

# Hybrid Computational Approach applied to the Positioning of Small Cells in 5G Networks considering Real Data

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One of the key technologies in smart cities is the use of next generation networks such as 5G Networks. Mainly because this new mobile technology offers massive connections in dense populated areas in smart cities, thus playing a crucial role for numerous subscribers anytime and anywhere. Indeed, all the most important infrastructure to promote a connected world is being related to next generation networks. Specifically, the Small Cells transmitters is one of the 5G technologies more relevant to provide more connections and to attend the high demand in smart cities. . In this paper, a smart small cell positioning is proposed in the context of a smart city. The work proposal aims to do this through the development of a hybrid clustering algorithm with meta-heuristic optimizations to serve users, with real data, of a region satisfying coverage criteria. Furthermore, the problem to be solved will be the best location of the small cells, with the minimization of attenuation between the Base Stations and its users. The possibilities of using multi-objective optimization algorithms based on bioinspired computing, such as Flower Polination and Cuckoo Search, will be verified. It will also be analyzed by simulation which power values would allow the continuity of the service with emphasis on three 5G spectrums used around the world: 700 MHz, 2.3 GHz and 3.5 GHz.

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## ABSTRACT

One of the key technologies in smart cities is the use of next generation networks such as 5G Networks. Mainly because this new mobile technology offers massive connections in dense populated areas in smart cities, thus playing a crucial role for numerous subscribers anytime and anywhere. Indeed, all the most important infrastructure to promote a connected world is being related to next generation networks. Specifically, the Small Cells transmitters is one of the 5G technologies more relevant to provide more connections and to attend the high demand in smart cities. In this paper, a smart small cell positioning is proposed in the context of a smart city. The work proposal aims to do this through the development of a hybrid clustering algorithm with meta-heuristic optimizations to serve users, with real data, of a region satisfying coverage criteria. Furthermore, the problem to be solved will be the best location of the small cells, with the minimization of attenuation between the Base Stations and its users. The possibilities of using multi-objective optimization algorithms based on bioinspired computing, such as Flower Polination and Cuckoo Search, will be verified. It will also be analyzed by simulation which power values would allow the continuity of the service with emphasis on three 5G spectrums used around the world: 700 MHz, 2.3 GHz and 3.5 GHz.

## INTRODUCTION

The emerging concept of Smart Cities is being promoted with the deployment of 5G technologies. Considering the increasing amount of industrialization with urbanization, the huge demand for resources and their ubiquitous use are catalyzing the emergence deployment of smart city technologies and applications. All urbanization enablers like transportation and mobility, health care, natural resources, electricity and energy, homes and buildings, commerce and retail, society and workplace, industry, agriculture and the environment, are hugely dependant of a suitable communication and safe capabilities to support these smart cities application domains.

Meanwhile, the fifth generation of wireless communications, the 5G system, is currently being integrated, with an extensive range of applications and frequency channels for its operation. According to Dahlman et al. (2014), 5G operation aims at a 1,000 times greater traffic capacity and a pulled bandwidth capacity capable of working with a latency response of 1 ms with data rates in the order of 1 Gbps to 10 Gbps. The development of 5G systems is divided into indoor and outdoor spreads. Generally, the sub-6 GHz band is applied outdoors because it is easier to transmit and propagate, and communication companies are already testing and applying 5G systems in this band for commercial purposes, in different parts of the world, as reports from Viavi (2022) have shown. In Brazil, it is no different - all major operators already have 5G systems in operation for several capitals in the country. AgênciaBrasil (2021) and Reuters (2021)

46 inform that the main frequencies to operate 5G in the country, according to government body Anatel, are  
47 700 MHz, 2.5 GHz and 3.5 GHz for outdoor systems, and 26 GHz for indoor deployments.

48 Along the difficulties tied to the deployment of 5G heterogeneous networks (5G HetNet), are the  
49 challenges to optimize their user coverage and user capacity, allowing for an increased number of services  
50 provided whilst keeping network costs low. And, as Rappaport et al. (2013) has stated, 5G coverage  
51 should be available everywhere, to anyone. That is, user coverage needs to be as closer to a hundred  
52 percent as ever.

53 And so, a number of studies and surveys have dealt with the necessity of coverage optimization.  
54 Agiwal et al. (2021), for instance, dedicates a whole survey on the applications of 4G-5G inter-operations,  
55 and how those can be better achieved. This is because implementation of 5G networks till this day are  
56 much costing, and changes cannot be applied overnight. Meanwhile, 4G-LTE cells can provide service  
57 coverage while 5G is still expanding. Another survey that is worth noticing, written by Shayea et al.  
58 (2020), focuses on user mobility management and how user equipments (UEs) are prone to disconnect if  
59 there are no satisfactory solutions to coverage, capacity and handoff problems and challenges.

60 The study herein proposed aims to provide a solution to the coverage problem for future 5G network  
61 applications, focusing especially in the range of Small Cells. The positioning of Small Cells is a key  
62 concept of densification offering a potential solution for the ultra-dense traffic in Smart Cities. Otherwise,  
63 to add to the traditional cell planning in this work two types of computational intelligence techniques will  
64 be tested, i.e., metaheuristic optimization through the utilization of a bioinspired computing algorithm  
65 (BIC) and a clustering technique. It is possible to group a set of users into an intelligent network coverage  
66 system, that aims to not only optimize the number of Small Cells but also deal with energy efficiency  
67 measures (such as controlling the transmitted power used in the cells).

68 Bioinspired computational methods are mainly based on natural selection. They are set to mimic  
69 the natural behavior of nature, in which the best and most surviving individuals prevail. With that in  
70 mind, these bioinspired algorithms serve as good optimization methods for mathematical and engineering  
71 problems, especially those where metaheuristic techniques (trial and error) can be applied to achieve one  
72 or more concrete goals. They have been applied to a multitude of areas where non-linear, multimodal  
73 optimization is required. E.g. Li et al. (2022) cite some areas of robotics where they might be useful,  
74 Nguyen et al. (2020) exposes some challenges in smart energy management that can be overcome with  
75 bioinspired solutions, and Gill and Buyya (2019) shows that some of them are even used on big data  
76 analysis and as aid to digitization of important documents into digital libraries.

77 The clustering method chosen for this application is K-Means, which is extensively utilized in the  
78 literature for its simplicity and efficiency Ahmed et al. (2020). As for the bioinspired methods, two are to  
79 be tested in conjunction with K-Means: the Cuckoo Search (CS) and the Flower Pollination Algorithm  
80 (FPA). As the aim of the work is to both maximize user coverage and minimize transmitted power, it is  
81 needed to use their multi-objective counterparts (that is, MOCS and MOFPA).

82 By using real data from open and free database OpenCellid, see Khan et al. (2020), it is possible to  
83 pre-select cells with the greatest amount of user traffic in 4G-LTE in order to plan out how future 5G  
84 Small Cells shall behave in order to provide good coverage of service to users. More details about this are  
85 to be explained in the Methodology section.

86 The proposed hybridization of clustering and bioinspired algorithms is to be tested in simulations to  
87 determine an optimal user coverage for the three aforementioned frequencies that have been auctioned to  
88 operate in Brazil: 700 MHz, 2.3 GHz and 3.5 GHz. In total, two hybrid algorithms have been produced:  
89 MOCS + K-Means (MOCS-KM) and MOFPA + K-Means (MOFPA-KM).

90 The main contributions of this study are the provision of a fairly simple metaheuristic method to  
91 achieve optimal network coverage with low-power Small Cells, and to provide data that can be adapted  
92 to an densely urban but with a rainforest climate such as the city of Belém, Brazil - which is where our  
93 OpenCellid data is from. A considerable area of the city has been selected to test the intelligent UE  
94 clustering simulations for 5G Small Cell implementation.

95 The paper is organized into the following sections: Related Works discourses about some of the  
96 state-of-the-art solutions for coverage and capacity optimization for 5G as well as bioinspired/clustering  
97 algorithm hybrids; Methodology explains how the study was conducted, the theory behind the algorithms  
98 utilized and gives information on the propagation model chosen for path loss and user coverage modeling;  
99 Results demonstrate the simulation of the algorithms for the different frequency ranges; and Conclusions  
100 expose our final considerations of the study.

## 101 RELATED WORKS

102 This section is to be divided into two topics: Coverage and Capacity Optimizations for applications in 5G  
103 systems, and Bioinspired Algorithm Hybridizations focusing on clustering of data.

### 104 Coverage and Capacity Optimization of Future 5G Networks

105 An analytical study on the Coverage, Handoff and Cost optimization for Heterogeneous 5G Networks (5G-  
106 HetNet) has been written by Ouamri et al. (2020). A path loss model is suggested for both Line-of-Sight  
107 (LoS) and Non-Line-of-Sight (NLoS) situations, with different path loss exponents, and the handling  
108 of coverage and handoff probability is done by Stochastic Geometry with values in SINR (Signal to  
109 Interference-Plus-Noise Ratio). By the method of Cellular Network Planning (CNP), network investment  
110 cost issues are optimized.

111 Khan et al. (2020) talks about a heuristic method to predict the employment of 5G base-stations  
112 in Spain by obtaining user and traffic data from LTE networks, using the free database of OpenCellid.  
113 This dimensioning of a 5G network takes into consideration the various aspects of this technology:  
114 heterogeneous architecture, the necessity for a high Quality of Experience (QoE) and smart resource  
115 allocation. Their objectives are achieved by separating the highest traffic areas, and then deciding where  
116 5G cells are to be deployed.

117 Khan et al. (2022), however, improves on their model of 5G planning by assigning a clustering  
118 algorithm to the task of deploying 5G base-stations into high data traffic areas. A K-Means algorithm  
119 has been utilized, using the Elbow heuristic as a benchmark. Not only does it deal with the coverage  
120 characteristics of the network, but also demonstrates an extensive study on its capacity dimensioning. The  
121 goal of the study is to decrease the network cost, as well as provide a more robust way to interpret the  
122 data for network planning decision.

123 Another paper that talks about coverage area optimization for 5G is found in Wang et al. (2020). It is  
124 mathematically complex, as the goal is to provide numerical solutions for the employment of Macro and  
125 Small Cells in 5G. Therefore, different clustering approaches are suggested by the authors, as well as  
126 models to prevent noise and interference. Numerical case examples are given for different scenarios and,  
127 as it deals with heterogeneous networks, the coverage simulations can be seen with generally one or two  
128 Macro Cells and several Small Cells around them.

### 129 Bioinspired Algorithm Hybridizations for Data Clustering

130 Jensi and Jiji (2015) have accomplished to generate a FPA hybrid with K-Means, a similar method to  
131 the study presented herein. In the paper, they present this technique to test and clusterize eight different  
132 datasets, with promising results. It is attested that the hybridization has given better average fitness results  
133 for all tests, thus proving it to be more efficient.

134 However, the hybridization process shown in the paper takes the current best solution in the FPA and  
135 executes a local search around it using the K-Means. This is different from the implementation we have  
136 provided, to be further explained in the Methodology section.

137 Hatamlou (2017) is another paper that deals with nature-inspired algorithms, with their proposed  
138 technique of utilizing Particle Swarm Optimization (PSO) with the Big Bang-Big Crunch (BB-BC). The  
139 objective, like in Jensi and Jiji (2015), is to provide an efficient method of data clustering, and both of  
140 them use five equal datasets (Iris, Wine, Glass, CMC, Cancer) in order to test their techniques. However,  
141 for all the same datasets, the PSO-BB-BC hybrid has shown better average fitness than its FPA-KM  
142 counterpart.

143 Another robust work in the subject is found in Logesh et al. (2020). Based on TripAdvisor travel  
144 recommendations data, the authors propose several hybrid solutions. These are based on swarm intelli-  
145 gence algorithms, such as an improved PSO model, Brainstorm Optimization (BSO), Quantum-Behaved  
146 Brainstorm Optimization (QBSO) and the Immune Genetic (IG) technique. In most cases, the best  
147 optimizer is the novel QBSO-IG hybrid that they have proposed themselves. This study also provides  
148 many details on recommendation systems and draws a comparison on many other papers that have dealt  
149 with its data clustering optimizations.

150 Khan et al. (2019) have proposed a clustering technique for Flying Ad-Hoc Networks (FANETs),  
151 named Bio-Inspired Clustering Scheme for FANETs (BICSF), that consist of organizing drones in the air  
152 based on their positioning and energy management. The goal is to reduce energy consumption, elevate  
153 the air time of the devices and minimize the time that the drones take to organize themselves into clusters.

154 The hybrid is between the glowworm swarm optimization (GSO) and krill herd (KH) algorithms, and it is  
155 tested against more commonly found bioinspired ones - Grey Wolf Optimization (GWO) and Ant Colony  
156 Optimization (ACO), to specify.

157 Pitchaimanickam and Murugaboopathi (2020) also proposes a hybrid approach for network clustering,  
158 however, with an emphasis on ameliorating battery life and information management in Wireless Sensor  
159 Networks. The creation of clusters itself is done by a LEACH-C algorithm, which is then optimized  
160 with a conjunction of a PSO and the Firefly Algorithm (FA). HFAPSO, as the hybridization is abbreviated,  
161 proves to be considerably more efficient than the separated techniques in a simulation of 100 sensors and  
162 an area of  $(100 \times 100) m^2$ . Results have shown that not only does it better coordinates the clusters, but it  
163 sustains the battery life of sensor nodes for longer.

164 Cao et al. (2021) demonstrates a heterogeneous Wireless Sensor Network (WSN) coverage area  
165 optimization, in which a Chaos-Improved Social Spider Optimization (CSSO) is used to accomplish the  
166 task. The solution aims to deploy the sensors by saving as much energy consumption and network cost as  
167 possible, as well as reducing coverage redundancy and trying to cover blind spots as best as possible.

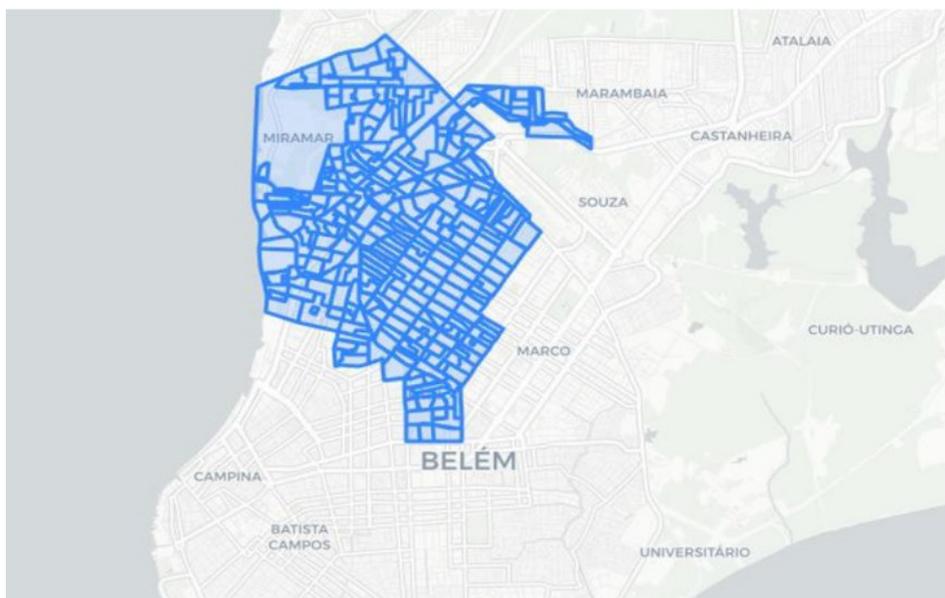
168 Lastly, a study that also uses K-Means in a hybrid bioinspired computing setting is conducted by  
169 Aswani et al. (2018). It is combined with a Firefly Algorithm, but also with a modified, Lévy flight  
170 and chaos-induced version of it (LFA-chaos). This clustering technique is then tested against a Fuzzy  
171 C-Means (FCM) algorithm, and its application is to find spam accounts on social media website Twitter.  
172 It uses many significant behavioral factors of the user as input to solve this problem, such as its hashtag  
173 frequency, number of mentions, tweet count, follower count and many more, up to a total of 13. The Lévy  
174 flight applied to this FA is similar to the one used in the FPA exposed in the Methodology section.

## 175 METHODOLOGY

176 In this section, details about the objectives, the methods and optimization techniques used in this study  
177 are elucidated.

178 In general terms, the aim of the study presented herein is to acquire real-life LTE user data from  
179 OpenCellid to aid in the deployment of 5G cells in a four-neighborhood area from the city of Belém,  
180 Brazil. The involved neighborhood names are Sacramento, Barreiro, Miramar and Pedreira, and the area  
181 is represented in Figure 1.

**Figure 1.** Area of interest inside Belém, Brazil.



182 For that matter, by selecting the LTE cells with the greater traffic according to OpenCellid data,  
183 and inspired by the data mining process of Khan et al. (2022), a total of 19 LTE cells were selected to  
184 provide the highest data traffic areas and aid our deployment proposal. Therefore, by taking learning data

185 from these cells, we have made a hybrid clustering/bioinspired technique that aims to solve the coverage  
186 problem in 5G frequency bands of 700 MHz, 2.3 GHz and 3.5 GHz.

187 Two problems to be optimized show up when thinking of providing coverage for a medium-to-high  
188 density urban area so large such as this: the number of  $k$  cells (or clusters of users) that is required to  
189 achieve a good user coverage percentage, and also, for matters of energy efficiency, how much power  $P_i$   
190 should be applied to these cells in order to reach the best coverage by spending less energy. Given that  
191 our approach aims to minimize both these variables, network costs should also be minimized throughout  
192 the process. So, a simulation with an  $N$  number of users normally distributed in the aforementioned area  
193 is drawn to test how much coverage the proposed metaheuristic setup will achieve.

194 The Methodology from here is separated in various subsections. Firstly, the bioinspired algorithms  
195 shall be revised, then an explanation on the K-Means clustering algorithm is given. Lastly, the hy-  
196 bridization process is explained, as well as the path loss propagation model for producing the objective  
197 functions.

198 In order to utilize multi-objective functions, the simplest way is to involve all objectives into a  
199 single mathematical sentence, as shown in (1):

$$f = \sum_{i=1}^n w_i f_i, \sum_{i=1}^n w_i = 1, \quad (1)$$

200 in which  $w_i$  are the weights given to each objective,  $f_i$  are the single objectives and the sum of all  
201 weights must be equal to 1.

### 202 Multi-Objective Cuckoo Search (MOCS)

203 The Cuckoo Search algorithm (CS) has been coined by Yang and Deb (2009), proving itself to be a very  
204 effective metaheuristic algorithm for all sorts of applications in mathematics, industry and engineering,  
205 according to Shehab et al. (2017). The main bioinspired idea behind this method is the computational  
206 modeling of the parasitic behavior of cuckoo-type birds, that often lay their eggs inside the nests of  
207 other types of birds. This is a natural occurrence in nature, as the host species often does not perceive  
208 the cuckoo's "alien" egg inside the nest, or either choose to ignore it completely or abandon the nest  
209 altogether, choosing another place to lay its eggs on. However, if the egg is ignored and left to grow inside  
210 the host bird's nest, the cuckoo hatchling is born, and reaches maturity much faster than the other eggs,  
211 pushing the host bird's eggs outward. Thus, the cuckoo baby bird expels the other eggs from the nest,  
212 resulting in a higher food share for it, and becoming well-fed.

213 Thus, the whole process is based upon three major rules:

- 214 1. Each cuckoo lays one egg at a time, and deposits it in a random nest. Each egg is considered a  
215 potential solution – metaheuristic
- 216 2. The best nests carry the best eggs (solutions), and these will survive the next generations due the  
217 parasitic nature of the cuckoo hatchlings – elitism.
- 218 3. The number of available nests is constant, and defined by the code developer. The probability of  
219 a cuckoo egg being discovered by the host bird is defined as  $Pa \in [0, 1)$ . After this, the bird may  
220 choose to discard this egg or abandon its nest – discarding the worst solutions.

221 The latter rule can also be described by indicating that a probability fraction  $Pa$  from the various  $n$   
222 nests of host birds are replaced by new nests, presenting randomized solutions.

223 The cuckoo birds in this method move according to the so-called Lévy Flights. This device provides a  
224 random flight path that which each cuckoo (in a number of  $i$  cuckoo birds) will trek to find nests. Equations  
225 (2) and (3) are a mathematical representation of the Lévy Flight and Lévy Distribution, respectively, to be  
226 implemented in code form:

$$X_i^{t+1} = X_i^t + \alpha \oplus Levy(\beta) \quad (2)$$

$$Levy(\beta) \cong u = t^{-(\beta+1)}; (1 < \beta \leq 3) \quad (3)$$

227 In which  $i$  is the maximum number of cuckoo birds in the current generation, and  $t$  is the current code  
228 iteration. Constant  $\alpha$  is the step size to be utilized in the code, and is adaptable to the developer's need –  
229 it must always be greater than zero, and in this study the value is set to  $\alpha = 1$ .

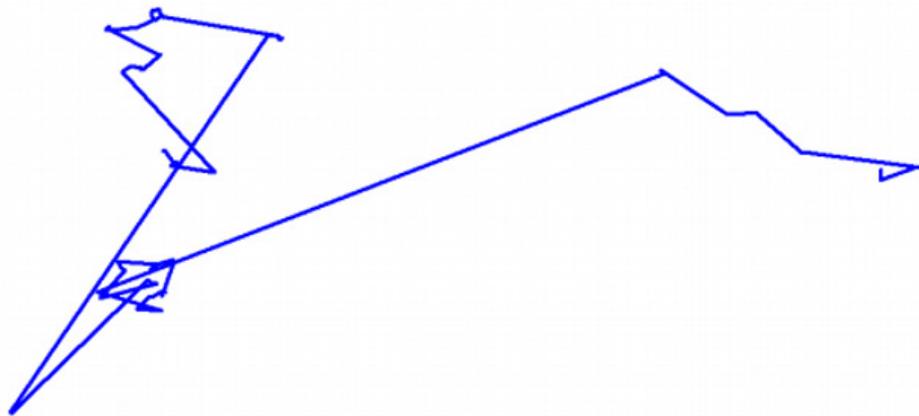
230 In equation (2), the Lévy Distribution is associated to the Lévy Flight with the product  $\oplus$ , which  
231 means “entrywise multiplication” – a kind of product between two matrices of the same size. In the PSO  
232 algorithm, a similar product can be found, however, for the Lévy Flight method, the search space can be  
233 much better harnessed.

234 As for equation (3), this is about the Lévy Distribution. It possesses infinite variance and average  
235 values. The variable  $\beta$  is the random step length, needed for providing a variable magnitude to the random  
236 walk performed by the Lévy Flight.

237 Given that the Lévy distribution presents infinite variance, the search space is virtually limitless,  
238 meaning that the length of the flight taken could be very short or incredibly long. However, generally,  
239 the new solutions are generated through the Lévy method around the best obtained solution on a given  
240 instant, accelerating the process and concentrating the computational effort in a part of the search space.  
241 Oftentimes, however, solutions are generated randomly across the space – this is good to prevent the  
242 algorithm from getting stuck in local optima, which are not the globally best possible solution.

243 An illustration showing a Lévy flight with around a hundred steps can be found in 2.

**Figure 2.** Representation of a 100-step Lévy flight in its search space



244 A pseudocode of the CS algorithm, as well as its multi-objective counterpart, can be found in the  
245 article in which it was proposed by Yang and Deb (2009). Below, in algorithm 1, a transcription of this  
246 code is presented.

**Algorithm 1** Multi-Objective Cuckoo Search Algorithm

Define the objective functions as  $f_n(x), x = (x_1, \dots, X_d)^t$   
 Generate the initial population of  $n$  host nests  $x_i (i = 1, 2, \dots, n)$

**while** ( $t <$  number of iterations) or (stop criterion) **do**  
   Select a cuckoo randomly via Lévy Flight (2)  
   Evaluate the cuckoo's fitness (represented by F)  
   Draft a random nest (say,  $j$ ) out of the  $n$  available  
  
   **if**  $F_i < F_j$  **then**  
     Replace randomly drafted  $j$  by the new solution  $x_i$   
   **end if**  
  
   Discard a fraction  $P_a$  of worse nests and build new ones  
   Keep the best / better quality solutions  
   Rank the best nest set and find the current best  
  
**end while**

Post-process and visualize results

247 **Multi-Objective Flower Pollination (MOFPA)**

248 A solution based on the behavior of natural flower pollinators has been proposed by Yang (2012), the  
 249 same author of the cuckoo search, which also utilizes the Lévy flight method of optimal space search. Its  
 250 efficiency, in many single and multi-objective applications is proven to be greater than Particle Swarm  
 251 and Genetic optimization algorithms. Its multi-objective counterpart has been proposed in 2013, also by  
 252 Yang et al. (2013).

253 As for the stages of the algorithm, four rules are defined thusly:

- 254 1. Biotic and cross-pollination is considered as global pollination process with pollen-carrying polli-  
 255 nators performing Lévy flights.
- 256 2. Abiotic and self-pollination are considered as local pollination.
- 257 3. Flower constancy can be considered as the reproduction probability and is proportional to the  
 258 similarity of two flowers involved.
- 259 4. Local pollination and global pollination is controlled by a switch probability  $p \in [0, 1]$ . Due to the  
 260 physical proximity and other factors such as wind, local pollination can have a significant fraction  
 261  $p$  in the overall pollination activities.

262 Two kinds of pollination are considered and simulated: global and local pollination. This assures  
 263 that the code does not only fall for local solutions, healthily seeking to encounter a global solution to the  
 264 objectives. For simplicity manners, the algorithm is based on the idea that every plant possesses only one  
 265 flower and can pollinate also just one other flower at a time, when in true biological terms they can hold a  
 266 few flowers and millions of pollinating gametes. This is so that a plant / flower / pollinating gamete are all  
 267 considered to be part of one solution altogether.

268 Hence, the first rule (global pollination) and third rule (flower constancy) of FPA are mathematically  
 269 represented as shown in (4):

$$X_i^{t+1} = X_i^t + L(X_i^t - g^*) \quad (4)$$

270 Where  $X_i^t$  is the pollen  $i$  or solution vector  $X_i$  at iteration  $t$ , and  $g^*$  is the current best solution among  
 271 all solutions at the current iteration.

272 Pollination strength  $L$  is dealt via Lévy flight, in which it is a measure of each flight's step size, as  
 273 denoted in (5). Here, the flights symbolize the path of insects and pollinator animals in a given area -

274 in the algorithm, this area is the optimization's global search space. However, the equation used in this  
 275 algorithm differs from the one found in cuckoo flights, as it is based on producing Lévy flights via the  
 276 Mantegna algorithm. This is basically a technique to generate pseudo-random step sizes via normal  
 277 distributions in order to provide an optimal performance whilst still maintaining the demands of the Lévy  
 278 distribution.

$$L \approx \frac{\lambda \Gamma(\lambda) \sin(\pi\lambda/2)}{\pi s^{1+\lambda}}, \quad (5)$$

279 in which  $\Gamma(\lambda)$  is the standard, classic gamma function found in Lévy flights, and other probabilistic  
 280 and complex number applications.

281 The Mantegna step size algorithm can be explained as the equation (6).

$$s = \frac{U}{|V|^{\frac{1}{\lambda}}}, \quad (6)$$

282 with  $s$  being the step size,  $U$  being drawn from a Gaussian distribution of variance  $\sigma^2$  and  $V$  also being  
 283 drawn from a Gaussian distribution but with unitary variance, as can be verified in Yang et al. (2014).  
 284 Generally, the lambda is treated as a parametric value and it is safe to assume that it is a constant with a  
 285 possible value of around  $\lambda \in [0.5, 1.5]$ . When  $\lambda = 1$ , the variance also equals 1, and results are in such  
 286 case easier to predict.

287 For the purpose of Rule 2 (local pollination), the flower constancy is mimicked for a limited neighbor-  
 288 hood near to the reproductive flower's position. It is represented as

$$X_i^{t+1} = X_i^t + \varepsilon(X_j^t - X_k^t), \quad (7)$$

289 where  $X_j^t$  and  $X_k^t$  are pollens from different flowers of the same plant species.

290 The fourth rule is a probabilistic switch between global and local pollination, and the probability  $p$   
 291 can be parametrically and singularly adjusted to improve optimization performance, depending on the  
 292 need of the objective function.

293 All stages of the algorithm are represented in pseudocode form by the recommendations in Yang  
 294 (2012), which are transcribed in algorithm 2. Some details previously discussed can be noticed, such as  
 295 an if/else switch for global and local pollination, which are done by Lévy flights and random selection,  
 296 respectively.

**Algorithm 2** Multi-Objective Flower Pollination Algorithm

Define the objective functions as  $f_n(x), x = (x_1, \dots, X_d)^t$   
 Generate an initial population of flowers/pollens as random solutions  
 Find, within this population, the best solution  $g_*$   
 Define the switch probability  $p \in [0, 1]$

**while** ( $t <$  number of iterations) or (stop criterion) **do**  
   **for** all  $n$  flowers in the population **do**  
     **if**  $rand < p$  **then**  
       Generate a step vector  $L$  which obeys a Lévy distribution  
       Execute global pollination as in (4)  
     **else**  
       Pick a uniformly distributed number from  $\varepsilon = [0, 1]$   
       Randomly choose individuals  $j$  and  $k$  from all solutions  
       Do local pollination according to (7)  
     **end if**  
  
     Evaluate new solutions  
     Update solutions that are better into the population  
  
   **end for**  
  
 Find the best current solution, represented by  $g_*$   
  
**end while**  
 Post-process and visualize results

297 **The K-Means Algorithm**

298 An unsupervised learning method of computational intelligence, the K-Means clustering algorithm has  
 299 the goal of grouping similar data points. Each of those  $k$  amount of clusters, then, possesses a centroid,  
 300 which is the mean value  $M$  of all positions of the data points. Due to being fast and easy to reproduce, it  
 301 is one of the most popular clustering algorithms. Sinaga and Yang (2020) defines the objective function of  
 302 K-Means according to the following equation:

$$J(A, Z) = \sum_{i=1}^n \sum_{k=1}^c z_{ik} \|x_i - a_k\|^2 \quad (8)$$

303 in which  $x_i$  is a data point  $i$  belonging to a dataset  $X = \{x_1, x_2, \dots, x_n\}$  spread over an Euclidean space  
 304  $\mathbb{R}^d$  of  $d$ -dimensions,  $a_k \in A = \{a_1, a_2, \dots, a_n\}$  is the centroid of the  $k$ -th cluster and  $z_{ik}$  is a binary variable  
 305 (either 0 or 1) that signals if the user  $i$  belongs to cluster  $k$ . Given that the objective function needs to be  
 306 minimized, the algorithm then proceeds to alter the centroids by also minimizing the Euclidean distance  
 307 between them and the data points that belong to them, according to (9):

$$a_k = \frac{\sum_{i=1}^n z_{ik} x_i}{\sum_{i=1}^n z_{ik}}, \quad z_{ik} = \begin{cases} 1, & \text{if } \|x_i - a_k\|^2 = \min_{(1 \leq k \leq c)} \|x_i - a_k\|^2. \\ 0, & \text{otherwise.} \end{cases} \quad (9)$$

308 where  $\|x_i - a_k\|^2$  is the Euclidean distance.

309 **The ECC-33 Propagation Model**

310 A channel path loss model is required to evaluate which users are connected to the network. This  
 311 propagation model should both belong to a frequency range where the 5G-NR channels are going to  
 312 be propagated, as well as adapt to the environment in which it shall be applied. For those reasons, an  
 313 ECC-33 model was chosen, which is adapted to the urban but forested environments of the city of Belém,  
 314 as proposed by de Carvalho et al. (2021).

315 ECC-33 is derived from the famous Okumura-Hata model, but taking into consideration the behavior  
 316 of higher frequencies, thus extending the frequency range. In Mollel and Michael (2014), experimental  
 317 results have been drawn by comparing different path loss models conducted in Dar es Salaam, Tanzania.  
 318 The COST-231 and ECC-33 models had the lesser Root Mean Square Error (RMSE), meaning that - for  
 319 urban, suburban and rural settings - they had the most approximate results to measured signal data.

320 Therefore, the model used in this work is defined thusly:

$$PL_{ECC} = A_{fs} + A_{bm} - GF_t - GF_r \quad (10)$$

321 in which  $A_{fs}$  is the free-space attenuation,  $A_{bm}$  is the base median path loss and  $GF_t$  and  $GF_r$  are  
 322 the transmitting antenna gain factor and received antenna gain factor, respectively. The values used for  
 323 the model correspond to the large city scenario, as all acquired data correspond to an urban region of  
 324 medium-to-high density. The following equations (11), (12), (13) and (14) further detail the variables of  
 325 the model:

$$A_{fs} = 92.4 + 20\log(d) + 20\log(f_c) \quad (11)$$

$$A_{bm} = 20.41 + 9.83\log(d) + 7.89\log(f_c) + 9.56(\log(f_c))^2 \quad (12)$$

$$GF_t = \log\left(\frac{h_{BS}}{200}\right)(13.958 + 5.8\log(d))^2 \quad (13)$$

$$GF_r = 0.759(h_{UE}) - 1.862 \quad (14)$$

326 in which  $f_c$  is the central frequency,  $h_{BS}$  is the base-station antenna height,  $h_{UE}$  is the user device's  
 327 antenna height. While  $d$  is the distance between a user and a base-station, that in this study is calculated  
 328 by the haversine distance formula, as it appears on Gade (2010) and Chopde and Nichat (2013):

$$d = 2R \arcsin \sqrt{\sin^2\left(\frac{\mu_2 - \mu_1}{2}\right) + \cos(\mu_1)\cos(\mu_2)\sin^2\left(\frac{\lambda_2 - \lambda_1}{2}\right)} \quad (15)$$

329 where  $\lambda$  are the latitudinal positions,  $\mu$  are the longitudinal positions, and  $R$  is the approximate radius  
 330 of the Earth ( $6.371 \cdot 10^6$  meters). Furthermore, the received power for an user is represented in (16):

$$P_r = P_t - PL_{ECC} + G_t + G_r, \quad (16)$$

331 in which  $G_t, G_r$  are the transmitting (Tx) antenna gain and receiving (Rx) antenna gain.

### 332 The Hybridization Process

333 In real-life scenarios, not often is the number of clusters to achieve optimal results is known beforehand.  
 334 For that, there are some heuristic methods that can be utilized to get approximations of how many clusters  
 335 one might need to satisfy an application. For instance, Khan et al. (2022) have chosen the Elbow heuristic.  
 336 However, given that one might need a more complex and sophisticated way of deciding how to cluster,  
 337 and how much to cluster, like in a scenario of network dimensioning and coverage area optimization,  
 338 these heuristics may not provide optimal solutions. This is why a metaheuristic method, like a bioinspired  
 339 algorithm, is more suited for this task. The hybridization of a clustering algorithm like K-Means and a  
 340 metaheuristic BIC means that both of those methods benefit from each other. The K-Means provides the  
 341 base-station coordinates on a given area, and the BIC provides the values of the ideal number of clusters,  
 342 taking into consideration multiple inputs that will decide how much clustering there must be. Figure 3  
 343 demonstrates the whole process of the study. Please notice how the K-Means processes a geographical

**Algorithm 3** The Hybrid K-Means + BIC Algorithm

Define the constant values of  $h_{BS}$ ,  $h_{UE}$ ,  $f_c$  and antenna gains  
 Initialize one of the bioinspired optimization techniques (MOCS or MOFPA)  
 Generate an initial population with random solutions for  $k$  clusters and  $P_{BSi}$  transmitted power

**while** (Iterations  $\leq$  Max Iterations) **do**

Initialize the K-Means for each  $k$  given by the BIC

**for** (all the clusters  $k$  in the K-Means) **do**

**for** (all the users associated to cluster  $k$ ) **do**

Calculate the distance between the user and its clusters' centroid via (15)

Calculate the ECC path loss, present in (10)

Calculate the received power  $P_r$  as in (16), with  $P_{BSi}$  given by the BIC

**if** ( $P_r \geq -90\text{dBm}$ ) **then**

Count the user as within the coverage area

**end if**

**end for**

**end for**

Calculate the percentage of connected users in relation to the total number of users

Evaluate, with the BIC, the outputs in a single objective function

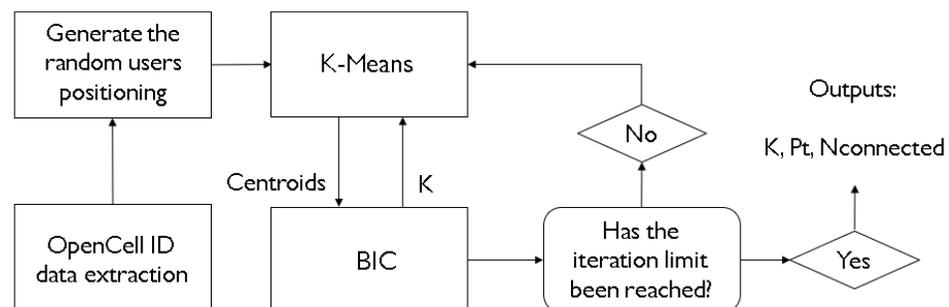
Update the best solutions into the population

**end while**

Post-process and visualize results

344 position for cluster centers and the BIC returns it a number of clusters to attempt and see if an optimal  
 345 result is reached. This process has the goal, in our study, to provide an optimal value of  $k$  clusters, as well  
 346 as a satisfactory transmitted power value.

**Figure 3.** Flowchart of the processes involved in this study



347 A pseudocode displaying the structure of the hybridization can be found in 3. For each iteration of  
 348 the BIC, the K-Means will run alongside it, providing cluster center (or centroid) values that the BIC  
 349 shall take and calculate the received power for each and every user, one cluster at a time. If the user  
 350 has a received power of -90 dBm or greater, it will be considered as connected to the network and, thus,  
 351 covered.

## 352 RESULTS

353 A total of 2000 users have been randomly generated within the simulated area where the Small Cells shall  
 354 actuate. This is to ensure that there are users in every corner of the area, and to assure that the clusters can  
 355 manage to provide coverage for them.

356 It is worth to denote that the received power threshold to consider a user as connected to its respective  
 357 cluster is  $P_r \geq -90\text{dBm}$ . This value has been chosen as a reasonable target for 5G mobile, heterogeneous  
 358 networks to main good signal strength and capacity. Furthermore, as per stated in Ayad et al. (2022),  
 359 values of between  $-100 \leq P_r \leq -80$  dBm are acceptable for this kind of application.

360 The objective function for the simulations can be defined as:

$$f = 0.7N_{outage} + 0.3P_{diff}, \quad N_{outage} = \frac{N_{users} - N_{connected}}{N_{users}}, \quad P_{diff} = P_t - 30, \quad (17)$$

361 in which  $P_{diff}$  is the difference of transmitted power to the ideal minimum value of 30 dBm,  $N_{users}$  is  
 362 the total number of users to be attended by the network,  $N_{connected}$  are the number of users connected to  
 363 the Small Cells and  $N_{outage}$  is the percentage of users which are experiencing outage (i.e. disconnected  
 364 from any cell). Therefore, the main objectives are to minimize the number of users that are excluded from  
 365 the network whilst maintaining the lowest transmitted power possible, that is,  $N_{outage} = 0$  and  $P_{diff} = 0$ .

366 The search space bounds on the number of clusters and transmitting power are:  $L_b = (1$  cluster, 30  
 367 dBm) and  $U_b = (100$  clusters, 40 dBm). These power values for  $P_t$  are the limits generally found in Small  
 368 Cells, as stated by Khan et al. (2020). So, the objective for  $P_t$  is to approach its minimum value, that is,  
 369  $P_t = 30\text{dBm}$ . It also can be noticed that, since the main goal of the study is to achieve better coverage for  
 370 users in 5G networks, there is a 0.7-0.3 weight towards coverage over transmitted power optimization in  
 371 the objective function (17).

372 Table 1 refers to the constant and variable values that have been coded into the algorithms and the  
 373 propagation model:

Parameters	Values
Tx antenna height ( $h_{BS}$ )	40 m
Rx antenna height ( $h_{UAV}$ )	1.6 m
Tx antenna gain	3 dBi
Rx antenna gain	0 dBi
Central frequencies ( $f_c$ )	[700 MHz, 2.3 GHz, 3.5 GHz]
Number of clusters (k) bounds	1 to 100 clusters
Transmitted power ( $P_t$ ) bounds	30 to 40 dBm
Nest discard probability (for MOCS)	0.25
Switch probability (for MOFPA)	0.5

**Table 1.** Values of interest for the simulations

374 The simulation and its algorithms have been coded in MATLAB, and are run on a personal computer  
 375 with these characteristics: AMD Ryzen 3 CPU with 3.7 GHz clock and 16GB DDR4 RAM.

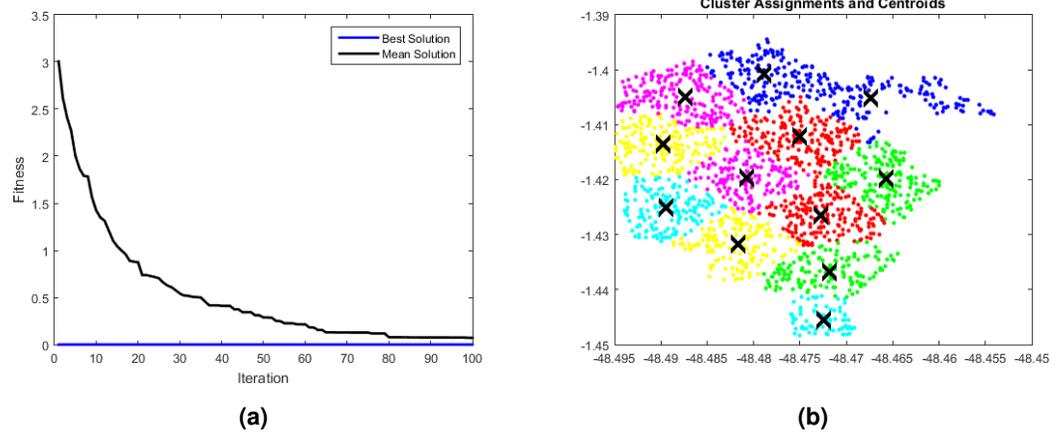
### 376 Results for 700 MHz

377 Firstly, Figures 4 and 5 display the results achieved for the 700 MHz frequency band for, respectively, the  
 378 MOCS-KM and MOFPA-KM. This is a band that possesses a fairly low data rate and bandwidth, but since it  
 379 is one of the auctioned bands for 5G operation in Brazil, it is included here as means of comparison and  
 380 to test the BIC + K-Means hybrids.

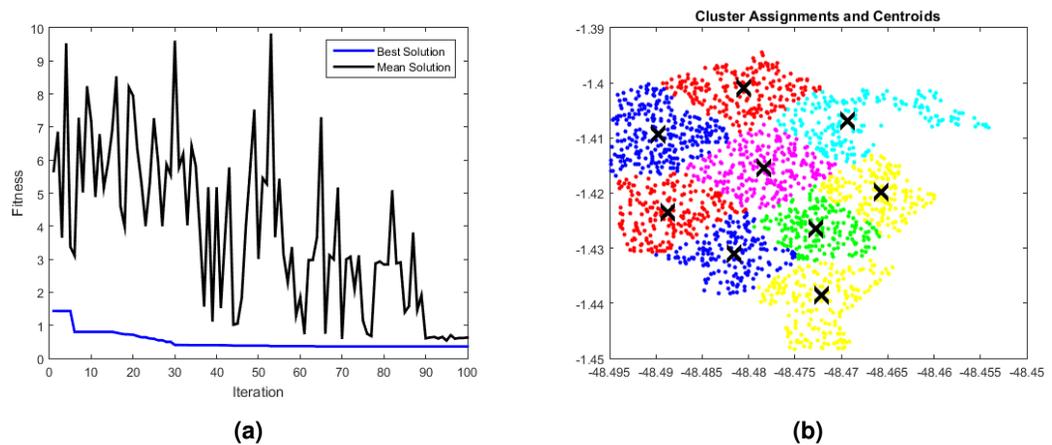
381 The X symbols in the figures displaying the clusters are referent to the position of centroids, and the  
 382 colored dots correspond to the users.

383 Here, the algorithm had no problems whatsoever in optimizing for zero fitness, needing only a few  
 384 iterations to converge. This is because path loss is less intense for lower frequencies, and so a small group  
 385 of small cells can already provide perfect coverage.

386 The best solver in this case is MOCS-KM, with a solution of 12 clusters and power of 30dBm.  
 387 However, MOFPA-KM comes very close to a zero fitness value as well, with an inferior number of  
 388 clusters of only 9 and 30 dBm power.



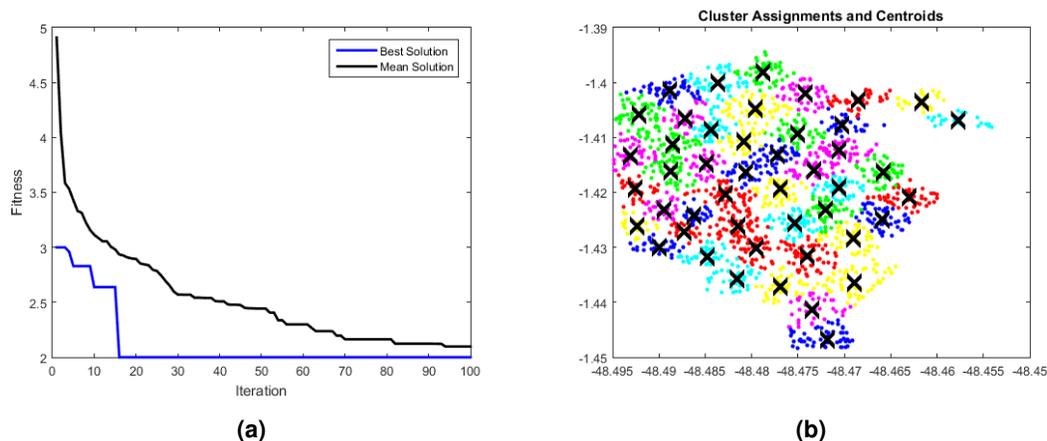
**Figure 4.** Results for 700 MHz: (a) Fitness plot of MOCS-KM and (b) Cluster formation given by the technique



**Figure 5.** Results for 700 MHz: (a) Fitness plot of MOFPA-KM and (b) Cluster formation given by the technique

### 389 Results for 2.3 GHz

390 The band that promises to function both in LTE and in 5G is shown next. Figures 6 and 7 are the results  
 391 for the 2.3 GHz frequency band. It is expected to operate in smaller cities as a means of digital inclusion,  
 392 providing more bandwidth to 4G-LTE demands, or in urban centers as a complementary traffic alternative  
 393 to the main band of 5G, which is 3.5 GHz.

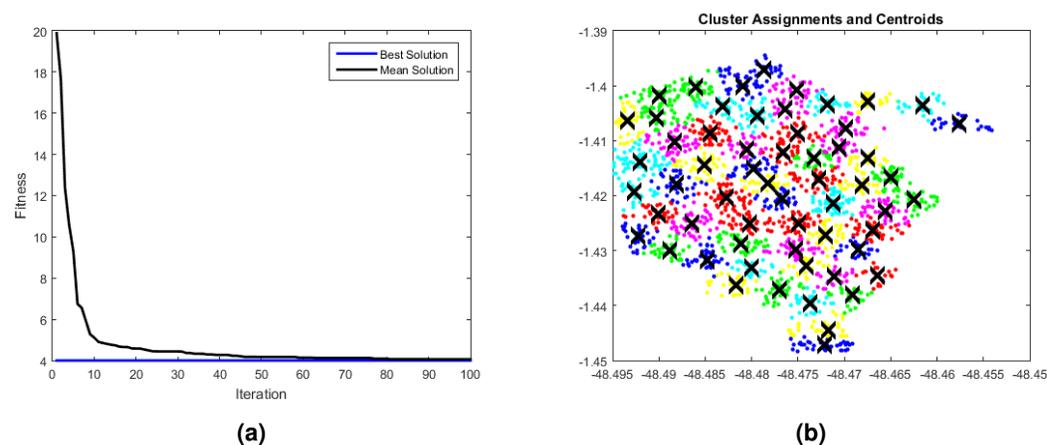


**Figure 6.** Results for 2.3 GHz: (a) Fitness plot of MOCS-KM and (b) Cluster formation given by the technique

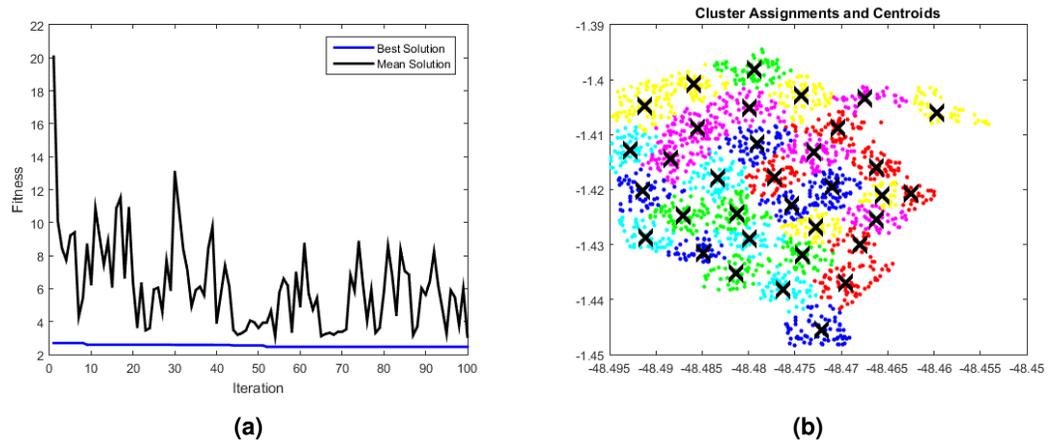
394 Results for this band are already harder to solve than 700 MHz, with the best fitness results coming  
 395 from MOCS-KM once again. It has achieved  $f_{best} = 2$ , with 46 clusters and a satisfactory transmitted  
 396 power of 31 dBm. MOFPA-KM has proposed a higher  $P_t$  value with less clusters, resulting in  $f_{best} =$   
 397  $2.4267$ ,  $k = 34$ , and  $P_t = 33.3352$  dBm.

### 398 Results for 3.5 GHz

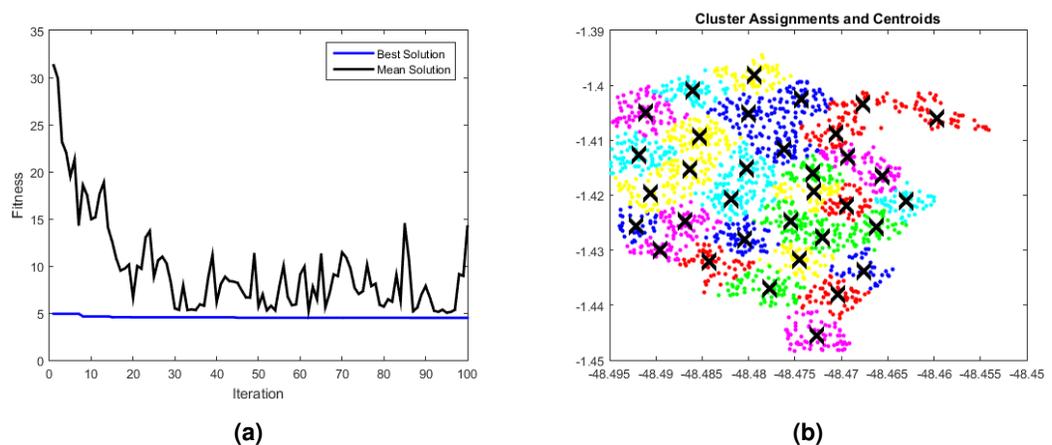
399 Finally, the main and most used frequency band of 5G. The 3.5 GHz spectrum possesses up to 80 MHz of  
 400 band per operator in Brazil, and is set to expand in highly-urbanized areas, as it can handle greater traffic  
 401 and provide faster data rates than the other two. Figures 8 and 9 demonstrate the results of the simulation  
 402 for this frequency.



**Figure 8.** Results for 3.5 GHz: (a) Fitness plot of MOCS-KM and (b) Cluster formation given by the technique



**Figure 7.** Results for 2.3 GHz: (a) Fitness plot of MOFPA-KM and (b) Cluster formation given by the technique



**Figure 9.** Results for 3.5 GHz: (a) Fitness plot of MOFPA-KM and (b) Cluster formation given by the technique

403 For this case, the results are basically the same in terms of coverage, but fitness values turn greater  
 404 because of the choice in both algorithms to utilize more transmitted power instead of increasing the  
 405 number of clusters too much. In terms of fitness, MOCS-KM marginally wins again, with  $f_{best} = 4.006$ .  
 406 That being said, MOFPA-KM has converged to a solution with 34 clusters again - the same number from  
 407 the 2.3 GHz simulation. It has, however, increased the transmitted power to its maximum value of 40  
 408 dBm in order to achieve that.

#### 409 Table of Results

410 In Table 2, results for the optimization processes of MOCS-KM and MOFPA-KM hybrids are shown. For  
 411 the best generated population (the one which produced  $f_{best}$ ), it records the maximum, medium and best  
 412 fitness values, as well as the outputs and the running time of the respective simulations.

#### 413 CONCLUSIONS

414 Smart cities will bring forth many future challenges, and this work proposed a novel Small Cell positioning  
 415 system using a hybrid approach to provide better user coverage and to save more energy. The presented  
 416 scheme deals with a method of clustering and optimizing for the implementation of 5G Small Cells  
 417 according to user traffic, using the city of Belém, Brazil as a simulational example. Optimization was  
 418 provided by the two hybrid methods, MOCS-KM and MOFPA-KM.

Simulation	$k$	$P_t$	$N_{outage}$	$P_{diff}$	$f_{max}$	$f_{avg}$	$f_{best}$	Time (s)
700 MHz (MOCS-KM)	12	30	0	0	0.7892	0.1327	0	886
700 MHz (MOFPA-KM)	9	30	0.5133	0	1.9397	0.6075	0.3593	992
2.3 GHz (MOCS-KM)	46	31	2.4285	1	10.9882	2.1649	2	1542
2.3 GHz (MOFPA-KM)	34	33.3352	2.0373	3.3352	4.7515	2.7564	2.4267	1558
3.5 GHz (MOCS-KM)	59	38	2.2857	8	5.5686	4.1163	4.006	1637
3.5 GHz (MOFPA-KM)	34	40	2.0421	10	6.3954	4.7312	4.4295	2804

**Table 2.** Results for each best iteration of the hybrid techniques.

419 In general the simulations were satisfactory, as user outage is never greater than 2.5% for all cases,  
 420 making the amount of connected users over 97%. Transmitted power levels have been kept within Small  
 421 Cell ranges, providing good implementation opportunities. That being said, the techniques have a sort of  
 422 preference that differentiate themselves. In Table 2, it can be denoted that MOCS-KM prefers to increase  
 423 the amount of clusters to reduce the transmitted power, whilst MOFPA-KM is the opposite.

424 Therefore, the usage of said hybridizations should be a matter of preference for the network planner  
 425 professional that intends to use them. For coverage optimization both present similar and adequate results,  
 426 but MOFPA-KM keeps cluster numbers to a bare minimum and optimizes for greater power usage;  
 427 and MOCS-KM is a bit more precise and uses less power per cluster but produces a higher amount of  
 428 clustering. So, these variables are bound to limitations and cost of implementation issues that are up to  
 429 which of those are less costly to produce.

430 Further challenges to enrich the study would be to implement more 5G capacity variables into the  
 431 simulation. The focus of this paper has been mostly on coverage problems, but there is much to add in  
 432 concern to capacity dimensioning according to the problems found in many papers present throughout our  
 433 study, mainly in Shayea et al. (2020) and Ouamri et al. (2020). Further opportunities for research involve  
 434 further minimization and measurement of network cost and maximizing throughput of data per area, as  
 435 per the work of Khan et al. (2022) manages to accomplish.

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