Forecasting stock indices with the Covid-19 infection rate as an exogenous variable

Mohammad S Patwary [1] , **Kumer P. Das** Corresp. [2]

1 Mathematical Sciences, Butler University, Indianapolis, IN, United States

2 Research, Innovation, and Economic Development, University of Louisiana at Lafayette, Lafayette, Louisiana, United States

Corresponding Author: Kumer P. Das
Email address: kumer.das@louisiana.edu

Forecasting stock market indices is challenging because stock prices are usually nonlinear and non- stationary. Covid-19 has had a significant impact on stock market volatility, which makes forecasting more challenging. Since the number of confirmed cases significantly impacted the stock price index; hence, it has been considered a covariate in this analysis. The primary focus of this study is to address the challenge of forecasting volatile stock indices during Covid-19 by employing time series analysis. In particular, the goal is to find the best method to predict future stock price indices in relation to the number of Covid-19 infection rates. In this study, the effect of covariates has been analyzed for three stock indices: S & P 500, Morgan Stanley Capital International (MSCI) World stock index, and Chicago Board Options Exchange (CBOE) Volatility Index (VIX). Results show that parametric approaches can be good forecasting models for the S & P 500 index and the VIX index. On the other hand, a random walk model can be adopted to forecast the MSCI index. Moreover, among the three random walk forecasting methods for the MSCI index, the naïve method provides the best forecasting model.

Forecasting Stock Indices with the Covid-19 Infection Rate as an Exogenous Variable

Mohammad Shaha A. Patwary[1] **and Kumer P. Das**[2]

[1]**Assistant Professor, Department of Mathematical Sciences, Butler University, 4600 Sunset Ave, Indianapolis, Indiana 46028, USA.**
[2]**Assistant Vice President for Research, Innovation and Economic Development and Assistant Provost, University of Louisiana at Lafayette, 537 Cajundome Blvd, Lafayette, Louisiana 70506, USA.**

Corresponding author:
Kumer P. Das[2]

Email address: kumer.das@louisiana.edu

ABSTRACT

Forecasting stock market indices is challenging because stock prices are usually nonlinear and non-stationary. Covid-19 has had a significant impact on stock market volatility, which makes forecasting more challenging. Since the number of confirmed cases significantly impacted the stock price index; hence, it has been considered a covariate in this analysis. The primary focus of this study is to address the challenge of forecasting volatile stock indices during Covid-19 by employing time series analysis. In particular, the goal is to find the best method to predict future stock price indices in relation to the number of Covid-19 infection rates. In this study, the effect of covariates has been analyzed for three stock indices: S & P 500, Morgan Stanley Capital International (MSCI) World stock index, and Chicago Board Options Exchange (CBOE) Volatility Index (VIX). Results show that parametric approaches can be good forecasting models for the S & P 500 index and the VIX index. On the other hand, a random walk model can be adopted to forecast the MSCI index. Moreover, among the three random walk forecasting methods for the MSCI index, the naïve method provides the best forecasting model.

1 INTRODUCTION

The world has struggled and passed through one or more pandemics almost every century. All pandemics affect the world and make it vulnerable to all extents, including but not limited to the health, social, and economic system. In the past 100 years and its vicinity, the world has been affected by the pandemics such as the Spanish flu in 1918, the Asian flu in 1957, the Hong Kong flu in 1968, and the Swine flu in 2009. World equity markets have experienced a turbulent trade recently as investors keep watch of a deadly viral outbreak of SARS-CoV-2 (Covid-19). The virus has affected over 210 countries and territories worldwide and two international conveyances. It has stopped the world and its economy. Massacres in the health care system have impacted cross-border relationships by locking down countries, further slowing the economy. Increasing fears over the continued spread of Covid-19 have led to aberrant behaviors in the stock market (see Figure 1), broadly impacting the global economy. The reaction to the virus spread is quite dominating as the recent fall in the oil price and stock composite indices around the world. Baker et al. (2020) have identified the Covid-19 pandemic as having the most significant impact on stock market volatility in the history of pandemics. After the shock, markets are tending to stabilize in recent days. According to economists and financial analysts, expecting a quick recovery from this volatile economic situation would be unrealistic. Economic and financial experts say the world economy will have to deal with Covid-19 for many years.

The statistical analysis of the stock market index is critically important to explore the impact of confirmed cases of Covid-19 on the overall stock price index. Dey and Das (2022) provided an analysis of the effect of the Covid-19 outbreak on the crude oil price. A very recent analysis revealed the volatility spillovers and co-movements among energy-producing, extracting, and transporting corporations' stock prices and

47 evaluate how the Covid-19 pandemic creates negative WTI oil prices (Corbet et al., 2020). A recent study
48 by Dey et al. (2021) showed that Covid-19 cases and deaths, their local spread, and Google searches
49 impact abnormal stock prices between January 2020 to May 2020. Understanding the market performance
50 during the onset of deadly infectious diseases is important for many reasons.

51

52 Moreover, the Covid-19 pandemic has caused significant economic disruption, with stock markets world-
53 wide experiencing sharp declines and volatility. The pandemic has created a new challenge for stock
54 market forecasting models, as the infection rate and associated public health measures have become
55 critical exogenous variables affecting market behavior. Gupta et al. (2020) used a vector autoregressive
56 (VAR) model to examine the impact of Covid-19 on the stock market in India. They found that the
57 infection rate was a significant predictor of stock market returns, with negative effects on both short- and
58 long-term returns. The authors suggested that incorporating the infection rate into forecasting models
59 could improve accuracy. Another recent study by Peng et al. (2021) used a hybrid model combining
60 wavelet transform and artificial intelligence techniques to forecast the Shanghai Composite Index during
61 the Covid-19 pandemic. The infection rate was included as an exogenous variable in the model, and the
62 authors found that it had a significant impact on stock market returns. The authors concluded that the
63 hybrid model outperformed traditional models in forecasting accuracy. A similar study used a machine
64 learning-based model to predict the stock market index in Taiwan during the Covid-19 pandemic (Huang
65 et al., 2020). The authors included the infection rate and other exogenous variables in the model and found
66 that they significantly improved forecasting accuracy. They suggested that including the infection rate in
67 stock market forecasting models could help investors better understand the impact of the pandemic on
68 the market. Zaremba and Kizys (2021) used wavelet coherence analysis to study the impact of Covid-19
69 on the US stock market and found evidence of significant linkages between the two. Similarly, Chen
70 et al. (2020) used the Generalized AutoRegressive Conditional Heteroskedasticity (GARCH) model to
71 analyze the volatility of the US stock market during the pandemic and found that the volatility increased
72 significantly.

73

74 Furthermore, several other studies have also investigated the impact of the Covid-19 pandemic on the
75 stock market using different modeling techniques. For example, Ozer et al. (2021) used daily stock prices
76 and technical indicators data from 2015 to 2020, which includes both the pre-Covid-19 period and the
77 Covid-19 period, to train and test the models. The results show that both Random Forest (RF) and Deep
78 Neural Network (DNN) models provide promising results in terms of forecasting accuracy and that the
79 DNN model outperforms the RF model in terms of forecasting performance during the Covid-19 period.
80 Similarly, another study used the ARIMA model to forecast the Karachi Stock Exchange (KSE) index
81 during the pandemic period and found that the model accurately predicted the trend in the index (Hasan
82 et al., 2021). Besides, Al-Awadhi et al. (2021) used the Bayesian structural time series (BSTS) model to
83 forecast the Kuwait Stock Exchange (KSE) index during the pandemic period. They found that the model
84 provided accurate forecasts.Zaremba et al. (2020) have focused on understanding the impact of Covid-19
85 on the US stock market volatility. None of these studies has focused on time series analysis to forecast
86 stock indexes. Moreover, even though several studies have focused on a specific country's stock index, no
87 attempt has been made to study world stock index, such as MSCI.

88

89 Thus, our primary focus is to employ time series analysis to predict future stock price indices concerning
90 Covid-19 infection rates. We believe that the number of confirmed cases significantly impacts the stock
91 index, and hence it will be considered a covariate in our analysis. In this research, the effect of covariates
92 will be analyzed for S & P 500 stock Index data, MSCI World stock Index data, and CBOE volatility index
93 (VIX) data. The description and details of the data are given the Section 2. The data will be divided into a
94 training set to train our model and a validation set to validate our model to see the model's performance on
95 the test set. Finally, we will provide a prediction interval for the stock price index. The rest of the article
96 is organized into four sections. Section 2 describes the data sets used in this study, Section 3 discusses the
97 methods used, Section 4 checks stationarity assumptions, and we conclude with results and discussion in
98 Section 5.

99

Figure 1. World epidemics and global stock market performance

2 DATA DESCRIPTION

In this study, we have considered the weekly average of Covid-19 infection data for the USA and 23 MSCI Countries, including Hong Kong. The number of individuals infected from December 31, 2019, to February 12, 2021, has been included. December 31 has been chosen because the World Health Organization has confirmed and declared Covid-19 cases on this date. But, in the USA first Covid-19 case was reported on January 21, 2020, and in the MSCI countries, the first Covid-19 case was reported on January 15, 2020. Therefore, for the USA, we have 56 weeks of data. Among these, we have used the first 47 weeks (January 21, 2020 - December 11, 2020) data to train our model and the last nine weeks' data (December 12, 2020 - February 12, 2021) to validate our model. The Covid-19 confirmed cases in the USA and twenty-three MSCI countries are displayed in Figure 2. In this research, the following three stock indices have been considered.

2.1 S & P 500 Index:

The S & P 500 index measures the stock performance of 500 large companies listed on stock exchanges in the United States. Many consider it one of the best representations of the U.S. stock market. S & P 500 weekly index data from January 21, 2020, to February 12, 2021, has been analyzed in this study. We have considered weekly indices for the first 47 weeks (January 21, 2020 - December 11, 2020) to train the model and weekly indices for the last nine weeks (December 12, 2020 - February 12, 2021) to validate the trained model. The visualization of the training dataset for S & P 500 index is provided in panel (a) of Figure 3, and summary statistics of this dataset are presented in Table 1. It has been observed that the sample range ($Y_{max} - Y_{min}$) and interquartile range ($Q_3 - Q_1$) are higher as compared to the pre-Covid time.

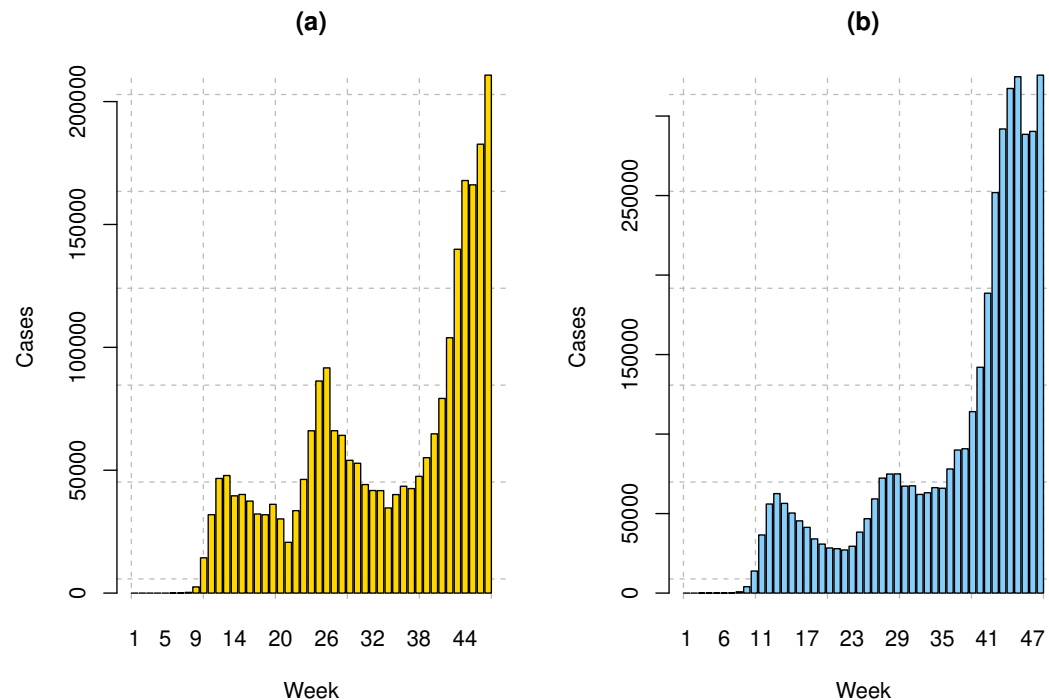



Figure 2. Covid-19 Weekly Confirmed Cases in the (a) USA and (b) Twenty-three MSCI Countries

2.2 MSCI World Index:

The MSCI World Index is a market-cap-weighted stock market index of 1,643 stocks from companies across 23 developed countries worldwide. The U.S., Canada, 15 European Countries, Australia, New Zealand, Israel, Japan, Hong Kong, and Singapore are included in this index. The index covers approximately 85% of each country's free float-adjusted market capitalization. This common benchmark for global stock funds is intended to represent a broad cross-section of global markets and is maintained by MSCI, formerly Morgan Stanley Capital International. The Weekly MSCI index data from January 15, 2020, to February 12, 2020, has been considered for this study. The MSCI indices for the first 48 weeks (January 15, 2020 - December 11, 2020) have been considered training sets, and the indices for the last nine weeks (December 12, 2020 - February 12, 2021) have been considered as the validation set. Like S & P 500, the visualization of the training dataset for the MSCI world index is provided in panel (b) of Figure 3, and summary statistics of this dataset are presented in Table 1. Similarly, as S & P 500 index, it is not surprising to observe that the sample range and interquartile range for the MSCI index are also higher compared to the normal time.

2.3 CBOE Volatility Index (VIX):

The Chicago Board Options Exchange (CBOE) volatility index is a popular measure of the stock market's expectation of volatility based on S & P 500 index options. The VIX is often referred to as the fear index or fear gauge and is calculated and disseminated on a real-time basis by the CBOE. Portfolio managers and investors use the VIX to measure the level of risk, fear, or stress in the market when making investment decisions. The VIX index values move up when the market is falling. The reverse is true when the market advances. The data from January 21, 2020, to February 12, 2021, have been included in this study. The weekly VIX data from January 21, 2020, to December 11, 2020 (47 weeks) comprise the training set, and from December 12, 2020, to February 12, 2021, (9 weeks) include the validation set. Following the previous two indices, the visualization of the training dataset for VIX is provided in panel (c) of Figure 3, and summary statistics of this dataset are presented in Table 1. Trending with the previous two indices, it has been found that the sample range and interquartile range are higher compared to the normal time, but peaks and valleys in the data are more fluctuated than the previous two indices.

148   Moreover, to compare the spread of the three datasets, we compute the coefficient of variation (CV)
149    $\left(= \frac{SD}{\bar{Y}} \times 100\% \right)$. We have found that the CVs for S & P 500, VIX, and MSCI are 9.72, 39.72, and 9.90
150   percent, respectively. These results indicate that VIX data has the highest spread from its sample mean,
151   while that of S & P 500 has the least. Additionally, the last column of Table 1 presents the measures
152   of kurtosis (γ) for the three aforementioned datasets. Kurtosis is a measure of whether or not a data
153   distribution is heavy- or light-tailed relative to a normal distribution. The measure of kurtosis for a normal
154   distribution is 3. Since the values of kurtosis are very close to 3 (2.94 and 3.05) for S & P 500 and MSCI,
155   these two datasets seem to be normally distributed without having many outliers or extreme observations
156   as compared to the normal distribution. In contrast, the kurtosis measure for the VIX dataset is around
157   6.5 which indicates the data distribution is leptokurtic, which means the data is prone to produce more
158   outliers or extreme observations than the normal distribution.

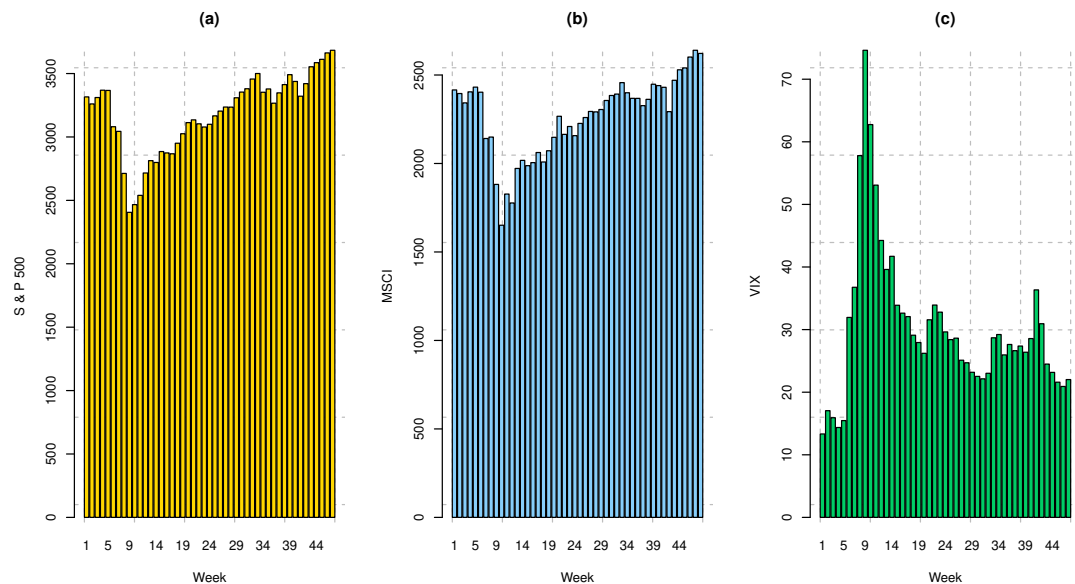



Figure 3. Weekly Price Index for (a) S & P 500; (b) MSCI; and (c) VIX

Data	n	Y_{min}	Q_1	Q_2	$\bar{Y}$	SD	Q_3	Y_{max}	γ
S & P 500	47	2406	3035	3260	3185	309.55	3379	3683	2.94
VIX	47	13.32	23.17	28.40	30.34	12.05	32.70	74.62	6.49
MSCI	48	1651	2146	2316	2264	224.22	2407	2640	3.05

Table 1. Summary Statistics (Sample Size, Minimum, First Quartile, Median, Mean, Standard Deviation, Third Quartile, Maximum, and Kurtosis) of S & P 500, VIX, and MSCI

3 METHODOLOGY

3.1 Parametric Forecasting Methods

161   In the time series analysis, autoregressive moving average (ARMA) models were first introduced by Whit-
162   tle (1951) and improved later by Whittle (1963) and Whittle (1983) to provide a parsimonious description
163   of a stationary stochastic process in terms of two lower-order polynomials, one for the autoregressive
164   (AR) part and the other for the moving average (MA) part (Hannan, 1988). But the models are also known
165   as Box-Jenkins models (Box and Genkins, 1970) after the names of Box and Jenkins, who popularized
166   the models. For a given time series, the ARMA model is one of the variants of Box-Jenkins model class
167   which is a potent tool for understanding and predicting the future value of that series.
168

If the model includes AR terms of order p and MA terms of order q then the overall model is referred to as ARMA(p,q). Formally, the process $\{Y_t, t = 0, \pm 1, \pm 2, \ldots\}$ is said to be an ARMA(p,q) process if $\{Y_t\}$ is stationary and if for every t (Brockwell and Davis, 2009),

$$Y_t = \sum_{i=1}^{p} \phi_i Y_{t-i} + Z_t + \sum_{i=1}^{q} \theta_i Z_{t-i} \tag{1}$$

where $\phi_1, \phi_2, \ldots, \phi_p, \theta_1, \theta_2, \ldots, \theta_q$ are parameters, and $Z_t, Z_{t-1}, \ldots, Z_{t-q}$ are white noise error terms which follow $\{Z_t\} \sim WN(0, \gamma(h))$, where $\gamma(h) = \begin{cases} \sigma^2 & \text{if } h = 0 \\ 0 & \text{if } h \neq 0. \end{cases}$

Equation 1 can be written in a more compact form using a backward shift operator as follows:

$$Y_t - \sum_{i=1}^{p} \phi_i Y_{t-i} = Z_t + \sum_{i=1}^{q} \theta_i Z_{t-i} \implies \phi(B) Y_t = \theta(B) Z_t, \qquad \forall t \tag{2}$$

where ϕ and θ are the pth and qth degree autoregressive and moving average polynomials, respectively in the above difference equations and are given by

$$\phi(x) = 1 - \phi_1 x - \phi_2 x^2 - \ldots - \phi_p x^p,$$

$$\theta(x) = 1 + \theta_1 x + \theta_2 x^2 + \ldots + \theta_q x^q$$

and B is the backward shift or lag operator defined as

$$B_j Y_t = Y_{t-j}, \quad j = 0, \pm 1, \pm 2, \ldots \ldots$$

Clearly, if $\theta(x) \equiv 1$ in Equation 2, then the process

$$\phi(B) Y_t = Z_t, \qquad \forall t$$

is known as AR process of order p and is symbolically denoted by AR(p). Furthermore, if $\phi(x) \equiv 1$ in Equation 2, then the process

$$Y_t = \theta(B) Z_t, \qquad \forall t$$

is known as MA process of order q and is denoted by MA(q).

ARMA models can be estimated by using the Box–Jenkins methodology, which is further divided into three major components.

- Identification: Identifying orders p and q for ARMA (p,q)

- Estimation: Estimating model parameters ϕs, θs, and σ^2.

- Diagnostics: Checking for overfitting and verifying the model assumptions using residual.

Since we wish to include covariate(s) in our analysis, we must incorporate the independent variables in ARMA(p,q) model defined in Equation 1. However, these models are uncommon and are known as autoregressive–moving-average with exogenous inputs model (ARMAX model). ARMAX model with p autoregressive terms, q moving average terms, and r exogenous inputs terms is referred to as ARMAX(p,q,r), which contains the AR(p), MA(q), and a linear combination of r terms of known and external time series X_t. Thus, an ARMAX(p,q,r) is given by (Brockwell and Davis, 2009)

$$Y_t = \sum_{i=1}^{p} \phi_i Y_{t-i} + Z_t + \sum_{i=1}^{q} \theta_i Z_{t-i} + \sum_{i=1}^{r} \beta_i X_{t-i} \tag{3}$$

where $\beta_1, \beta_2, \ldots, \beta_r$ are the parameters of exogenous input X_t.

3.2 Random Walk Forecasting Methods

The theory of random walks usually raises many challenging questions primarily because many "technical analysts" and "chartists" ask whether the random walk theory accurately describes reality. Indeed, the random walk approach is radically different from market analysis and starts from the premise that the stock exchanges are examples of efficient markets. In an efficient market, at any point in time, the actual price of a stock will be a reasonable estimate of its intrinsic value. The theory of random walk states that a series of stock price changes have no memory- the series' history can not be used to predict the future meaningfully. The future path of the price level is no more predictable than the path of a series of cumulated random numbers (Fama, 1970).

3.2.1 Average method

The forecasts of all future values are equal to the average (or "mean") of the data at hand. If we let the existing data be denoted by $Y_1, Y_2, \ldots, Y_T$, then for forecast horizon h, forecasts for Y_{T+h} are given by

$$\hat{Y}_{T+h|T} = \frac{\sum_{t=1}^{T} Y_t}{T} = \bar{Y}, \quad h \in \mathbb{Z} \tag{4}$$

Here, h is an integer such that $h \geq 1$.

3.2.2 Naïve method

In the Naïve forecast, for any forecast horizon h, the forecast value will be the last observed value in the series.

$$\hat{Y}_{T+h|T} = Y_T, \quad h \in \mathbb{Z} \tag{5}$$

This method dominates other methods in many situations in economic and financial time series. Since the forecast from Naïve approach is optimal when data follow a random walk, this method is also known as the random walk forecast method.

3.2.3 Drift method

An alternative to the naïve method is to allow the forecasts to increase or decrease over time, where the amount of change over time (also known as drift) is set to be the average change in the data at hand. Thus, the forecast for horizon h is $\hat{Y}_{T+h|T}$ and is given by:

$$\hat{Y}_{T+h|T} = Y_T + \frac{h}{T-1} \sum_{t=2}^{T} (Y_t - Y_{t-1}) = Y_T + h \left(\frac{Y_T - Y_1}{T-1} \right) \tag{6}$$

This method is equivalent to drawing a line between the first and last observations in the series and extrapolating it into the future.

3.3 Tests for Stationarity

It is important to check the stationarity of a series before fitting it to a model. In other words, it needs to be determined whether the time series is constant in mean and variance. We employ a couple of methods to check stationarity, as outlined below.

3.3.1 Autocorrelation Function (ACF)

The ACF (Autocorrelation Function) test is a statistical method used to determine the presence of autocorrelation in a time series data set. It measures the correlation between a series and its lags, i.e., the correlation between the data points separated by a given lag interval (Venables and Ripley, 2002). The mathematical formula for ACF is as follows:

$$ACF(l) = \frac{1}{n} \sum_{t=1}^{n} \frac{(Y_t - \bar{Y})(Y_{t-l} - \bar{Y})}{S^2}$$

where l is the lag interval; n is the number of observations in the time series; Y_t is the value of the time series at time t; $\bar{Y}$ is the mean of the time series; and S^2 is the variance of the time series.

217 The ACF test is used to determine whether a time series is stationary or not. If the autocorrelation is zero
218 or close to zero, the time series is stationary, and the ACF plot will resemble white noise. However, if
219 the autocorrelation is high, then the time series is non-stationary, and the ACF plot will show a pattern
220 of spikes or waves (Box et al., 2015; Brockwell and Davis, 2002). The ACF test is widely used in
221 econometrics, finance, and other fields to analyze time series data. It is a valuable tool for detecting trends,
222 seasonal patterns, and other types of time series behavior (Box et al., 2015).

223 *3.3.2 The Ljung-Box Test*

The Ljung-Box test is a standard method for model selection and is often used in time series analysis. The
Ljung-Box test examines whether there is significant evidence for non-zero correlations at given lags,
with the null hypothesis of independence or stationarity in a given time series (Harvey, 1993; Ljung and
Box, 1978; Box and Pierce, 1970; Brockwell and Davis, 2002). The Ljung-Box test statistic is calculated
as follows:

$$Q(k) = n(n+2) \sum_l \frac{r_l^2}{n-l}$$

224 where n is the sample size, k is the number of lags to consider, r_l is the ACF at lag l, and $Q(k)$ is the test
225 statistic which follows chi-squared distribution with k degrees of freedom.
226 A low p-value (e.g. $p < 0.10$ or 0.05) will indicate the non-stationarity of the series.

227 *3.3.3 Augmented Dickey–Fuller(ADF) Test*

Another common and familiar statistical method for stationarity in time series literature is the Augmented
Dickey–Fuller (ADF) test used to test for the presence of a unit root in time series data (Banerjee et al.,
1993; Said and Dickey, 1984). A unit root is a feature of a time series that indicates the presence of
a stochastic trend. The ADF test helps determine if a time series is stationary or non-stationary. The
mathematical formula for the ADF test is as follows:

$$\Delta Y_t = \rho Y_{t-1} + \delta_t + \varepsilon_t$$

228 , where ΔY_t is the first difference of the time series data; ρ is the coefficient of the lagged dependent
229 variable; δ_t is a constant term that includes any deterministic trends in the data, and ε_t is the error term.
230 The null hypothesis of the ADF test is that the time series has a unit root, meaning it is non-stationary
231 (Dickey and Fuller, 1979). The alternative hypothesis is that the time series is stationary. The ADF test
232 statistic is compared to a critical value based on the significance level and the sample size. If the test
233 statistic is less than the critical value, the null hypothesis is rejected, and the time series is considered
234 stationary.
235 The ADF test is commonly used in time series analysis to evaluate the stationarity of a time series and to
236 determine the order of differencing required to make the time series stationary (Stock and Watson, 1993).
237 If the time series is found to be non-stationary, it may be necessary to take first differences or higher order
238 differences to make the time series stationary.

239 *3.3.4 Kwiatkowski-Phillips-Schmidt-Shin (KPSS) Test*

The KPSS test (Kwiatkowski and Phillips, 1992) is a statistical method used to test for the presence of
a unit root in time series data. Unlike the ADF test, the KPSS test assumes that the null hypothesis is
stationarity and the alternative hypothesis is non-stationarity. The mathematical formula for the KPSS test
is as follows:

$$Y_t = \mu_t + \varepsilon_t$$

240 where Y_t is the time series data; μ_t is the deterministic trend function; and ε_t is the error term.
241 The null hypothesis of the KPSS test is that the time series is stationary, and the alternative hypothesis
242 is that it is non-stationary. The test statistic is calculated based on the sum of squared deviations from
243 the estimated trend function. If the test statistic exceeds the critical value, the null hypothesis is rejected,
244 and the time series is considered non-stationary. The KPSS test is commonly used in time series analysis
245 to evaluate the stationarity of a time series and to determine if differencing is required to make the time
246 series stationary.

3.4 Test for Randomness

In time series analysis, it is often a matter of interest to assess whether the series is a random walk or autocorrelated. To check this issue, we have several statistical hypothesis tests, namely, Wald-Wolfowitz Runs test (Siegel and Castellan, 1988; Siegel, 1956) and Bartels test (Bartels, 1982). Bartels test is typically more potent than the Runs test. Thus, we conclude the null hypothesis of the sequence generated by a random process versus the alternative hypothesis of the sequence generated by a process containing either persistence or frequent changes in direction using the Bartels test.

3.5 Association Analysis Between Prices (or indices) and Covid-19 Cases

We aim to assess the feasibility of incorporating Covid-19-confirmed cases as a potential regressor into parametric analysis. To accommodate the number of Covid-19 cases into Box-Jenkin's methodology for forecasting prices or indices, it is recommended to assess the significance of the association between the number of weekly Covid-19 cases and weekly stock prices (or indices). Here, we have tested the significance of the Pearsonian product-moment correlation.

4 RESULTS AND DISCUSSION

4.1 Stationarity Assumptions

4.1.1 For S & P 500 Data

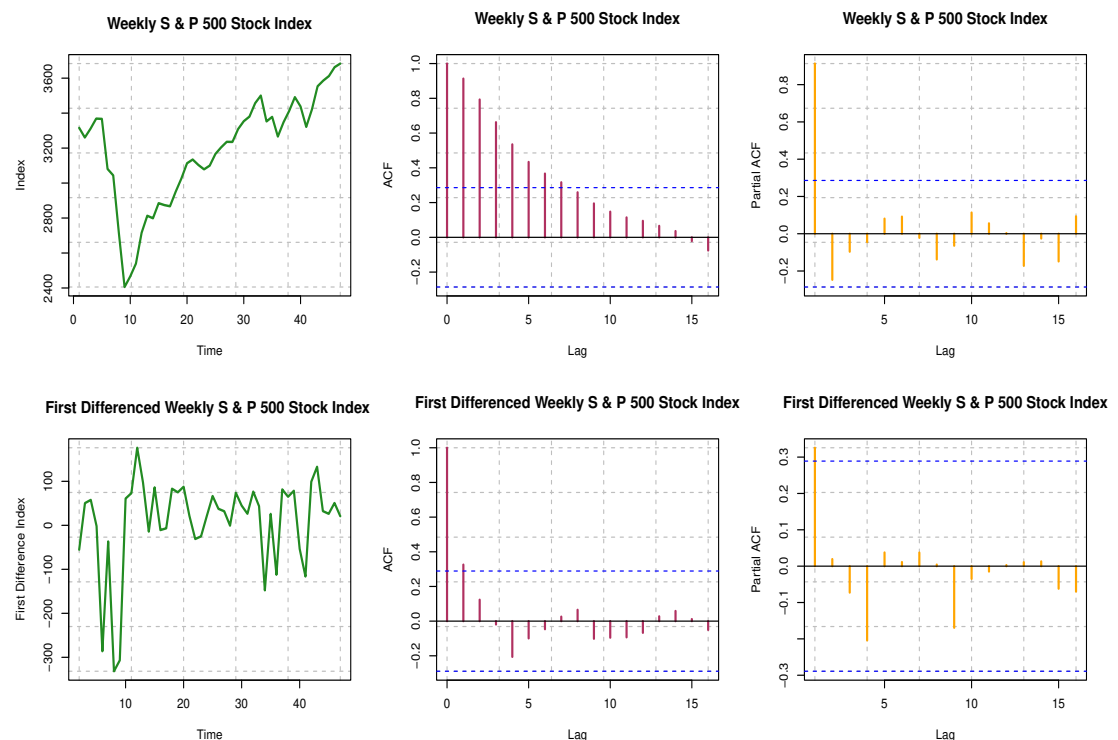



Figure 4. Statinarity Assumptions of S & P 500 Index Data

For the original series, ACF is not decaying fast for different time lags, so the series is visually non-stationary (see Figure 4). In contrast, for the first difference of the series, ACF decays very quickly, which is indicative of the stationarity of the differenced series. Further, we must perform a statistical hypothesis test to substantiate the stationarity. We have performed the quantitative tests for testing stationarity by the Ljung-Box test. For the original series (S & P data), p-value $< 2.2 \times 10^{-16}$; and for the first difference series, the p-value is 0.4127. Thus, though the original series is a non-stationary series, the first difference series is stationary by the Ljung-Box test, and these outcomes are consistent with what we have seen from ACF plots. For the original series, the p-value < 0.01; for the first difference series, the p-value is 0.01967 from the ADF test. Thus, both the original series and the first difference series do not have unit roots.

272 That is, both the original and the first difference series are stationary by the ADF test. KPSS test provides
273 the p-value of 0.0642 for the original series, and that for the first difference series is greater than 0.10.
274 The original series is not a trend stationary series, but the first difference series is indeed a trend stationary
275 series by quantitative statistical hypotheses tests. Overall, we conclude that the original series of weekly S
276 & P 500 stock indices are not stationary, but the first differences considered here are stationary.

4.1.2 MSCI Data

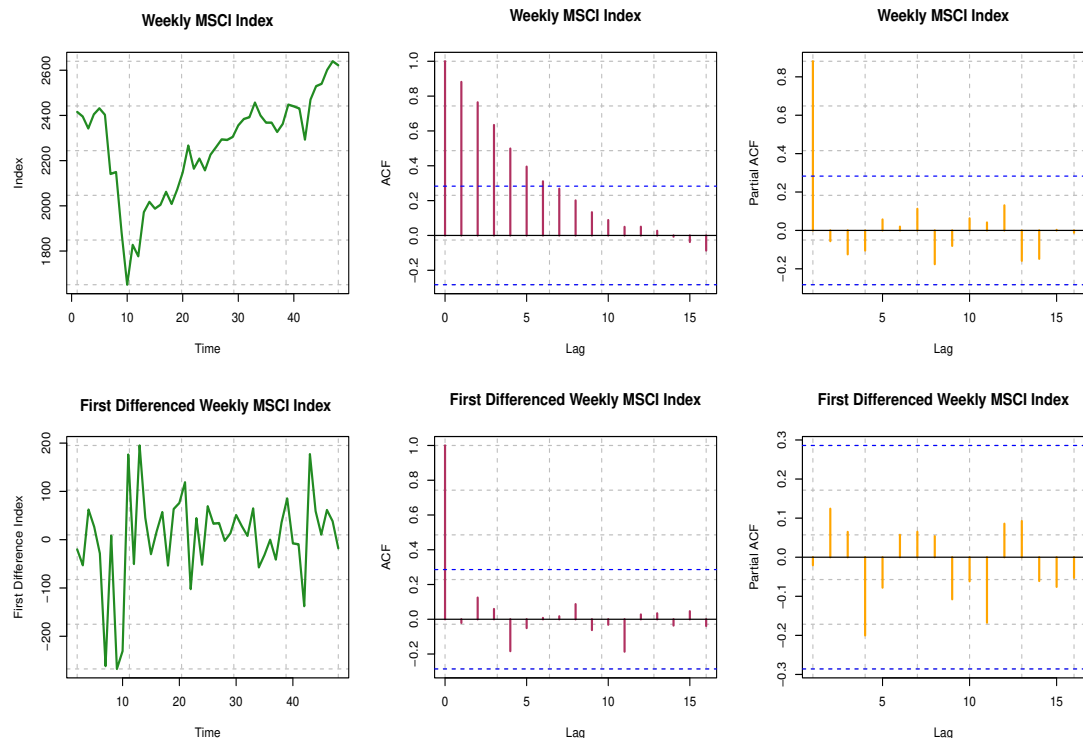



Figure 5. Stationarity Assumption of MSCI World Index Data

278 ACF is not decaying fast for different time lags for the original series, so the series is visually non-
279 stationary (see Figure 5). For the first difference of the series, ACF decays very quickly, which indicates
280 stationarity, but we need further statistical tests to confirm stationarity. For the original series, the Box-
281 Ljung test provides a p-value of $< 2.2 \times 10^{-16}$; but for the first difference series, the p-value is 0.9605.
282 Based on the results presented here, the original series is non-stationary, but the first difference series
283 is stationary. For the original series, the p-value is 0.06524; for the first difference series, the p-value
284 is 0.02559 from the ADF test. Thus, with the smaller nominal significance level ($\alpha = 0.05$), we may
285 conclude that the first difference series for MSCI is stationary. Therefore, the original series seems to
286 have unit roots, but the first difference series does not. For the original series, the p-value is 0.03821;
287 for the first difference series, the p-value is > 0.1 from the KPSS test. The difference series seems trend
288 stationary, but the original series was not. Overall, we may conclude that the original series of MSCI stock
289 indices considered here is not stationary, but the first difference of the series is found to be stationary.

4.1.3 VIX Data

291 ACF is not decaying for different time lags for the original series, so the series is visually non-stationary
292 (see Figure 6). In contrast, for the first difference of the series, ACF decays relatively faster, which
293 is indicative of stationarity. Further, we must perform a statistical hypothesis test to substantiate the
294 stationarity. For the original series, the p-value is 7.737×10^{-16}; for the first difference series, the p-value
295 is 0.1808 from the Box-Ljung test. Consequently, though the original series is non-stationary, the first
296 difference series is stationary. For the original series, the p-value is less than 0.01; for the first difference
297 series, the p-value is 0.02095 from the ADF test. Hence, both the original and the first difference series are

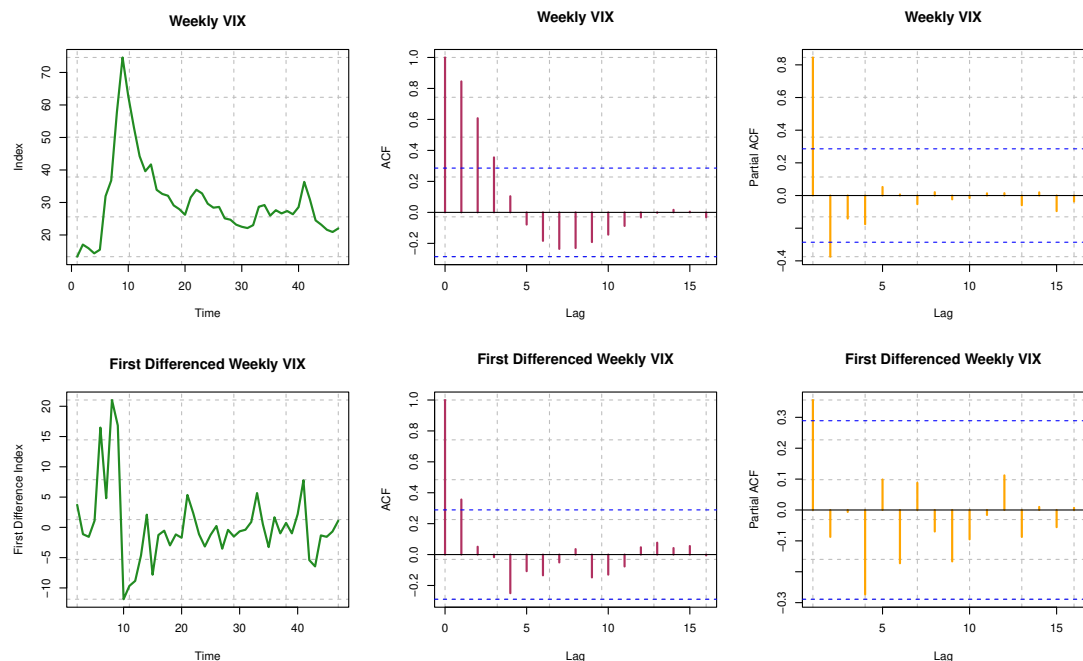



Figure 6. Stationarity Assumption of VIX Data

likely to be stationary. Again, p-values are more significant than 0.01 from the KPSS test for the original and first difference series. Both series are trend stationary. Overall, we may conclude that the original series of the VIX index seems to be trend stationary, but the first difference of the series is undoubtedly stationary.

4.2 Randomness Assumption

4.2.1 S & P 500 Data

For the original series, the *p*-value is 1.949×10^{-10} indicating that the original series is not a random walk. Likewise, for the first difference series, the *p*-value is 0.09555, meaning that the first difference series is also not a random walk if the nominal significance level is 0.10. Thus, in this research, we can employ Box-Jenkin's methodology for the prediction of S & P 500 stock indices using the first difference series.

4.2.2 MSCI Data

For the original series, the *p*-value is 8.692×10^{-10} indicating that the original series is not a random walk. In contrast, for the first difference series, the *p*-value of 0.4891 leaves the trace that the first difference series is a random walk.

4.2.3 VIX Data

For the original series, the *p*-value is 5.915×10^{-09} indicates that the original series is not a random walk. Similarly, for the first difference series, the *p*-value of 0.04727 demonstrates that the first difference series is also not a random walk at a nominal significance level of 0.05.

However, when a time series is non-stationary, the general practice is to make the series difference stationary. Moreover, if the difference stationary series is not autocorrelated, the original series is a random walk. If so, any parametric time series modeling should be used for forecast purposes. In our preliminary analysis, we have found that the first difference series of S & P and VIX are stationary and autocorrelated (not random walk). Still, the first difference series of MSCI is a stationary but random walk. Thus, we may employ a parametric method for price or index forecasting for the first difference between S & P 500 series and VIX, which is Box-Jenkin's methodology. On the other hand, we may deploy random walk forecasting methods for MSCI index forecasting.

4.3 Association Analysis

4.3.1 S & P 500 Weekly Indices and Weekly Covid-19 Cases

Here, we have considered weekly data for both S & P 500 index and Covid-19 cases in the USA. The Pearsonian product-moment correlation between S & P 500 weekly index and Weekly Covid-19 cases in the USA is 0.5500 with a p-value of $6.204 10^{-05}$. Therefore, the number of confirmed Covid-19 cases is significantly correlated with S & P 500 stock indices.

4.3.2 Weekly VIX and Weekly Covid-19 Cases

Here, we have considered weekly data for VIX and Covid-19 cases in the USA. The Pearsonian product-moment correlation between VIX and Weekly Covid-19 cases in the USA is -0.2487 with a p-value of 0.09184. Therefore, the number of confirmed Covid-19 cases significantly correlates with VIX at a nominal significance level of 0.10.

4.4 Forecast Using Box-Jenkin's Method

In forecasting prices or indices using Box-Jenkin's methodology for stationary time series or difference stationary time series, it is desirable to develop an appropriate order of autoregressive (AR) and moving average (MA) terms. In this research, we select the orders of AR and MA using the cross-validation method. This is one of the most useful statistical and machine learning methods in order selection.

We consider Akaike Information Criterion (AIC) (Akaike, 1974) as our model selection criterion, which is calculated by AIC = -2 log L + 2p, where L is the maximum value of the likelihood function of the model, and p is the number of estimated parameters in the model. The AIC value is calculated based on the number of parameters used in the model and the log-likelihood function, which measures how well the model fits the data. A lower AIC value indicates a better fit of the model to the data.

We select the order of AR and MA that provide the model with the smallest AIC value. For each of the data, we present the order and AIC (see Table 2) and ACF plot (see Figure 7) of residual of final models for S & P 500 and VIX. Detail guidelines for model selection can be found in Hyndman and Khandakar (2008) and Wang et al. (2006). Estimates of the corresponding model parameters and their test of significance have been presented in Table 3. The AR and MA parameters are highly significant for S & P 500 and VIX data, whereas the parameter for Covid-19 infection rate is somewhat significant for both the data.

Data	ARIMA Order	AIC
S & P 500	(1, 1, 0)	557.01
VIX	(2, 0, 1)	300.49

Table 2. Order of ARIMA and AIC Values of Optimum Models

Data	Model	Estimates	SE	*p*-value
S & P 500	ARIMA(1, 1, 0)	$\hat{\phi}_1 = 0.324$	0.138	0.019
		$\hat{\beta}_1 = 0.125$	0.068	0.066
VIX	ARIMA (2, 0, 1)	$\hat{\phi}_1 = 1.246$	0.130	<0.000
		$\hat{\phi}_2 = -0.435$	0.136	0.001
		$\hat{\theta}_1 = 32.316$	7.116	<0.000
		$\hat{\beta}_1 = 0.103$	.061	0.091

Table 3. Estimates of Model Parameters along with Standard Error (SE) and Test of Significance of Model Parameters

4.4.1 S & P 500 Index Data

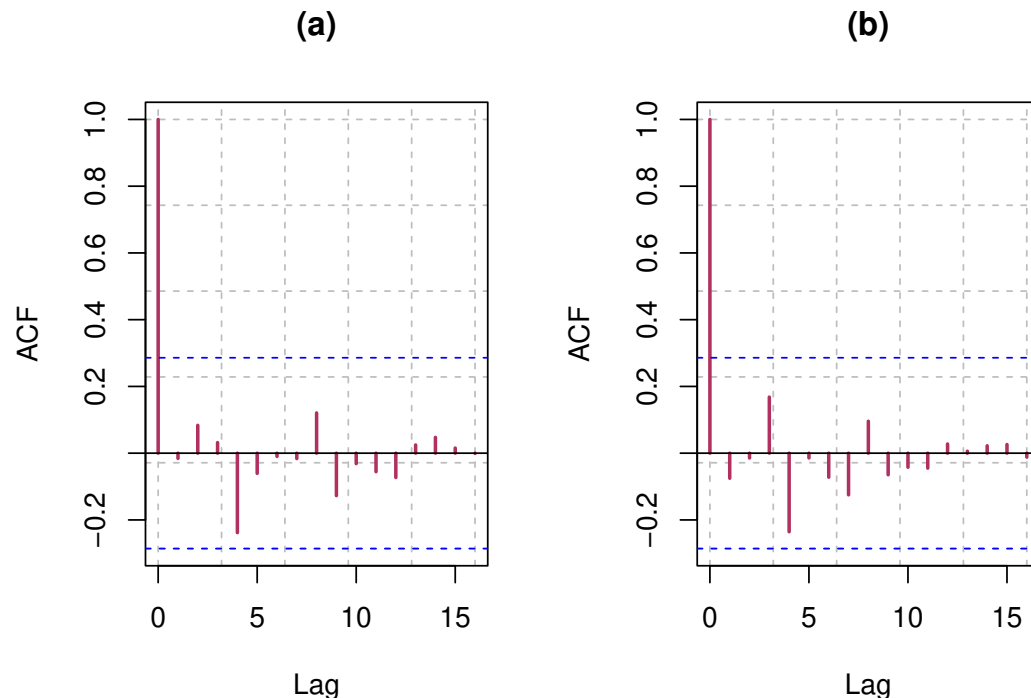
In this study, we have considered the weekly number of Covid-19 confirmed cases as a regressor and weekly S & P 500 indices from December 12, 2020, to February 12, 2021 (9 weeks) for forecasting using our optimum trained model. Forecast indices and 80%, 95%, and 99% Prediction intervals are presented in the following table (see Table 4). The visualization of these results has been presented in Figure 8.

(a)   **(b)**

Figure 7. (a) ACF Plot of Residuals from Optimum Model for S & P 500 Index; (b) ACF Plot of Residuals from Optimum Model for VIX

4.4.2 VIX Data

Similar to S & P 500, we have considered the weekly number of Covid-19 confirmed cases as a predictor variable and weekly VIX data from December 12, 2020, to February 12, 2021 (9 weeks) for forecasting using our optimum trained model. Forecast indices, along with 80%, 95%, and 99% Prediction intervals, are presented in the following table (see Table 5). These results have been displayed in Figure 9 along with the original series. Since VIX is an index and it cannot take a negative value. To address this issue, we fit the model on natural logarithm-transformed data and, later on, exponentiated the results to bring them back to their original scale.

4.4.3 MSCI Data

Like S & P 500 Index, we have considered the weekly MSCI Index from December 12, 2020, to February 12, 2021 (9 weeks) for forecasting using our train model. Here, forecasts have been made using three different random walk forecasting methods: the mean method, the naïve method, and the drift method, as described in Section 4. Forecast of the index along with 80%, 95%, and 99% Prediction intervals are presented in the following tables (see Table 6, 7, and 8) for the aforementioned methods. These results have been shown schematically in Figure 10, along with the original series.

From the accuracy measures (Hyndman and Athanasopoulos, 2018; Hyndman and Koehler, 2006; Armstrong, 1978) presented in Table 9, it can be concluded that the best method for MSCI data forecasting, based on the RMSE and MPAE, is the drift method, which suggests that the trend is more important than the seasonality in this series.

5 CONCLUDING REMARKS

Forecasting methodologies and modeling are always challenging due to strict assumptions behind the time series forecasting methods. Even assumptions are intrinsically strict for applying any parametric methods

Horizon	Forecast	80% PI	95% PI	99% PI
48	3681.536	(3555.140, 3807.932)	(3488.230, 3874.842)	(3427.489, 3935.583)
49	3649.608	(3439.857, 3859.359)	(3328.822, 3970.394)	(3228.024, 4071.192)
50	3656.062	(3379.217, 3932.906)	(3232.665, 4079.458)	(3099.624, 4212.499)
51	3727.503	(3394.535, 4060.470)	(3218.273, 4236.732)	(3058.262, 4396.743)
52	3704.052	(3322.462, 4085.642)	(3120.461, 4287.644)	(2937.083, 4471.022)
53	3610.386	(3185.505, 4035.267)	(2960.586, 4260.186)	(2756.404, 4464.368)
54	3563.579	(3099.368, 4027.790)	(2853.629, 4273.529)	(2630.546, 4496.611)
55	3510.924	(3010.446, 4011.402)	(2745.509, 4276.339)	(2504.999, 4516.850)
56	3459.464	(2925.170, 3993.758)	(2642.332, 4276.596)	(2385.571, 4533.357)

Table 4. Forecast for S & P 500 Indices along with 80%, 95%, and 99% Prediction Intervals (PIs) from ARIMAX Method

Horizon	Forecast	80% PI	95% PI	99% PI
48	22.741	(15.752, 29.731)	(12.051, 33.432)	(8.692, 36.791)
49	23.642	(12.472, 34.812)	(6.559, 40.725)	(1.191, 46.093)
50	23.092	(9.456, 36.727)	(2.238, 43.945)	(0.013, 50.498)
51	20.565	(5.685, 35.445)	(0.111, 43.322)	(0.000, 50.473)
52	20.833	(5.418, 36.248)	(0.064, 44.408)	(0.000, 51.815)
53	23.233	(7.629, 38.837)	(0.532, 47.098)	(0.000, 54.596)
54	24.374	(8.718, 40.030)	(0.431, 48.318)	(0.001, 55.841)
55	25.769	(10.105, 41.434)	(1.812, 49.727)	(0.003, 57.255)
56	27.192	(11.527, 42.857)	(3.234, 51.150)	(0.014, 58.678)

Table 5. Forecast for VIX along with 80%, 95%, and 99% Prediction Intervals (PIs) from ARIMAX Method

of forecasting. In this research, we have started with three different worldwide stock or stock-related indices, namely, S & P, MSCI, and VIX, for modeling their data to forecast the future indices in conjunction with the Covid-19 confirmed cases. Other challenges in this research are gathering, compiling, and manipulating stock indices data to align with Covid-19 confirmed cases because of discrepancies in reporting stock indices (5 days a week) and Covid-19 confirmed cases (7 days a week). For the datasets considered in this research, S & P and VIX data satisfied the assumptions for parametric forecasting methods. In contrast, MSCI data satisfied the assumptions for the random walk forecasting method.

It has been observed that the variant integrated ARMAX of Box-Jenkins parametric methods of forecasting for the S & P index and VIX does a good job of modeling the data. From Table 4, 5 and Figure 8, 9, it has been found that the forecasted indices are close to the original test set of data. In addition, the shortest of the three forecast intervals among 80%, 95%, and 99% contains the forecasted series, which is an indication that the adopted methodology performed well in capturing the underlying structure in the training data in connection with the Covid-19 confirmed cases which are further substantiated in the test data.

Nonstationarity data are not uncommon. Unlike S & P 500 and VIX, MSCI data showed nonstationarity behavior. One possible reason for such behavior could be due to the nature of the MSCI index, which spans over 23 countries throughout the world, and most likely has more noise than any other traditional index. Nonstationary data are challenging to model.

Nonetheless, random walk forecasting methods seem to perform a good modeling job in capturing the underlying structure in the training set of MSCI data substantiated by the test dataset. We have considered the mean, naïve, and drift methods of random walk forecasting. It has been found that (see Table 6, 7, 8 and Figure 10) in all the methods the forecasted indices are included by the 95% prediction intervals. However, for the naïve method, the forecasted series is even closer to the original series and are also

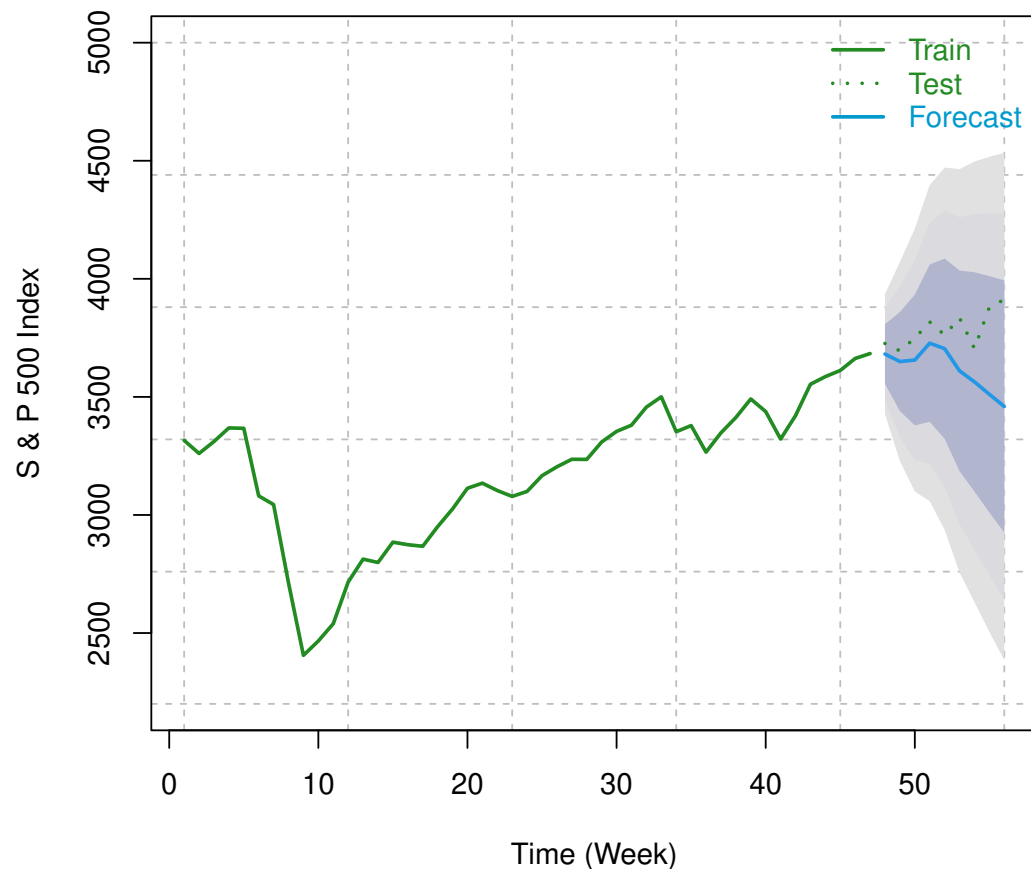



Figure 8. Train Series, Test Series, and Forecast for S & P 500 Index along with 80% (inner most), 95% (middle), and 99% (outer most) Prediction Bands.

409   contained by the shortest prediction intervals. Since no study investigated the impact of Covid-19 infection
410   rates on stock indices such as MSCI, no comparative analysis has been performed.

411

412   As the three indices investigated in this study are from different parts of the world, it was challenging to
413   get uniform data as different countries have different holiday calendars for their stock markets. Moreover,
414   as the reporting of the Covid-19 infection data varied from country to country significantly, it can be
415   considered a limitation of the study.

CONFLICT OF INTEREST STATEMENT

417   On behalf of all authors, the corresponding author states that there is no conflict of interest.

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419   The authors are very grateful to the editorial members and the reviewers for their meaningful feedback,
420   which helped us to improve the quality of the manuscript.
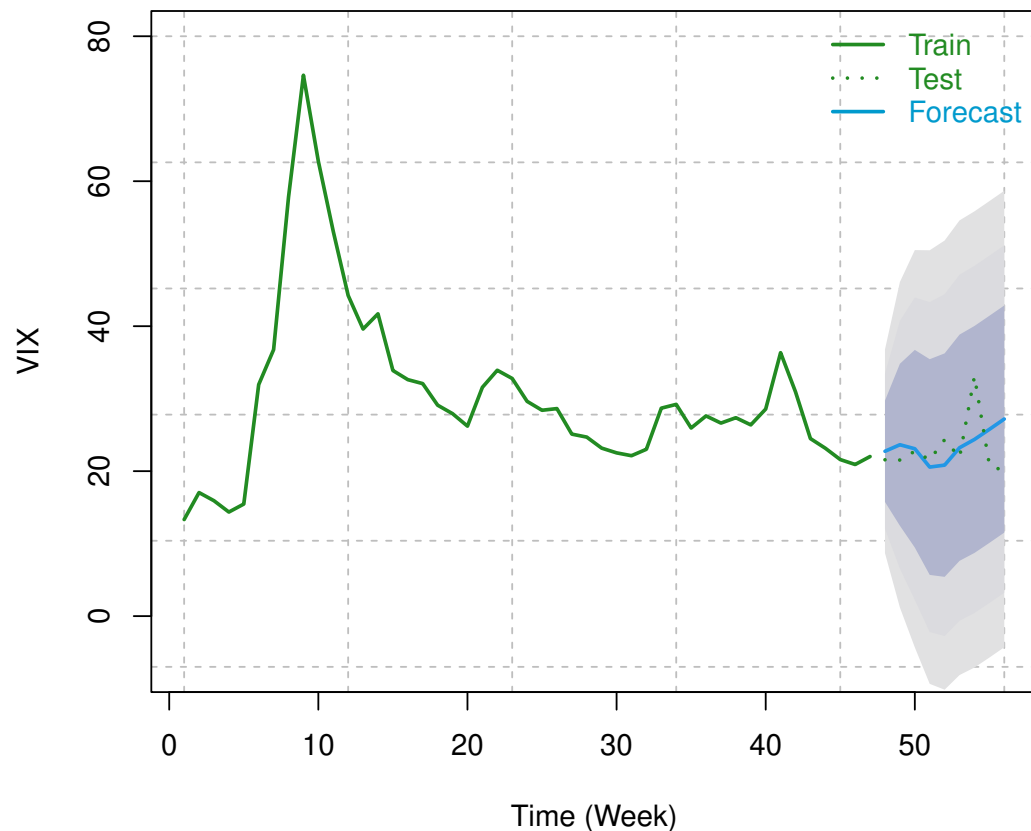
Figure 9. Train Series, Test Series, and Forecast for VIX along with 80% (innermost), 95% (middle), and 99% (outermost) Prediction Bands.

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Horizon	Forecast	80% PI	95% PI	99% PI
49	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
50	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
51	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
52	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
53	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
54	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
55	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
56	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279, 2872.59)
57	2264.435	(1969.974, 2558.895)	(1808.698, 2720.172)	(1656.279 2872.59)

Table 6. Forecast for MSCI World Indices along with 80%, 95%, and 99% Prediction Intervals (PIs) form Mean Method

Horizon	Forecast	80% PI	95% PI	99% PI
49	2621.89	(2502.025, 2741.755)	(2438.572, 2805.208)	(2380.969, 2862.811)
50	2621.89	(2452.375, 2791.405)	(2362.639, 2881.141)	(2281.176, 2962.604)
51	2621.89	(2414.277, 2829.503)	(2304.373, 2939.407)	(2204.602, 3039.178)
52	2621.89	(2382.159, 2861.621)	(2255.253, 2988.527)	(2140.048, 3103.732)
53	2621.89	(2353.863, 2889.917)	(2211.978, 3031.802)	(2083.174, 3160.606)
54	2621.89	(2328.281, 2915.499)	(2172.854, 3070.926)	(2031.756, 3212.024)
55	2621.89	(2304.756, 2939.024)	(2136.875, 3106.905)	(1984.473, 3259.307)
56	2621.89	(2282.859, 2960.921)	(2103.388, 3140.392)	(1940.462, 3303.318)
57	2621.89	(2262.294, 2981.486)	(2071.935, 3171.845)	(1899.127, 3344.653)

Table 7. Forecast for MSCI World Indices along with 80%, 95%, and 99% Prediction Intervals (PIs) form Naïve Method

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Horizon	Forecast	80% PI	95% PI	99% PI
49	2626.281	(2505.253, 2747.309)	(2441.185, 2811.377)	(2383.024, 2869.538)
50	2630.672	(2457.702, 2803.642)	(2366.137, 2895.207)	(2283.014, 2978.330)
51	2635.063	(2421.023, 2849.103)	(2307.718, 2962.409)	(2204.858, 3065.268)
52	2639.454	(2389.793, 2889.115)	(2257.631, 3021.278)	(2137.653, 3141.256)
53	2643.845	(2361.938, 2925.752)	(2212.706, 3074.985)	(2077.232, 3210.459)
54	2648.236	(2336.410, 2960.063)	(2171.339, 3125.134)	(2021.487, 3274.986)
55	2652.627	(2312.593, 2992.662)	(2132.590, 3172.665)	(1969.182, 3336.073)
56	2657.019	(2290.093, 3023.944)	(2095.855, 3218.182)	(1919.524, 3394.513)
57	2661.410	(2268.640, 3054.180)	(2060.720, 3262.100)	(1871.969, 3450.850)

Table 8. Forecast for MSCI World Indices along with 80%, 95%, and 99% Prediction Intervals (PIs) form Drift Method
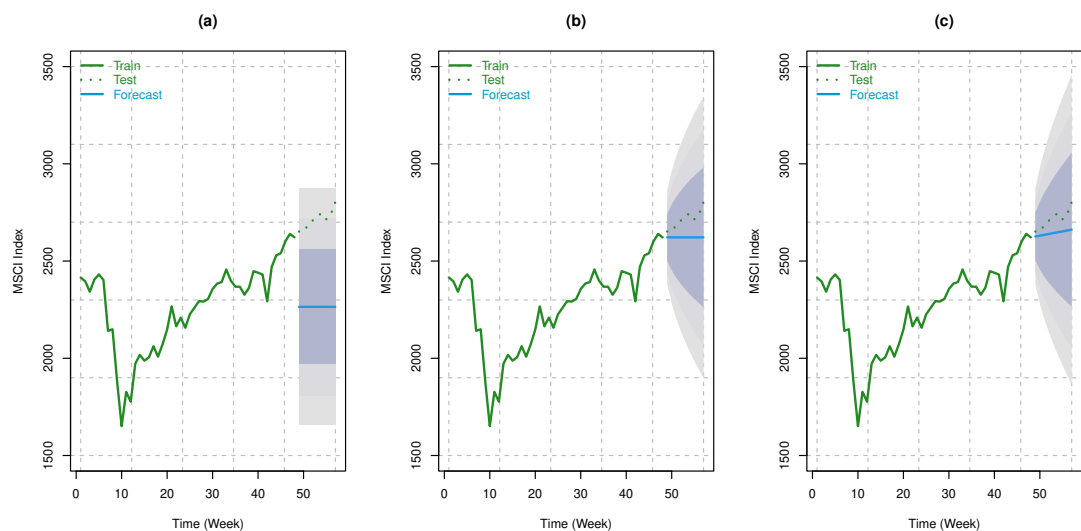
Figure 10. Train Series, Test Series, and Forecast for MSCI Index along with 80% (innermost), 95% (middle), and 99% (outermost) Prediction Bands. (a) Using Mean Method; (b) Using Naïve Method; (c) Using Drift Method.

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Data	Model	ME	RMSE	MAE	MPE	MAPE
S & P (Training)	ARIMA(1, 1, 1)	-0.340	95.428	68.961	-0.050	2.269
S & P (Test)	ARIMA(1, 1, 1)	168.710	219.978	168.710	4.395	4.395
VIX (Training)	ARIMA (2, 0, 1)	0.255	5.217	3.512	-1.930	11.770
VIX (Test)	ARIMA (2, 0, 1)	-0.428	4.386	3.365	-4.117	14.198
MSCI (Training)	Mean	0.000	221.867	179.527	-1.061	8.325
MSCI (Test)	Mean	450.385	452.692	450.385	16.566	16.566
MSCI (Training)	Naïve	4.391	93.531	66.280	0.069	3.125
MSCI (Test)	Naïve	92.930	103.535	92.930	3.396	3.396
MSCI (Training)	Drift	0.000	93.428	65.626	-0.127	3.099
MSCI (Test)	Drift	70.975	79.374	70.975	2.593	2.593

Table 9. Accuracy Measures (ME: Mean Error, RMSE: Root Mean Squared Error, MAE: Mean Absolute Error, MPE: Mean Percent Error, MAPE: Mean Absolute Percent Error) of Forecast Models for Different Datasets

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Figure 1

World epidemics and global stock market performance

Figure 2

Covid-19 Weekly Confirmed Cases in the (a) USA and (b) Twenty-three MSCI Countries
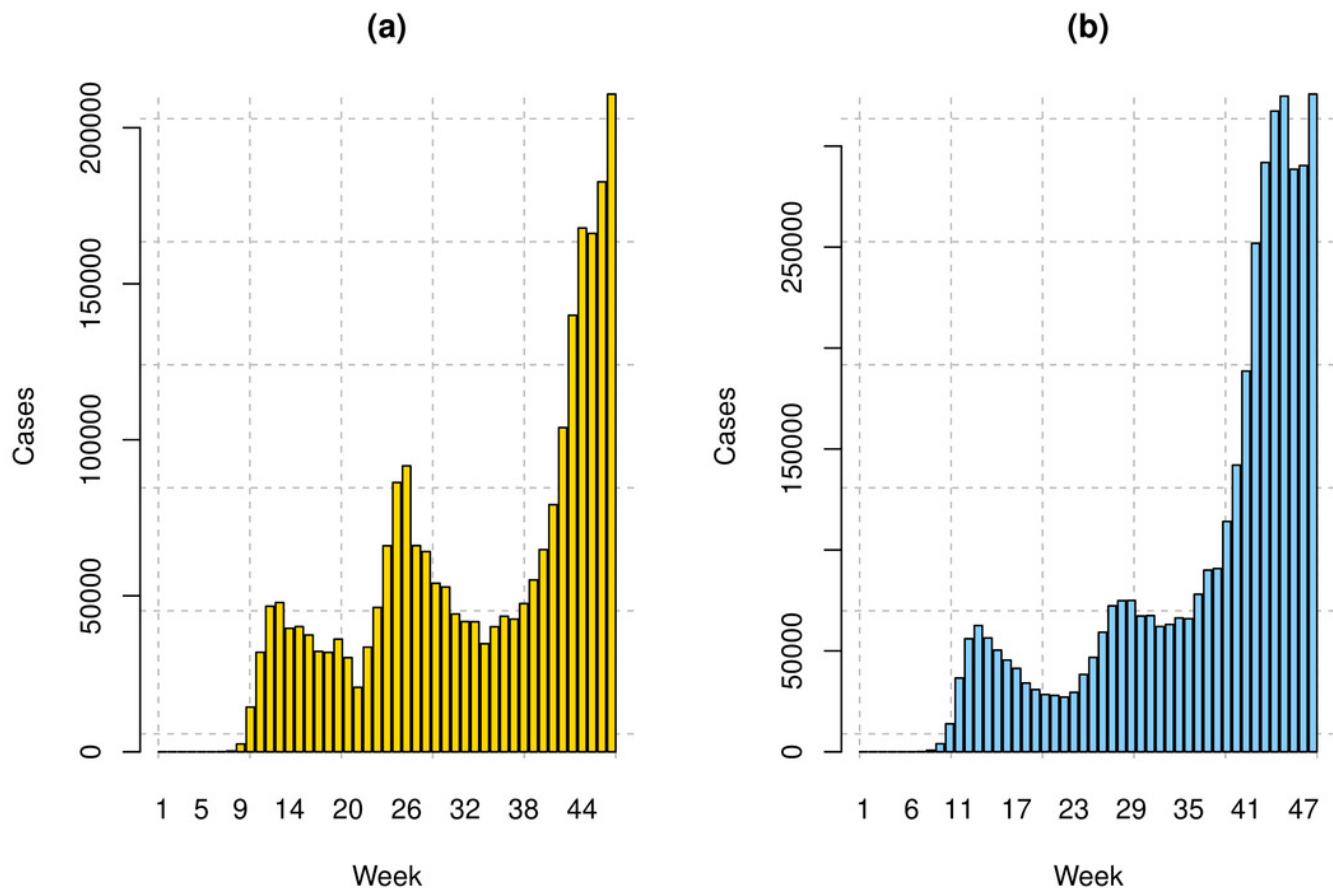
Figure 3

Weekly Price Index for (a) S & P 500; (b) MSCI; and (c) VIX
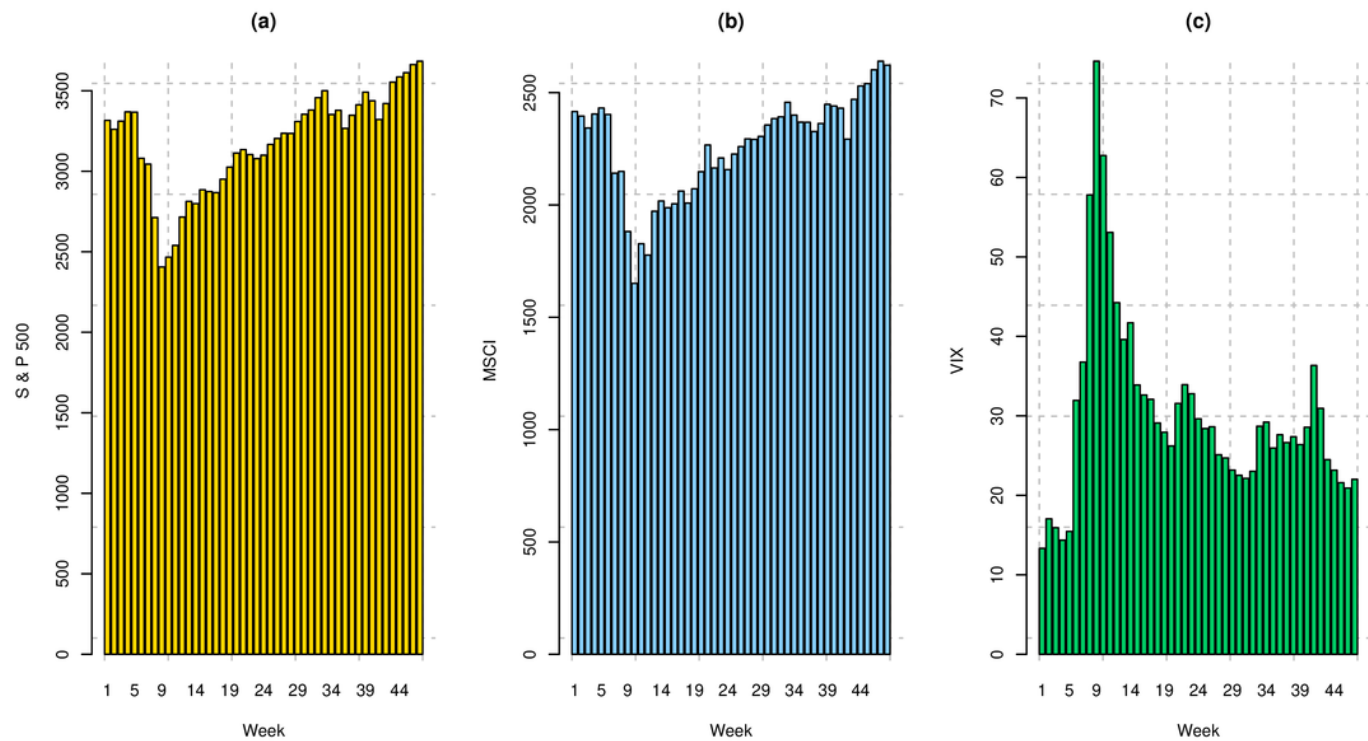
Figure 4

Statinarity Assumptions of S & P 500 Index Data
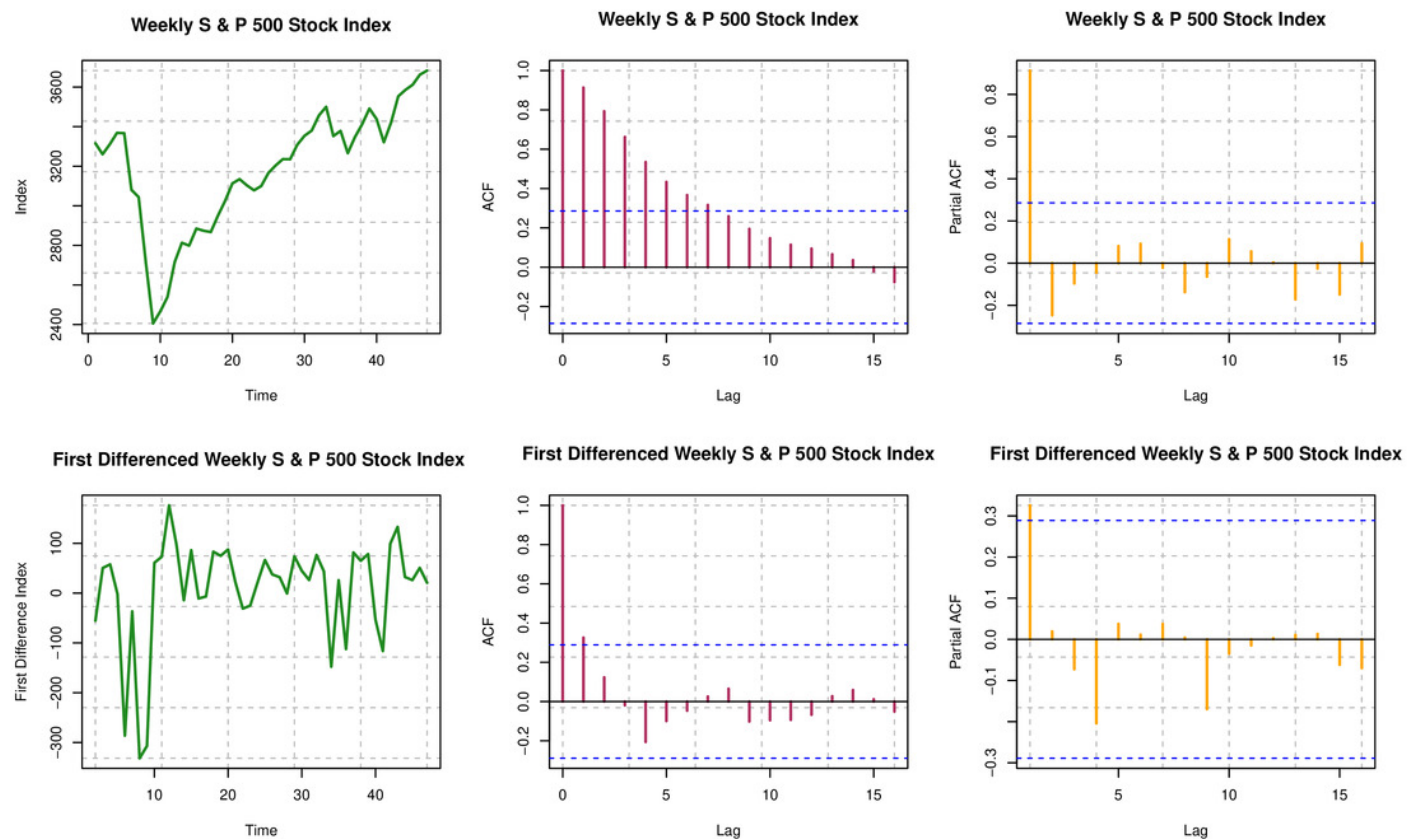
Figure 5

Stationarity Assumption of MSCI World Index Data
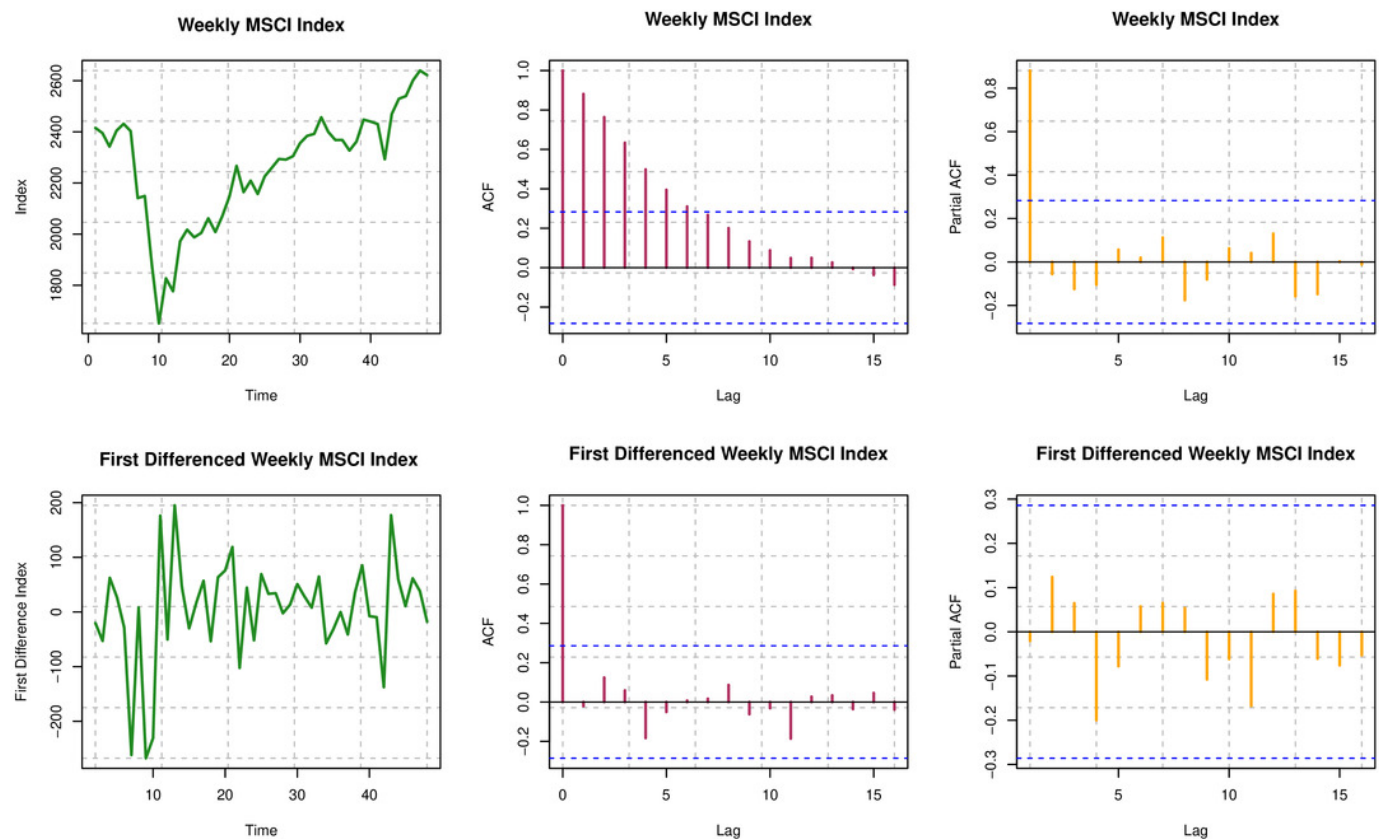
Figure 6

Stationarity Assumption of VIX Data
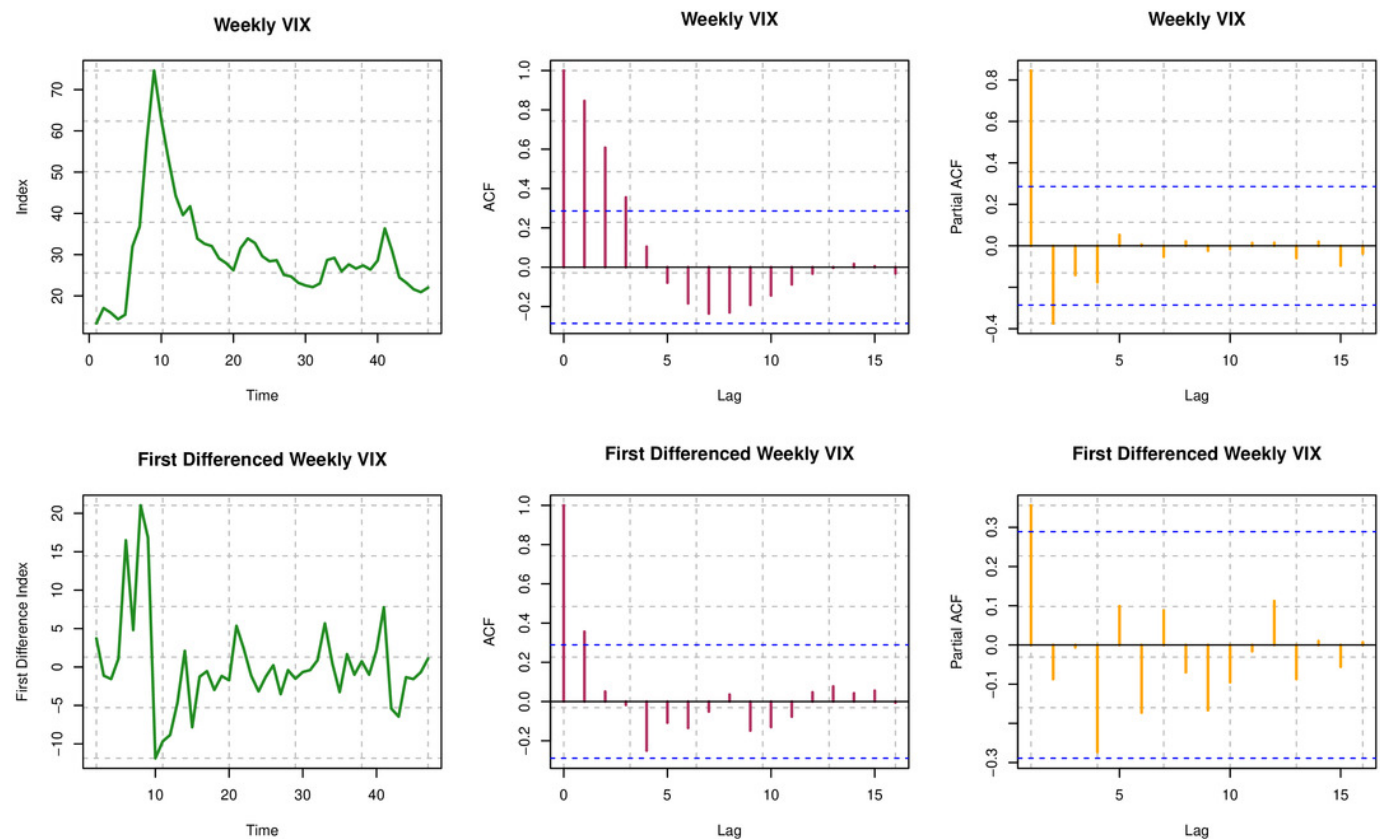
Figure 7

(a) ACF Plot of Residuals from Optimum Model for S & P 500 Index; (b) ACF Plot ofResiduals from Optimum Model for VIX
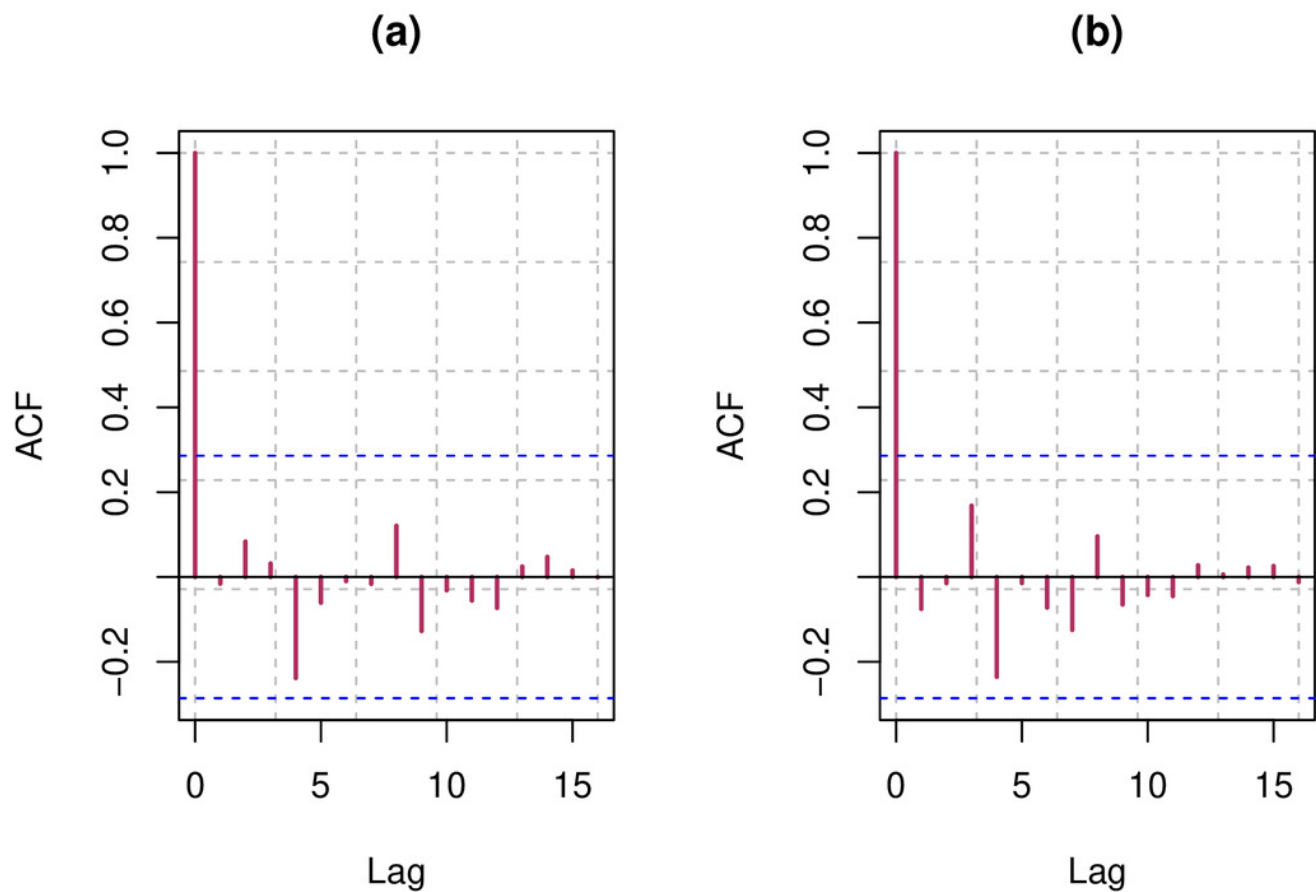
Figure 8

Train Series, Test Series, and Forecast for S & P 500 Index along with 80% (inner most), 95%(middle), and 99% (outer most) Prediction Bands.

Figure 9

Train Series, Test Series, and Forecast for VIX along with 80% (innermost), 95% (middle),and 99% (outermost) Prediction Bands

Figure 10

Train Series, Test Series, and Forecast for MSCI Index along with 80% (innermost), 95%(middle), and 99% (outermost) Prediction Bands. (a) Using Mean Method; (b) Using Na¨ıve Method; (c)Using Drift Method