

Millimeter-Wave Channel Modeling in a VANETs using Coding Techniques

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Vehicular ad-Hoc Network (VANET) is envisioned to ensure wireless transmission with ultra-high reliability. In the presence of fading and mobility of vehicles, error-free information between Vehicle to Vehicle (V2V) and Vehicle to Infrastructure (V2I) requires extensive investigation. The current literature lacks in designing an ultra-reliable comprehensive tractable model for VANET using millimeter wave. Ultra-reliable communication is needed to support autonomous vehicular communication. This article aims to provide a comprehensive tractable model for Vehicular ad-Hoc Network (VANET) over millimeter waves using Space-Time-Block-Coding (STBC) concatenated with Reed Solomon (RS) coding. The designed model provides the fastest way of designing and analyzing VANET networks on 60 GHz. By using the derived BER expressions and Reed Solomon coded Doppler expression ultra-reliable vehicular networks can be build meeting the demands of massive growing volume of traffic. The performance of the model is compared with previous BER computational techniques and existing VANET communication systems, i.e. IEEE 802.11bd and 3rd Generation Partnership Project Vehicle to Everything (3GPP V2X). The findings show that our proposed approach outperforms IEEE 802.11bd and the results are comparable with V2X NR. Packet Error Rate (PER), Packet Reception Ratio (PRR) and throughput are used as performance metrics. We have also evaluated the model on higher velocities of vehicles. Further, the simulation and numerical findings show that the proposed system surpass the existing BER results comprising of various modulation and coding techniques. The simulation results are verified by the numerical results there-by, showing the accuracy of our derived expressions.

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14 **ABSTRACT**

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17 (V2V) and Vehicle to Infrastructure (V2I) requires extensive investigation. The current literature lacks in
18 designing an ultra-reliable comprehensive tractable model for VANET using millimeter wave. Ultra-reliable
19 communication is needed to support autonomous vehicular communication. This article aims to provide
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24 be build meeting the demands of massive growing volume of traffic. The performance of the model is
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27 show that our proposed approach outperforms IEEE 802.11bd and the results are comparable with V2X
28 NR. Packet Error Rate (PER), Packet Reception Ratio (PRR) and throughput are used as performance
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33 **INTRODUCTION**

34 In recent years, there has been significant demand for communication in Vehicular ad-Hoc Network
35 (VANET) at high data rates. To meet the enormous communication demand in VANET, it is necessary
36 to utilize the scarce resources, such as power and bandwidth, as effectively as feasible. Reliability,
37 throughput, and accuracy are significant factors because of multipath fading and the rapid mobility of
38 vehicle nodes. VANET communication system is susceptible to a certain level of noise, shadowing and
39 fading. The Line of Sight (LOS) obstruction by vehicles results in an extra loss of the received power
40 of approximately 10 dB (abbas2015measurement). In (va2016millimeter) atmospheric attenuation at
41 60 GHz is studied for number of vehicles, which is 15dB/km and excessive path loss of 30 dB occurs
42 for three obstructing vehicles. Analytical research on a Markov chain model is used in VANETs to
43 examine the impact of channel fading on IEEE 802.11p. The performance is evaluated on Nakagami-m,
44 Rayleigh, and Rician fading channels using BER (shah2022influence). Highly mobile vehicular nodes
45 and rapidly changing network topology throws many challenges in the dissemination of critical messages
46 in VANET (giripunje2022routing). Furthermore, the multipath propagation also leads to signal distortion

and burst errors. Therefore, transmission reliability is very challenging in wireless channels. Forward Error Correction (FEC) is one of the most commonly used techniques to provide reliable communication. The new Task Group TGbd was recently formed with the goal of exploring the future road map for Vehicle to Everything (V2X) and working towards a new standard known as Next-Generation V2X (NGV). 802.11bd is an 802.11p modification that specifies changes to the IEEE 802.11 Medium Access Control (MAC) and Physical Layer (PHY) layers for V2X communications in the 5.9 GHz and 60 GHz frequency bands. Currently, millimeter-wave (mmWave) massive Multi-Input Multi-Output (MIMO) is the most potential technology for vehicular communication (yi2020novel). The mmWave signals are susceptible to high free-space path loss caused by high atmospheric attenuation (shen2019channel). Beamforming techniques are used in mmWave systems to mitigate the effects of large path losses by providing enough channel space (kuty2015beamforming). The traditional MIMO system performance is enhanced due to multiple antennas systems at both links end. Thus providing an effective solution for future wireless communications systems as they provide high data rates. Beamforming signal processing techniques enable transmission and reception in the needed directions by applying appropriate antenna port phases and amplitudes by using what is known as the "weighting approach". An adaptive algorithm instantly calculates the complex weights w_k to steer the null antenna pattern toward competing signals and the maximum antenna radiation pattern toward the chosen vehicular node. In this research work, a VANET architecture is proposed using concatenated Space Time Block Coding - Reed Solomon (STBC-RS) coding in which the reliability of VANET communication is targeted. Error control coding technique using mmWave for minimizing errors is still a topic for rigorous investigation. Currently for ITS 5G communication, ultra-reliable networks are required meeting the demands of $1-10^{-5}$ as indicated in (ghafoor2020millimeter). Moreover autonomous vehicles require reliable connectivity $1-10^{-7}$ (schulz2017latency).

Rayleigh fading channel is used in the proposed approach to model the fading characteristics of the channel. Because signal amplitude follow Rayleigh distribution when the line of sight (LOS) component gradually diminishes in Vehicle to Vehicle (V2V) communication. Rayleigh fading is most suitable in congested city roads, as concluded as a result of extensive simulations (jameel2017performance).

Contributions

The main contributions of this study are as follows:

- An ultra-reliable manipulable mathematical model is presented using RS coding along with 4*4 STBC. Transmit beamforming is employed by a complex weight expression of beamforming in the model.
- Two closed-form expressions for RS coding in the AWGN channel and in Rayleigh fading are derived. The numerical and simulation results have been obtained, which also verify our theoretical formulations.
- The results show that AWGN BER approximation outperforms conventional 64-QAM and M-PSK systems.
- The results also show that the proposed approach outmatched previous BER computation approaches i.e, (al2017enhancing), (mergu2016performance), (Tiwari2013BERPO), (indoonundon2021overview), (saleh2019improving), (hajiyat2019channel), (hamarsheh2022robust) shown in results and discussion section.
- The performance of the proposed model is compared with IEEE 802.11bd and V2X NR. The Packet Error Probability (PEP), throughput and Packet Reception Ratio (PRR) are used as performance metrics. The results are compared in Table 4, Table 5 and Table 6. On comparing, it can be remarked that the proposed model outperforms IEEE 802.11bd. For designing V2X architectures RS error control coding performs better.
- MIMO-STBC along with RS can be used as a physical layer advancement technique in 802.11bd.
- We have also evaluated our results on higher velocities, achieving the BER of 10^{-6} to 10^{-7} . Atlast the designed model is meeting the demands of ultra-reliability i.e $1-10^{-5}$ which is .99999.

RELATED WORK

In (abuqamar2021stbc) STBC was combined with Orthogonal Frequency Division Multiplexing with Sub carrier-Power Modulation (OFDM-SPM) to analyze combination on a multi-path Rayleigh fading channel. BER and throughput were used as a performance metrics. It was concluded that using STBC the performance of original OFDM-SPM can be improved in terms of reliability. In ((indoonundon2021overview) to achieve ultra-reliable low latency communication in 5G, a detailed analysis of coding schemes was conducted. LDPC, polar codes, turbo codes were simulated using Quadrature Amplitude Modulation (16QAM) and 64QAM. In this work, lower BER is obtained on increasing modulation order M in QAM modulation. RS coding was used in Cooperative-Intelligent Transport System (C-ITS) communications. The performance was analyzed and compared with Wyner–Ash codes. The result showed RS code outperformed with Wyner–Ash codes. Our designed model and derivations can be used in various C-ITS communications (bocharova2019low). RS performance was evaluated using STBC-MIMO systems concatenated with M-ary Quadrature Amplitude Modulation (M-QAM) and M-ary Phase-Shift Keying (MPSK) ((mane2020evaluation). The performance of existing Cooperative MIMO (C-MIMO) was improved using C-MIMO-STBC (hai2021space). It has been proved that wireless link quality can be improved by MIMO STBC while keeping transmitted power or frequency bandwidth constant. The performance of IEEE 802.11p was improved by implementing Multiple Input Single-Output (MISO) with Orthogonal Frequency-Division Multiplexing (OFDM) system. The authors analyzed the impact of time-varying channel on the performance of Alamouti STBC in OFDM systems ((youssefi2020performance). 802.11p could not offer multi antenna communication. STBC-OFDM was used to analyze the performance of multi antennas. We have used STBC-RS channel model for improving reliability in VANET communication. In (triwinarko2021phy) LDPC along with Multi-Input Multi-Output-Space Time Block Coding (MIMO-STBC) was used to improve the physical layer of 802.11p. STBC was combined with Orthogonal Frequency Division Multiplexing with Sub carrier-Power Modulation (OFDM-SPM) to analyze combination on a multi-path Rayleigh fading channel. BER and throughput were used as a performance metrics. It was concluded that using STBC the performance of original OFDM-SPM can be improved in terms of reliability. RS code was combined with Spatial Modulation (SM) and STBC along with cooperated source and relay (zhao2022optimized). Two closed-form approximations for BER Bose–Chaudhuri–Hocquenghem (BCH) coding and Alamouti Space Time Block Coding (BCH-ASTBC) were proposed for millimeter-wave VANET communication. The performance of conventional ASTBC equation was improved and the results were compared on different code rates (electronics10090992). The performance of WDM using M-ary DPPM schemes was enhanced under Amplified Spontaneous Emission (ASE) noise effects, Interchannel Crosstalk (ICC), and Atmospheric Turbulence (AT) (el-sayed2022performance). Due to multi-path fading and vehicle mobility, VANET communication is difficult in terms of reliability and throughput. The high mobility of vehicular communications, randomness in channel dynamics, and link interference are all significant challenges for vehicular networking. Many approaches have been investigated in this context to improve the efficiency of V2V and V2I communication. Researchers have expressed interest in using cooperative communications within vehicular networks to mitigate the impact of these challenges and improve reliability by allowing nodes to collaborate (ahmed2018cooperative). Spatial multiplexing MIMO was employed by modifying the existing IEEE 802.11p standard for high throughput. Spatial multiplexing MIMO supports real-time data transfer in a non-line-of-sight environment (dey2020high). Cochannel interference degrades the system performance of mmWave radars mounted on vehicles. VANET-assisted interference mitigation approach was proposed that enables vehicles to coordinate their spectrum usage via multiple access. The proposed scheme was tested via a case study to show that the proposed scheme is useful in dense traffic with high mobility of vehicles (zhang2020vanet). MIMO systems are reliable and have high capacity. A beamformer transceiver design was proposed for the MIMO Orthogonal Frequency-Division Multiplexing (OFDM) system. It was used for highly reliable and spectrally efficient operation under the most damaging jamming attacks (jagannath2020high). In (ali2019simulation) an architecture using massive MIMO was proposed. In the proposed architecture, vehicles are controlled using Global System Mobile (GSM) towers. GSM towers are equipped with 5G technology where towers can send and receive real-time information like the weather forecast, current temperature and city situation that comes under tower’s control. The diversity gain was obtained by the STBC in wireless communication. The basic idea of exploiting

transmit diversity was first developed by Vahid Tarokh and then a simpler structure was later introduced by Alamouti. Later on, Alamouti's work was extended and developed to originate space time block codes. Full Duplex Non-Orthogonal Multiple Access (NOMA)-MIMO was employed in V2X systems and closed-form approximations for ergodic capacity were derived (zhang2019performance). The transmission of multiple copies of data stream via the number of antennas can be achieved using Space-time block codes MIMO. MIMO systems are used to improve data-transfer reliability by utilizing the various received data versions. The decoding algorithm is simple in nature and accomplishes full diversity specified by the number of transmit antennas at a radio receiver. STBC are complex and have same key features like Alamouti. Further, their encoding and decoding schemes are also similar (santumon2012space). The data stream is first encoded in blocks when using STBC. These data blocks are then distributed across multiple antennas that are spaced apart. In (ehsanfar2022performance), the performance of three different frame structures of IEEE 802.11p, IEEE 802.11bd-draft, and a Unique-Word (UW)-based physical layer (PHY) were compared for vehicle-to-everything communication. Based on simulation results, it was determined that the UW-based PHY achieved interference-free channel estimation performance using a low complexity technique. IEEE 802.11p does not perform well for high mobility networks. It uses Distributed Coordination Function (DCF) for communication between wireless nodes. In (hussain2017efficient), a RSU-based efficient channel access scheme was proposed for VANETs under high traffic and mobility.

PROPOSED MODEL

A system model for VANET communication is described in Figure 1 in which V2V and Vehicle-to- Road Side Unit (V2RSU) communication occurs. The sensors placed on vehicles receive information via four receiving antennas. The received information is passed to the Data Fusion Unit which comprises of RS and STBC, where the received information via multiple antennas is fused. The information is sent to Distributed Processing Unit, where the data is processed and then it is transferred to other vehicle.

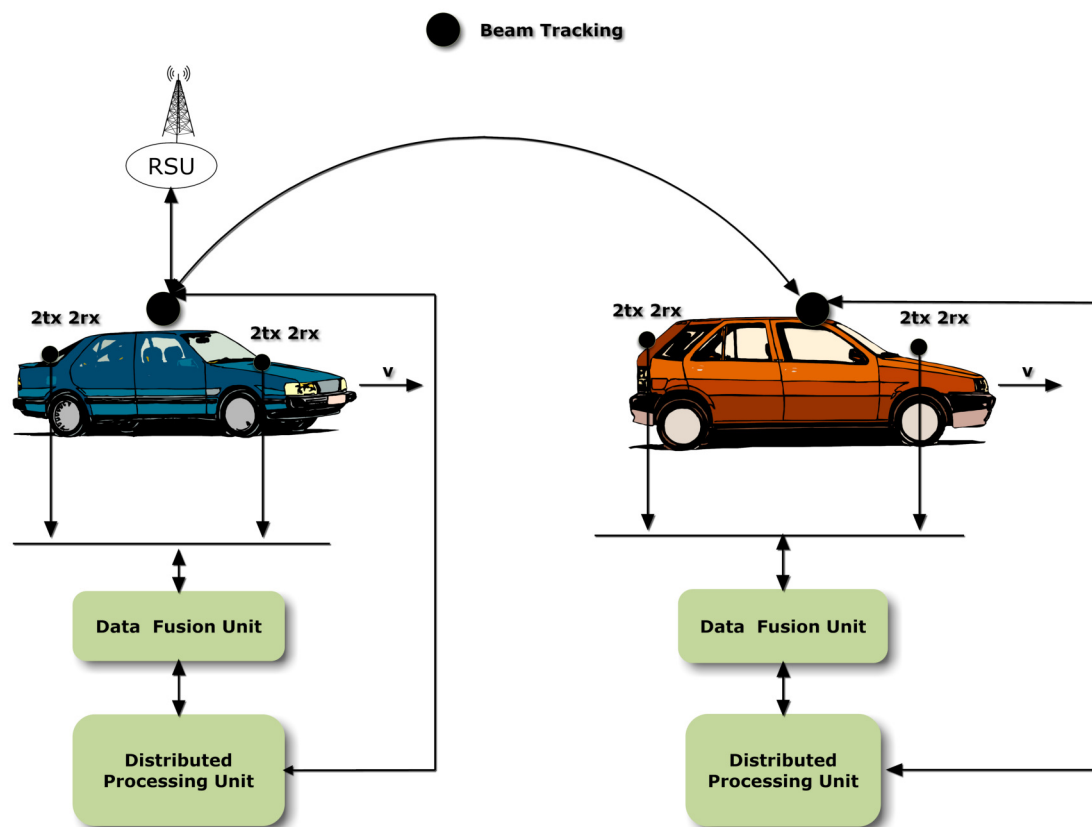


Figure 1. System Model for RS-STBC

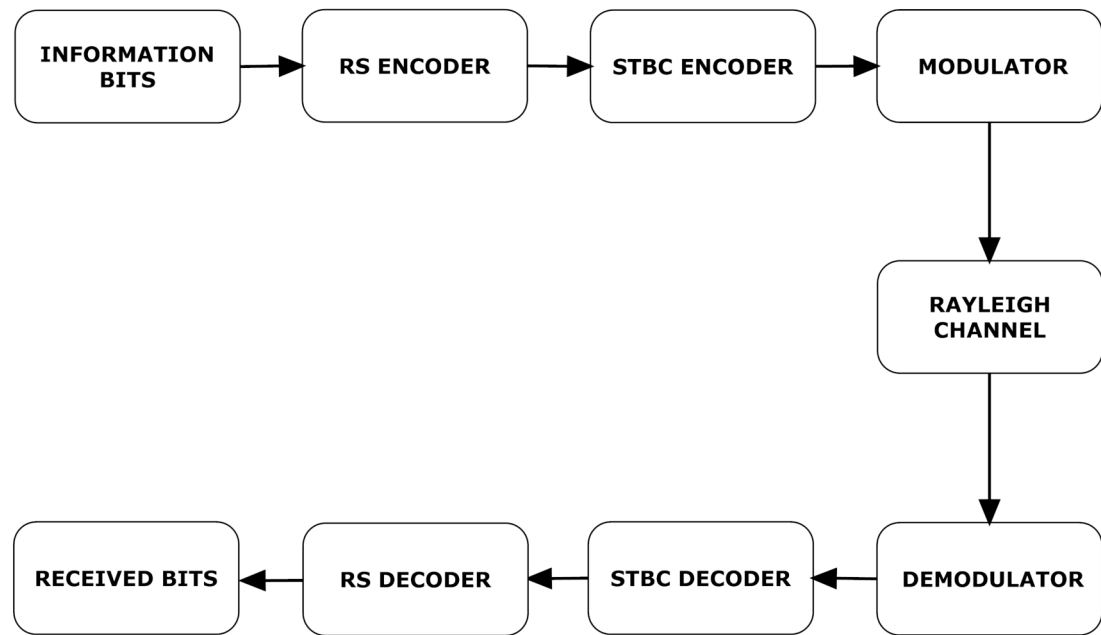


Figure 2. VANET Communication Process

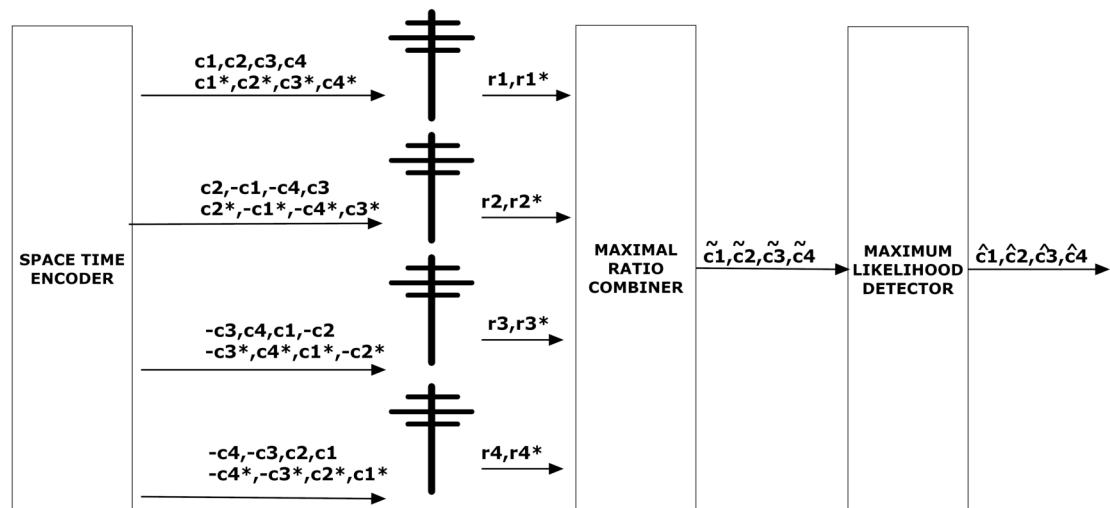


Figure 3. STBC Encoder and Decoder

177 A detailed communication process is illustrated in Figure 2. Information bits are encoded with RS
 178 encoder. Let $i(x)$ denote information bits and $g(x)$ denote generator polynomial. RS encoded bits can be
 179 written as,

$$c(x) = i(x)g(x)$$

180 where $c(x)$ represents RS encoded message bits. Now $c(x)$ is transmitted via four transmitting antennas
 181 using STBC coding. These signals are modulated and transmitted through a channel.

Figure. 3 depicts the STBC encoder and STBC decoder. STBC decoder comprises of Maximal Ratio Combining (MRC) and Maximum Likelihood (ML) respectively. Since there are four receivers in the

system model, each receiver will receive either 0 or 1. The received signals can be represented as,

$$\begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_5 \\ r_6 \\ r_7 \\ r_8 \end{bmatrix} = \begin{bmatrix} c_1 & c_2 & c_3 & c_4 \\ -c_2 & c_1 & -c_4 & c_3 \\ -c_3 & c_4 & c_1 & -c_2 \\ -c_4 & -c_3 & c_2 & c_1 \\ c_1^* & c_2^* & c_3^* & c_4^* \\ -c_2^* & c_1^* & -c_4^* & c_3^* \\ -c_3^* & c_4^* & c_1^* & -c_2^* \\ -c_4^* & -c_3^* & c_2^* & c_1^* \end{bmatrix} \times \begin{bmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \end{bmatrix} \times \begin{bmatrix} w_1 \\ w_2 \\ w_3 \\ w_4 \end{bmatrix}$$

where w represents transmit beamforming weight vector i.e $w=[w_1,w_2,w_3,w_4]^T$ and $[h_1,h_2,h_3,h_4]^T$ is channel response.

In the above matrix, signals transmitted and received by four antennas are mentioned in Figure. 3. The output of the MRC in Figure 3 is explained in equation (4). Above matrices can be written as,

$$\begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_5 \\ r_6 \\ r_7 \\ r_8 \end{bmatrix} = \begin{bmatrix} h_1 & h_2 & h_3 & h_4 \\ -h_2 & h_1 & -h_4 & h_3 \\ -h_3 & h_4 & h_1 & -h_2 \\ -h_4 & -h_3 & h_2 & h_1 \\ h_1^* & h_2^* & h_3^* & h_4^* \\ -h_2^* & h_1^* & -h_4^* & h_3^* \\ -h_3^* & h_4^* & h_1^* & -h_2^* \\ -h_4^* & -h_3^* & h_2^* & h_1^* \end{bmatrix} \times \begin{bmatrix} c_1 \\ c_2 \\ c_3 \\ c_4 \end{bmatrix} \times \begin{bmatrix} w_1 \\ w_2 \\ w_3 \\ w_4 \end{bmatrix}$$

which can be represented as,

$$\bar{r} = H_{\text{ef}} C \bar{w} \quad (1)$$

182 In equation (1) H_{ef} is effective channel response.

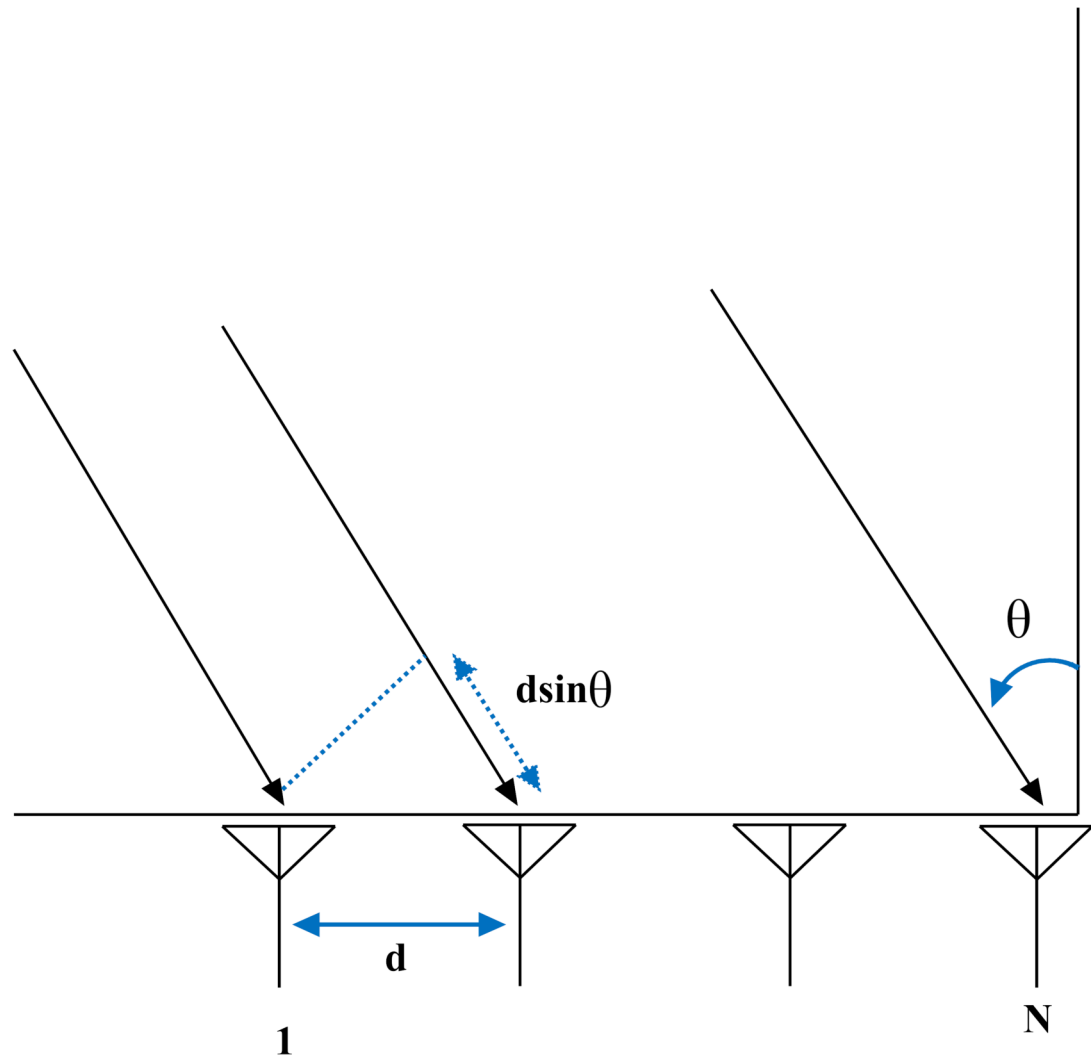


Figure 4. Beamforming in VANET

Corresponding weights w_i can be described below where w_i represents array factor and amplitude weight are applied by w_b (stepanets2019beamforming),

$$w_i = \sum_{b=1}^N w_b \exp^{jN\psi} \quad (2)$$

Equation (2) can be further simplified to normalized equation (3).

$$|w_i|^2 = \frac{1}{N} \left| \frac{\sin(\frac{N\sin\psi}{2})}{\sin\frac{\psi}{2}} \right| \quad (3)$$

where N represents the transmitting antennas, and ψ corresponds to the far-zone phase difference between adjacent elements, which can be calculated using the expression below (whitemillimeter).

$$\psi = s d \sin \theta \sin \phi + \Delta \psi$$

where θ represents angle of arrival described in Table 1 and ϕ represents angle of reflection. s corresponds to periodicity of complex weight which is $s = 2\pi/\lambda$ and d represents equidistant spacing between elements N as described in Figure. 4. $\Delta \psi$ can be computed using beam steering formula as follows.

$$\Delta \psi = \frac{2\theta}{\lambda}$$

The main lobe of an antenna array can be steered to a certain angle θ using phase offset $\Delta\psi$. ϕ is computed using expression $\phi = \pi \sin \theta$.

Maximal Ratio Combining (MRC) at Receiver End

In MRC, multiple receivers are used for signal reception. Equation (4) describes the relation between the signal arrived at MRC and transmitted by the MRC to ML (pericsoarua2012ber).

$$\tilde{c} = H_{ef}^H r \quad (4)$$

In equation (4) \tilde{c} is output of MRC (four output signals), r represents input of MRC and H_{ef}^H corresponds to Hermitian matrix of effective channel response (pericsoarua2012ber).

Equation (4) can be written as,

$$\begin{bmatrix} \tilde{c}_1 \\ \tilde{c}_2 \\ \tilde{c}_3 \\ \tilde{c}_4 \end{bmatrix} = \begin{bmatrix} h_1^* & h_2^* & h_3^* & h_4^* & h_1 & h_2 & h_3 & h_4 \\ h_2^* & -h_1^* & -h_4^* & h_3^* & h_2 & -h_1 & -h_4 & h_3 \\ h_3^* & h_4^* & -h_1^* & -h_2^* & h_3 & h_4 & -h_1 & -h_2 \\ -h_4^* & -h_3^* & h_2^* & -h_1^* & -h_4 & -h_3 & h_2 & -h_1 \end{bmatrix} \times \begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_1^* \\ r_2^* \\ r_3^* \\ r_4^* \end{bmatrix}$$

The probability of error in MRC Rayleigh fading is described in equation (5) (goldsmith2005wireless)[eq (7.18)].

$$p_e = \left(\frac{1-\Gamma}{2}\right)^L \sum_{l=0}^{L-1} \binom{L-1+l}{l} \left(\frac{1+\Gamma}{2}\right)^l \quad (5)$$

where L represents the number of the receiver. In equation (5), Γ can be written as,

$$\Gamma = \sqrt{\frac{\gamma}{1+\gamma}} \quad (6)$$

Maximum Likelihood (ML) Estimator

After MRC, signals $c(x)$ are sent to ML estimator as mentioned in equation (7). Afterward RS decoder receives signals and processes them.

$$y(x) = c(x) + e(x) \quad (7)$$

The signal-to-noise ratio per receive antenna can be written as,

$$\gamma_l = \frac{w_i \cdot m \cdot P_t \cdot N \cdot R_c}{\sigma^2} \quad (8)$$

Where P_t represents transmitted power in dB, m represents modulation index, σ corresponds to standard deviation and R_c denotes code rate. SNR per symbol can be computed as,

$$\gamma^{STBC} = \frac{\tilde{\gamma}}{NR_c} (\|H\|_F)^2 \quad (9)$$

Where $\|H\|_F^2$ represents Frobenius norm of matrix H .

RS Error Probability in Rayleigh Channel (Non Line of Sight Model)

In this subsection, RS channel probability in Rayleigh fading is determined, i.e, Non Line of Sight (NLOS) model. RS can detect and correct $t = n-k/2$ symbol errors where n represents the number of coded bits and k corresponds to the number of information bits. For detection and correction of errors d_{\min} should be more than $n-k+1$.

Probability of symbol error P_s is given as,

$$P_s = \sum_{j=t+1}^n \binom{n}{j} p_e^j (1-p_e)^{n-j} \quad (10)$$

where p_e is calculated using equation (4) and $j=t+1$. The probability of error of RS in Rayleigh fading is written as,

$$P_e = \int_0^{+\infty} P_s \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} dp_e \quad (11)$$

Substituting Eq. (10) into Eq. (11) gives,

$$P_e = \int_0^{+\infty} \sum_{j=t+1}^n \binom{n}{j} p_e^j (1-p_e)^{n-j} dp_e \cdot \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \quad (12)$$

Using(gradshteyn1963table)[eq.(1.111),p.25]

$$(a+x)^n = \sum_{j=0}^n \binom{n}{j} a^j x^{n-j} \quad (13)$$

Expression (12) can be modified to,

$$P_e = \int_0^{+\infty} (p_e+x)^n \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} dp_e \quad (14)$$

Applying integration,

$$P_e = \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \int_0^{+\infty} (p_e+x)^n dp_e - \int_0^{+\infty} \left(\frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \frac{d}{dp_e} \right) \int_0^{+\infty} (p_e+x)^n dp_e \quad (15)$$

$$P_e = \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \cdot \frac{(p_e+x)^{n+1}}{n+1} - \int_0^{+\infty} \left(\frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \frac{d}{dp_e} \right) \frac{(p_e+x)^{n+1}}{n+1} dp_e \quad (16)$$

Applying limits to p_e .

$$P_e = -\frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \frac{(x)^{n+1}}{n+1} - \int_0^{+\infty} \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \frac{d}{dp_e} \left(-\frac{(x)^{n+1}}{n+1} \right) dp_e \quad (17)$$

Applying differentiation,

$$P_e = -\frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \frac{(x)^{n+1}}{n+1} + \int_0^{+\infty} \frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \left(-\frac{1}{\gamma} \right) \frac{(x)^{n+1}}{n+1} dp_e \quad (18)$$

Applying integration finally we have,

$$P_e = -\frac{1}{\gamma} \exp^{-\frac{p_e}{\gamma}} \frac{(x)^{n+1}}{n+1} - \frac{1}{\gamma^2} \frac{1}{\gamma} \frac{(x)^{n+1}}{n+1} \quad (19)$$

The equation (19) represents closed-form approximation of BER of RS in Rayleigh fading.

203 RS Error Probability in AWGN Channel (Line of Sight Model)

BER of AWGN Channel can be written as (goldsmith2005wireless)[eq (6.3)],

$$BER = \frac{P_e}{\log_2 M} \quad (20)$$

The BER of RS in AWGN channel can be written as,

$$P_e = \int_0^{+\infty} \frac{P_e}{\log_2 M} \sum_{i=1}^n \binom{n}{i} \cdot P_e^i (1 - P_e)^{n-i} dP_e \quad (21)$$

Using expression (14), we have,

$$P_e = \int_0^{+\infty} (P_e + x)^n \frac{P_e}{\log_2 M} dP_e \quad (22)$$

After manipulating above expression,

$$P_e = \frac{P_e}{\log_2 M} \frac{(P_e + x)^{n+1}}{n+1} - \int_0^{+\infty} \left(\frac{1}{\log_2 M} \frac{(P_e + x)^{n+1}}{n+1} \right) dP_e \quad (23)$$

After solving above expression,

$$P_e = -\frac{P_e}{\log_2 M} \frac{x^{n+1}}{n+1} + \int_0^{+\infty} \frac{1}{\log_2 M} \frac{x^{n+1}}{n+1} dP_e \quad (24)$$

After integration, second term becomes 0.

$$P_e = \frac{P_e}{\log_2 M} \frac{x^{n+1}}{n+1} \quad (25)$$

204 Equation (25) represents closed-form approximation of bit error probability of RS in AWGN channel.

205 Doppler Effect in Proposed Model

Consider the proposed model in Figure 1 in which the vehicles are traveling with velocity v which is varying from 25 km/h to 250 km/h. The closed-form expression of RS BER probability in Rayleigh fading i.e equation (19) is mentioned below,

$$P_e = -\frac{1}{\bar{\gamma}} \exp^{-\frac{P_e}{\bar{\gamma}}} \frac{(x)^{n+1}}{n+1} - \frac{1}{\bar{\gamma}^2} \frac{1}{\bar{\gamma}} \frac{(x)^{n+1}}{n+1} \quad (26)$$

SNR under Doppler effect can be written as,

$$\bar{\gamma} = \frac{A^2}{2 * \sigma^2} f_d$$

where A corresponds to magnitude of signal and f_d represents Doppler shift. Plugging value of $\bar{\gamma}$ in expression (26),

$$P_e = \frac{2 \cdot \sigma^2}{f_d} \cdot \exp^{-\frac{P_e \cdot 2 \cdot \sigma^2}{f_d}} \cdot \frac{x^{n+1}}{n+1} + \frac{2 \cdot \sigma^2}{f_d} \cdot \frac{x^{n+1}}{n+1}$$

Probability density function of f_d can be written as,

$$P_{ed} = \int_0^{+\infty} \frac{1}{\gamma} \cdot \exp^{-\frac{f_d}{\gamma}} \cdot P_e df_d \quad (27)$$

Substituting P_e in above expression,

$$P_{ed} = \int_0^{+\infty} \left(\frac{1}{\gamma} \cdot \exp^{-\frac{f_d}{\gamma}} \right) \cdot \left(\frac{2 \cdot \sigma^2}{f_d} \cdot \exp^{-\frac{P_e \cdot 2 \cdot \sigma^2}{f_d}} \cdot \frac{x^{n+1}}{n+1} + \frac{2 \cdot \sigma^2}{f_d} \cdot \frac{x^{n+1}}{n+1} \right) df_d \quad (28)$$

$$P_{ed} = \int_0^{+\infty} \frac{1}{\gamma} \cdot \exp^{-\frac{f_d}{\gamma} - \frac{p_e \cdot 2 \cdot \sigma^2}{f_d}} \cdot \frac{x^{n+1}}{n+1} \cdot \frac{2 \cdot \sigma^2}{f_d} + \frac{1}{\gamma} \cdot \exp^{-\frac{f_d}{\gamma}} \cdot \frac{2 \cdot \sigma^2}{f_d} \cdot \frac{x^{n+1}}{n+1} df_d \quad (29)$$

206 Manipulating above expression,

$$P_{ed} = \frac{1}{\gamma} \cdot \frac{x^{n+1}}{n+1} \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma} - \frac{p_e \cdot 2 \cdot \sigma^2}{f_d}} \cdot \frac{2 \cdot \sigma^2}{f_d} + \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma}} \cdot \frac{2 \cdot \sigma^2}{f_d} \quad (30)$$

Applying integration by parts,

$$P_{ed} = \frac{1}{\gamma} \cdot \frac{x^{n+1}}{n+1} \cdot \left(\frac{2 \cdot \sigma^2}{f_d} \cdot \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma} - \frac{p_e \cdot 2 \cdot \sigma^2}{f_d}} - \int_0^{+\infty} \left(\frac{2 \cdot \sigma^2}{f_d} \frac{d}{df} \right) \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma} - \frac{p_e \cdot 2 \cdot \sigma^2}{f_d}} + \exp^{-\frac{f_d}{\gamma}} \int_0^{+\infty} \frac{2 \cdot \sigma^2}{f_d} - \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma}} \frac{d}{df} \cdot \int_0^{+\infty} \frac{2 \cdot \sigma^2}{f_d} \right) df_d \quad (31)$$

In (gradshteyn1963table)[eq.(3.325),p.336],

$$\int_0^{+\infty} \exp^{-\frac{f_d}{\gamma} - \frac{p_e \cdot 2 \cdot \sigma^2}{f_d}} = \frac{1}{2} \cdot \sqrt{\frac{\pi i}{\frac{1}{\gamma}}} \cdot \exp^{-2 \cdot \sqrt{\frac{2 \cdot \sigma^2 \cdot p_e}{\gamma}}}$$

Replacing above expression in expression (31) yields,

$$P_{ed} = \frac{1}{\gamma} \cdot \frac{x^{n+1}}{n+1} \cdot \left(\frac{2 \cdot \sigma^2}{f_d} \cdot \frac{1}{2} \cdot \sqrt{\frac{\pi i}{\frac{1}{\gamma}}} \cdot \exp^{-2 \cdot \sqrt{\frac{2 \cdot \sigma^2 \cdot p_e}{\gamma}}} + \int_0^{+\infty} \left(\frac{2 \cdot \sigma^2}{f_d^2} \right) \cdot \frac{1}{2} \cdot \sqrt{\frac{\pi i}{\frac{1}{\gamma}}} \cdot \exp^{-2 \cdot \sqrt{\frac{2 \cdot \sigma^2 \cdot p_e}{\gamma}}} + \exp^{-\frac{f_d}{\gamma}} \int_0^{+\infty} \frac{2 \cdot \sigma^2}{f_d} - \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma}} \frac{d}{df} \cdot \int_0^{+\infty} \frac{2 \cdot \sigma^2}{f_d} \right) \quad (32)$$

Applying integration and limits,

$$P_{ed} = \frac{1}{\gamma} \cdot \frac{x^{n+1}}{n+1} \cdot \left(\frac{2 \cdot \sigma^2}{f_d} \cdot \frac{1}{2} \cdot \sqrt{\frac{\pi i}{\frac{1}{\gamma}}} \cdot \exp^{-2 \cdot \sqrt{\frac{2 \cdot \sigma^2 \cdot p_e}{\gamma}}} - \exp^{-\frac{f_d}{\gamma}} \cdot 2 \cdot \sigma^2 + 2 \cdot \sigma^2 \cdot \frac{1}{\gamma} \cdot \int_0^{+\infty} \exp^{-\frac{f_d}{\gamma}} \right) \quad (33)$$

Manipulating above expression yields to,

$$P_{ed} = \frac{1}{\gamma} \cdot \frac{x^{n+1}}{n+1} \cdot \left(\frac{2 \cdot \sigma^2}{f_d} \cdot \frac{1}{2} \cdot \sqrt{\frac{\pi i}{\frac{1}{\gamma}}} \cdot \exp^{-2 \cdot \sqrt{\frac{2 \cdot \sigma^2 \cdot p_e}{\gamma}}} - \exp^{-\frac{f_d}{\gamma}} \cdot 2 \cdot \sigma^2 + \frac{1}{\gamma} \cdot \frac{1}{\gamma} \cdot 2 \cdot \sigma^2 \right) \quad (34)$$

207 Applying integration and limits,

$$P_{ed} = \frac{1}{\gamma} \cdot \frac{x^{n+1}}{n+1} \cdot \left(\frac{2 \cdot \sigma^2}{f_d} \cdot \frac{1}{2} \cdot \sqrt{\frac{\pi}{\gamma}} \cdot \exp^{-2 \cdot \sqrt{\frac{2 \cdot \sigma^2 \cdot p_e}{\gamma}}} - \exp^{-\frac{f_d}{\gamma}} \right) \cdot \exp^{-\frac{f_d}{2 \cdot \sigma^2 + 2 \cdot \sigma^2}} \quad (35)$$

Equation (35) represents RS coded Doppler shift expression in Rayleigh fading.

RESULTS AND DISCUSSION

This section comprises of results and discussion of the proposed model. Matlab is used as a simulation platform.

In this research, LOS, NLOS, number of antenna elements N, equidistant spacing d (30 mm, 40 mm, 50 mm) and relative velocity v (25 km/h, 100 km/h, 250 km/h) are used as use cases.

Figure. 5 and Figure. 6 show the impact of the number of transmitting antennas and their equidistant spacing on directivity.

The simulation parameters are shown in Table 1.

Table 1. Beamforming Simulation Parameters

Parameter	Value
Frequency	60GHz
θ	-15° to 15°
N	2,3,4
d	30 mm, 40 mm, 50 mm

From Figure. 5 it can be remarked that by increasing the number of transmitting antennas i.e. N which is varying from 2 to 4, directivity increases. When directivity increases, the beam gain increases and thus, the probability of signal loss reduces. d=50 mm is used in simulation. However, the effect of increasing the number of transmitting antennas results in a larger number of side lobes as shown in Figure. 5. In beamforming, linear arrays with increasing equidistant element spacing will also produce grating lobes as described in Figure. 6. These grating lobes are unwanted energy that will be radiated to or received from undesired directions. If the equidistant spacing exceeds half a wavelength grating lobes start to appear in the visible region. To avoid this phenomenon following condition must be kept as,

$$d < \frac{\lambda}{2}$$

In case the distance between transmitting antennas exceeds one wavelength, the grating lobe levels start to equal the main lobe level. Since the array factor is periodic in nature, grating lobes will start to appear in the visible region coming from the invisible region. In this case, scan angle will be restricted. So the maximum value of scan angle must be,

$$\sin|\theta| = \frac{\lambda}{d} - 1$$

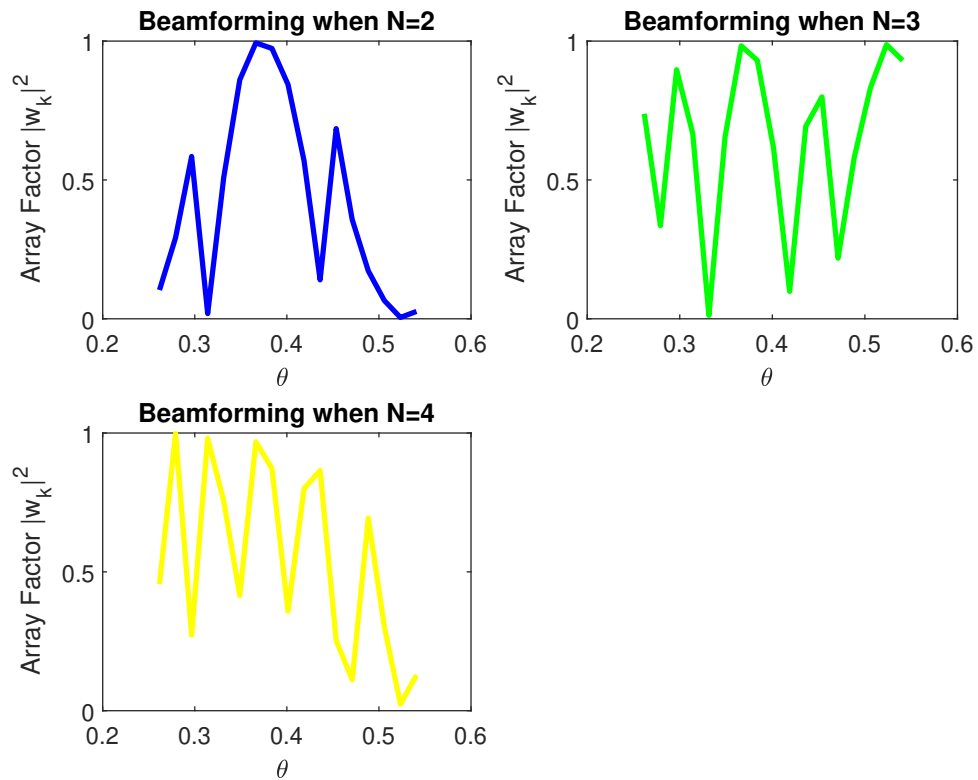


Figure 5. Signal received after Beamforming when number of elements are increasing

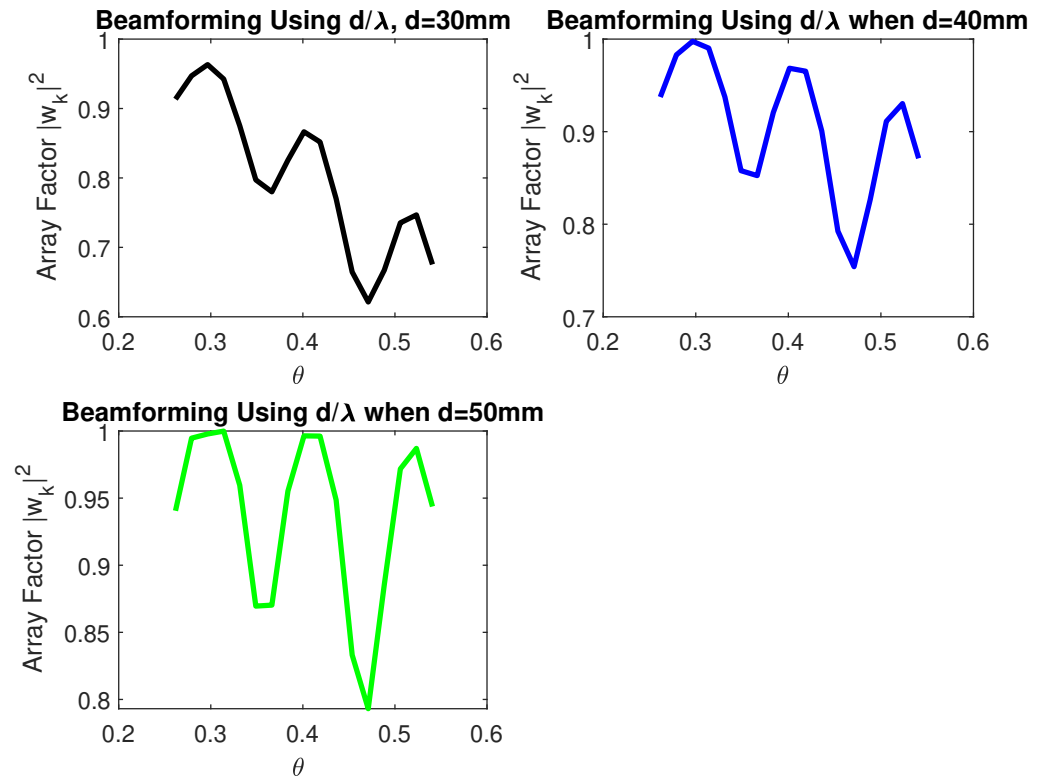


Figure 6. Signal received after Beamforming when distance between elements is increasing

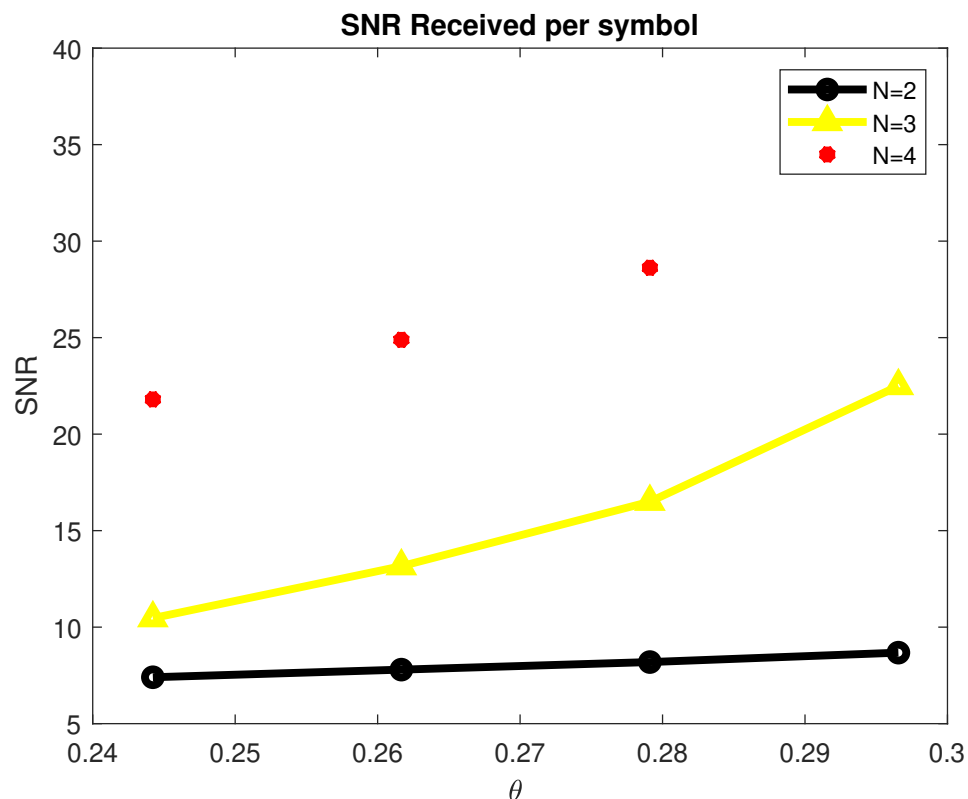


Figure 7. SNR per symbol in Maximal Likelihood Detector

Table 2. Simulation Parameters

Parameter	Value
No. of transmitting elements N	4
Transmit power P_t	10dB
modulation index m	1
standard deviation σ^2	9
Code Rate R_c	.9
Carrier frequency f_c	60 GHz
Data rate	7.31 Mbps
Packet size	100 Bytes

For SNR calculation equation (8) is used. Simulation parameters are describe in Table 2. SNR per symbol is computed in a ML detector using expression (9). Figure. 7 displays the graph of SNR per symbol versus angle of reflection theta. When increasing the angle of reflection, SNR per symbol also rises. By increasing the number of transmitters to $N=4$, SNR also gets high. The capacity of a system is directly proportional to the number of transmitters. The capacity of our system is 2.5 bits/s/Hz when there are four transmitters as shown in Figure. 8.

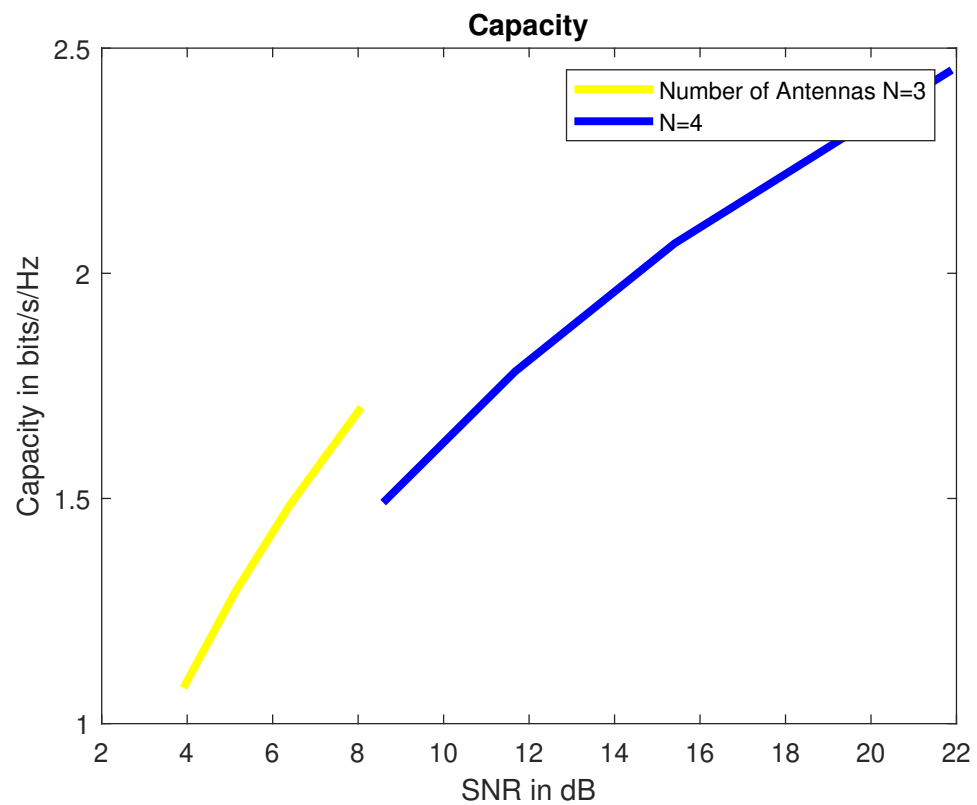


Figure 8. Capacity in bits/s/Hz

BER Comparison of 64 QAM with Proposed Approximation in AWGN Channel

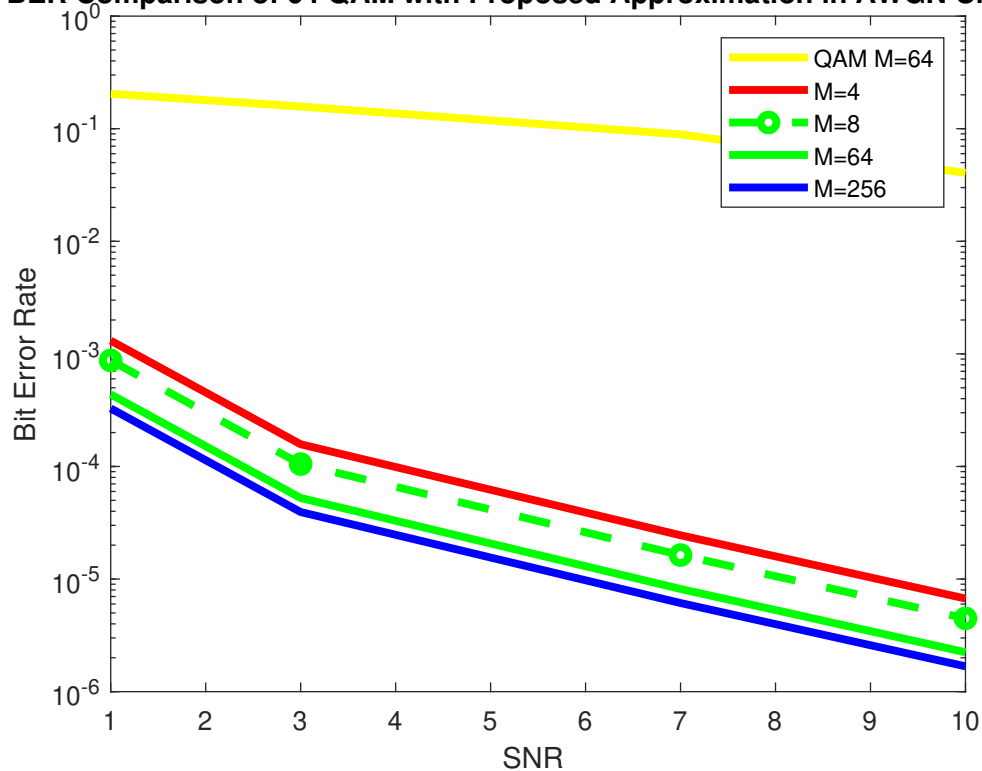


Figure 9. RS BER Comparison of 64QAM with Proposed Approximation

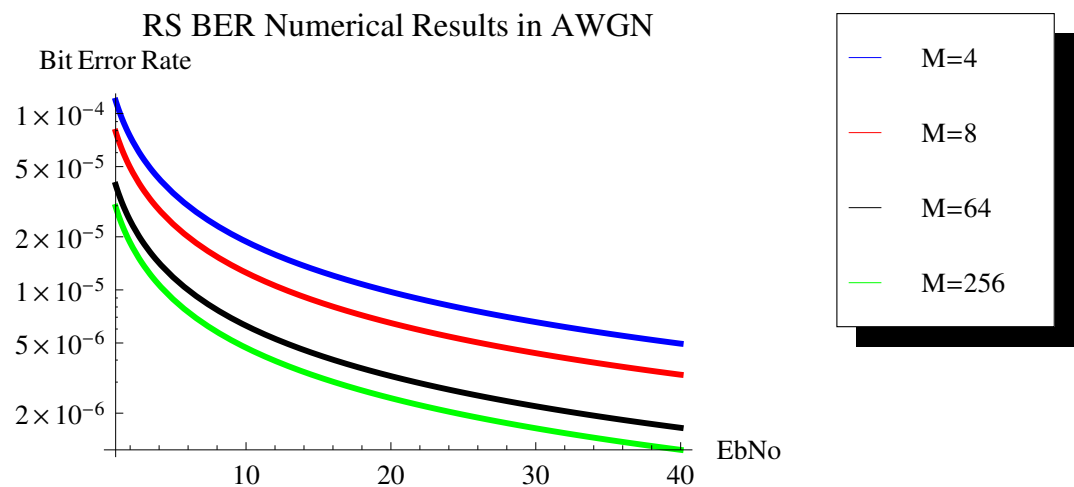


Figure 10. RS BER Comparison of 64QAM with Proposed Approximation

BER Comparison of 4 PSK with Proposed Approximation in AWGN Channel

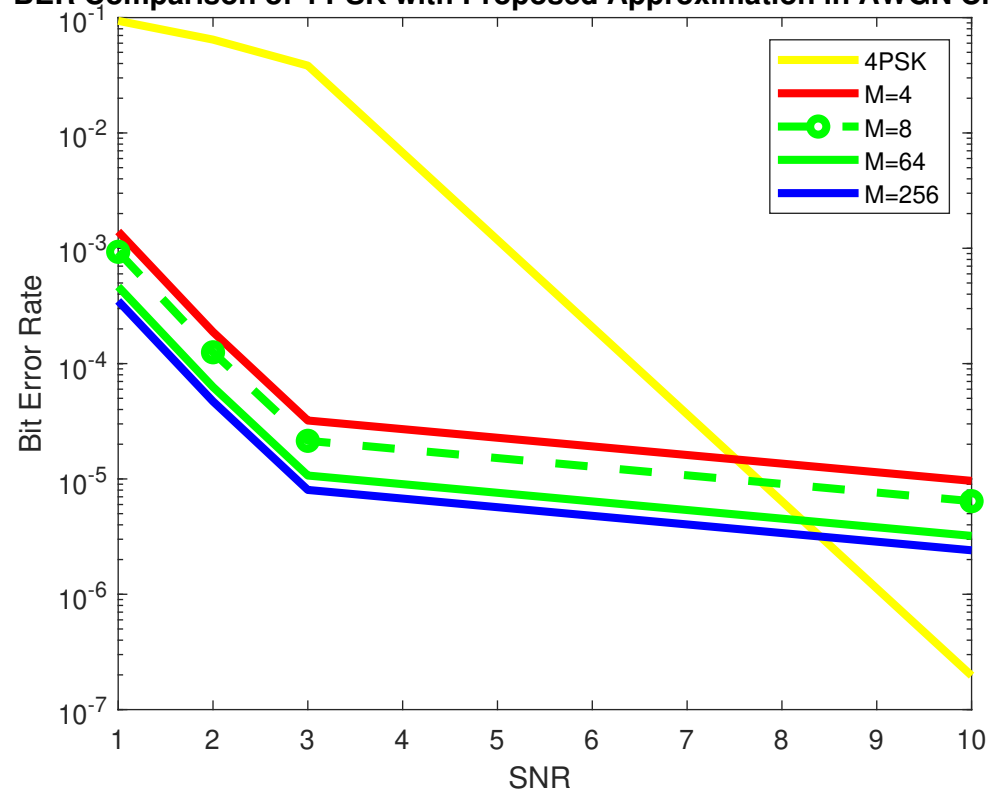


Figure 11. RS BER Comparison of 4PSK with Proposed Approximation

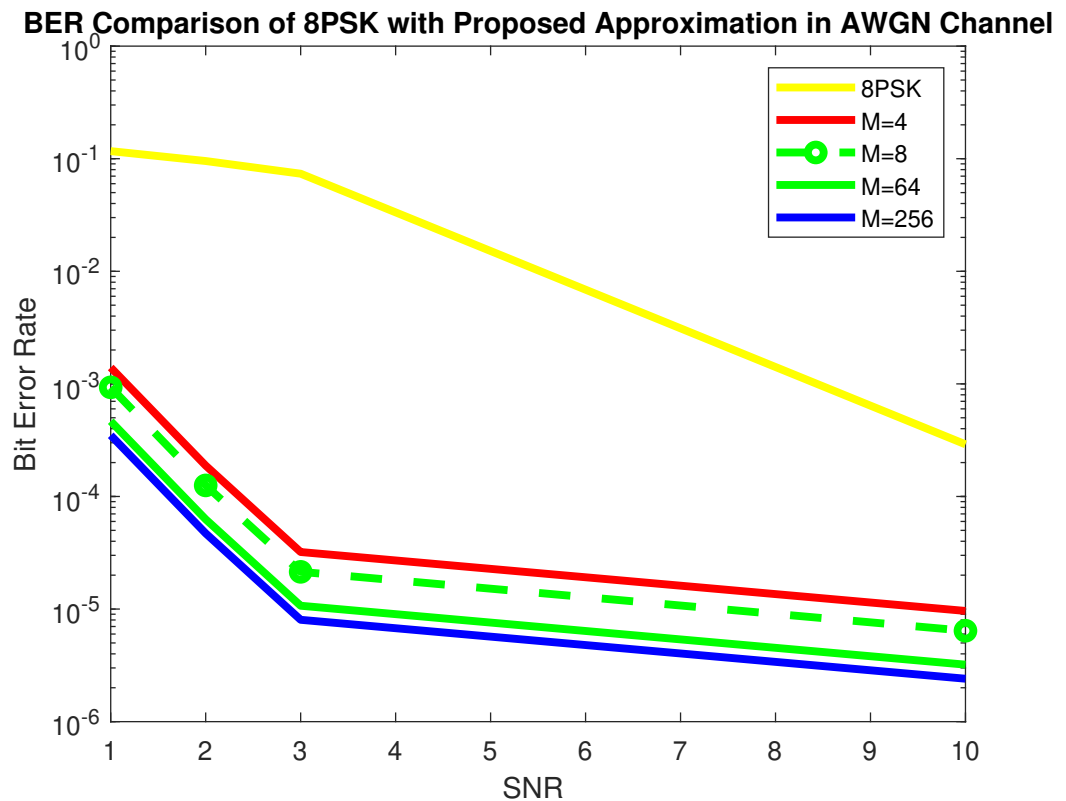


Figure 12. RS BER Comparison of 8PSK with Proposed Approximation

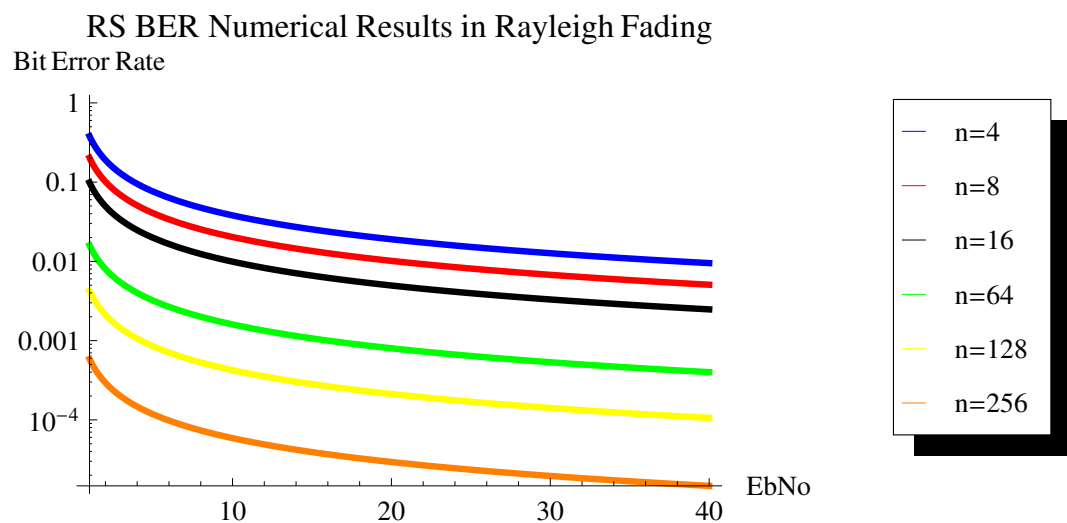


Figure 13. RS BER Proposed Approximation Numerical Results in Rayleigh Channel

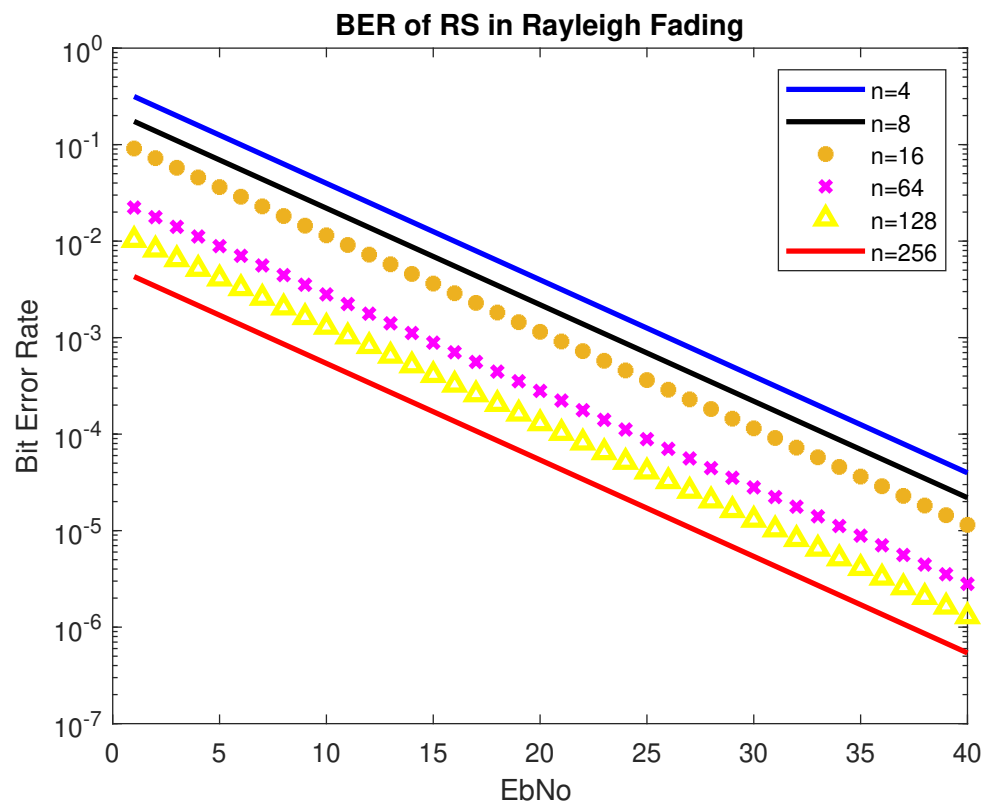


Figure 14. BER of RS in Rayleigh Fading

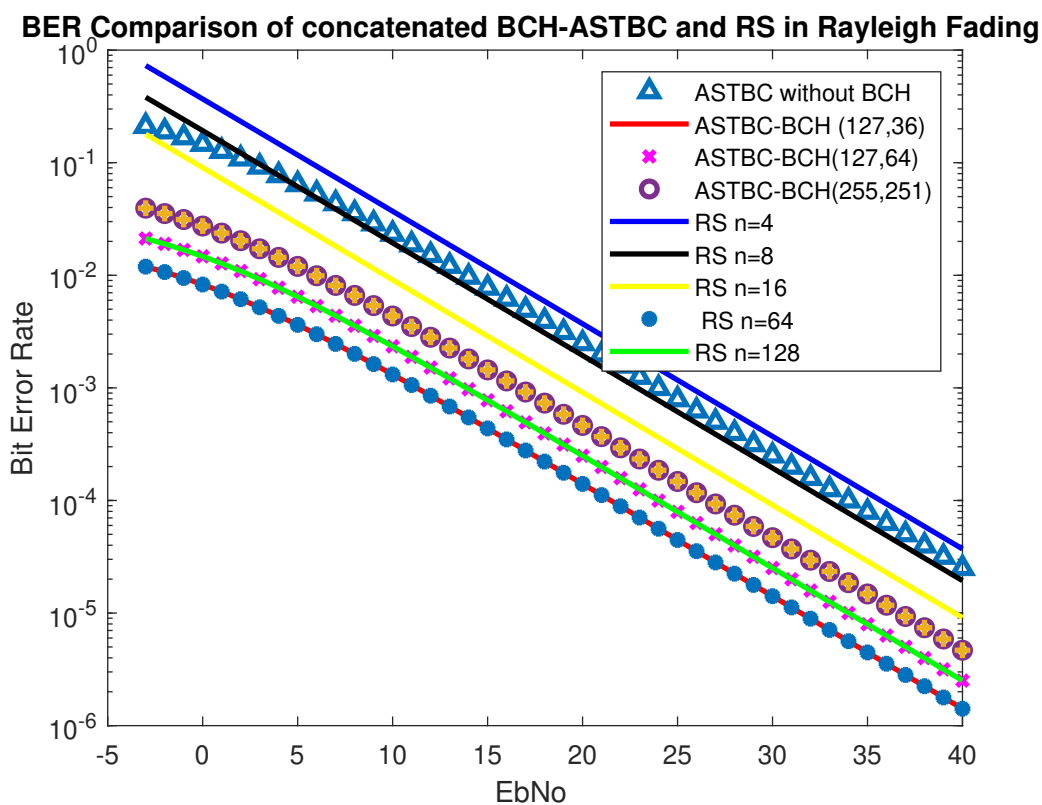


Figure 15. Comparison of BER of STBC-RS with BCH-ASTBC

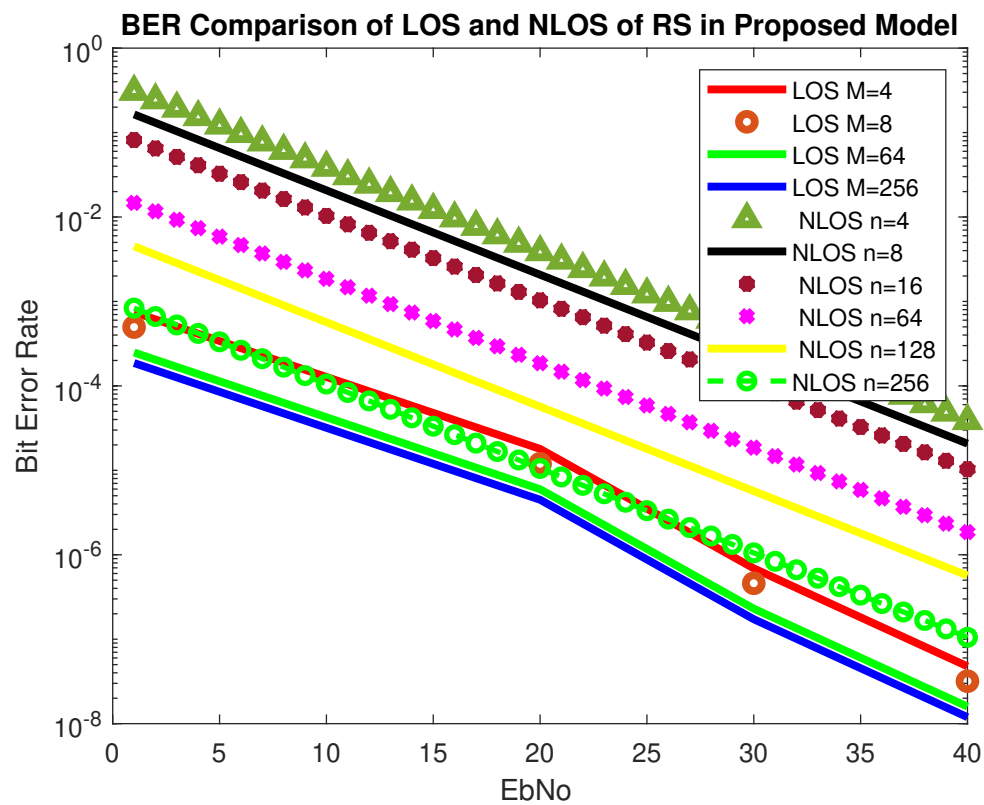


Figure 16. BER Comparison of RS in Rayleigh Fading and AWGN Channel

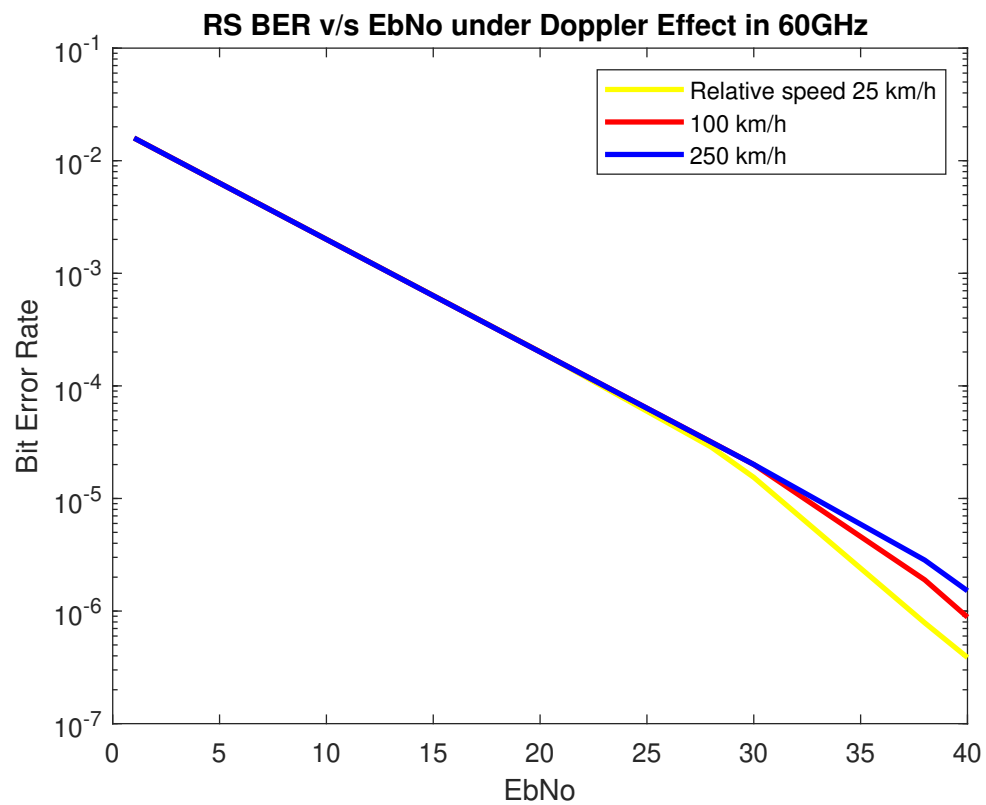


Figure 17. BER of RS Under Doppler Effect

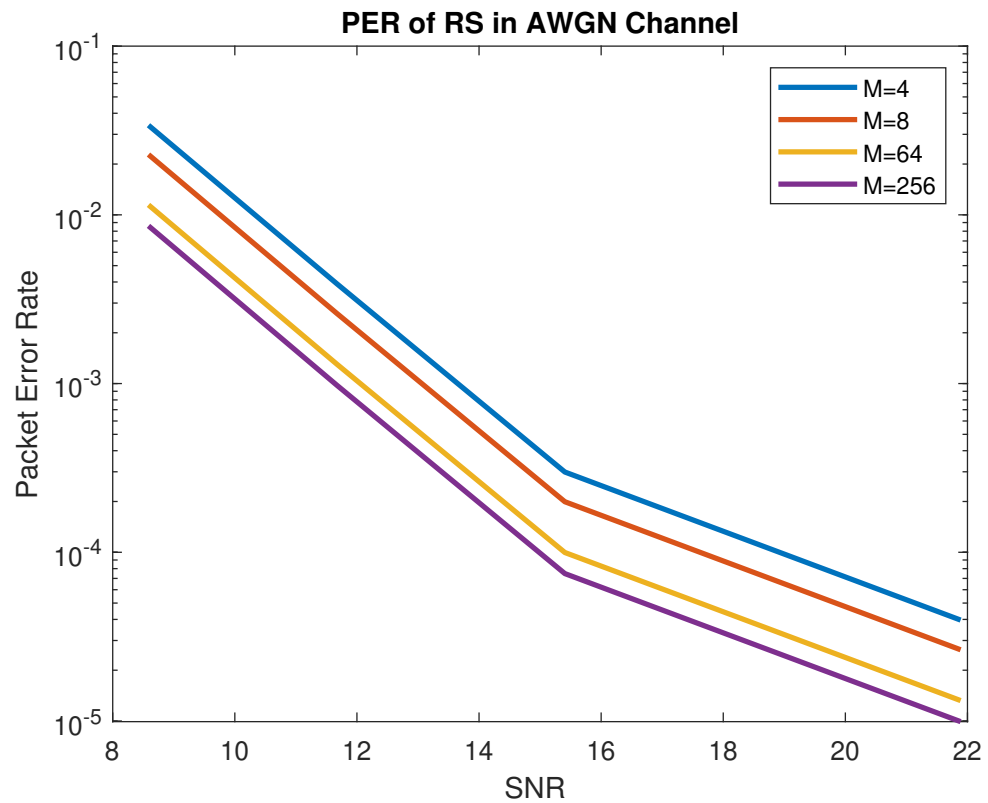


Figure 18. PER (Packet size = 100 Bytes) of RS in AWGN Channel

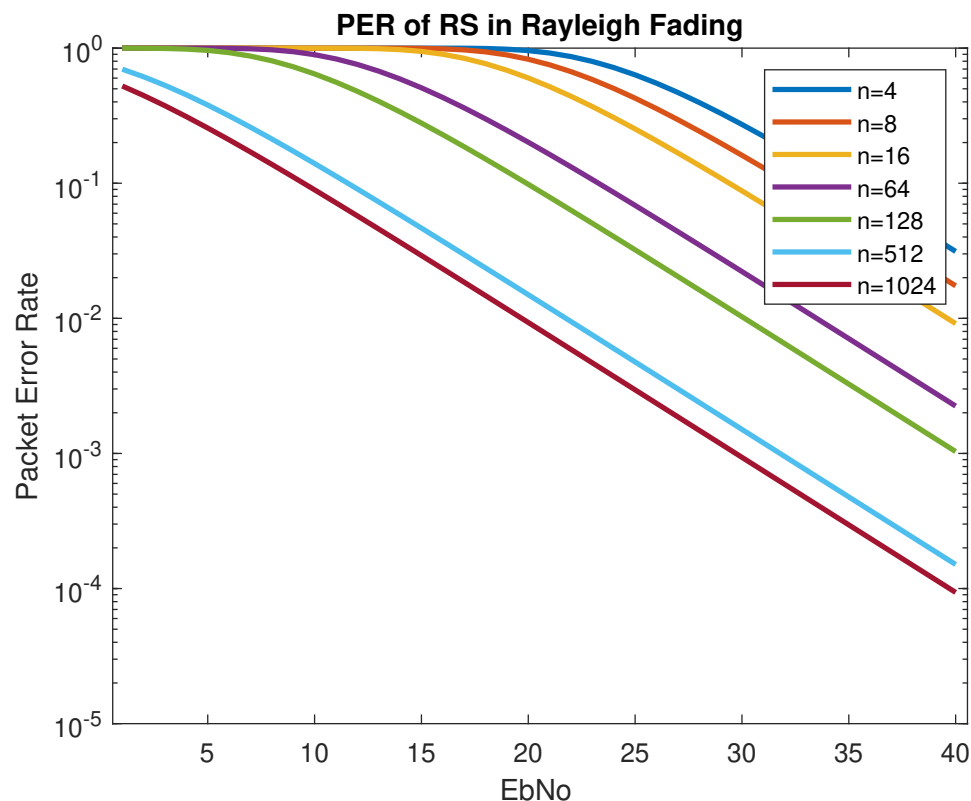


Figure 19. PER (Packet size = 100 Bytes) of RS in Rayleigh Fading

Figure. 9 shows the simulation results and Figure. 10 depicts the numerical results of closed-form approximation of RS BER in the AWGN channel. It can be remarked from both figures that the results verify each other. On comparing our result with the traditional 64-QAM system it can figure out that the BER of 64-QAM is higher than our proposed approximation. The BER of the M-PSK is compared with our expression described in Figure. 11 and Figure. 12. The BER of M-PSK system is getting low on account of decreasing modulation order M. The BER of the 4PSK system is lower than the 8PSK system. However, the BER of proposed approximation gets low on account of increasing modulation order M. So our result outperforms both the 64-QAM and M-PSK system. The simulation parameter described in Table 2.

Figure. 13 and Figure. 14 show the numerical results and simulation results of closed-form approximation of RS error probability in the Rayleigh channel. On comparing results based on n, it can be observed that error probability is getting depleted by increasing n.

Table 3. Comparative Analysis of proposed model with previous studies in terms of BER

Sr No.	Paper	Approach	BER (Propagation Channel NLOS/LOS)	BER (Modulation and Coding)	Comparison With Proposed Technique using Modulation and Coding	Comparison With Proposed Technique LOS/NLOS
1	(al2017enhancing)	RS performance is increased using multi-path propagation in LOS and NLOS scenario	10^{-5}	x	x	$10^{-5}, 10^{-6}$
2	(mergu2016performance)	RS performance is analyzed using RS codes concatenated with Convolutional Codes over AWGN Channel	10^{-2}	Convolutional Codes, 10^{-2}	10^{-5}	10^{-5}
3	(Tiwari2013BERPO)	Comparison Analysis of LDPC and RS codes on multiple antennas using AWGN channel	10^{-2} to 10^{-3}	BPSK, QPSK, LDPC, RS, 10^{-2} to 10^{-3}	10^{-5}	10^{-5}
4	(indoonundon2021overview)	To achieve ultra reliable low latency communication in 5G, a detailed analysis of coding schemes was conducted	x	BER lies between 10^{-6} to 10^{-7}	10^{-7}	x
5	(saleh2019improving)	Communication reliability was improved using different diversity schemes	x	BPSK, MRC outperforms other techniques 10^{-7}	10^{-5}	x
6	(hajiyat2019channel)	The reliability of VANET was evaluated using turbo, Low Density Parity Check Code (LDPC), Polar code, Systematic Convolutional Codes (SCC), and Non-Systematic Convolutional Codes (NSCC) coding types	x	10^{-7}	10^{-6}	x
7	(hamarsheh2022robust)	MIMO-FFH-OFDM	x	10^{-4}	10^{-5}	x

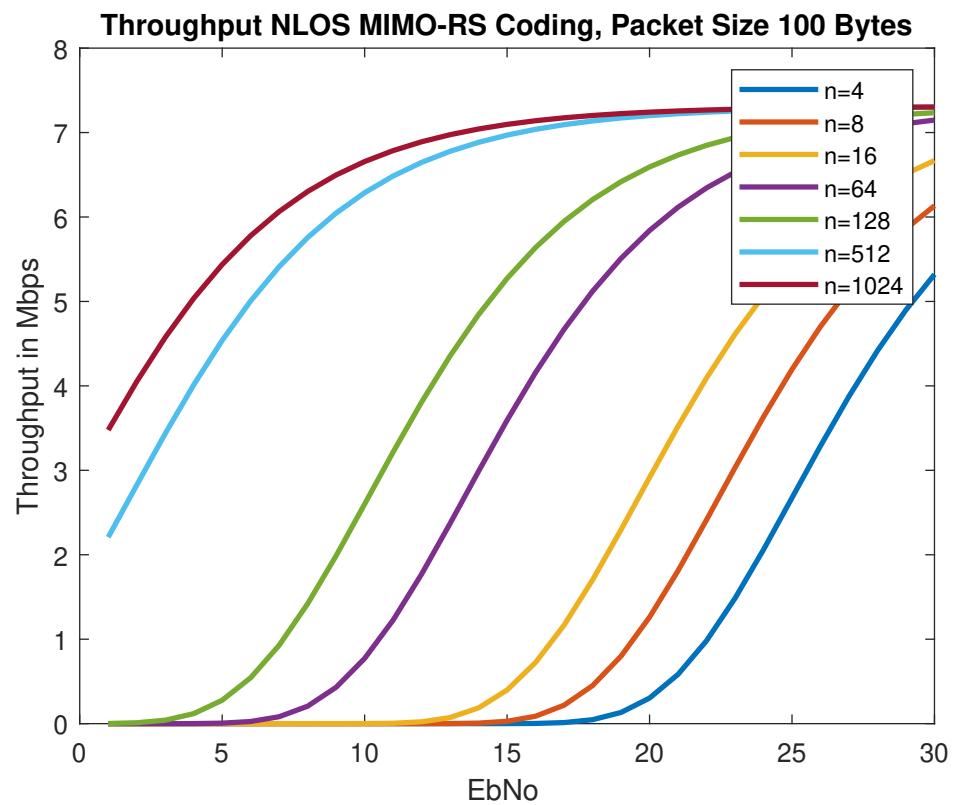


Figure 20. Throughput of MIMO-RS (Packet size = 100 Bytes) in NLOS

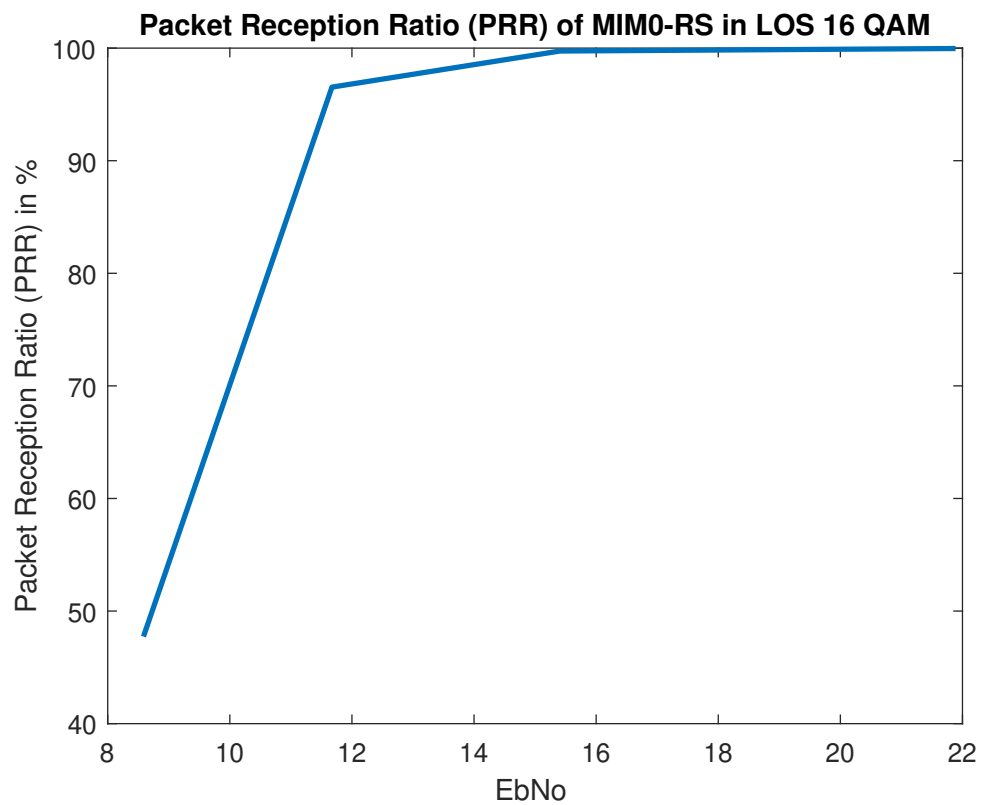


Figure 21. Packet Reception Ratio (PRR) of MIMO-RS in LOS (Packet size = 100 Bytes)

Table 4. PER Analysis of Proposed Approach (Modulation) with IEEE 802.11p and NR V2X

Comparison Analysis of Proposed Approach with IEEE 802.11bd and V2X (anwar2019physical)		
VANET Communication Standards	Modulation	PER
IEEE 802.11bd	QPSK/64 QAM	10^{-3}
NR V2X	QPSK/64 QAM	$10^{-3} / 10^{-2}$
Proposed Methodology	BPSK/16/QAM/64QAM	$10^{-4}/10^{-5}$

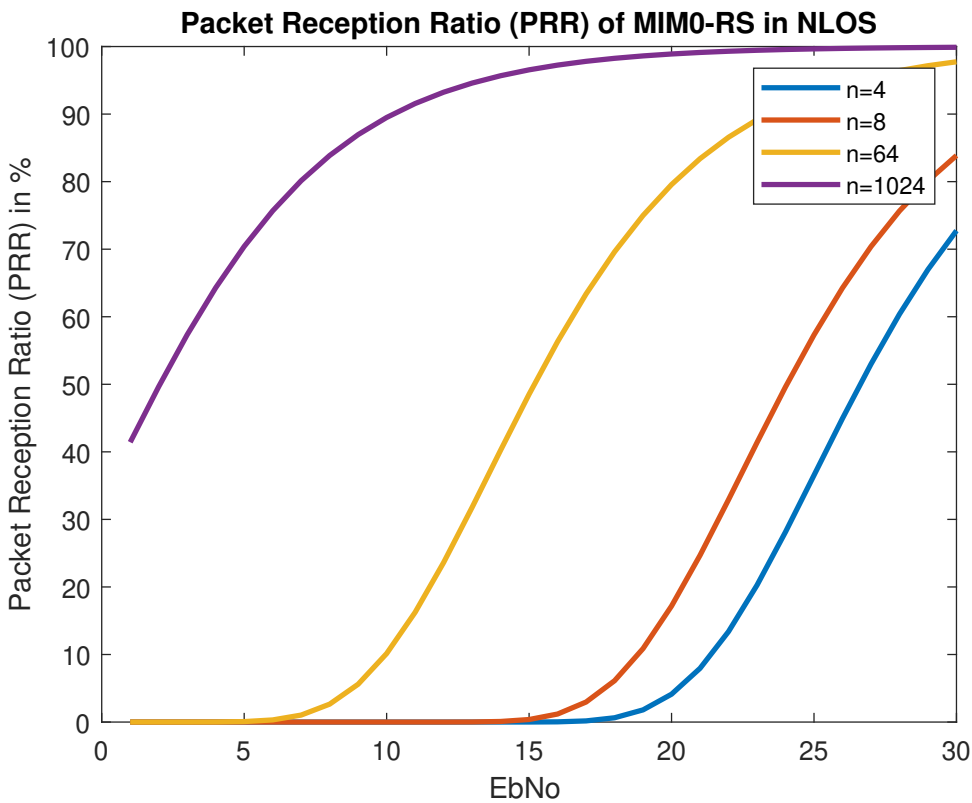


Figure 22. Packet Reception Ratio (PRR) of MIMO-RS in NLOS (Packet size = 100 Bytes)

Table 3 illustrates the comparative analysis of proposed model with previous studies in terms of BER. The results are analyzed using NLOS/LOS cases and modulation and coding types from different studies. The performance of the proposed system is compared with (electronics10090992) in which concatenated BCH-ASTBC was used for VANET communication. Results are described in Figure. 15. The performance of BCH-ASTBC with code rate (127,36) is similar to RS BER at n=64. The similar curve was also obtained for BCH-ASTBC with code rate (127,64) and RS BER at n=128. The BER curve of ASTBC without BCH code is in between RS BER at n=4 and RS BER at n=8. Figure. 16 depicts the comparative analysis of AWGN channel and Rayleigh channel. Figure. 17 displays result of Doppler shift in RS coding. The change in frequency causes frequency offset is the main source of high BER in VANET communications.

Comparison Analysis of proposed approach with IEEE 802.11bd and 3GPP V2X Communication

Table 5. PER Analysis of Proposed Approach (Coding) with IEEE 802.11p and NR V2X

Comparison Analysis of Proposed Approach with IEEE 802.11bd and V2X (anwar2020performance)			
VANET Communication Standards	Modulation	Coding	PER
IEEE 802.11bd	BPSK	Convolutional, LDPC, Turbo, Polar	10^{-3}
NR V2X	BPSK	Convolutional, LDPC, Turbo, Polar	10^{-3}
Proposed Methodology	BPSK	RS	10^{-4} , 10^{-5}

Table 6. Throughput Analysis of Proposed Approach with IEEE 802.11p and NR V2X

Throughput Analysis of Proposed Approach with IEEE 802.11bd and V2X (anwar2020performance) (triwinarko2021phy)		
VANET Standards	Communication	Coding
IEEE 802.11bd		LDPC
V2X		Convolutional, Turbo, Polar
Proposed Methodology		RS
		Throughput
		7 Mbps
		4 Mbps
		7 Mbps

257 In this subsection, the performance of the proposed system is compared with IEEE 802.11bd and
258 5G NR V2X standard. The PER of LOS model is described in Figure. 18. The PER of NLOS model
259 (Rayleigh fading) is shown in Figure. 19.

260 The performance of upcoming technologies i.e 5G NR V2X and IEEE 802.11bd V2V communications
261 was analyzed in (anwar2019physical). Comparing RS Packet Error Rate (PER) in AWGN channel shown
262 in Figure. 18 with 802.11 bd and NR V2X 64-QAM in (anwar2019physical) it can be observed that the
263 performance of our proposed RS model is optimal. Results are displayed in Table 4.

264 According to (anwar2020performance) the performance of LDPC is marginal in V2X communication.
265 The performance of proposed model outperforms LDPC, Turbo, Polar and Convolutional coding. Because
266 the reliability of the system gets better since low PER is received in Figure. 19. Table 5 displays
267 the comparison between proposed method with IEEE 802.11bd and V2X using PER. Comparing RS
268 performance under Doppler Effect shown in Figure. 17, it can be remarked that RS performance is
269 optimal.

In (triwinarko2021phy) the performance of various modulations schemes was evaluated on IEEE
802.11bd using LDPC. The packet size of 100 bytes was used for simulation. It can be observed that the
RS error control coding gives us high reliability, as mentioned in Figure. 18 and Figure. 19.
Throughput of the proposed model is analyzed using equation below.

$$\text{Throughput} = R.(1 - PEP)$$

270 where R corresponds to data rate. Results are described in Figure. 20. The results outperform with
271 (anwar2020performance) and are comparable with (triwinarko2021phy) as described in Table 6. 5G
272 NR was integrated with Spatial Multiplexing MIMO while keeping other DSRC specifications the same
273 (dey2020modified). Convolution coding was used in the system. The performance of the 4*4 MIMO
274 concatenated with 5G NR was analyzed using MMSE and ZF equalizers (dey2020modified). We have
275 used for 4*4 MIMO system. According to (obi2021mimo), among Maximum Likelihood (ML) Estimator
276 Zero Forcing (ZF) and Minimum Mean Square Error (MMSE), ML performance is optimal.
277 Figure. 21 and Figure. 22 depict PRR of both NLOS and LOS. Our proposed approach for channel
278 modeling in VANET i.e MIMO-STBC can be adopted in V2X communication and IEEE 802.11bd.
279 Researchers are considering inducing MIMO-STBC in current VANET communication systems as
280 mentioned above.

281 CHALLENGES AND LIMITATIONS OF THE PROPOSED MODEL

282 In the proposed model, multiple antennas and other hardware systems are used, so hardware complexity is
283 higher. Since mathematical algorithms are used in the design of the beamforming system, a cutting-edge,
284 highly processing DSP chip is required. Beamforming systems cost more than non-beamforming systems
285 because they use more hardware resources and more sophisticated DSP chips. The use of more resources
286 results in a higher power requirement for beamforming systems. Consequently, the beamforming system's
287 battery drains more quickly.

288 In some cases, Perfect Channel State Information (CSI) is considered at the receiver. Reed Solomon codes
289 work well for M-ary modulations schemes than BPSK systems.

290 CONCLUSION

291 The future of VANET will be driven by mmWave communications. In this manuscript, a tractable model
292 using STBC-RS is proposed for achieving ultra-reliability of $1 - 10^{-5}$. The closed-form approximations of
293 BER using RS in the AWGN channel and Rayleigh fading are derived. The results show that the proposed
294 model outmatches previous BER estimation approaches of RS and STBC in 5G VANET networks. On
295 comparing the model with existing VANET communicating systems it can be concluded that the proposed
296 model performance is better than IEEE 802.11bd. We recommend that for designing V2X architectures,
297 MIMO-STBC along with RS coding provides more useful results, since low PEP is received. The designed
298 model can also be employed in 802.11p as a physical layer enhancement technique.

299 This research work provides the guidelines for quantitating the BER and PER in error control coding
300 and a road map to design various VANET architectures. In future work, RS error probability can be
301 analyzed for more number of antennas. Further, a VANET channel model for V2X communication can be
302 developed using large antenna array sizes.

303 LIST OF ABBREVIATIONS

304	ASE	Amplified Spontaneous Emission
305	ASTBC	Alamouti Space Time Block Coding
306	AT	Atmospheric Turbulence
307	BCH	Bose–Chaudhuri–Hocquenghem [C-ITS] Cooperative-Intelligent Transport System
308		communications
309	FEC	Forward Error Correction
310	GSM	Global System Mobile
311	ICC	Interchannel Crosstalk
312	LOS	Line of Sight
313	MAC	Medium Access Control
314	MIMO	Multi-Input Multi-Output
315	NGV	Next-Generation V2X
316		item [NOMA] Non-Orthogonal Multiple Access
317	OFDM	Orthogonal Frequency Division Multiplexing
318	PHY	Physical Layer
319	PER	Packet Error Rate
320	PRR	Packet Reception Ratio
321	3GPP	3rd Generation Partnership Project
322	16QAM	Quadrature Amplitude Modulation
323	RS	Reed Solomon
324	STBC	Space-Time-Block-Coding
325	SPM	Sub carrier-Power Modulation
326	VANET	Vehicular ad-Hoc Network
327	V2I	Vehicle to Infrastructure
328	V2X	Vehicle to Everything
329	V2V	Vehicle to Vehicle

330 LIST OF NOTATIONS AND DEFINITIONS

331	H_{ef}^H	conjugate transpose of H_{ef}
332	km/h	Kilo meter per hour
333	γ	Signal-to -Noise Ratio
334	ψ	far-zone phase difference between adjacent elements
335	θ	represents angle of arrival in beamforming
336	ϕ	represents angle of reflection
337	s	corresponds to periodicity of complex weight
338	N	transmitting antennas
339	d	equidistant spacing between elements
340	f_d	Doppler shift
341	v	Relative velocity
342	n	Coded bits

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