

# beadplexr: Reproducible and automated analysis of multiplex bead assays

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Multiplex bead assays are an extension of the commonly used sandwich ELISA. The advantage over ELISA is that they make simultaneous evaluation of several analytes possible. Several commercial assay systems, where the beads are acquired on a standard flow cytometer, exist. These assay systems come with their own software tool for analysis and evaluation of the concentration of the analyzed analytes. However, these tools are either tied in to particular commercial software or impose limitations to the number of beads that can be analyzed. In addition, all these solutions are ‘point and click’ which potentially obscures the steps taken in the analysis. Here we present beadplexer, an open-source R-package for the reproducible analysis of multiplex bead assay data. The package makes it possible to automatically identify bead clusters, and makes it easy to fit a standard curve and calculate the concentrations of the analyzed analytes. beadplexer is available from CRAN and from <https://gitlab.com/ustervbo/beadplexr>.

## 1 **beadplexr: Reproducible and automated analysis of multiplex bead assays**

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### 9 **Abstract**

10 Multiplex bead assays are an extension of the commonly used sandwich ELISA. The advantage  
11 over ELISA is that they make simultaneous evaluation of several analytes possible. Several  
12 commercial assay systems, where the beads are acquired on a standard flow cytometer, exist.  
13 These assay systems come with their own software tool for analysis and evaluation of the  
14 concentration of the analyzed analytes. However, these tools are either tied in to particular  
15 commercial software or impose limitations to the number of beads that can be analyzed. In  
16 addition, all these solutions are ‘point and click’ which potentially obscures the steps taken in the  
17 analysis. Here we present **beadplexer**, an open-source R-package for the reproducible analysis  
18 of multiplex bead assay data. The package makes it possible to automatically identify bead  
19 clusters, and makes it easy to fit a standard curve and calculate the concentrations of the  
20 analyzed analytes. **beadplexer** is available from CRAN and from  
21 <https://gitlab.com/ustervbo/beadplexr>.

### 22 **Introduction**

23 The enzyme-linked immunosorbent assay (ELISA) is a commonly used method to determine the  
24 concentration of soluble analytes such as cytokines. It is a single point assay and query into  
25 several analytes can be time consuming. Development in polystyrene bead preparations made it  
26 possible to construct assays that allow for query of several analytes at the same time. Similar to  
27 the ELISA, the analytes of interest are captured by a primary antibody. The captured analytes are  
28 subsequently labelled with a secondary antibody and finally detected with a fluorochrome  
29 conjugated tertiary antibody (Figure 1A). The detection antibody is specific for the secondary  
30 antibody. In a multiplex bead assay, the primary antibody is fixed on a polystyrene bead, and

31 physical properties as well as colors of the beads are used to distinguish the different analytes  
32 studied. The data is usually collected using a standard flow cytometer.

33 The LEGENDplex system from BioLegend, the CBA system from BD Biosciences, and the  
34 MACSPlex from Miltenyi Biotec are all bead based multiplex systems. The systems differ  
35 slightly in terms of properties and colors used, and in the number of analytes that can be  
36 simultaneously identified. The Bio-Plex system from Bio-Rad works in a similar manner as those  
37 described here, but requires a dedicated instrument and does not produce files suitable for  
38 analysis with **beadplexr**. The individual assays that can be analyzed with **beadplexr** are  
39 described below.

40 **LEGENDplex:** Beads fall into two large groups based on forward and side scatter properties.  
41 Within each group, the individual analytes detected are discriminated by the intensity of  
42 Allophycocyanin (APC) of the beads. The concentration of the analyte is related to the intensity  
43 of Phycoerythrin (PE).

44 **CBA:** All beads have similar forward and side scatter properties. The individual analytes are  
45 discriminated by the intensity of APC and APC-Cy7 of the bead. The concentration of the  
46 analyte is related to the intensity of PE.

47 **MACSPlex:** All beads have similar forward and side scatter properties. The individual analytes  
48 are discriminated by the intensity of PE and Fluorescein isothiocyanate (FITC) of the bead. The  
49 concentration of the analyte is related to the intensity of APC.

50 All multiplex systems come with their own analysis software. However, these solutions might  
51 come with an added price tag because of binding to a particular piece of software, or because the  
52 analysis software allows analysis of only a limited number of beads. In addition, the usability  
53 and flexibility of the analysis solutions are restricted and often impractical for experiments with a  
54 large number of samples. Currently no open source alternative exists.

55 Here the general usage of the **beadplexr** package for R (R Core Team, 2018) is introduced. It  
56 will be demonstrated how to load the FACS-files, identify bead populations, draw standard  
57 curves and calculate concentration of the test samples.

## 58 **Materials & Methods**

59 The functionality of the package is illustrated using the LEGENDplex example data set included  
60 in the package. The data are from an unpublished "Human Growth Factor Panel (13-plex)"  
61 (BioLegend) experiment performed in our laboratory. The dataset consists of eight controls  
62 samples and a serum sample from a single healthy volunteer. All samples were processed in  
63 duplicates and per manufacturer's instructions. The data was acquired on a CytoFLEX cytometer  
64 (Beckman Coulter). An example fcs-file is also included in the package.

65 Data was analyzed with R, version 3.4.4, (R Core Team, 2018) and plots created with ggplot2  
66 (Wickham, 2009) and cowplot (Wilke, 2017).

## 67 Results

### 68 Package overview

69 The released package can be installed from CRAN and the development version from GitLab:

```
70 # From CRAN
71 install.packages("beadplexr")
72 # From GitLab using devtools
73 # install.packages("devtools")
74 devtools::install_git("https://gitlab.com/ustervbo/beadplexr")
75 #
76 # Or with vignettes built
77 # devtools::install_git("https://gitlab.com/ustervbo/beadplexr",
78 #                        build_vignettes = TRUE)
```

79 The package provides several steps to extract the analyte concentration from the raw data (Figure  
80 1B). The functions for interacting with the data are flexible, but sensible defaults make them  
81 accessible to the novice R-user.

### 82 Reading fcs-files

83 **beadplexr** works with Flow Cytometry Standard (FCS) files (Seamer et al., 1997), which is the  
84 usual output of a flow cytometer. The function `read_fcs()` loads the given fcs-file using the  
85 functionality provided by the Bioconductor package **flowcore** (Ellis et al., 2017) and performs  
86 the following steps:

- 87 1. Apply an arcsinh transformation of the bead channels
- 88 2. Remove boundary events of the forward and side scatter channels
- 89 3. Optionally subset the channels to contain just bead events – this might improve  
90 identification of the beads
- 91 4. Convert the FACS-data to a `data.frame`

92

```
93 library(beadplexr)
94
95 .file_name <- system.file("extdata",
96                           "K2-C07-A7.fcs",
97                           package = "beadplexr")
98 .data <- read_fcs(
```

```
99   .file_name = .file_name,  
100  .fsc_ssc = c("FSC-H", "SSC-H"),  
101  .bead_channels = c("FL6-H", "FL2-H"),  
102  .filter = list(  
103    "FSC-H" = c(3.75e5L, 5.5e5L),  
104    "SSC-H" = c(4e5L, 1e6L),  
105    "FL6-H" = c(7L, Inf)  
106  )  
107 )
```

108 It might get a bit of trying to get the settings correct for an experiment, but once established it  
109 should remain stable. However, this provides that there are no change of cytometer, and that  
110 there is no particular drift in the used cytometer.

111 The loaded FACS data can be visualized with the `facs_plot()` convenience function (Figure 2),  
112 which make use of `ggplot2` (Wickham, 2009).

### 113 Identification of analyte MFI

114 The first step of the experiment analysis is to get the mean fluorescence intensity (MFI) of each  
115 analyte. In the case of LEGENDplex data, this requires the identification of each analyte per size  
116 and APC intensity and the MFI of in the PE channel. The function  
117 `identify_legendplex_analyte()` is a convenience function for identifying the bead  
118 populations and their MFIs for an experiment based on the LEGENDplex assay.

119 Identification of analytes is achieved with the function `identify_analyte()`, which finds  
120 analyte clusters and sort the analyte clusters based on their centres. Several methods for  
121 automatic cluster identification can be evoked by the function. The default function is `clara()`  
122 (clustering large applications) from the package `cluster`. (Maechler et al., 2017). The base  
123 `kmeans()` as well as `dbscan()` from the `fpc` package, and `mclust()` from the `mclust` package  
124 are also interfaced (Hennig, 2015; Scrucca et al., 2016). We have found that `dbscan()` is the best  
125 clustering for the forward-side scatter population identification, but requires some (and  
126 sometimes a lot) trial and error to get the parameters right. `clara()` is a great all-rounder, but in  
127 some cases - such as this - `mclust()` is the better choice. The best function depends on the data,  
128 and finding it is a matter of trial and error.

129 `identify_legendplex_analyte()` make use of structured Panel Information to identify the  
130 two bead populations according to their forward and side scatter properties, and for each of these  
131 subpopulations, the analytes are identified. The package comes with a set of LEGENDplex panel  
132 definitions, and more are being added. The Panel Information can be loaded by passing the name  
133 or a name pattern to the `load_panel()` function. The information file is in YAML format, and  
134 contains name and start concentration for each bead ID, the name of the panel, the fold dilution  
135 of the standards, and the units of the analytes. It is also possible to specify a file outside the

136 package. The panel definition is not required, but makes sense if the assay is repeated across  
137 several projects.

```
138 library(dplyr)
139 library(purrr)
140
141 data(lplex)
142
143 panel_info <-
144   load_panel(.panel_name = "Human Growth Factor Panel (13-plex)")
145
146 args_ident_analyte <-
147   list(
148     fs = list(
149       .parameter = c("FSC-A", "SSC-A"),
150       .column_name = "Bead group",
151       .method = "mclust"
152     ),
153     analytes = list(.parameter = "FL6-H",
154                   .column_name = "Analyte ID")
155   )
156
157 analytes_identified <- lplex %>%
158   lapply(
159     identify_LEGENDplex_analyte,
160     .analytes = panel_info$analytess,
161     .method_args = args_ident_analyte
162   )
```

163 The analyte IDs for the “Human Growth Factor Panel (13-plex)” bead group A are A4, A5, A6,  
164 A7, A8, A10 and for group B the analyte IDs are B2, B3, B4, B5, B6, B7, B9. In this case, the  
165 beads are arranged from low to high, that is the lowest analyte ID has lowest intensity in the  
166 APC channel (Figure 3).

167 This initial and crucial step of the analysis has been successfully performed with unpublished  
168 data from a CBA experiment and from a MACSPlex experiment using the function  
169 `identify_analyte()`.

170 With the analytes identified and the bead populations documented the MFI of each analyte can  
171 finally be calculated. `beadplexr` provides the possibility to calculate geometric, harmonic, and  
172 arithmetic mean. We combine the list of FACS-data to a `data.frame` with Sample, analyte ID,  
173 and the MFI because the creation of a standard curve in the next steps needs the MFI of several  
174 standard samples.

```

175 analyte_mfi <- analytes_identified %>%
176   filter(!is.na(`Analyte ID`)) %>%
177   map_df(calc_analyte_mfi,
178         .parameter = "FL2-H",
179         .column_name = "Analyte ID",
180         .mean_fun = "geometric",
181         .id = "Sample") %>%
182   mutate(`FL2-H` = log10(`FL2-H`))

```

### 183 Calculation of standard and test samples

184 The calculation of the analytes requires two steps:

- 185 1. Create a standard curve by fitting a function to the MFI of the standard analytes and their  
186 known concentration.
- 187 2. Estimate the concentration of each sample analyte from the fitted function.

188 Split the `data.fame` with the MFI information into standard and samples.

```

189 # ALL standard samples have the pattern C[number]
190 standard_data <- analyte_mfi %>%
191   filter(grepl("C[0-9]", Sample))
192
193 # ALL non-standards are samples... we could also filter on S[number]
194 sample_data <- analyte_mfi %>%
195   filter(!grepl("C[0-9]", Sample))

```

196 The first thing needed to calculate the standard curve for each analyte is the concentration of the  
197 analyte. This we can calculate using the function `calc_std_conc()`, when we know the order of  
198 the samples, the start concentration, and the dilution factor.

199 The order of the samples usually ranges from 0 to 7. If the nomenclature on the LEGENDplex  
200 assay protocol is followed, 7 indicates the highest concentration of the standard analyte, 1  
201 indicates the lowest concentration and 0 indicates blank. The start concentration for each analyte  
202 is stored in the Panel Information (depending on the panel it might differ from analyte to  
203 analyte). The dilution factor is also given in the Panel Information and is usually 4 (the  
204 concentration of each standard analyte is 4 times lower than the previous concentration). If - for  
205 some reason - you do not use the same dilution factor throughout all analytes and standards you  
206 need to indicate the appropriate dilution factors by hand.

```

207 # Helper function to extract the sample number
208 as_numeric_standard_id <- function(.s){
209   .s %>%
210     stringr::str_extract("C[0-9]") %>%
211     stringr::str_sub(start = -1L) %>%

```

```

212     stringr::as.numeric()
213 }
214
215 standard_data <- standard_data %>%
216   mutate(`Sample number` = as_numeric_standard_id(Sample)) %>%
217   left_join(as_data_frame_analyte(panel_info$analytes),
218           by = "Analyte ID") %>%
219   group_by(`Analyte ID`) %>%
220   mutate(
221     Concentration = calc_std_conc(
222       `Sample number`,
223       concentration,
224       .dilution_factor = panel_info$std_dilution
225     )
226   ) %>%
227   mutate(Concentration = log10(Concentration)) %>%
228   select(-concentration, -`Bead group`)

```

229 The next step is to fit a standard curve for each analyte. With the standard curve we can calculate  
 230 the concentration of the experimental samples (the purpose of the initial work), we can check the  
 231 quality of the measurements - and the standard curve - by back calculate the standard  
 232 concentration and compare this to the expected concentration, and we can plot the experimental  
 233 samples on the standard curve ([beadplexr](#) provides easy functions for all of this).

234 However, in each case we need to ensure that the correct standard curve is used with the correct  
 235 data, which means we have to juggle at least three structures: A [data.frame](#) with the standard  
 236 data, a [data.frame](#) with the experimental sample data and the models for each analyte (probably  
 237 a list). It quickly becomes tedious to ensure that everything is in the correct order - and to be sure  
 238 it is error prone.

239 To circumvent this, we can use the [nest\(\)](#) and its inverse [unnest\(\)](#) functions of the [tidyr](#)  
 240 package (Wickham & Henry, 2018).

```

241 library(tidyr)
242
243 standard_data <- standard_data %>%
244   ungroup() %>%
245   nest(-`Analyte ID`, -name, .key = "Standard data")
246
247 sample_data <- sample_data %>%
248   ungroup() %>%
249   nest(-`Analyte ID`, .key = "Sample data")
250

```

```
251 plex_data <-  
252   inner_join(standard_data, sample_data, by = "Analyte ID")
```

253 With everything in a neatly arranged `data.frame` we can now focus on the actual task at hand,  
254 namely calculation of the standard curve for each analyte. For this we use the function  
255 `fit_standard_curve()`, which interfaces the `drm()` function from the `drc` package (Ritz et al.,  
256 2015).

```
257 # When clustering is performed with mclust, the package mclust is  
258 # loaded in the background (an unfortunate necessity). The mclust  
259 # package also has a function called `map`, so an unlucky side effect  
260 # of clustering with mclust, is that we need to be specify which map  
261 # function we use  
262 plex_data <- plex_data %>%  
263   group_by(`Analyte ID`) %>%  
264   mutate(`Model fit` = purrr::map(`Standard data`,  
265     fit_standard_curve))
```

266 We can plot the standard curve using the built in `plot_std_curve()` function (Figure 4A). With  
267 the standard curve created we can estimate the concentrations of the samples, but also of the  
268 standards. The latter is to help us verify that the standard measurements were all fine, and that  
269 we can trust the estimation of the sample concentrations.

270 After calculating the concentrations we can plot the known standard concentrations versus the  
271 estimated standard concentrations using the function `plot_target_est_conc()` (Figure 4B) and  
272 visualize where the samples fall on the standard curve with `plot_target_est_conc()` (Figure  
273 4C).

```
274 plex_data <- plex_data %>%  
275   group_by(analyte.ID) %>%  
276   mutate(`Standard data` =  
277     purrr::map2(`Standard data`, `Model fit`,  
278       calculate_concentration)) %>%  
279   mutate(`Sample data` =  
280     purrr::map2(`Sample data`, `Model fit`,  
281       calculate_concentration)) %>%  
282   mutate(`Std conc` =  
283     purrr::map(`Standard data`,  
284       plot_target_est_conc)) %>%  
285   mutate(`Est curve` =  
286     purrr::pmap(  
287       list(`Sample data`, `Standard data`, `Model fit`, name),  
288       plot_estimate  
289     ))
```

290 Lastly we fulfill the purpose of everything above and extract the concentration of each analyte  
291 for each sample.

```
292 plex_data %>%  
293   unnest(`Sample data`) %>%  
294   mutate( Calc.conc = 10 ^ Calc.conc,  
295           `Calc.conc error` = 10 ^ `Calc.conc error` )
```

## 296 Discussion

297 Multiplex bead assays make simultaneous evaluation of several analytes possible. Because of  
298 this, they are an attractive alternative to the commonly used sandwich ELISA. Commercial  
299 systems are available for acquisition on a standard flow cytometer. For the data analysis, these  
300 commercial systems make use of their own proprietary software, which impose different  
301 limitations to the analysis. The R-package **beadplexr**, released under the MIT license, is meant  
302 as an open-source alternative to these commercial systems. The package is available from CRAN  
303 and from <https://gitlab.com/ustervbo/beadplexr>.

304 A critical step in the analysis multiplex bead assays is the identification of bead populations  
305 corresponding to each analyte. A single function in **beadplexr** acts as an interface to several  
306 common, and tested, cluster functions, making it easy to find the best suited cluster function.  
307 Future versions of the package will see improvements in this part, with inclusion of other  
308 clustering methods and perhaps a heuristic for automatic method selection.

309 Flow cytometry data are inherently noisy. The R-package only provides a rudimentary function  
310 for removing lonely points and lets the cluster functions determine which events are considered  
311 noisy. However, a very noisy data set might make it difficult for an optimal identification of the  
312 bead clusters. De-noising multidimensional data is not trivial, but work is planned in this  
313 direction for a future release.

## 314 Conclusion

315 **beadplexr** provides a frame work for easy and reproducible analysis of multiplex bead assays  
316 for the experienced and the novice user alike.

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338

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## 341 **Competing Interests**

342 The authors declare that they have no competing interests.

## 343 **Author Contributions**

344 US performed the experiments, authored the R-package, prepared the figures, and authored the  
345 paper. TW and NB designed the study and authored the paper.

346 **Figure legends**

347 **Figure 1: Overview of assay principle and the package workflow.**

348 A) Schematic overview of the principle of a LEGENDplex assay. B) Steps in analysis of a  
349 multiplex bead assay with accompanying visualizations.

350 **Figure 2: Visualization of FACS data.**

351 A) Common monochrome dot-plot. B) Pseudo-colored dot-plot (requires the R-package [hexbin](#)  
352 to be installed).

353 **Figure 3: Bead identification and visualization of LEXENDplex data.**

354 A) Identification of the two bead populations 'A' and 'B' in a LEGENDplex data set. B)  
355 Identification of analytes of the bead population 'A'. B) Identification of analytes of the bead  
356 population 'B'. Noisy data points are assigned the group 'None' or 'NA'.

357 **Figure 4: Visualization of standard and test samples for Angiopoietin-2.**

358 A) The standard curve of Angiopoietin-2 ranging from 50,000.0 to 12.21 pg/ml. B) Correlation  
359 between the standard concentration (x-axis) and the calculated concentration of the standard  
360 samples (y-axis). The back calculation is done using the fit in (A) and the MFI of the samples.  
361 C) Position of the test samples on the standard curve.

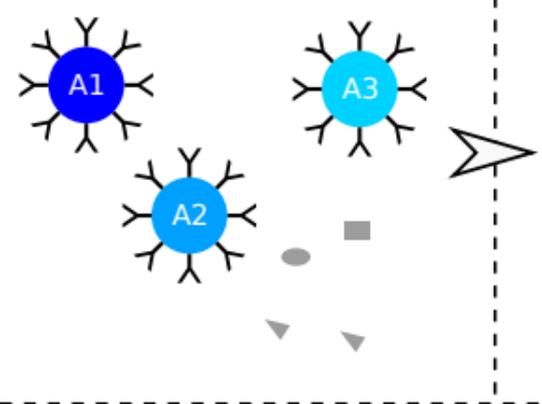
**Figure 1** (on next page)

Overview of assay principle and the package workflow

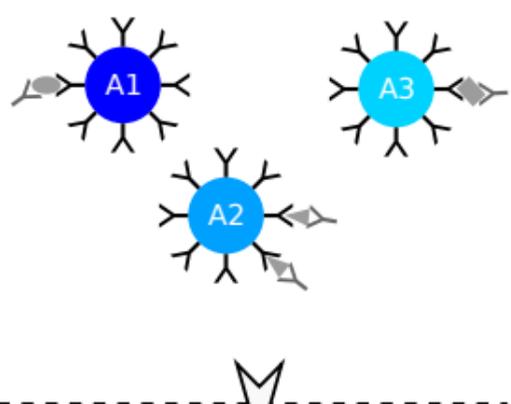
A) Schematic overview of the principle of a LEGENDplex assay. B) Steps in analysis of a multiplex bead assay with accompanying visualizations.

**A**

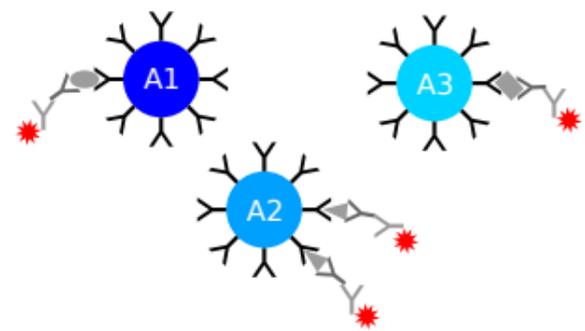
Mix beads and samples



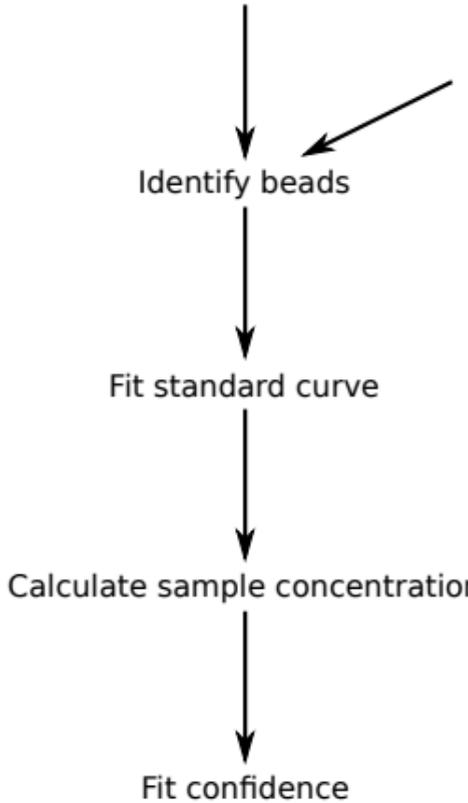
Incubate with secondary antibody



Incubate with tertiary antibody

**B**

Load and process FACS-files



- Dot-plot
- Pseudo color plot

Parse panel information

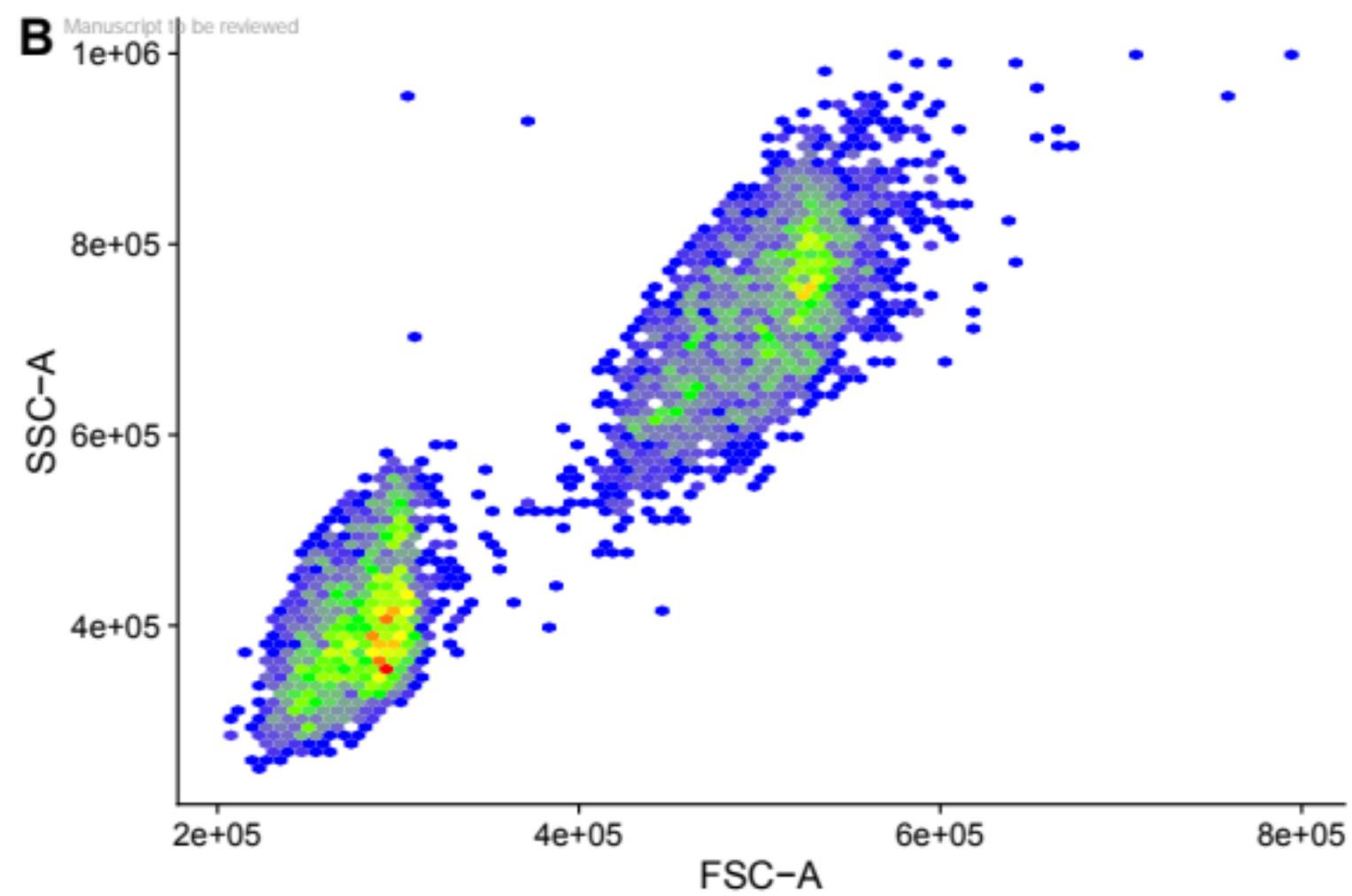
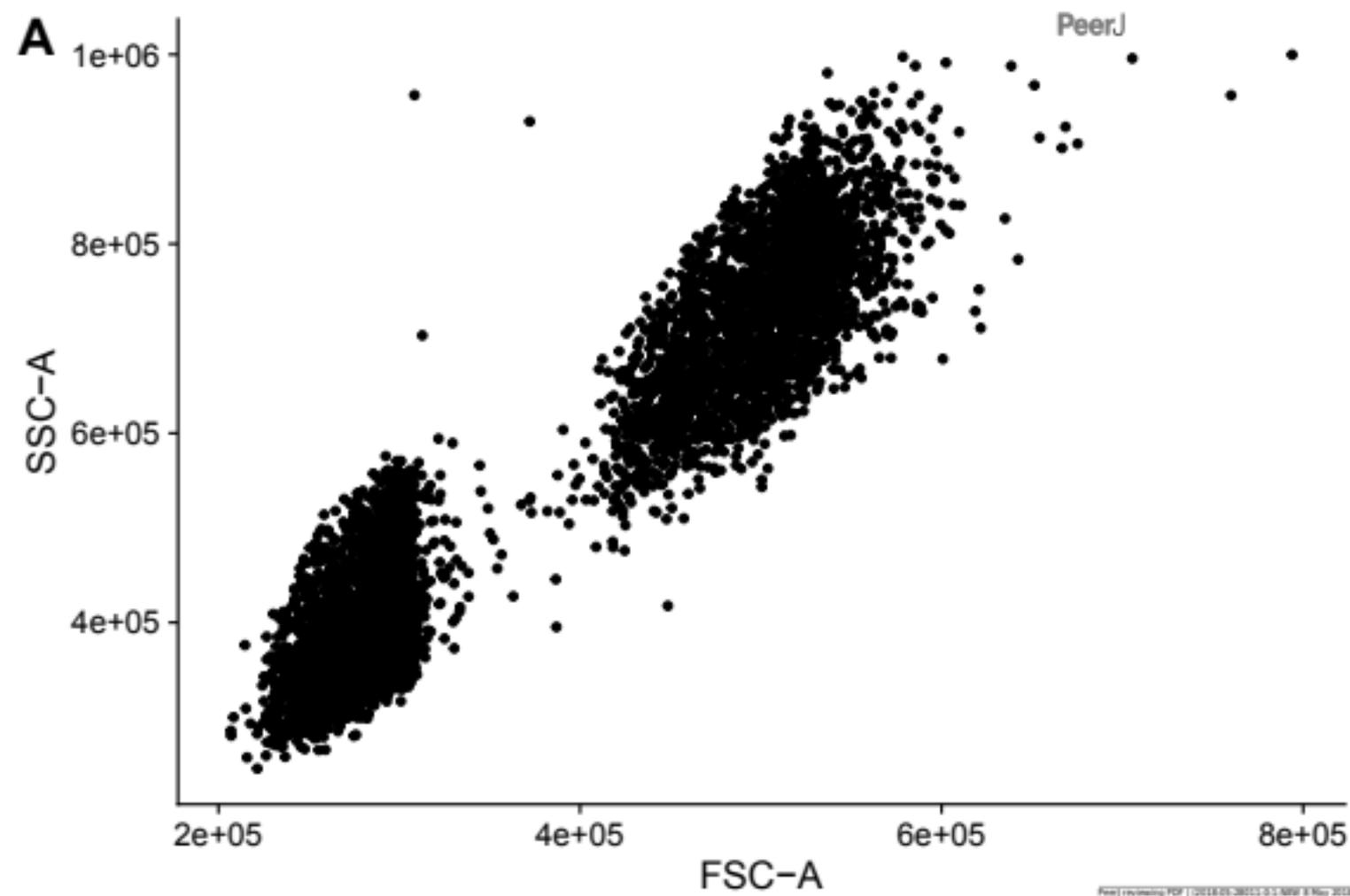
- Dot-plot
- Histogram

- Standard curve
- Expected vs. calculated standard concentration
- Analyte on standard curve

**Figure 2** (on next page)

Visualization of FACS data

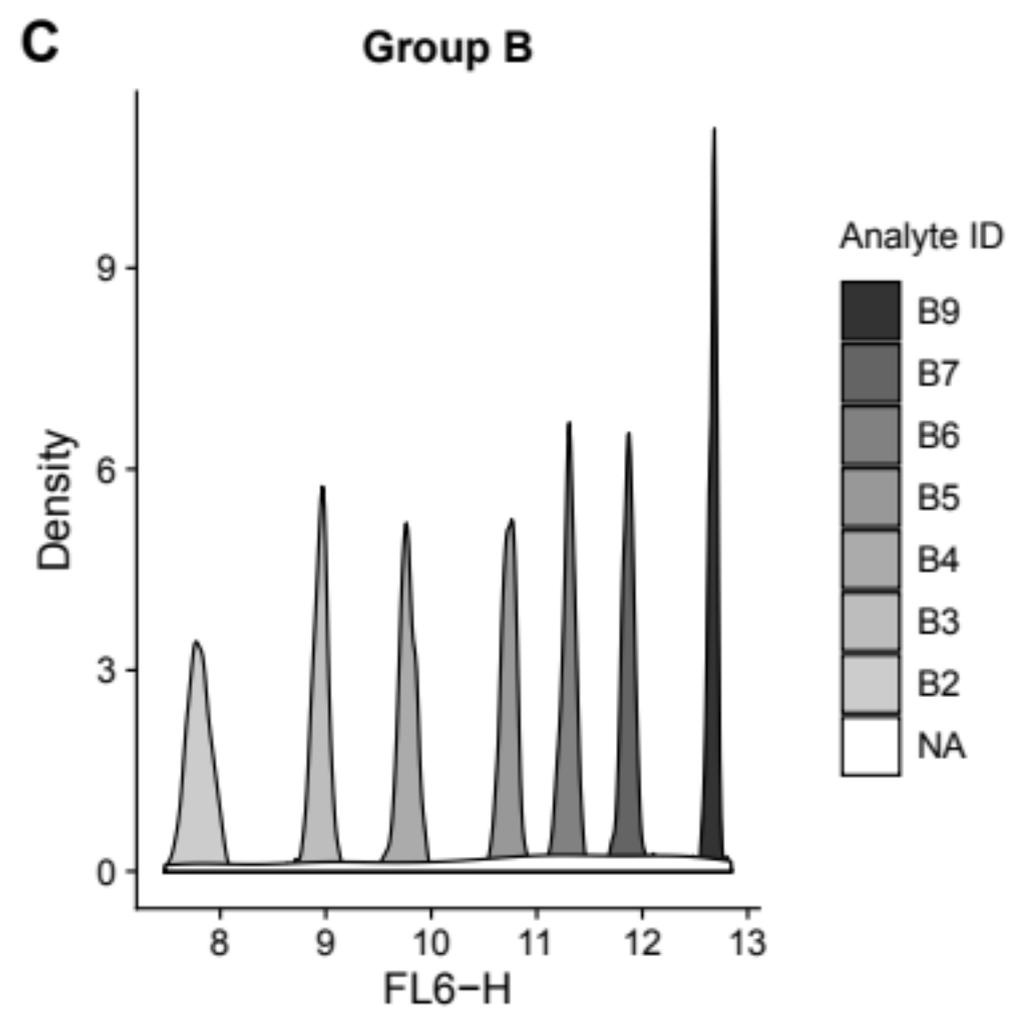
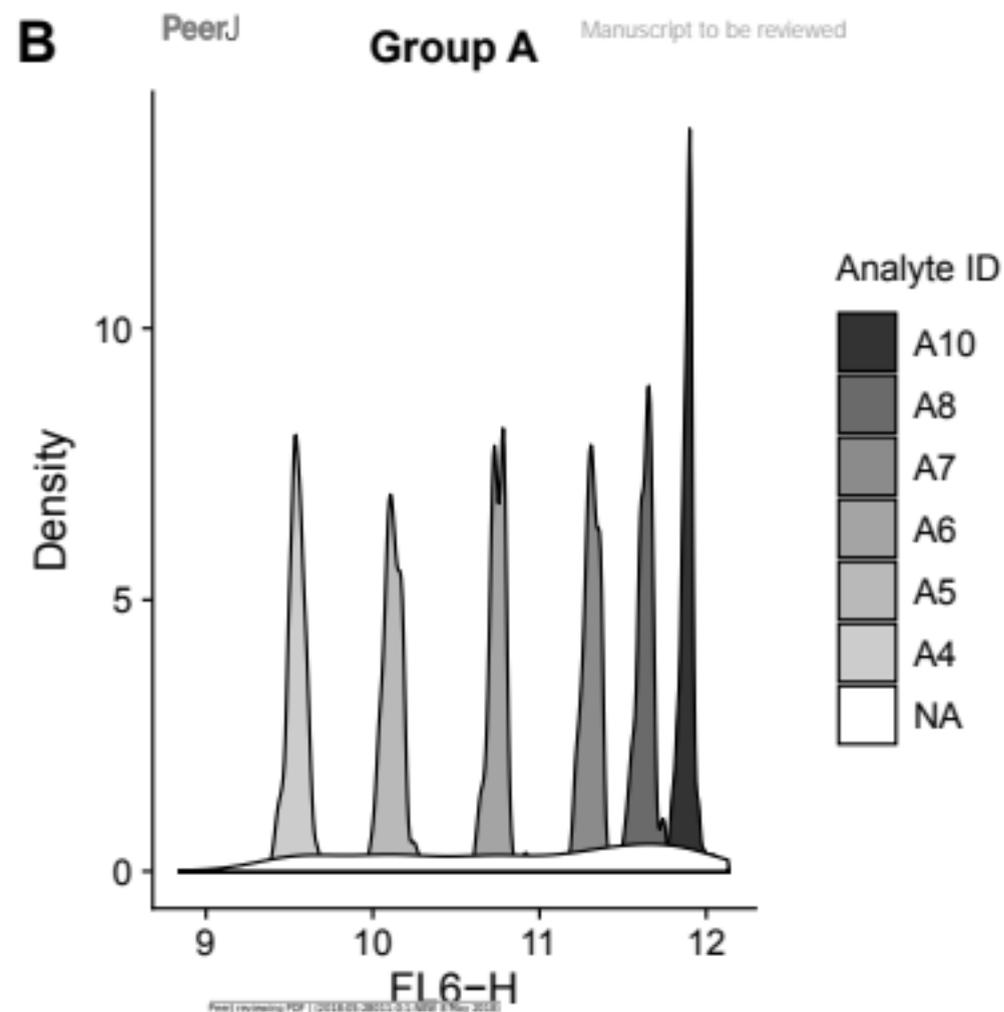
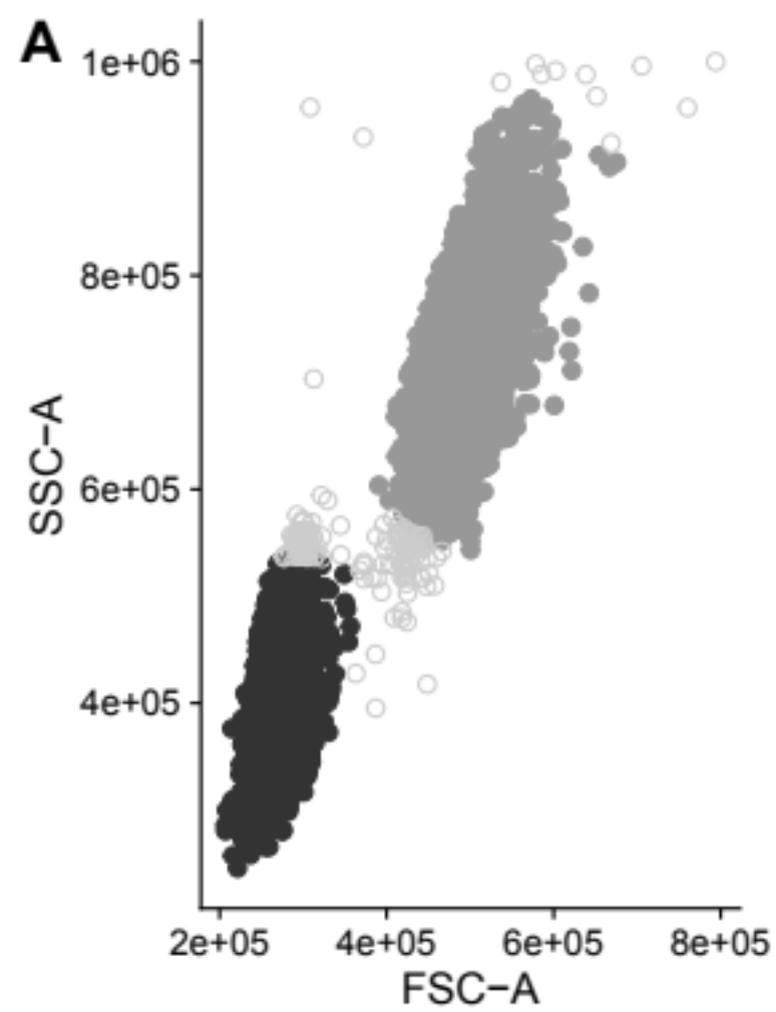
A) Common monochrome dot-plot. B) Pseudo-colored dot-plot (requires the R-package hexbin to be installed).



**Figure 3**(on next page)

Bead identification and visualization of LEXENDplex data

A) Identification of the two bead populations 'A' and 'B' in a LEGENDplex data set. B) Identification of analytes of the bead population 'A'. B) Identification of analytes of the bead population 'B'. Noisy data points are assigned the group 'None' or 'NA'.



**Figure 4**(on next page)

Visualization of standard and test samples for Angiopoietin-2

A) The standard curve of Angiopoietin-2 ranging from 50,000.0 to 12.21 pg/ml. B) Correlation between the standard concentration (x-axis) and the calculated concentration of the standard samples (y-axis). The back calculation is done using the fit in (A) and the MFI of the samples. C) Position of the test samples on the standard curve.

