algorithms derived from their base have
280 been applied in several fields with promising outcomes. Some noteworthy examples of metaheuristics
281 applied to optimization problems include examples for crude oil price forecasting (Jovanovic et al., 2022;
282 Al-Qaness et al., 2022), Ethereum and Bitcoin prices predictions (Stankovic et al., 2022b; Milicevic et al.,
283 2023; Petrovic et al., 2023; Gupta and Nalavade, 2022), industry 4.0 (Jovanovic et al., 2023b; Dobrojevic
284 et al., 2023; Para et al., 2022), medicine (Zivkovic et al., 2022a; Bezdani et al., 2022; Budimirovic et al.,
285 2022; Stankovic et al., 2022a), security (Zivkovic et al., 2022b; Savanović et al., 2023; Jovanovic et al.,
286 2023c; Zivkovic et al., 2022c), cloud computing (Thakur and Goraya, 2022; Mirmohseni et al., 2022;
287 Bacanin et al., 2022d; Zivkovic et al., 2021), and environmental sciences (Jovanovic et al., 2023d; Bacanin
288 et al., 2022b; Kiani et al., 2022).

289 3 PROPOSED METHOD

290 This section begins with a short overview of the basic HHO algorithm along the explanation and justifica-
291 tions of the modifications that were made to the original method.

292 3.1 Original Harris hawk optimization

293 The inspiration for the HHO are the attack strategies of the bird with the same name. The phases of
294 attacks can be differentiated as exploration, the transition to exploitation, and the exploitation. The

295 algorithm was introduced by Heidari et al. (Heidari et al., 2019) and has been used for a wide variety of
 296 optimization-related applications such as machine scheduling (Jouhari et al., 2020) and neural network
 297 optimization (Ali et al., 2022).

298 In the first phase, the exploration, the goal is the global optimum. Multiple locations in the population
 299 serve for random initialization which mimics the hawk's search for prey. The parameter q controls this
 300 process as it switches between two strategies of equal probability:

$$X(t+1) = \begin{cases} X_{rand}(t) - r_1|X_{rand}(t) - 2r_2X(t)|, q \geq 0 \\ (X_{best}(t) - X_m(t)) - r_3(LB + r_4(UB - LB)), q < 0.5, \end{cases} \quad (4)$$

301 in which the random number from the range $[0, 1]$ are r_1 , r_2 , r_3 , and r_4 as well as q and these numbers are
 302 updated on an iteration basis. The position vector of the solution in the next iteration is $X(t+1)$, and the
 303 positions of the solutions of the best, current, and average solutions in the current iteration t are given
 304 respectively as $X_{best}(t)$, $X(t)$ and $X_m(t)$, while the lower bound is LB and the upper bound is UB . The
 305 average position is provided by a simple averaging approach:

$$X_m(t) = \frac{1}{N} \sum_{i=1}^N X_i(t), \quad (5)$$

306 for which N shows the total solutions number, and the individual X at iteration t is shown as $X_i(t)$.

307 The term prey energy is introduced as it indicates if the algorithm should revert back to exploration
 308 and so forth. The solutions updates strength in each iteration as:

$$E = 2E_0(1 - \frac{t}{T}), \quad (6)$$

309 for T as iteration maximum for a run, the prey's initial energy E_0 which varies inside the $[-1, 1]$ interval.

310 The exploitation phase represents the literal attack of the hawk and maps out its behavior as it is
 311 closing in. The mathematical translation is given as $|E| \geq 0.5$ for more passive attacking, and $|E| < 0.5$
 312 otherwise.

313 In cases where the prey of the hawk is still at large, the hawks encircle the prey with the goal of
 314 exhaustion which is modeled as follows:

$$X(t+1) = \Delta X(t) - E|JX_{best}(t) - X(t)| \quad (7)$$

315

$$\Delta X(t) = X_{best}(t) - X(t), \quad (8)$$

316 for which the vector difference of the best solution (prey) and the current solution in iteration t is shown
 317 as $\Delta X(t)$. The strategy of the prey's escape is controlled by the random attribute J which differs from
 318 iteration to iteration:

$$J = 2(1 - r_5), \quad (9)$$

319 for which the interval $[0, 1]$ maps out the random value r_5 . For $r \geq 0.5$ and $|E| < 0.5$ the prey is considered
 320 exhausted and more aggressive attack strategies are applied. The current position in this case is updated
 321 as:

$$X(t+1) = X_{best}(t) - E|\Delta X(t)| \quad (10)$$

322 If the prey is still not giving up the hawks apply another attack strategy called zig-zag movements
 323 commonly known as leapfrog movements. Following equation evaluates if such behavior should be
 324 applied:

$$Y = X_{best}(t) - E|JX_{best}(t) - X(t)|, \quad (11)$$

325 while the leapfrog movements are modeled as:

$$Z = Y + S \times LF(D), \quad (12)$$

326 in which the problem dimension is given as D , a random vector of $1 \times D$ size as S , and the levy flighth LF
 327 calculated by:

$$LF(x) = 0.01 \times \frac{u \times \sigma}{|v|^{\frac{1}{\beta}}}, \sigma = \left(\frac{\Gamma(1+\beta) \times \sin(\frac{\pi\beta}{2})}{\Gamma(\frac{1+\beta}{2}) \times \beta \times 2^{(\frac{\beta-1}{2})}} \right)^{\frac{1}{\beta}} \quad (13)$$

328 Consequently, the position updating mechanism is provided:

$$X(t+1) = \begin{cases} Y, & \text{if } F(Y) < F(X(t)) \\ Z, & \text{if } F(Z) < F(X(t)), \end{cases} \quad (14)$$

329 where the eqs. (11) and (12) are utilized for calculating the Y and Z .

330 Lastly, for the case of $r \leq 0.5$ and $|E| < 0.5$ the prey is considered to be out of energy, and stronger
 331 attacks are applied with rapid drive progressively. The distance between the target before its acquisition is
 332 modeled as:

$$X(t+1) = \begin{cases} Y, & \text{if } F(Y) < F(X(t)) \\ Z, & \text{if } F(Z) < F(X(t)), \end{cases} \quad (15)$$

333 for which the Y and Z are obtained by the next two equations:

$$Y = X_{best}(t) - E|JX_{best}(t) - X(t)| \quad (16)$$

$$334 \quad Z = Y + S \times LF(D) \quad (17)$$

335 **3.2 Proposed enhanced Harris hawk optimization algorithm**

336 **3.2.1 New initialization scheme**

337 The applied approach exploits a novel initialization strategy of populations:

$$x_{i,j} = lb_j + \psi \cdot (ub_j - lb_j), \quad (18)$$

338 in which the j -th component of i -th solution is given as $x_{i,j}$, the upper and lower bounds are represented
 339 by ub_j and lb_j for the parameter j , and a pseudo-random number is drawn between $[0, 1]$ and given as ψ .

340 The quasi-reflection-based learning (QRL) procedure has proven to give results (Jovanovic et al.,
 341 2023b) where applied with the goal of sarge space enlargement for the case of those generated by the
 342 (18). The purpose of the QRL procedure is reflected in the fact that if the observed solution falls in the
 343 suboptimal region of the search space, there is a fair chance that its opposite will fall in more promising
 344 areas of the search domain, as reported by several authors recently (Bacanin et al., 2023a; Basha et al.,
 345 2021; Nama, 2022; Çelik, 2023; Lei et al., 2022; Bacanin et al., 2021; Xue, 2022). Hence the x_j^{qr} ,
 346 quasi-reflexive-opposite component for all parameters of a solution x_j is provided as in the following
 347 equation:

$$X_j^{qr} = \text{rnd} \left(\frac{lb_j + ub_j}{2}, x_j \right), \quad (19)$$

348 while at $\left[\frac{lb_j + ub_j}{2}, x_j \right]$ interval a pseudo-random number is chosen as rnd .

349 **3.2.2 Mechanism for maintaining population diversity**

350 Diversification is observed as a parameter of the convergence/divergence ratio during the search process
 351 as in (Cheng and Shi, 2011).

352 $L1$ norm (Cheng and Shi, 2011) applies two-component diversification for the solutions and the
 353 dimensions of the problem. Important information for the search process can be derived from the
 354 dimension-wise metric with the $L1$ norm.

355 The number of total individuals is marked with m and the dimensions number as n , the $L1$ norm is
 356 given as in Eqs. 20 -22:

Algorithm 1 QRL pseudo-code initialization scheme

- 1: P^{init} population with $N/2$ solutions created by Eq. (18).
- 2: P^{qr} population by QRL from P^{init} by Eq. 19.
- 3: Merge P^{init} and P^{qr} ($P \cup P^{qr}$) resulting in the starting population.
- 4: Fitness calculation of every solution in P
- 5: P sorted by fitness

$$\bar{x} = \frac{1}{m} \sum_{i=1}^m x_{ij} \quad (20)$$

$$D_j^p = \frac{1}{N} \sum_{i=1}^N \left| x_{ij} - \bar{x}_j \right| \quad (21)$$

$$D^p = \frac{1}{n} \sum_{i=1}^n D_j^p \quad (22)$$

357 in which every individual's position mean is represented as \bar{x} vector over all dimensions, the hawk's
 358 position vector of diversity as $L1$ norm is shown as D_j^p , while the scalar form is shown as D^p for the
 359 entire population. Using regular strategies of initialization usually results in higher diversity with weaker
 360 convergence towards later iterations. The described metric is used for $L1$ determination of the threshold
 361 D_t for the diversity. Firstly, the D_{t0} is calculated by Eq. 23, which is followed by condition $D^p < D_t$ for
 362 the satisfactory value of diversity, the worst solutions are replaced with randomly generated solutions nrs
 363 with the same strategy for population initialization. The nrs value is another control parameter.

$$D_{t0} = \sum_{j=1}^n \frac{(ub_j - lb_j)}{2 \cdot n} \quad (23)$$

364 The Eq. (1) and Algorithm 1 indicate close generation of solutions towards the bounds of the search
 365 space's mean. The value D_t falls off as shown in:

$$D_{t,iter+1} = D_{t,iter} - D_{t,iter} \cdot \frac{iter}{T}, \quad (24)$$

366 in which the current and subsequent iterations are given as $iter$ and $iter + 1$, and the number of iterations
 367 at the maximum is T . According to this mechanism, the D_t falls off in no relation to the D^p and still will
 368 not trigger the mechanism.

3.2.3 Inner workings and complexity of proposed method

369 Taking inspiration from applied mechanisms to the original solution the proposed new algorithm is
 370 diversity directed HHO (DDHHO). It is important to note that the computational complexity of the
 371 original algorithm is not lower than that of the novel solution. In modern literature, it is a practice to
 372 measure this in FFEs as it is the most resource-demanding technique, hence the complexity of the DDHHO
 373 for the worst scenario is (Yang and He, 2013): $O(DDHHO) = O(N) + O(T \cdot N^2)$. In comparison to other
 374 metaheuristics algorithms, the complexity of the DDHHO is similar. For instance, firefly algorithm (Yang
 375 and Slowik, 2020) is more complex as it evaluates at most $N * N$ solutions in each iteration.

3.3 Hyperparameter optimization using HHO

377 To optimize the hyperparameters of the Luong attention-based RNN model, we perform the following
 378 steps:

379 **Define the search space:** Identify the hyperparameters to be optimized and specify their respective
 380 ranges or discrete sets of possible values. For instance, for the number of hidden layers, we may specify a
 381

Algorithm 2 Pseudo-code of the basic HHO algorithm implementation

Inputs: The population size N and maximum number of iterations T
Outputs: The location of the rabbit and its fitness value
Initialize the random population $X_i (i = 1, 2, \dots, N)$
Initialize population $X_i, (i = 1, 2, 3, \dots, N)$ according to Algorithm 1
Determine values of D_{t0} and D_t
while (stopping condition is not met) **do**
 Calculate the fitness values of hawks
 Set X_{rabbit} as the location of rabbit (best location)
 for (each hawk (X_i)) **do**
 Update the initial energy E_0 and jump strength J
 Update the E using Eq. (6)
 if ($|E| \geq 1$) **then**
 Update the location vector using Eq. (4)
 end if
 if ($|E| < 1$) **then**
 if ($r \geq 0.5$ and $|E| \geq 0.5$) **then**
 Update the location vector using Eq. (7)
 else if ($r \geq 0.5$ and $|E| < 0.5$) **then**
 Update the location vector using Eq. (10)
 else if ($r < 0.5$ and $|E| \geq 0.5$) **then**
 Update the location vector using Eq. (14)
 else if ($r < 0.5$ and $|E| < 0.5$) **then**
 Update the location vector using Eq. (15)
 end if
 end if
 end for
 Calculate D^P
 if ($D^P < D_t$) **then**
 Replace worst nrs with solutions created as in (18)
 end if
 Update D_t by expression (24)
end while
Return X_{rabbit}

382 range of values, e.g., from 1 to 5. Similarly, we define the search space for other hyperparameters such as
383 the number of hidden units per layer, type of RNN cell, attention mechanism, attention scoring function,
384 learning rate, dropout rate, batch size, and sequence length.

385 **Initialize the population:** Generate an initial population of candidate solutions, where each candidate
386 solution represents a combination of hyperparameter values within the defined search space.

387 **Evaluate candidate solutions:** For each candidate solution, train the Luong attention-based RNN
388 model using the specified hyperparameter values, and evaluate the performance on a validation set using
389 one or more performance metrics (e.g., MAE, RMSE, and MAPE). This step may require cross-validation
390 or other validation techniques to obtain reliable performance estimates.

391 **Apply optimization algorithm:** Utilize the chosen metaheuristic optimization algorithm for search
392 space exploration and find the best combination of hyperparameter values that minimizes the chosen
393 performance metric(s). In each iteration, the algorithm updates the candidate solutions based on the
394 optimization strategy specific to the chosen algorithm, and the performance of the updated solutions is
395 re-evaluated on the validation set.

396 **Termination condition:** The optimization process is ongoing until a predefined termination condition
397 is met, such as a maximum iteration number, a minimum performance improvement threshold, or a
398 predefined computational budget.

399 **Select the optimal solution:** Once the termination condition is reached, select the candidate solution
400 with the best performance on the validation set as the optimal combination of hyperparameter values for

401 the Luong attention-based RNN model.

402 **Final model training and evaluation:** Train the Luong attention-based RNN model using the optimal
403 hyperparameter values on the entire training set, and evaluate its performance on the test set to obtain an
404 unbiased estimate of the model's forecasting accuracy.

405 **4 DATASET DESCRIPTION AND EXPERIMENTS**

406 This section aims to provide an overview of the datasets utilized in the experiments and the experimental
407 setup established for all methods employed in the comparative analysis.

408 **4.1 Utilized Datasets**

409 **4.1.1 Spain Solar Energy Dataset**

410 The first dataset, concerning photovoltaic power generation in Spain, is constructed from real-world
411 originating from two different sources. The ENTSO-E portal ¹ provides hourly energy demand and
412 generation considering the renewable energy in Spain, while the weather data is provided by OpenWeather
413 API ² for the location of Valencia, Spain.

414 Considering the large amount of data available, a smaller dataset segment was utilized during experi-
415 mentation. The datasets cover hourly data from 1.8.2018. to 31.12.2018. and covered a total of 3670 data
416 points. The hourly metrics that were the most relevant are included for multivariate forecasting as well
417 as the data and support metrics of generated photovoltaic power. The dataset was then further separated
418 and with 70% of the data used for training, 10% for validation, and the remaining 20% for testing. The
419 included features include generated photovoltaic power, as well as humidity, rainfall, cloud cover, and
420 ambient temperature. With the generated photovoltaic power feature being the prediction target.

421 **4.1.2 China Wind Farm Dataset**

422 The Global Energy Forecasting Competition 2012 (GEFCom2012) is a competition that aimed to promote
423 the development of state-of-the-art forecasting models for various aspects of the energy industry. The
424 dataset related to wind farms in China used in a competition ³. Seven wind farms from mainland China
425 were selected and anonymized for this dataset. Power generation data has been normalized as well due to
426 anonymity concerns.

427 Relevant wind data is collected every 12h while the dataset includes forecasts in intervals of 24h.
428 The direction and speed of the wind and meridional wind components are provided as well. The dataset
429 consists of hourly measurements of wind power generation from seven wind farms located in China,
430 spanning from January 1, 2011, to September 30, 2012. Each wind farm has different installed capacities,
431 which makes the forecasting task more challenging. For experimentation, hourly resolution data has
432 been split into predictions of 12h and then further combined with normalized real-world data of power
433 generation for each farm by the hour. Due to the last year of data not being available, the dataset consists
434 of four years of data. The included features are Wind speed, wind direction, and zonal and meridional
435 wind components for each wind farm while the target feature is the amount of generated power.

436 The first 70% of the available data points were utilized for training, while the later 10% and 20% were
437 used for validation and testing.

438 **4.1.3 Data Preprocessing**

439 Before using the dataset for renewable power generation forecasting, some preprocessing steps may be
440 necessary:

- 441 1. **Missing Data Imputation:** The dataset may contain values that are missing, which are required to
442 be imputed before using the data for model training and evaluation. Various imputation techniques
443 can be employed, such as linear interpolation or more advanced methods based on machine learning
444 models.
- 445 2. **Data Splitting:** The division of the dataset into training, validation, and testing subsets. The
446 training and validation sets can be used for model development and hyperparameter tuning, while
447 the testing set can be used for final performance evaluation of the model's forecasting.

¹<https://transparency.entsoe.eu/>

²<https://openweathermap.org/guide>

³<https://www.kaggle.com/competitions/global-energy-forecasting-competition-2012-load-forecasting/data>

448 3. **Feature Engineering:** Extract additional features from the dataset that may be relevant for the
449 forecasting task, such as lagged values of wind power, moving averages, or other temporal features
450 that can help in pattern and dependency capturing in the data.

451 4. **Normalization/Standardization:** Scale the input features and target variable to ensure that they
452 are on a similar scale, which is able of improving the performance and stability.

453 Once the dataset is preprocessed, it can be used to train and evaluate various forecasting models, such
454 as the Luong attention-based RNN model discussed earlier. By incorporating techniques like time-series
455 decomposition, attention mechanisms, and hyperparameter optimization, the forecasting models can
456 be tailored to the specific characteristics and challenges of the wind power generation data, ultimately
457 improving the accuracy and reliability of the forecasts.

458 4.2 Experimental Setup

459 The following setup regards all 4 test cases that have been executed. Two stages are differentiated during
460 experimentation. During the first, the data is decomposed for both test cases. Afterward, the signal
461 components and residual signals are provided to the RNN for forecasting. VMD was employed for feature
462 engineering, and min-max scaling was utilized as scaling option. Every tested model was provided in the
463 same manner with historic data of six input points per model for three steps ahead predictions.

464 The data was split in the same manner for all four test cases, with the training set amounting to 70%,
465 the validation set of 10%, and the testing set of 20%. The split of each the solar dataset target features is
466 visualized with Figure 1 to illustrate the time intervals that were employed in each of the three mentioned
467 subsets. Similarly, the wind dataset is shown in Figure 2.

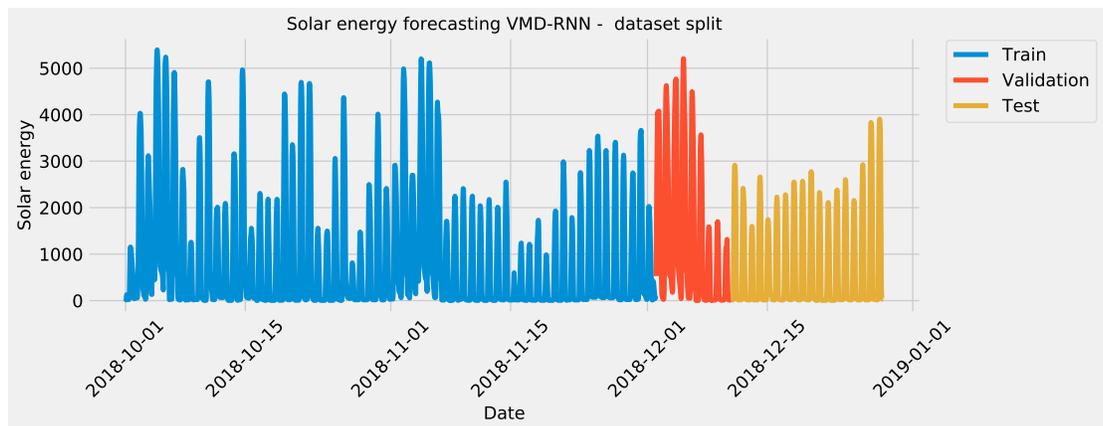


Figure 1. Solar energy generation target feature split

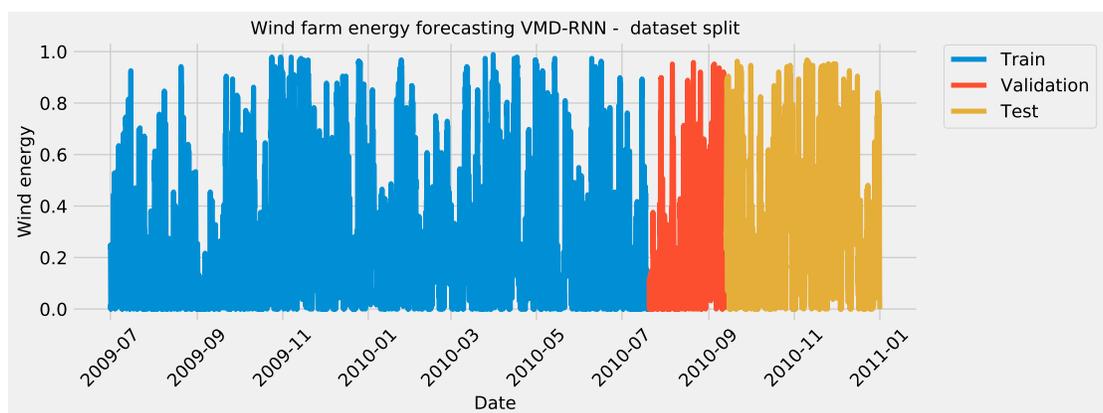


Figure 2. Wind energy generation target feature Split

468 The challenge of parameter optimization for the prediction models was tested on the following
 469 contemporary metaheuristics: GA (Mirjalili and Mirjalili, 2019), PSO (Kennedy and Eberhart, 1995),
 470 ABC (Karaboga, 2010), FA (Yang and Slowik, 2020), COLSHADE (Gurrola-Ramos et al., 2020), and
 471 self-adaptive step size algorithm (Tang and Gibali, 2020). Additionally, to the mentioned metaheuristics
 472 the original HHO and the DDHHO were evaluated. Each algorithm was executed with 8 solutions in the
 473 population and 5 iterations.

474 The parameters for the VMD were empirically established and the parameter $K = 3$, while the α
 475 parameter represents the length of the used dataframe. To ensure the objectivity of model evaluation
 476 30 independent runs were performed due to the stochastic nature of the optimization algorithms. The
 477 selected parameters for optimization of the RNN are given in the following text due to their impact on the
 478 performance of the model. The ranges of the parameters alongside their descriptions are given: [50, 100]
 479 number of neurons, [0.0001, 0.01] learning rate, [100, 300] training epochs, [0.05, 0.1] dropout rate, and
 480 [1, 3] for the total layer number of a network.

481 Lastly, an early stopping mechanism is incorporated for overfitting prevention with the threshold
 482 empirically determined as $\frac{epochs}{3}$. The purpose of such a mechanism is to terminate the model early if no
 483 improvements are observed for $\frac{epochs}{3}$. It should be noted that computational resource waste is reduced as
 484 an effect of this approach.

485 This study employs five performance metrics commonly used to evaluate the accuracy and effec-
 486 tiveness of the proposed attention-based recurrent neural network (A-RNN) model for renewable power
 487 generation forecasting. These performance metrics are mean absolute error (MAE), root mean squared
 488 error (RMSE), mean absolute error (MAE), Coefficient of determination (R^2) and the index of alignment
 489 (IA).

490 MAE is the average of the absolute differences between the predicted values and the actual values. It
 491 measures the magnitude of errors in the forecasts without considering their direction. The MAE is defined
 492 as:

$$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i| \quad (25)$$

493 for which the N represents data points total, y_i the actual value, and \hat{y}_i the predicted value.

494 RMSE is the square root of the average of the squared differences between the predicted values and
 495 the actual values. It provides a measure of the overall model's performance by penalizing larger errors
 496 more than smaller errors. The RMSE is defined as:

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2} \quad (26)$$

497 MAE is the average of the absolute differences between the predicted values and the actual values.
 498 It can be useful for comparing the performance of different models across various scales. The MAE is
 499 defined as:

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i| \quad (27)$$

500 where the $||$ denotes the absolute value.

501 R^2 indicates the proportion of the variance in the dependent variable that can be explained by the
 502 independent variables in the model. It ranges from 0 to 1, with higher values indicating a better fit between
 503 the model and the data. R^2 is defined as:

$$R^2 = 1 - \frac{\sum_i (y_i - \hat{y}_i)^2}{\sum_i (y_i - \bar{y})^2} \quad (28)$$

504 where the \bar{y} refers to the mean of the actual values.

505 IA measures the extent to which the model's predicted outcomes align with the true outcomes or the
 506 intended goals. A higher Alignment Index indicates a stronger alignment, suggesting that the model is
 507 performing well. AI is defined as:

$$IA = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (|y_p - \bar{y}| + |y_i - \bar{y}|)^2} \quad (29)$$

508 These performance metrics, MAE, RMSE, and MAPE, are used to evaluate the accuracy and effec-
 509 tiveness of the proposed A-RNN model in comparison to the regular RNN model for renewable power
 510 generation forecasting. A lower value for each metric indicates better forecasting performance.

511 A flowchart of the utilized experimental framework is provided in Figure 3.

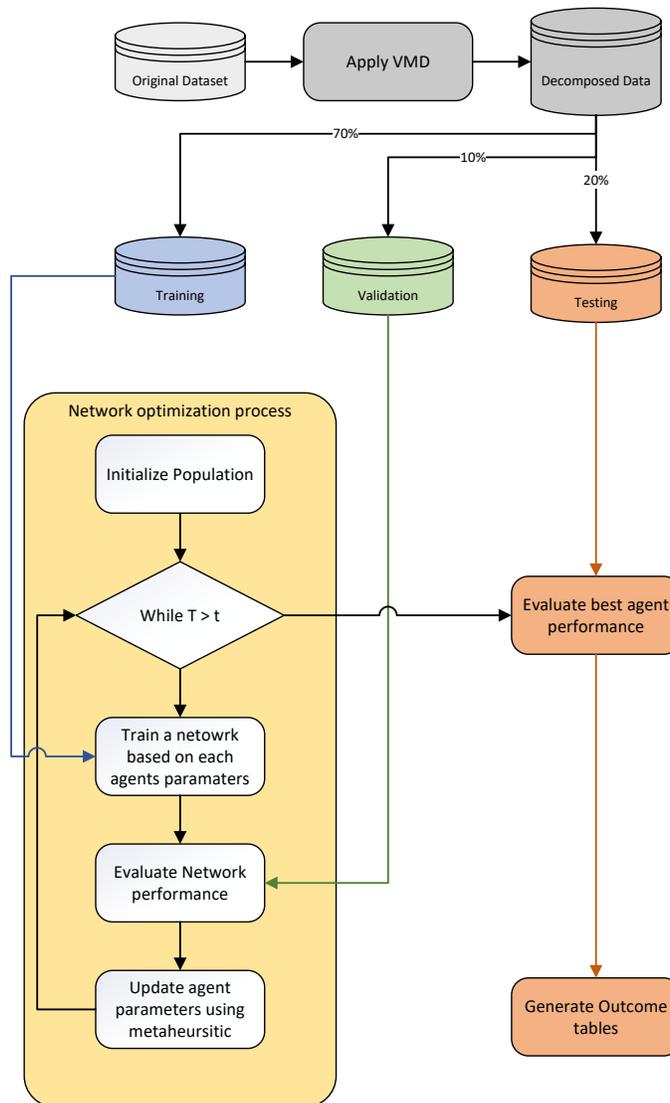


Figure 3. Experimental framework flowchart

512 5 RESULTS AND COMPARISON

513 This section exhibits obtained experimental findings in terms of captured performance metrics. The best
 514 metrics in all tables were marked with bold style to more clearly visualize the best performing methods.

518 **5.1 Spain Solar Energy Forecasting**

516 In Table 1 the objective function outcomes for the best, worst, mean, and median executions, alongside
 517 the standard deviance with variance are shown for 30 independent runs of each metaheuristic.

Table 1. VMD-RNN solar energy forecasting objective function overall outcomes

| Method | Best | Worst | Mean | Median | Std | Var |
|------------------|-----------------|-----------------|-----------------|-----------------|-----------------|--------------------|
| VMD-RNN-DDHHO | 0.006284 | 0.007320 | 0.006855 | 0.006931 | 0.000389 | 1.513667E-7 |
| VMD-RNN-HHO | 0.006990 | 0.007890 | 0.007366 | 0.007282 | 0.000344 | 1.183526E-7 |
| VMD-RNN-GA | 0.006664 | 0.007559 | 0.007061 | 0.007228 | 0.000341 | 1.163809E-7 |
| VMD-RNN-PSO | 0.007186 | 0.007458 | 0.007345 | 0.007425 | 0.000115 | 1.320113E-8 |
| VMD-RNN-ABC | 0.006499 | 0.007231 | 0.006830 | 0.006801 | 0.000251 | 6.319240E-8 |
| VMD-RNN-FA | 0.007005 | 0.007542 | 0.007184 | 0.007014 | 0.000229 | 5.253891E-8 |
| VMD-RNN-COLSHADE | 0.007159 | 0.008009 | 0.007478 | 0.007182 | 0.000357 | 1.273813E-7 |
| VMD-RNN-SASS | 0.007057 | 0.007405 | 0.007264 | 0.007240 | 0.000135 | 1.829039E-8 |

518 As Table 1 suggests, the introduced algorithms attained the best results when optimizing a RNN in the
 519 best run. However, admirable stability was demonstrated by the PSO. Furthermore, when considering the
 520 worst case execution the ABC attained the best results as well as in the mean and median runs. This is to
 521 be expected as per the NFL (Wolpert and Macready, 1997) no single approach works equally well in all
 522 execution cases.

523 Further detailed metrics for the best run, for each forecasting step and every tested metaheuristic are
 524 demonstrated in Table 2.

Table 2. The VMD-RNN solar energy metrics per each step

| Step | Metric | VMD-RNN-DDHHO | VMD-RNN-HHO | VMD-RNN-GA | VMD-RNN-PSO | VMD-RNN-ABC | VMD-RNN-FA | VMD-RNN-COLSHADE | VMD-RNN-SASS |
|------------|----------------|----------------------|---------------|----------------------|---------------------|---------------|-----------------|------------------|---------------|
| One Step | R ² | 0.601739 | 0.549365 | 0.627364 | 0.528460 | 0.585500 | 0.544636 | 0.543719 | 0.559259 |
| | MAE | 384.294171 | 432.200603 | 396.006180 | 427.516283 | 404.377133 | 418.018708 | 411.089031 | 412.655917 |
| | MSE | 400081.633100 | 452694.787317 | 374338.747453 | 473694.873874 | 416895.063424 | 457445.578253 | 458366.263037 | 442755.336455 |
| | RMSE | 632.520065 | 672.825971 | 611.832287 | 688.254948 | 645.674115 | 676.347232 | 677.027520 | 665.398630 |
| | IA | 0.886044 | 0.870430 | 0.896802 | 0.870911 | 0.877714 | 0.875709 | 0.875988 | 0.877386 |
| Two Step | R ² | 0.8896686 | 0.878472 | 0.844966 | 0.868775 | 0.876350 | 0.885817 | 0.873014 | 0.8760918 |
| | MAE | 195.801662 | 227.673953 | 246.869567 | 233.834781 | 227.774440 | 204.845965 | 216.919114 | 219.607867 |
| | MSE | 110835.615218 | 122082.984352 | 155742.443523 | 131825.249471 | 124214.713878 | 114704.662015 | 127566.656326 | 124474.546886 |
| | RMSE | 332.919833 | 349.403755 | 394.642172 | 363.077470 | 352.441079 | 338.680767 | 357.164747 | 352.809505 |
| | IA | 0.970558 | 0.966796 | 0.960179 | 0.966048 | 0.965562 | 0.969940 | 0.968305 | 0.966947 |
| Three Step | R ² | 0.962557 | 0.964848 | 0.948636 | 0.978350 | 0.973942 | 0.960881 | 0.961240 | 0.951496 |
| | MAE | 122.562368 | 137.209296 | 165.046855 | 105.082911 | 112.980142 | 141.060131 | 124.093137 | 141.036372 |
| | MSE | 37613.696545 | 35313.037867 | 51598.255163 | 21749.216531 | 26177.198226 | 39297.213129 | 38936.684159 | 48725.218704 |
| | RMSE | 193.942508 | 187.917636 | 227.152493 | 147.4761560 | 161.793690 | 198.235247 | 197.323805 | 220.737896 |
| | IA | 0.9901459 | 0.990594 | 0.986690 | 0.994450 | 0.992991 | 0.989871 | 0.990657 | 0.987153 |
| Overall | R ² | 0.817988 | 0.797562 | 0.806989 | 0.791861 | 0.811765 | 0.797111 | 0.792658 | 0.795616 |
| | MAE | 234.219400 | 265.694617 | 269.307534 | 255.477992 | 248.377238 | 254.641602 | 250.700427 | 257.766719 |
| | MSE | 182843.648288 | 203363.603179 | 193893.148713 | 209089.779959 | 189095.658509 | 203815.817799 | 208289.867841 | 205318.367348 |
| | RMSE | 427.602208 | 450.958538 | 440.332998 | 457.263360 | 434.851306 | 451.459652 | 456.387848 | 453.120698 |
| | IA | 0.948916 | 0.942607 | 0.947890 | 0.943803 | 0.945423 | 0.945173 | 0.944983 | 0.943829 |

525 As it can be observed from Table 2 the introduced method attained the best overall results in all cases
 526 except the R² metric, where the PSO attained better results. As the guiding objective function during the
 527 optimization process was MSE this is to be expected. Additionally the introduced method also attained
 528 the best results when making forecasts two steps ahead, as well MAE for one step ahead. The best results
 529 for R², MSE and IA where attained by the GA, while the best RMSE results where attained by the PSO.
 530 Nevertheless when making forecasts three steps ahead the PSO attained the best results across all metrics
 531 except R² where the FA attained the best outcomes.

532 To help demonstrated the improvements made by the introduced method visualizations are provided
 533 for the distribution of both MSE and R² are shown in Figure 4 followed by convergence plots for both
 534 functions in Figure 5 and swarm and KDE plots in Figure 6.

535 Finally, the parameters selected by each metaheuristic for their respective best models are shown in
 536 Table 3.

537 Similarly to the previous experiment, in Table 4 the objective function outcomes for the best, worst,
 538 mean, and median executions, alongside the standard deviance with variance are shown for 30 independent
 539 runs of each metaheuristic.

540 Interestingly, when optimizing the RNN-ATT models, the introduced metaheuristic demonstrated
 541 better performance overall most metrics. However, the ABC and SASS algorithms demonstrated a slightly
 542 higher degree of stability despite attaining less impressive results.

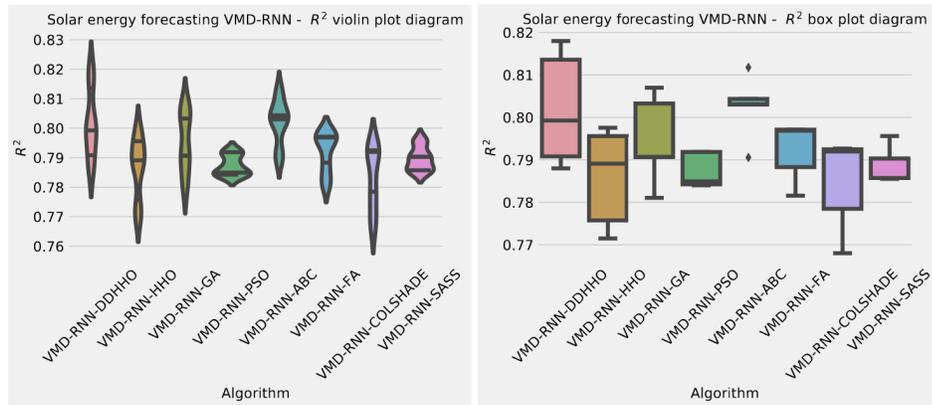


Figure 4. Solar dataset objective function and R^2 distribution plots for each metaheuristic without attention layer

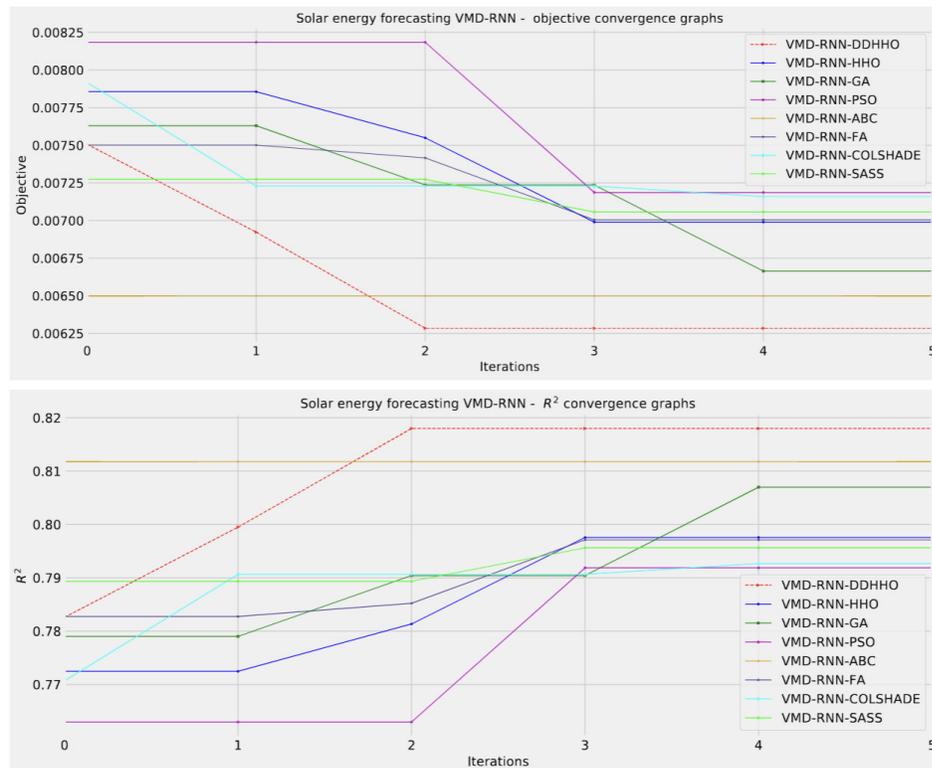


Figure 5. Solar dataset objective function and R^2 convergence plots for each metaheuristic without attention layer

543 Further detailed metrics for the best run, for each forecasting step and every tested metaheuristic are
 544 demonstrated in Table 5.

545 As it can be observed in Table 5 the introduced method attained the best overall results for MSE and
 546 MAE, while the HHO attained the best IA results, the ABC attained the best R^2 outcomes overall, while
 547 SASS attained the best outcomes for MAE. The introduced approach demonstrated the best performance
 548 when making predictions one step ahead, while two step ahead forecasts are done best by the PSO. No
 549 single approach performed the best for three steps ahead, while different metaheuristic attaining first
 550 place in different metrics further enforcing the NFL (Wolpert and Macready, 1997) theorem.

551 Visualizations of objective function and R^2 distributions are shown in Figure 7 followed by their

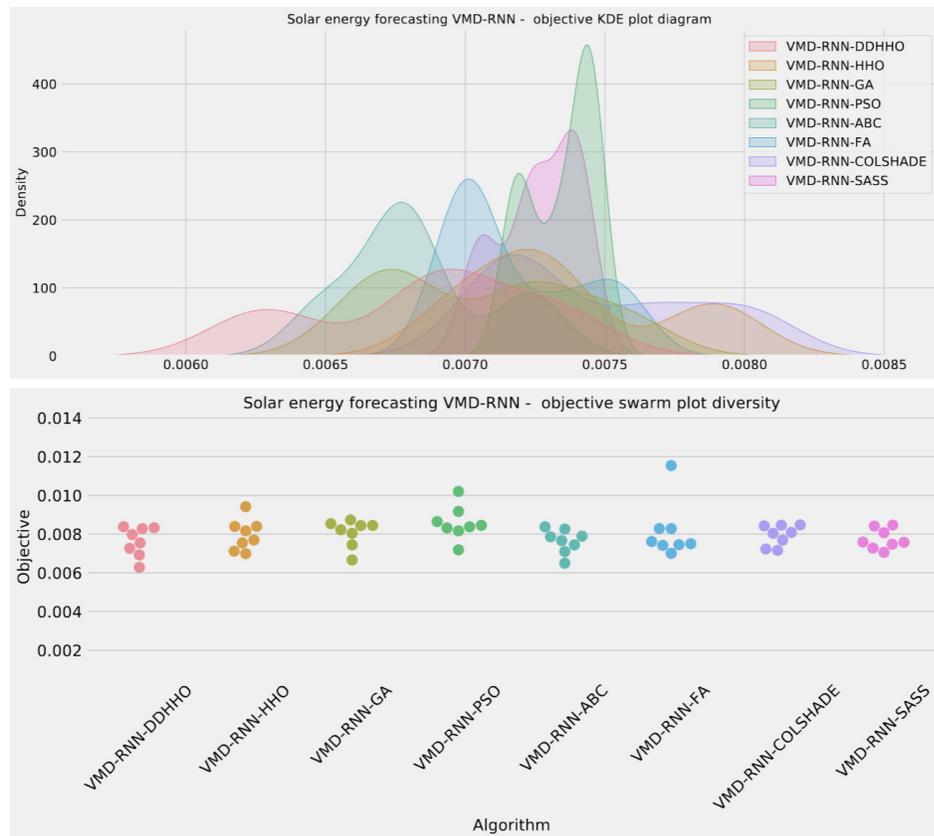


Figure 6. Solar dataset objective swarm and KDE plots for each metaheuristic without attention layer

Table 3. Parameters for best performing solar prediction RNN model optimized by each metaheuristic

| Method | Learning Rate | Drouput | Epochs | Layers | L1 Neurons | L2 Neurons | L3 Neurons |
|------------------|---------------|----------|--------|--------|------------|------------|------------|
| VMD-RNN-DDHHO | 0.007050 | 0.050000 | 232 | 3 | 50 | 100 | 100 |
| VMD-RNN-HHO | 0.007349 | 0.076853 | 206 | 3 | 64 | 50 | 100 |
| VMD-RNN-GA | 0.009097 | 0.091104 | 114 | 2 | 89 | 52 | / |
| VMD-RNN-PSO | 0.009329 | 0.069591 | 223 | 2 | 69 | 89 | / |
| VMD-RNN-ABC | 0.010000 | 0.100000 | 181 | 3 | 92 | 64 | 79 |
| VMD-RNN-FA | 0.010000 | 0.088052 | 238 | 2 | 50 | 50 | / |
| VMD-RNN-COLSHADE | 0.008718 | 0.063527 | 288 | 3 | 85 | 100 | 100 |
| VMD-RNN-SASS | 0.006645 | 0.096538 | 300 | 3 | 100 | 86 | 54 |

Table 4. VMD-RNN-ATT solar energy forecasting objective function overall outcomes

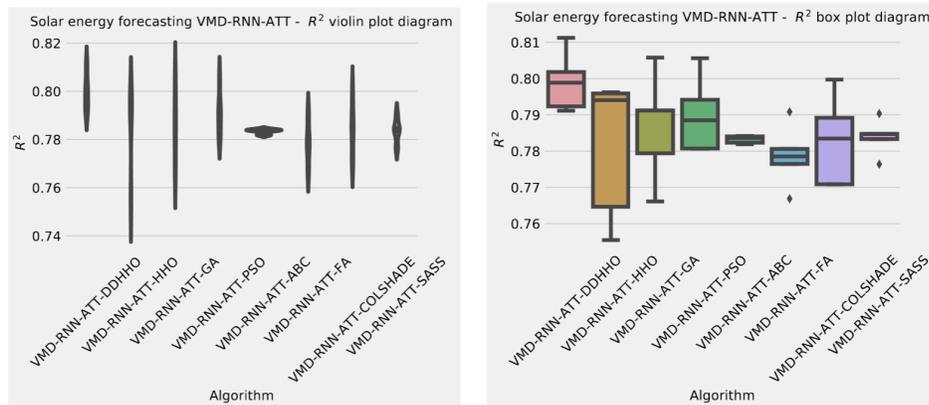
| Method | Best | Worst | Mean | Median | Std | Var |
|----------------------|-----------------|-----------------|-----------------|-----------------|-----------------|--------------------|
| VMD-RNN-ATT-DDHHO | 0.006517 | 0.007211 | 0.006923 | 0.006944 | 0.000250 | 6.265266E-8 |
| VMD-RNN-ATT-HHO | 0.007036 | 0.008443 | 0.007447 | 0.007111 | 0.000613 | 3.759833E-7 |
| VMD-RNN-ATT-GA | 0.006705 | 0.008075 | 0.007389 | 0.007209 | 0.000499 | 2.490886E-7 |
| VMD-RNN-ATT-PSO | 0.006711 | 0.007571 | 0.007233 | 0.007303 | 0.000297 | 8.818285E-8 |
| VMD-RNN-ATT-ABC | 0.007452 | 0.007531 | 0.007480 | 0.007470 | 0.000032 | 1.025433E-9 |
| VMD-RNN-ATT-FA | 0.007222 | 0.008049 | 0.007641 | 0.007647 | 0.000292 | 8.550797E-8 |
| VMD-RNN-ATT-COLSHADE | 0.006915 | 0.007912 | 0.007455 | 0.007476 | 0.000363 | 1.318140E-7 |
| VMD-RNN-ATT-SASS | 0.007238 | 0.007720 | 0.007472 | 0.007432 | 0.000164 | 2.673677E-8 |

552 respective convergence graphs in Figure 8. The KDE and swarm plots are also provided in Figure 9.

553 The parameters selected by each competing metaheuristic for their respective best-performing models
 554 are shown in Table 6.

Table 5. The VMD-RNN-ATT solar energy metrics per each step

| Step | Metric | VMD-RNN-ATT-DDHHO | VMD-RNN-ATT-HHO | VMD-RNN-ATT-GA | VMD-RNN-ATT-PSO | VMD-RNN-ATT-ABC | VMD-RNN-ATT-FA | VMD-RNN-ATT-COLSHADE | VMD-RNN-ATT-SASS |
|---------|----------------|----------------------|-----------------|----------------|----------------------|-----------------|---------------------|----------------------|-------------------|
| 1 | R ² | 0.715471 | 0.584499 | 0.598188 | 0.574065 | 0.603103 | 0.548291 | 0.616813 | 0.547094 |
| | MAE | 376.979586 | 442.064510 | 462.047919 | 435.538303 | 474.267738 | 435.524720 | 423.718303 | 416.220384 |
| | MSE | 285829.818133 | 417399.667275 | 403648.569532 | 427881.634339 | 398711.291244 | 453773.352978 | 384938.817726 | 454976.265366 |
| | RMSE | 534.630544 | 646.064755 | 635.333432 | 654.126620 | 631.435896 | 673.627013 | 620.434378 | 674.519285 |
| | IA | 0.9146240 | 0.889628 | 0.881474 | 0.871310 | 0.891814 | 0.873488 | 0.887386 | 0.861529 |
| 2 | R ² | 0.829019 | 0.876223 | 0.874955 | 0.888033 | 0.837797 | 0.868852 | 0.874406 | 0.861896 |
| | MAE | 252.954113 | 243.425326 | 260.158326 | 218.732420 | 290.688281 | 236.760030 | 252.883363 | 233.639125 |
| | MSE | 171762.088320 | 124342.580437 | 125616.779871 | 112478.817327 | 162944.638909 | 131747.397307 | 126168.484562 | 138735.683810 |
| | RMSE | 414.441900 | 352.622433 | 354.424576 | 335.378618 | 403.6640174 | 362.970243 | 355.202033 | 372.472393 |
| | IA | 0.951127 | 0.967796 | 0.965910 | 0.967226 | 0.958823 | 0.966348 | 0.966094 | 0.961092 |
| 3 | R ² | 0.889236 | 0.927962 | 0.9442501 | 0.954781 | 0.911610 | 0.955364 | 0.907969 | 0.962090 |
| | MAE | 244.240630 | 219.831502 | 179.063882 | 144.828299 | 232.407156 | 154.496558 | 244.166959 | 131.982225 |
| | MSE | 111269.990578 | 72366.697870 | 56004.659587 | 45425.756743 | 88793.700643 | 44840.040944 | 92451.964057 | 38082.907643 |
| | RMSE | 333.571567 | 269.010590 | 236.653036 | 213.133190 | 297.982719 | 211.754672 | 304.059146 | 195.14842 |
| | IA | 0.968308 | 0.980827 | 0.985080 | 0.987410 | 0.976862 | 0.988566 | 0.974996 | 0.989529 |
| Overall | R ² | 0.811242 | 0.796228 | 0.805798 | 0.805626 | 0.784170 | 0.790836 | 0.799729 | 0.790360 |
| | MAE | 291.391443 | 301.77378 | 300.423376 | 266.366341 | 332.454391 | 275.593769 | 306.922875 | 260.613911 |
| | MSE | 189620.632344 | 204702.981861 | 195090.002997 | 195262.069470 | 216816.543599 | 210120.263743 | 201186.422115 | 210598.285607 |
| | RMSE | 435.454512 | 452.441136 | 441.688940 | 441.884679 | 465.635634 | 458.388769 | 448.538094 | 458.909888 |
| | IA | 0.944686 | 0.946083 | 0.944154 | 0.941982 | 0.942500 | 0.942801 | 0.942826 | 0.937383 |

**Figure 7.** Solar dataset objective function and R^2 distribution plots for each metaheuristic with attention layer**Table 6.** Parameters for best performing solar prediction RNN-ATT model optimized by each metaheuristic

| Method | Learning Rate | Drouput | Epochs | Layers | L1 Neurons | L2 Neurons | L3 Neurons | ATT Neurons |
|----------------------|---------------|----------|--------|--------|------------|------------|------------|-------------|
| VMD-RNN-ATT-DDHHO | 0.010000 | 0.100000 | 100 | 3 | 100 | 100 | 50 | 50 |
| VMD-RNN-ATT-HHO | 0.009323 | 0.100000 | 100 | 1 | 98 | / | / | 50 |
| VMD-RNN-ATT-GA | 0.009990 | 0.080219 | 148 | 2 | 71 | 69 | / | 82 |
| VMD-RNN-ATT-PSO | 0.008559 | 0.097184 | 166 | 3 | 89 | 51 | 99 | 96 |
| VMD-RNN-ATT-ABC | 0.010000 | 0.067651 | 101 | 1 | 50 | / | / | 50 |
| VMD-RNN-ATT-FA | 0.006927 | 0.052260 | 216 | 2 | 90 | 87 | / | 97 |
| VMD-RNN-ATT-COLSHADE | 0.004221 | 0.050000 | 120 | 1 | 50 | / | / | 71 |
| VMD-RNN-ATT-SASS | 0.009982 | 0.099805 | 188 | 3 | 100 | 50 | 50 | 50 |

555 In Table 7 the objective function outcomes for the best, worst, mean, and median executions, alongside
 556 the standard deviance with variance are shown for 30 independent runs of each metaheuristic forecasting
 557 wind power generation.

558 5.2 China Wind Farm Forecasting

559 The introduced metaheuristic attained the best outcomes in the best, mean and median executions, with
 560 the ABC attained the best outcomes in the worst case executions. Furthermore, the highest stability was
 561 demonstrated by SASS. Further detailed metrics for the best run, for each forecasting step and every
 562 tested metaheuristic are demonstrated in Table 8.

563 As demonstrated in Table 8, the introduced metaheuristic outperformed all competing metaheuristic
 564 in overall outcomes. The introduces metaheuristic demonstrated the best results for one step ahead
 565 forecasts; However, the PSO attained the best results for two steps ahead forecasts, and COLSHADE
 566 attained the best outcomes for three steps ahead. These results further reinforce that no single approach
 567 is equally suited to all use-cases as per the NFL (Wolpert and Macready, 1997) Visualizations of the
 568 distribution and convergence rates of the mse and R^2 functions are shown in Figure 10 and Figures 11.
 569 Additionally, KDE and swarm diversity plots are provided in Figure 12.

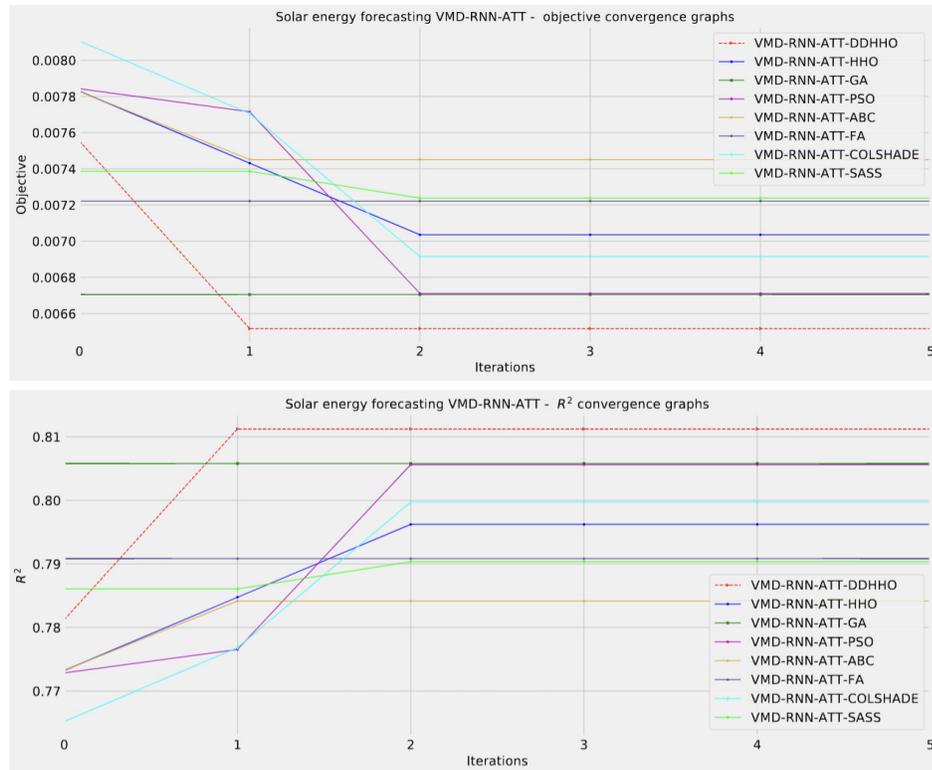


Figure 8. Solar dataset objective function and R^2 convergence plots for each metaheuristic with attention layer

Table 7. VMD-RNN wind energy forecasting objective function overall outcomes

| Method | Best | Worst | Mean | Median | Std | Var |
|------------------|-----------------|-----------------|-----------------|-----------------|-----------------|--------------------|
| VMD-RNN-DDHHO | 0.010465 | 0.011162 | 0.010747 | 0.010764 | 0.000244 | 5.930160E-8 |
| VMD-RNN-HHO | 0.011407 | 0.011707 | 0.011538 | 0.011517 | 0.000125 | 1.559006E-8 |
| VMD-RNN-GA | 0.011028 | 0.011461 | 0.011240 | 0.011256 | 0.000168 | 2.812603E-8 |
| VMD-RNN-PSO | 0.011000 | 0.011507 | 0.011258 | 0.011294 | 0.000186 | 3.459674E-8 |
| VMD-RNN-ABC | 0.010729 | 0.010977 | 0.010847 | 0.010834 | 0.000108 | 1.176703E-8 |
| VMD-RNN-FA | 0.010519 | 0.011483 | 0.011102 | 0.011134 | 0.000381 | 1.448697E-7 |
| VMD-RNN-COLSHADE | 0.010823 | 0.011382 | 0.011214 | 0.011341 | 0.000241 | 5.784354E-8 |
| VMD-RNN-SASS | 0.011042 | 0.011300 | 0.011231 | 0.011298 | 0.000100 | 9.963395E-9 |

Table 8. The VMD-RNN wind energy metrics per each step

| Step | Metric | VMD-RNN-DDHHO | VMD-RNN-HHO | VMD-RNN-GA | VMD-RNN-PSO | VMD-RNN-ABC | VMD-RNN-FA | VMD-RNN-COLSHADE | VMD-RNN-SASS |
|------------|--------|-----------------|-------------|------------|-----------------|-------------|-----------------|------------------|--------------|
| One Step | R^2 | 0.875214 | 0.855404 | 0.856190 | 0.849434 | 0.861770 | 0.872224 | 0.857508 | 0.861647 |
| | MAE | 0.077761 | 0.084168 | 0.083139 | 0.084909 | 0.081714 | 0.078881 | 0.083685 | 0.081844 |
| | MSE | 0.012012 | 0.013919 | 0.013843 | 0.014494 | 0.013306 | 0.012300 | 0.013716 | 0.013318 |
| | RMSE | 0.109599 | 0.117979 | 0.117658 | 0.120390 | 0.115352 | 0.110905 | 0.117117 | 0.115404 |
| | IA | 0.967674 | 0.960717 | 0.961990 | 0.958739 | 0.962434 | 0.966699 | 0.962278 | 0.962725 |
| Two Step | R^2 | 0.897775 | 0.892783 | 0.900496 | 0.903051 | 0.900259 | 0.902827 | 0.899419 | 0.899132 |
| | MAE | 0.070751 | 0.074085 | 0.070576 | 0.070070 | 0.070933 | 0.070237 | 0.071078 | 0.071742 |
| | MSE | 0.009840 | 0.010321 | 0.009578 | 0.009332 | 0.009601 | 0.009354 | 0.009682 | 0.009710 |
| | RMSE | 0.099198 | 0.101592 | 0.097869 | 0.096605 | 0.097986 | 0.096716 | 0.098397 | 0.098538 |
| | IA | 0.973272 | 0.971041 | 0.973894 | 0.974067 | 0.973158 | 0.974287 | 0.973057 | 0.973069 |
| Three Step | R^2 | 0.908009 | 0.904098 | 0.907150 | 0.9121979 | 0.910908 | 0.904295 | 0.913157 | 0.902638 |
| | MAE | 0.067910 | 0.071199 | 0.069404 | 0.0681129 | 0.068257 | 0.070842 | 0.066382 | 0.072017 |
| | MSE | 0.008855 | 0.009232 | 0.008938 | 0.0084520 | 0.008576 | 0.009213 | 0.008360 | 0.009372 |
| | RMSE | 0.094102 | 0.096081 | 0.094540 | 0.0919348 | 0.092607 | 0.095982 | 0.091431 | 0.096810 |
| | IA | 0.975517 | 0.974068 | 0.975414 | 0.9765410 | 0.976470 | 0.974705 | 0.976785 | 0.973296 |
| Overall | R^2 | 0.893666 | 0.884095 | 0.887945 | 0.8882271 | 0.890979 | 0.893116 | 0.890028 | 0.887805 |
| | MAE | 0.072141 | 0.076484 | 0.074373 | 0.0743641 | 0.073635 | 0.073320 | 0.073715 | 0.075201 |
| | MSE | 0.010236 | 0.011157 | 0.010787 | 0.0107594 | 0.010494 | 0.010289 | 0.010586 | 0.010800 |
| | RMSE | 0.101172 | 0.105627 | 0.103858 | 0.1037274 | 0.102443 | 0.101434 | 0.102888 | 0.103923 |
| | IA | 0.972154 | 0.968608 | 0.970433 | 0.9697823 | 0.970688 | 0.971897 | 0.970706 | 0.969697 |

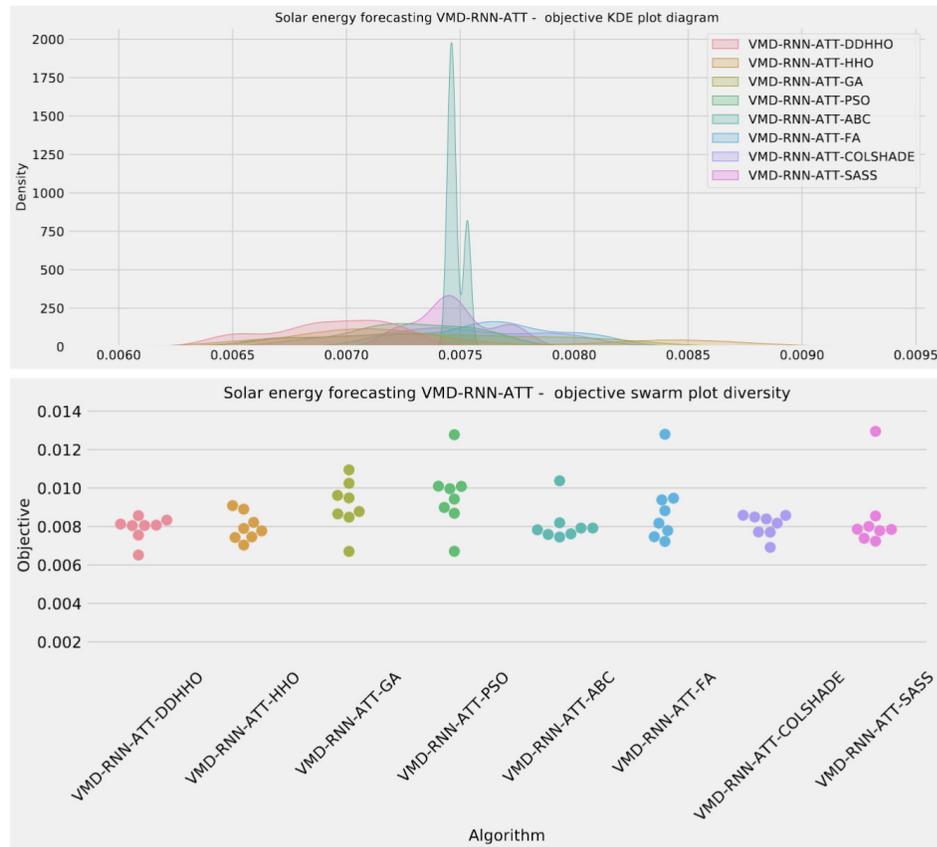


Figure 9. Solar dataset objective swarm and KDE plots for each metaheuristic with attention layer

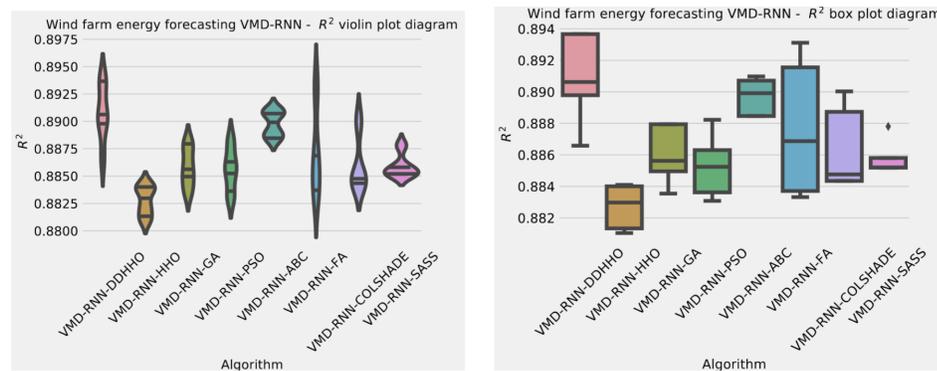


Figure 10. Wind dataset objective function and R^2 distribution plots for each metaheuristic without attention layer

570 The network hyperparameters selected by each metaheuristic for the respective best performing
571 models are shown in Table 9.

572 Similarly to the previous experiment, in Table 10 the objective function outcomes for the best, worst,
573 mean, and median executions, alongside the standard deviation with variance are shown for 30 independent
574 runs of each metaheuristic.

575 As it can be observed in Table 10 the introduced metaheuristic attained the best outcomes in all except
576 the medial case, where the ABC algorithms attained the best results. Further detailed metrics for the best
577 run, for each forecasting step and every tested metaheuristic are demonstrated in Table 11.

578 As Table 11 demonstrates, the introduces algorithms performed admirably, attaining the best outcomes

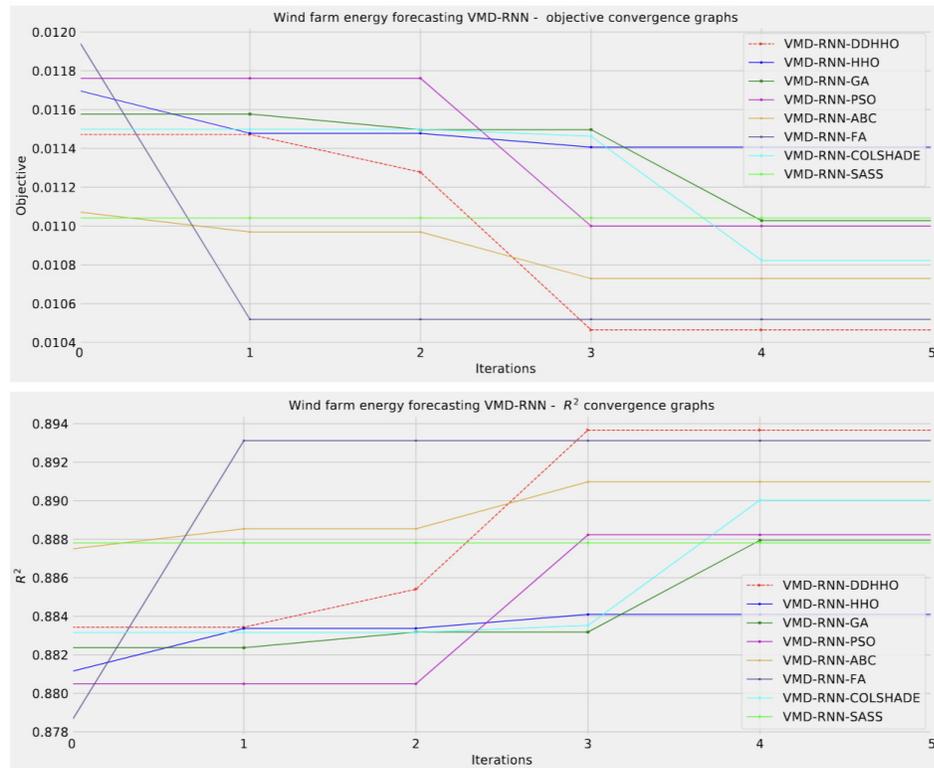


Figure 11. Wind dataset objective function and R^2 convergence plots for each metaheuristic without attention layer

Table 9. Parameters for best performing wind prediction RNN model optimized by each metaheuristic

| Method | Learning Rate | Drouput | Epochs | Layers | L1 Neurons | L2 Neurons | L3 Neurons |
|------------------|---------------|----------|--------|--------|------------|------------|------------|
| VMD-RNN-DDHHO | 0.010000 | 0.050755 | 300 | 3 | 97 | 94 | 100 |
| VMD-RNN-HHO | 0.006340 | 0.100000 | 200 | 1 | 100 | / | / |
| VMD-RNN-GA | 0.009989 | 0.067669 | 134 | 2 | 95 | 58 | / |
| VMD-RNN-PSO | 0.008124 | 0.053596 | 294 | 3 | 85 | 93 | 73 |
| VMD-RNN-ABC | 0.010000 | 0.100000 | 300 | 3 | 100 | 79 | 50 |
| VMD-RNN-FA | 0.010000 | 0.050000 | 300 | 2 | 100 | 50 | / |
| VMD-RNN-COLSHADE | 0.010000 | 0.096306 | 300 | 3 | 67 | 50 | 50 |
| VMD-RNN-SASS | 0.010000 | 0.050000 | 300 | 1 | 64 | / | / |

Table 10. VMD-RNN-ATT wind energy forecasting objective function overall outcomes

| Method | Best | Worst | Mean | Median | Std | Var |
|----------------------|-----------------|-----------------|-----------------|-----------------|-----------------|--------------------|
| VMD-RNN-ATT-DDHHO | 0.010359 | 0.011446 | 0.010993 | 0.011361 | 0.000475 | 2.254891E-7 |
| VMD-RNN-ATT-HHO | 0.010806 | 0.011496 | 0.011261 | 0.011424 | 0.000269 | 7.259626E-8 |
| VMD-RNN-ATT-GA | 0.011264 | 0.011672 | 0.011441 | 0.011387 | 0.000152 | 2.298042E-8 |
| VMD-RNN-ATT-PSO | 0.011167 | 0.011808 | 0.011455 | 0.011431 | 0.000251 | 6.293247E-8 |
| VMD-RNN-ATT-ABC | 0.010911 | 0.011524 | 0.011279 | 0.011259 | 0.000220 | 4.861609E-8 |
| VMD-RNN-ATT-FA | 0.011160 | 0.011554 | 0.011360 | 0.011420 | 0.000145 | 2.108468E-8 |
| VMD-RNN-ATT-COLSHADE | 0.011054 | 0.011368 | 0.011203 | 0.011184 | 0.000126 | 1.582216E-8 |
| VMD-RNN-ATT-SASS | 0.011269 | 0.011519 | 0.011392 | 0.011400 | 0.000096 | 9.213128E-9 |

579 on overall evaluations as well as two and three step ahead. The original HHO performed marginally better
 580 in one step ahead forecasts when considering at the MAE and IA metrics.

581 Further distribution and convergence graphs for the objective function and R^2 are shown in Figure 13
 582 and Figure 14. Accompanying KDE and swarm diversity plots are given in Figure 15.

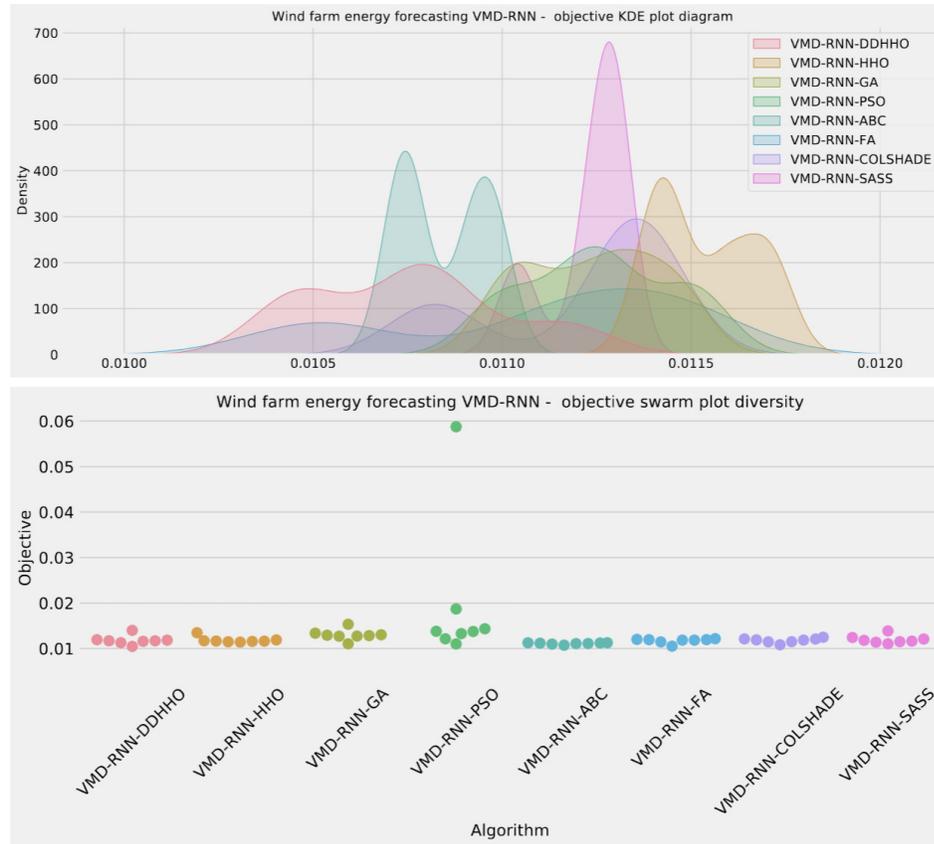


Figure 12. Wind dataset objective swarm and KDE plots for each metaheuristic without attention layer

Table 11. The VMD-RNN-ATT wind energy metrics per each step

| Step | Metric | VMD-RNN-ATT-DDHHO | VMD-RNN-ATT-HHO | VMD-RNN-ATT-GA | VMD-RNN-ATT-PSO | VMD-RNN-ATT-ABC | VMD-RNN-ATT-FA | VMD-RNN-ATT-COLSHADE | VMD-RNN-ATT-SASS |
|------------|----------------|-------------------|-----------------|----------------|-----------------|-----------------|----------------|----------------------|------------------|
| One Step | R ² | 0.869388 | 0.868300 | 0.863840 | 0.860679 | 0.861597 | 0.854800 | 0.860994 | 0.853326 |
| | MAE | 0.080227 | 0.079741 | 0.081451 | 0.083636 | 0.081330 | 0.083773 | 0.082541 | 0.083572 |
| | MSE | 0.012573 | 0.012678 | 0.013107 | 0.013411 | 0.013323 | 0.013977 | 0.013381 | 0.014119 |
| | RMSE | 0.112129 | 0.112595 | 0.114485 | 0.115806 | 0.115425 | 0.118225 | 0.115676 | 0.118823 |
| | IA | 0.964787 | 0.965400 | 0.963486 | 0.963898 | 0.963680 | 0.961305 | 0.963349 | 0.960917 |
| Two Step | R ² | 0.902255 | 0.898536 | 0.892452 | 0.895950 | 0.897634 | 0.898030 | 0.897528 | 0.895859 |
| | MAE | 0.070517 | 0.071214 | 0.073747 | 0.073326 | 0.071518 | 0.071795 | 0.072607 | 0.073126 |
| | MSE | 0.009409 | 0.009767 | 0.010353 | 0.010016 | 0.009854 | 0.009816 | 0.009864 | 0.010025 |
| | RMSE | 0.097000 | 0.098828 | 0.101748 | 0.100080 | 0.099267 | 0.099074 | 0.099318 | 0.100124 |
| | IA | 0.973859 | 0.973364 | 0.971348 | 0.972700 | 0.973169 | 0.973293 | 0.973173 | 0.972177 |
| Three Step | R ² | 0.912571 | 0.903750 | 0.900340 | 0.902971 | 0.908152 | 0.906962 | 0.904508 | 0.907307 |
| | MAE | 0.067887 | 0.070822 | 0.072048 | 0.071218 | 0.069180 | 0.070399 | 0.072522 | 0.071352 |
| | MSE | 0.008416 | 0.009265 | 0.009593 | 0.009340 | 0.008841 | 0.008956 | 0.009192 | 0.008923 |
| | RMSE | 0.091739 | 0.096255 | 0.097946 | 0.096644 | 0.094628 | 0.094636 | 0.095876 | 0.094460 |
| | IA | 0.976584 | 0.974331 | 0.973022 | 0.973790 | 0.975383 | 0.975599 | 0.974773 | 0.975041 |
| Overall | R ² | 0.894738 | 0.890195 | 0.885544 | 0.886533 | 0.889128 | 0.886597 | 0.887677 | 0.885497 |
| | MAE | 0.0728767 | 0.073925 | 0.075749 | 0.076060 | 0.074010 | 0.075322 | 0.075890 | 0.076017 |
| | MSE | 0.0101326 | 0.010570 | 0.011018 | 0.010922 | 0.010673 | 0.010916 | 0.010812 | 0.011022 |
| | RMSE | 0.1006610 | 0.102810 | 0.104965 | 0.104510 | 0.103309 | 0.104481 | 0.103982 | 0.104986 |
| | IA | 0.9717431 | 0.971032 | 0.969285 | 0.970130 | 0.970744 | 0.970066 | 0.970432 | 0.969378 |

583 Finally, the selected parameter for the best performing models optimized by each metaheuristic are
 584 shown in Table 12.

Table 12. Parameters for best-performing wind prediction RNN-ATT model optimized by each metaheuristic

| Method | Learning Rate | Drouput | Epochs | Layers | L1 Neurons | L2 Neurons | L3 Neurons | ATT Neurons |
|------------------|---------------|----------|--------|--------|------------|------------|------------|-------------|
| VMD-RNN-DDHHO | 0.010000 | 0.063597 | 267 | 3 | 69 | 100 | 50 | 77 |
| VMD-RNN-HHO | 0.010000 | 0.100000 | 222 | 1 | 74 | / | / | 54 |
| VMD-RNN-GA | 0.007046 | 0.060227 | 120 | 2 | 66 | 73 | / | 74 |
| VMD-RNN-PSO | 0.010000 | 0.050000 | 234 | 3 | 100 | 50 | 100 | 50 |
| VMD-RNN-ABC | 0.010000 | 0.100000 | 300 | 3 | 100 | 50 | 50 | 50 |
| VMD-RNN-FA | 0.010000 | 0.050000 | 300 | 3 | 50 | 100 | 81 | 98 |
| VMD-RNN-COLSHADE | 0.005840 | 0.100000 | 300 | 1 | 91 | / | / | 86 |
| VMD-RNN-SASS | 0.009995 | 0.100000 | 255 | 1 | 60 | / | / | 100 |

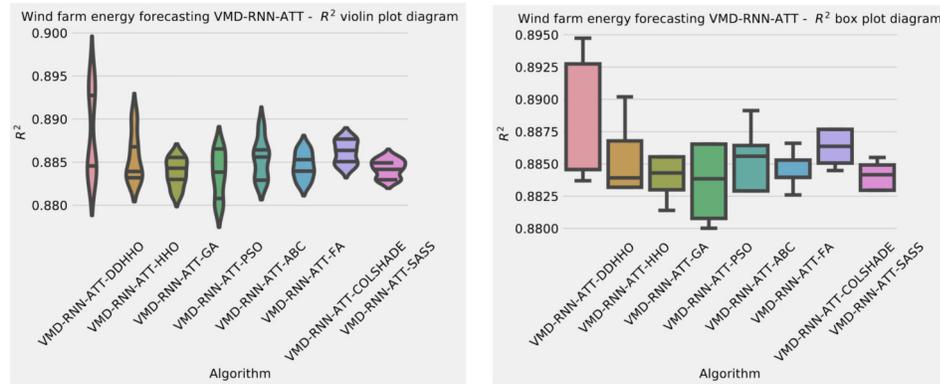


Figure 13. Wind dataset objective function and R^2 distribution plots for each metaheuristic with attention layer

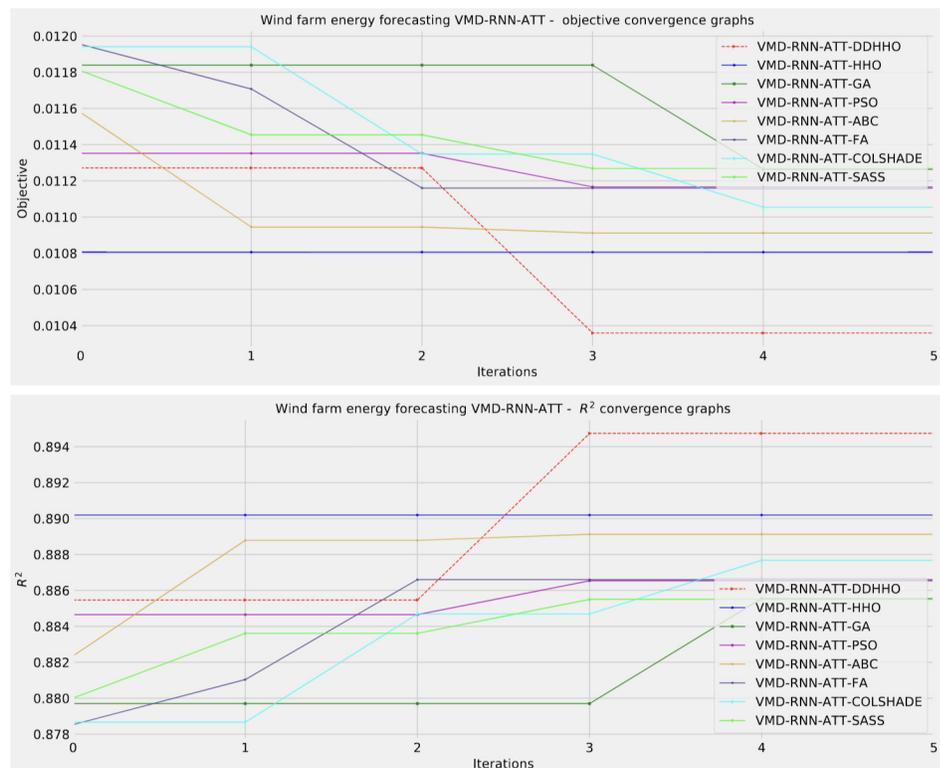


Figure 14. Wind dataset objective function and R^2 convergence plots for each metaheuristic with attention layer

585 6 DISCUSSION, STATISTICAL VALIDATION AND INTERPRETATION.

586 This section presents a discussion of the advantages of the techniques employed in the conducted research,
 587 as well as the statistical analysis of the methods used for comparisons, and the interpretation of the best
 588 models generated for both datasets.

589 6.1 Benefits of using attention mechanism for renewable power generation forecasting

590 The attention mechanism has emerged as a powerful tool in the field of machine learning, particularly
 591 for sequence-to-sequence learning problems like renewable power generation forecasting. By selectively
 592 focusing on different parts of the input sequence when generating the output, the attention mechanism can
 593 enhance the performance of forecasting models like the Luong attention-based RNN model. Below, we

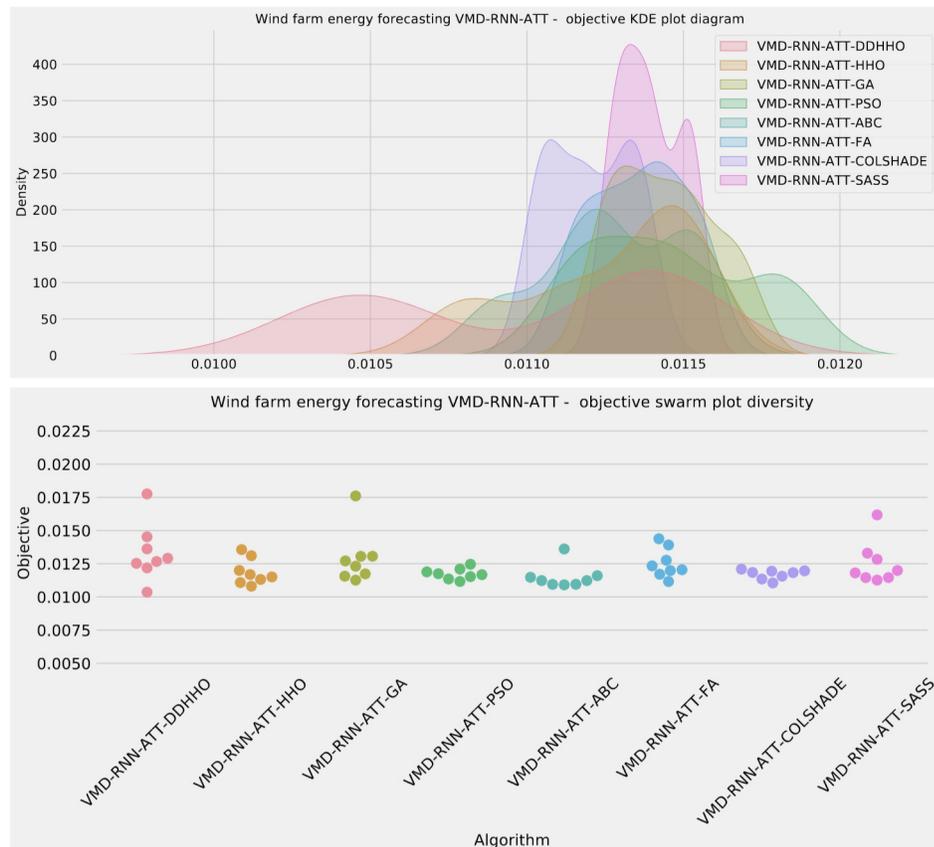


Figure 15. Wind dataset objective swarm and KDE plots for each metaheuristic with attention layer

594 discuss the key benefits of using attention mechanisms for renewable power generation forecasting:

595 **1. Improved Long-term Dependency Handling:** Renewable power generation data often exhibit
 596 long-term dependencies due to factors like seasonal patterns and weather trends. Traditional RNN
 597 models can struggle to capture these long-term dependencies effectively, leading to suboptimal forecasts.
 598 The mechanism of attention introduces different importance weights for separate input sequence parts,
 599 enabling it to focus on the most relevant information for generating the output, thus better handling
 600 long-term dependencies.

601 **2. Enhanced Forecasting Accuracy:** The attention mechanism can lead to more accurate forecasts
 602 by enabling the model to focus on the most relevant parts of the input sequence when generating the
 603 output. This selective focus allows the model to capture the underlying patterns and relationships within
 604 the renewable power generation data more effectively, resulting in improved forecasting performance.

605 **3. Interpretability:** Attention mechanisms provide a level of interpretability to the model's predictions
 606 by highlighting which parts of the input sequence have the most significant impact on the output. This
 607 interpretability can be particularly valuable in renewable power generation forecasting, as it allows domain
 608 experts to gain insights into the factors influencing the model's forecasts and to validate the model's
 609 predictions based on their domain knowledge.

610 **4. Robustness to Noise and Irrelevant Information:** Renewable power generation data can be
 611 subject to noise and irrelevant information (e.g., due to measurement errors or unrelated external factors).
 612 The attention mechanism can help in mitigating the impact of such disturbances on the model's forecasts
 613 by selectively focusing on the most relevant parts of the input sequence and down-weighting the influence
 614 of noise and irrelevant information.

615 **5. Scalability:** Attention mechanisms can scale well with large input sequences, as they allow the
 616 model to focus on the most relevant parts of the input sequence without the need to process the entire
 617 sequence in a fixed-size hidden state. This scalability can be particularly beneficial for renewable power
 618 generation forecasting problems, where the input data may consist of long sequences of historical power

619 generation measurements and environmental variables.

620 **6. Flexibility:** Attention mechanisms can be easily incorporated into various RNN architectures, such
621 as LSTM and GRU, providing flexibility in designing and adapting the forecasting model for different
622 renewable power generation scenarios and data characteristics.

623 An additional note needs to be made on attention mechanisms. The attained results suggest that
624 networks utilizing the attention mechanisms perform slightly worse than the basic RNN. This is likely
625 due to networks with attention layers having a deeper network architecture and thus require more training
626 epochs to improve performance.

627 6.2 Benefits of Time Series Decomposition and Integration

628 Incorporating time-series decomposition and integration into the Luong attention-based RNN model can
629 offer several benefits for renewable power generation forecasting:

630 **1. Improved Forecasting Accuracy:** By decomposing the time-series and accounting for its com-
631 ponents, the model can better capture the underlying patterns and dependencies in the data, potentially
632 leading to more accurate and reliable forecasts.

633 **2. Enhanced Model Interpretability:** Decomposition provides insights into the different components
634 of the time-series, making it easier to understand and interpret the model's predictions in terms of trend,
635 seasonality, and residual components.

636 **3. Robustness to Noise:** By separating the noise component from the trend and seasonal components,
637 the decomposition process can help in reducing the impact of noise and outliers on the model's forecasts,
638 making the model more robust to disturbances.

639 **4. Flexibility and Customizability:** Decomposition and integration techniques can be adapted and
640 fine-tuned to suit the specific characteristics and requirements of the renewable power generation data,
641 allowing for a more flexible and customizable forecasting approach.

642 **5. Improved Model Performance:** The integration of decomposed components into the RNN model
643 can help in better capturing the relationships between the components and the target variable, potentially
644 leading to improved model performance in terms of generalization and predictive accuracy.

645 6.3 Statistical analysis

646 When considering optimization problems, assessing models is an important topic. Understanding the
647 statistical significance of the introduced enhancements is crucial. Outcomes alone are not adequate to
648 state that one algorithm is superior to another one. Previous research suggests (Derrac et al., 2011)
649 that a statistical assessment should take place only after the methods being evaluated are adequately
650 sampled. This is done by ascertaining objective averages over several independent runs. Additionally,
651 samples need to originate from a normal distribution so as to avoid misleading conclusions. The use of
652 objective function averages is still for comparison of stochastic methods is still an open question among
653 researchers (Eftimov et al., 2017). To ascertain statistical significance of the observed outcomes the best
654 values over 30 independent executions of each metaheuristic have been used for creating the samples.
655 However, the safe use of parametric tests needed to be confirmed. For this, independence, normality,
656 and homoscedasticity of the data variances were considered as recommended by (LaTorre et al., 2021).
657 The independence criterion is fulfilled due to the fact that each run is initialized with an pseudo-random
658 number seed. However, the normality condition is not satisfied as the obtained samples do not stem
659 from a normal distribution as shown by the KED plots and proved by the Shapiro-Wilk test outcomes for
660 single-problem analysts (Shapiro and Francia, 1972). By performing the Shapiro-Wilk test, p -values are
661 generated for each method-problem combination, and these outcomes are presented in Table 13.

Table 13. Shapiro-Wilk scores for the single-problem analysis for testing normality condition

| Experiment | DDHHO | HHO | GA | PSO | ABC | FA | COLSHADE | SASS |
|-------------------|-------|-------|-------|-------|-------|-------|----------|-------|
| Solar VMD-RNN | 0.035 | 0.023 | 0.022 | 0.026 | 0.027 | 0.030 | 0.017 | 0.014 |
| Solar VMD-RNN-ATT | 0.035 | 0.032 | 0.037 | 0.019 | 0.022 | 0.025 | 0.037 | 0.033 |
| Wind VMD-RNN | 0.029 | 0.020 | 0.025 | 0.036 | 0.033 | 0.019 | 0.026 | 0.024 |
| Wind VMD-RNN-ATT | 0.021 | 0.028 | 0.025 | 0.037 | 0.035 | 0.024 | 0.026 | 0.041 |

662 The standard significance levels of $\alpha = 0.05$ and $\alpha = 0.1$ suggest that the null hypothesis (H_0) can
663 be refuted, which implies that none of the samples (for any problem-method combinations) are drawn

664 from a normal distribution. This indicates that the assumption of normality, which is necessary for the
 665 reliable use of parametric tests, was not satisfied, and therefore, it was deemed unnecessary to verify the
 666 homogeneity of variances.

667 As the requirements for the reliable application of parametric tests were not met, non-parametric
 668 tests were employed for the statistical analysis. Specifically, the Wilcoxon signed-rank test, which is
 669 a non-parametric statistical test (Taheri and Hesamian, 2013), was performed on the DDHHO method
 670 and all other techniques for all three problem instances (experiments). The same data samples used in
 671 the previous normality test (Shapiro-Wilk) were used for each method. The results of this analysis are
 672 presented in Table 14, where p -values greater than the significance level of $\alpha = 0.05$ are highlighted in
 673 bold.

Table 14. Wilcoxon signed-rank test findings

| DDHHO vs. others | HHO | GA | PSO | ABC | FA | COLSHADE | SASS |
|-------------------|-------|-------|-------|--------------|-------|----------|-------|
| Solar VMD-RNN | 0.035 | 0.046 | 0.036 | 0.062 | 0.043 | 0.029 | 0.040 |
| Solar VMD-RNN-ATT | 0.041 | 0.044 | 0.046 | 0.035 | 0.024 | 0.039 | 0.037 |
| Wind VMD-RNN | 0.024 | 0.043 | 0.039 | 0.052 | 0.045 | 0.044 | 0.038 |
| Wind VMD-RNN-ATT | 0.039 | 0.027 | 0.025 | 0.038 | 0.035 | 0.042 | 0.032 |

674 Table 14, which presents the p -values obtained from the Wilcoxon signed-rank test, demonstrate that,
 675 except for the ABC algorithm in the experiment where VMD-RNN was optimized and validated against
 676 solar and wind datasets, the proposed DDHHO method achieved significantly better performance than
 677 all other techniques in all three experiments. When compared with ABC, the calculated p – value was
 678 slightly above the 0.05 threshold (highlighted in bold in Table 14), suggesting that the DDHHO performed
 679 comparably to ABC. This was expected for the solar dataset, since the ABC in this simulation achieved
 680 moderately better mean value than the DDHHO, as demonstrated in Table 1.

681 The p -values for all other methods were lower than 0.05. Therefore, the DDHHO technique exhibited
 682 both robustness and effectiveness as an optimizer in these computationally intensive simulations. Based
 683 on the statistical analysis, it can be concluded that the DDHHO method outperformed most of the other
 684 metaheuristics investigated in all four experiments.

685 6.4 Best Model Interpretation and Feature Importance

686 SHAP (Lundberg and Lee, 2017) is a method that can be utilized to interpret the outputs of various
 687 AI models. Game theory provides a strong basis for SHAP. Though the use of SHAP the influence
 688 real-world factors have on model predictions can be determined. In order to determine the factors that
 689 play the highest role in energy production in solar and wind generation the best models with the highest
 690 performance output have been subjected to analysis. The outcomes for solar generation are shown in
 691 Figure 16, while wind generation is shown in Figure 17.

692 As demonstrated by Figure 16 a significant influence of previous solar generation instances can be
 693 observed. Cloud cover and humidity play a minor role in forecasting, with cloud cover decreasing the
 694 power produced by the photovoltaic cells.

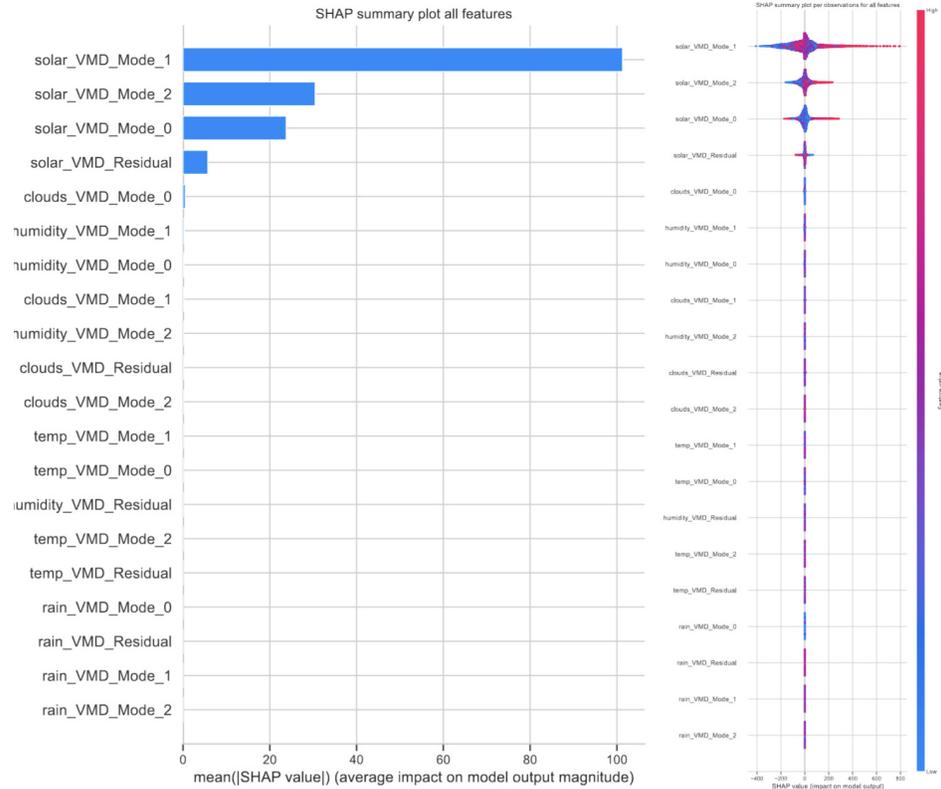


Figure 16. Feature impacts for the best performing RNN model for solar forecasting

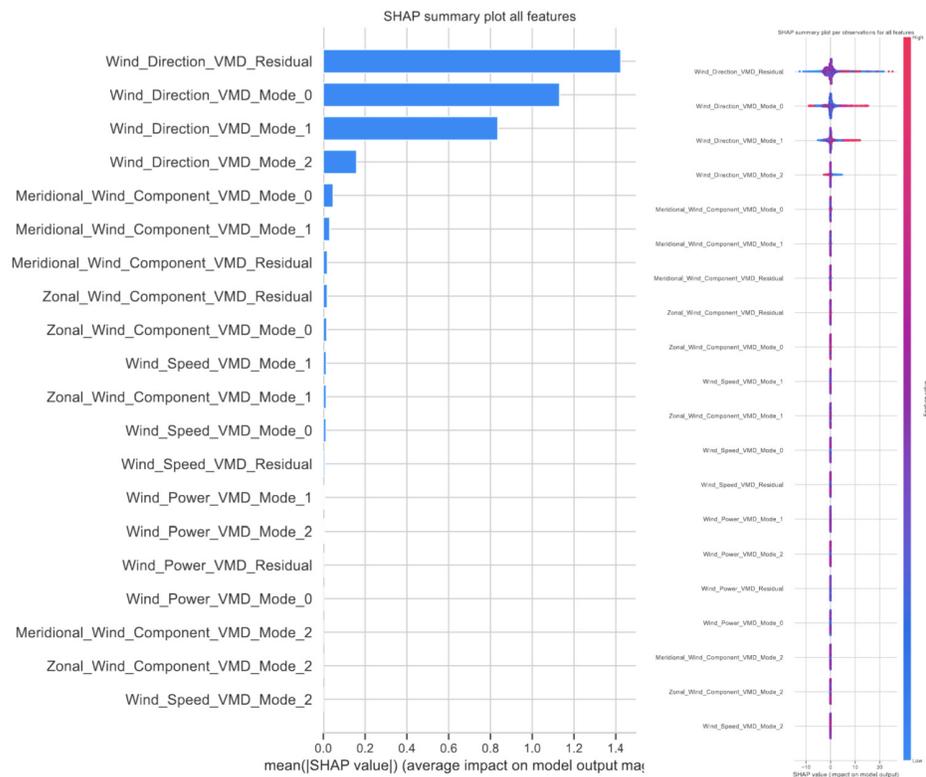


Figure 17. Feature impacts for the best performing RNN model for wind forecasting

695 Indicators from Figure 17 suggest that when forecasting wind power generation wind direction modes
696 have an important role. However, likely due to the sporadic nature of wind bursts wind generation residuals
697 have the highest impact on predictions. Finally, the meridional followed by zonal wind components play a
698 minor role in forecasting.

699 7 CONCLUSIONS

700 This study presents a novel attention-based recurrent neural network model for multistep ahead time-series
701 forecasting of renewable power generation, demonstrating improved forecasting accuracy on both Spain's
702 wind and solar energy datasets and China's wind farm dataset. The HHO algorithm is employed for
703 hyperparameter optimization, addressing the challenges posed by the large number of hyperparameters
704 in RNN-type networks. The attention model applied in the second group of experiments provides a
705 weighting system to the RNN, further enhancing the model's performance. The proposed approach has
706 the potential to significantly impact the transition towards a more sustainable future by addressing key
707 challenges related to the storage and management of renewable power generation.

708 As with any work this research has several limitations. Other methods exist for tackling time-series
709 forecasting and their potential remains yet to be explored. Further potential for improvement exist for the
710 HHO, as well as other metaheuristic algorithms yet to be applied to cloud forecasting. Additionally, other
711 approaches for interpreting feature influence exist such as through the analysis of n-Shapley Values.

712 Future research will focus on refining the HHO algorithm for hyperparameter optimization and
713 exploring additional decomposition methods to further improve the forecasting capabilities of the proposed
714 approach, as well as exploring additional metaheuristics applied to cloud load forecasting. Additionally,
715 further methods for feature impact interpretation will be explored.

716 REFERENCES

- 717 Abayomi-Alli, O. O., Sidekerskienė, T., Damaševičius, R., Siška, J., and Połap, D. (2020). *Empirical*
718 *Mode Decomposition Based Data Augmentation for Time Series Prediction Using NARX Network*,
719 volume 12415 LNAI of *Lecture Notes in Computer Science (including subseries Lecture Notes in*
720 *Artificial Intelligence and Lecture Notes in Bioinformatics)*.
- 721 Abuella, M. and Chowdhury, B. (2015). Solar power probabilistic forecasting by using multiple linear
722 regression analysis. In *SoutheastCon 2015*, pages 1–5. IEEE.
- 723 Akay, B., Karaboga, D., and Akay, R. (2022). A comprehensive survey on optimizing deep learning
724 models by metaheuristics. *Artificial Intelligence Review*, pages 1–66.
- 725 Al-Qaness, M. A., Ewees, A. A., Abualigah, L., AlRassas, A. M., Thanh, H. V., and Abd Elaziz, M. (2022).
726 Evaluating the applications of dendritic neuron model with metaheuristic optimization algorithms for
727 crude-oil-production forecasting. *Entropy*, 24(11):1674.
- 728 Ali, M. H., Jaber, M. M., Abd, S. K., Rehman, A., Awan, M. J., Vitkutė-Adžgauskienė, D., Damaševičius,
729 R., and Bahaj, S. A. (2022). Harris hawks sparse auto-encoder networks for automatic speech
730 recognition system. *Applied Sciences (Switzerland)*, 12(3).
- 731 Bacanin, N., Alhazmi, K., Zivkovic, M., Venkatachalam, K., Bezdán, T., and Nebhen, J. (2022a). Training
732 multi-layer perceptron with enhanced brain storm optimization metaheuristics. *Comput. Mater. Contin.*,
733 70:4199–4215.
- 734 Bacanin, N., Bezdán, T., Venkatachalam, K., Zivkovic, M., Strumberger, I., Abouhawwash, M., and
735 Ahmed, A. B. (2021). Artificial neural networks hidden unit and weight connection optimization by
736 quasi-reflection-based learning artificial bee colony algorithm. *IEEE Access*, 9:169135–169155.
- 737 Bacanin, N., Budimirovic, N., Venkatachalam, K., Jassim, H. S., Zivkovic, M., Askar, S., and
738 Abouhawwash, M. (2023a). Quasi-reflection learning arithmetic optimization algorithm firefly search
739 for feature selection. *Heliyon*, 9(4).
- 740 Bacanin, N., Jovanovic, L., Zivkovic, M., Kandasamy, V., Antonijevic, M., Deveci, M., and Strumberger,
741 I. (2023b). Multivariate energy forecasting via metaheuristic tuned long-short term memory and gated
742 recurrent unit neural networks. *Information Sciences*, page 119122.
- 743 Bacanin, N., Sarac, M., Budimirovic, N., Zivkovic, M., AlZubi, A. A., and Bashir, A. K. (2022b). Smart
744 wireless health care system using graph lstm pollution prediction and dragonfly node localization.
745 *Sustainable Computing: Informatics and Systems*, 35:100711.

- 746 Bacanin, N., Stoean, C., Zivkovic, M., Jovanovic, D., Antonijevic, M., and Mladenovic, D. (2022c).
747 Multi-swarm algorithm for extreme learning machine optimization. *Sensors*, 22(11):4204.
- 748 Bacanin, N., Stoean, C., Zivkovic, M., Rakic, M., Strulak-Wójcikiewicz, R., and Stoean, R. (2023c). On
749 the benefits of using metaheuristics in the hyperparameter tuning of deep learning models for energy
750 load forecasting. *Energies*, 16(3):1434.
- 751 Bacanin, N., Zivkovic, M., Bezdan, T., Venkatachalam, K., and Abouhawwash, M. (2022d). Modified fire-
752 fly algorithm for workflow scheduling in cloud-edge environment. *Neural computing and applications*,
753 34(11):9043–9068.
- 754 Bas, E., Egrioglu, E., and Kolemen, E. (2021). Training simple recurrent deep artificial neural network
755 for forecasting using particle swarm optimization. *Granul. Comput.* 7, page 411–420.
- 756 Basha, J., Bacanin, N., Vukobrat, N., Zivkovic, M., Venkatachalam, K., Hubálovský, S., and Trojovský,
757 P. (2021). Chaotic harris hawks optimization with quasi-reflection-based learning: An application to
758 enhance cnn design. *Sensors*, 21(19):6654.
- 759 Bezdan, T., Zivkovic, M., Bacanin, N., Chhabra, A., and Suresh, M. (2022). Feature selection by hybrid
760 brain storm optimization algorithm for covid-19 classification. *Journal of Computational Biology*,
761 29(6):515–529.
- 762 Boudraa, A.-O. and Cexus, J.-C. (2007). Emd-based signal filtering. *IEEE transactions on instrumentation*
763 *and measurement*, 56(6):2196–2202.
- 764 Budimirovic, N., Prabhu, E., Antonijevic, M., Zivkovic, M., Bacanin, N., Strumberger, I., and Venkat-
765 achalam, K. (2022). Covid-19 severity prediction using enhanced whale with salp swarm feature
766 classification. *Computers, Materials & Continua*, 72(1).
- 767 Çelik, E. (2023). Iegqo-aoa: information-exchanged gaussian arithmetic optimization algorithm with
768 quasi-opposition learning. *Knowledge-Based Systems*, 260:110169.
- 769 Cheng, S. and Shi, Y. (2011). Diversity control in particle swarm optimization. In *2011 IEEE Symposium*
770 *on Swarm Intelligence*, pages 1–9. IEEE.
- 771 Derrac, J., García, S., Molina, D., and Herrera, F. (2011). A practical tutorial on the use of nonparametric
772 statistical tests as a methodology for comparing evolutionary and swarm intelligence algorithms. *Swarm*
773 *and Evolutionary Computation*, 1(1):3–18.
- 774 Dobrojevic, M., Zivkovic, M., Chhabra, A., Sani, N. S., Bacanin, N., and Amin, M. M. (2023). Addressing
775 internet of things security by enhanced sine cosine metaheuristics tuned hybrid machine learning model
776 and results interpretation based on shap approach. *PeerJ Computer Science*, 9:e1405.
- 777 Dragomiretskiy, K. and Zosso, D. (2013). Variational mode decomposition. *IEEE transactions on signal*
778 *processing*, 62(3):531–544.
- 779 Drewil, G. I. and Al-Bahadili, R. J. (2022). Air pollution prediction using lstm deep learning and
780 metaheuristics algorithms. *Measurement: Sensors*, 24:100546.
- 781 Eftimov, T., Korošec, P., and Seljak, B. K. (2017). A novel approach to statistical comparison of meta-
782 heuristic stochastic optimization algorithms using deep statistics. *Information Sciences*, 417:186–215.
- 783 Foley, A. M., Leahy, P. G., Marvuglia, A., and McKeough, E. J. (2012). Current methods and advances in
784 forecasting of wind power generation. *Renewable energy*, 37(1):1–8.
- 785 Gao, T., Niu, D., Ji, Z., and Sun, L. (2022). Mid-term electricity demand forecasting using improved
786 variational mode decomposition and extreme learning machine optimized by sparrow search algorithm.
787 *Energy*, 261:125328.
- 788 Gupta, R. and Nalavade, J. E. (2022). Metaheuristic assisted hybrid classifier for bitcoin price prediction.
789 *Cybernetics and Systems*, pages 1–25.
- 790 Gurrola-Ramos, J., Hernández-Aguirre, A., and Dalmau-Cedeño, O. (2020). Colshade for real-world
791 single-objective constrained optimization problems. In *2020 IEEE congress on evolutionary computa-*
792 *tion (CEC)*, pages 1–8. IEEE.
- 793 Harvat, M. and Martín-Guerrero, J. D. (2022). Memory degradation induced by attention in recurrent
794 neural architectures. *Neurocomputing*, 502:161–176.
- 795 Heidari, A. A., Mirjalili, S., Faris, H., Aljarah, I., Mafarja, M., and Chen, H. (2019). Harris hawks
796 optimization: Algorithm and applications. *Future generation computer systems*, 97:849–872.
- 797 Huang, N. E., Shen, Z., Long, S. R., Wu, M. C., Shih, H. H., Zheng, Q., Yen, N.-C., Tung, C. C., and
798 Liu, H. H. (1998). The empirical mode decomposition and the hilbert spectrum for nonlinear and non-
799 stationary time series analysis. *Proceedings of the Royal Society of London. Series A: Mathematical,*
800 *Physical and Engineering Sciences*, 454(1971):903–995.

- 801 Jouhari, H., Lei, D., Al-qaness, M. A. A., Abd Elaziz, M., Damaševičius, R., Korytkowski, M., and Ewees,
802 A. A. (2020). Modified harris hawks optimizer for solving machine scheduling problems. *Symmetry*,
803 12(9).
- 804 Jovanovic, A., Dogandzic, T., Dobrojevic, M., Sarac, M., Bacanin, N., and Zivkovic, M. (2023a). Gold
805 prices forecasting using recurrent neural network with attention tuned by metaheuristics. In *2023 IEEE*
806 *World Conference on Applied Intelligence and Computing (AIC)*, pages 345–350. IEEE.
- 807 Jovanovic, L., Bacanin, N., Zivkovic, M., Antonijevic, M., Jovanovic, B., Sretenovic, M. B., and
808 Strumberger, I. (2023b). Machine learning tuning by diversity oriented firefly metaheuristics for
809 industry 4.0. *Expert Systems*, page e13293.
- 810 Jovanovic, L., Jovanovic, D., Antonijevic, M., Nikolic, B., Bacanin, N., Zivkovic, M., and Strumberger, I.
811 (2023c). Improving phishing website detection using a hybrid two-level framework for feature selection
812 and xgboost tuning. *Journal of Web Engineering*, 22(3):543–574.
- 813 Jovanovic, L., Jovanovic, D., Bacanin, N., Jovancai Stakic, A., Antonijevic, M., Magd, H., Thiru-
814 malaisamy, R., and Zivkovic, M. (2022). Multi-step crude oil price prediction based on lstm approach
815 tuned by salp swarm algorithm with disputation operator. *Sustainability*, 14(21):14616.
- 816 Jovanovic, L., Jovanovic, G., Perisic, M., Alimpic, F., Stanisic, S., Bacanin, N., Zivkovic, M., and Stojic,
817 A. (2023d). The explainable potential of coupling metaheuristics-optimized-xgboost and shap in
818 revealing vocs' environmental fate. *Atmosphere*, 14(1):109.
- 819 Karaboga, D. (2010). Artificial bee colony algorithm. *scholarpedia*, 5(3):6915.
- 820 Kennedy, J. and Eberhart, R. (1995). Particle swarm optimization. In *Proceedings of ICNN'95-*
821 *international conference on neural networks*, volume 4, pages 1942–1948. IEEE.
- 822 Kiani, F., Seyyedabbasi, A., Nematzadeh, S., Candan, F., Çevik, T., Anka, F. A., Randazzo, G., Lanza, S.,
823 and Muzirafuti, A. (2022). Adaptive metaheuristic-based methods for autonomous robot path planning:
824 sustainable agricultural applications. *Applied Sciences*, 12(3):943.
- 825 LaTorre, A., Molina, D., Osaba, E., Poyatos, J., Del Ser, J., and Herrera, F. (2021). A prescription of
826 methodological guidelines for comparing bio-inspired optimization algorithms. *Swarm and Evolution-*
827 *ary Computation*, 67:100973.
- 828 Lei, F., Senyurek, V., Kurum, M., Gurbuz, A. C., Boyd, D., Moorhead, R., Crow, W. T., and Eroglu, O.
829 (2022). Quasi-global machine learning-based soil moisture estimates at high spatio-temporal scales
830 using cygnss and smap observations. *Remote Sensing of Environment*, 276:113041.
- 831 Liu, T., Ma, X., Li, S., Li, X., and Zhang, C. (2022). A stock price prediction method based on
832 meta-learning and variational mode decomposition. *Knowledge-Based Systems*, 252:109324.
- 833 Loe, C. (2022). Energy transition will move slowly over the next decade.
- 834 Lundberg, S. M. and Lee, S.-I. (2017). A unified approach to interpreting model predictions. In Guyon,
835 I., Luxburg, U. V., Bengio, S., Wallach, H., Fergus, R., Vishwanathan, S., and Garnett, R., editors,
836 *Advances in Neural Information Processing Systems 30*, pages 4765–4774. Curran Associates, Inc.
- 837 Luong, M.-T., Pham, H., and Manning, C. D. (2015). Effective approaches to attention-based neural
838 machine translation. *arXiv preprint arXiv:1508.04025*.
- 839 Medsker, L. and Jain, L. C. (1999). *Recurrent neural networks: design and applications*. CRC press.
- 840 Milicevic, M., Jovanovic, L., Bacanin, N., Zivkovic, M., Jovanovic, D., Antonijevic, M., Savanovic,
841 N., and Strumberger, I. (2023). Optimizing long short-term memory by improved teacher learning-
842 based optimization for ethereum price forecasting. In *Mobile Computing and Sustainable Informatics:*
843 *Proceedings of ICMCSI 2023*, pages 125–139. Springer.
- 844 Mirjalili, S. and Mirjalili, S. (2019). Genetic algorithm. *Evolutionary Algorithms and Neural Networks:*
845 *Theory and Applications*, pages 43–55.
- 846 Mirmohseni, S. M., Tang, C., and Javadpour, A. (2022). Fpso-ga: a fuzzy metaheuristic load balancing
847 algorithm to reduce energy consumption in cloud networks. *Wireless Personal Communications*,
848 127(4):2799–2821.
- 849 Murariu, M.-G., Dorobanțu, F.-R., and Târniceriu, D. (2023). A novel automated empirical mode
850 decomposition (emd) based method and spectral feature extraction for epilepsy eeg signals classification.
851 *Electronics*, 12(9):1958.
- 852 Nama, S. (2022). A novel improved sma with quasi reflection operator: Performance analysis, appli-
853 cation to the image segmentation problem of covid-19 chest x-ray images. *Applied Soft Computing*,
854 118:108483.
- 855 Nematzadeh, S., Kiani, F., Torkamanian-Afshar, M., and Aydin, N. (2022). Tuning hyperparameters of

- 856 machine learning algorithms and deep neural networks using metaheuristics: A bioinformatics study
857 on biomedical and biological cases. *Computational biology and chemistry*, 97:107619.
- 858 Olah, C. and Carter, S. (2016). Attention and augmented recurrent neural networks. *Distill*, 1(9):e1.
- 859 Para, J., Del Ser, J., and Nebro, A. J. (2022). Energy-aware multi-objective job shop scheduling
860 optimization with metaheuristics in manufacturing industries: a critical survey, results, and perspectives.
861 *Applied Sciences*, 12(3):1491.
- 862 Pascanu, R., Mikolov, T., and Bengio, Y. (2013). On the difficulty of training recurrent neural networks.
863 In Dasgupta, S. and McAllester, D., editors, *Proceedings of the 30th International Conference on*
864 *Machine Learning*, volume 28 of *Proceedings of Machine Learning Research*, pages 1310–1318,
865 Atlanta, Georgia, USA. PMLR.
- 866 Petrovic, A., Jovanovic, L., Zivkovic, M., Bacanin, N., Budimirovic, N., and Marjanovic, M. (2023).
867 Forecasting bitcoin price by tuned long short term memory model. In *1st International Conference on*
868 *Innovation in Information Technology and Business (ICIITB 2022)*, pages 187–202. Atlantis Press.
- 869 Raffel, C., Luong, M.-T., Liu, P. J., Weiss, R. J., and Eck, D. (2017). Online and linear-time attention by
870 enforcing monotonic alignments. In *International conference on machine learning*, pages 2837–2846.
871 PMLR.
- 872 Savanović, N., Toskovic, A., Petrovic, A., Zivkovic, M., Damaševičius, R., Jovanovic, L., Bacanin, N., and
873 Nikolic, B. (2023). Intrusion detection in healthcare 4.0 internet of things systems via metaheuristics
874 optimized machine learning. *Sustainability*, 15(16):12563.
- 875 Shapiro, S. S. and Francia, R. (1972). An approximate analysis of variance test for normality. *Journal of*
876 *the American statistical Association*, 67(337):215–216.
- 877 Stankovic, M., Gavrilovic, J., Jovanovic, D., Zivkovic, M., Antonijevic, M., Bacanin, N., and Stankovic, M.
878 (2022a). Tuning multi-layer perceptron by hybridized arithmetic optimization algorithm for healthcare
879 4.0. *Procedia Computer Science*, 215:51–60.
- 880 Stankovic, M., Jovanovic, L., Bacanin, N., Zivkovic, M., Antonijevic, M., and Bisevac, P. (2022b). Tuned
881 long short-term memory model for ethereum price forecasting through an arithmetic optimization
882 algorithm. In *International Conference on Innovations in Bio-Inspired Computing and Applications*,
883 pages 327–337. Springer.
- 884 Stoean, C., Zivkovic, M., Bozovic, A., Bacanin, N., Strulak-Wójcikiewicz, R., Antonijevic, M., and
885 Stoean, R. (2023). Metaheuristic-based hyperparameter tuning for recurrent deep learning: Application
886 to the prediction of solar energy generation. *Axioms*, 12(3):266.
- 887 Taheri, S. and Hesamian, G. (2013). A generalization of the wilcoxon signed-rank test and its applications.
888 *Statistical Papers*, 54(2):457.
- 889 Tang, Y. and Gibali, A. (2020). New self-adaptive step size algorithms for solving split variational
890 inclusion problems and its applications. *Numerical Algorithms*, 83(1):305–331.
- 891 Tayebi, M. and El Kafhali, S. (2022). Performance analysis of metaheuristics based hyperparameters
892 optimization for fraud transactions detection. *Evolutionary Intelligence*, pages 1–19.
- 893 Thakur, A. and Goraya, M. S. (2022). Rafl: A hybrid metaheuristic based resource allocation framework
894 for load balancing in cloud computing environment. *Simulation Modelling Practice and Theory*,
895 116:102485.
- 896 Wolpert, D. H. and Macready, W. G. (1997). No free lunch theorems for optimization. *IEEE transactions*
897 *on evolutionary computation*, 1(1):67–82.
- 898 Wu, Z. and Huang, N. E. (2009). Ensemble empirical mode decomposition: a noise-assisted data analysis
899 method. *Advances in adaptive data analysis*, 1(01):1–41.
- 900 Xue, H. (2022). A quasi-reflection based sc-pso for ship path planning with grounding avoidance. *Ocean*
901 *Engineering*, 247:110772.
- 902 Yang, X.-S. and He, X. (2013). Firefly algorithm: recent advances and applications. *International journal*
903 *of swarm intelligence*, 1(1):36–50.
- 904 Yang, X.-S. and Slowik, A. (2020). Firefly algorithm. In *Swarm intelligence algorithms*, pages 163–174.
905 CRC Press.
- 906 Zhang, C., Peng, T., and Nazir, M. S. (2022). A novel integrated photovoltaic power forecasting model
907 based on variational mode decomposition and cnn-bigru considering meteorological variables. *Electric*
908 *Power Systems Research*, 213:108796.
- 909 Zhang, Y. and Zhao, M. (2023). Cloud-based in-situ battery life prediction and classification using
910 machine learning. *Energy Storage Materials*.

- 911 Zhao, J., Zhang, B., Guo, X., Qi, L., and Li, Z. (2022). Self-adapting spherical search algorithm with
912 differential evolution for global optimization. *Mathematics*, 10(23):4519.
- 913 Zivkovic, M., Bacanin, N., Antonijevic, M., Nikolic, B., Kvascev, G., Marjanovic, M., and Savanovic,
914 N. (2022a). Hybrid cnn and xgboost model tuned by modified arithmetic optimization algorithm for
915 covid-19 early diagnostics from x-ray images. *Electronics*, 11(22):3798.
- 916 Zivkovic, M., Bezdán, T., Strumberger, I., Bacanin, N., and Venkatachalam, K. (2021). Improved harris
917 hawks optimization algorithm for workflow scheduling challenge in cloud-edge environment. In
918 *Computer Networks, Big Data and IoT: Proceedings of ICCBI 2020*, pages 87–102. Springer.
- 919 Zivkovic, M., Petrovic, A., Venkatachalam, K., Strumberger, I., Jassim, H. S., and Bacanin, N. (2022b).
920 Novel chaotic best firefly algorithm: Covid-19 fake news detection application. In *Advances in Swarm
921 Intelligence: Variations and Adaptations for Optimization Problems*, pages 285–305. Springer.
- 922 Zivkovic, M., Tair, M., Venkatachalam, K., Bacanin, N., Hubálovský, Š., and Trojovský, P. (2022c). Novel
923 hybrid firefly algorithm: An application to enhance xgboost tuning for intrusion detection classification.
924 *PeerJ Computer Science*, 8:e956.