

A brief introduction to mixed effects modelling and multi-model inference in ecology

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The use of linear mixed effects models (LMMs) is increasingly common in the analysis of biological data. Whilst LMMs offer a flexible approach to modelling a broad range of data types, ecological data are often complex and require complex model structures, and the fitting and interpretation of such models is not always straightforward. The ability to achieve robust biological inference requires that practitioners know how and when to apply these tools. Here, we provide a general overview of current methods for the application of LMMs to biological data, and highlight the typical pitfalls that can be encountered in the statistical modelling process. We tackle several issues relating to the use of information theory and multi-model inference in ecology, and demonstrate the tendency for data dredging to lead to greatly inflated Type I error rate (false positives) and impaired inference. We offer practical solutions and direct the reader to key references that provide further technical detail for those seeking a deeper understanding. This overview should serve as a widely accessible code of best practice for applying LMMs to complex biological problems and model structures, and in doing so improve the robustness of conclusions drawn from studies investigating ecological and evolutionary questions.

1 A Brief Introduction to Mixed Effects Modelling and Multi-model Inference in Ecology

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25 ABSTRACT

26 The use of linear mixed effects models (LMMs) is increasingly common in the analysis of
27 biological data. Whilst LMMs offer a flexible approach to modelling a broad range of data
28 types, ecological data are often complex and require complex model structures, and the
29 fitting and interpretation of such models is not always straightforward. The ability to
30 achieve robust biological inference requires that practitioners know how and when to
31 apply these tools. Here, we provide a general overview of current methods for the
32 application of LMMs to biological data, and highlight the typical pitfalls that can be
33 encountered in the statistical modelling process. We tackle several issues relating to the
34 use of information theory and multi-model inference in ecology, and demonstrate the
35 tendency for data dredging to lead to greatly inflated Type I error rate (false positives)
36 and impaired inference. We offer practical solutions and direct the reader to key
37 references that provide further technical detail for those seeking a deeper
38 understanding. This overview should serve as a widely accessible code of best practice
39 for applying LMMs to complex biological problems and model structures, and in doing so
40 improve the robustness of conclusions drawn from studies investigating ecological and
41 evolutionary questions.

42 Introduction

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44 In recent years, the suite of statistical tools available to biologists and the complexity of
45 biological data analyses have grown in tandem (Low-Decarie et al 2014; Zuur & Ieno
46 2016; Kass et al 2016). The availability of novel and sophisticated statistical techniques
47 means we are better equipped than ever to extract signal from noisy biological data, but
48 it remains challenging to know how to apply these tools, and which statistical
49 technique(s) might be best suited to answering specific questions (Kass et al 2016).
50 Often, simple analyses will be sufficient (Murtaugh 2007), but more complex data
51 structures often require more complex methods such as linear mixed effects models
52 (Zuur et al 2009), generalized additive models (Wood et al 2015) or Bayesian inference
53 (Ellison 2004). Both accurate parameter estimates and robust biological inference
54 require that ecologists be aware of the pitfalls and assumptions that accompany these
55 techniques and adjust modelling decisions accordingly (Bolker et al 2009).

56 Linear mixed effects models (LMMs) and generalized linear mixed effects models
57 (GLMMs), have gained significant traction in the last decade (Zuur et al 2009; Bolker et
58 al 2009). Both extend traditional linear models to include a combination of fixed and
59 random effects as predictor variables. The introduction of random effects affords several
60 non-exclusive benefits. First, biological datasets are often highly structured, containing
61 clusters of non-independent observational units that are hierarchical in nature, and
62 LMMs allow us to explicitly model the non-independence in such data. For example, we
63 might measure several chicks from the same clutch, and several clutches from different
64 females, or we might take repeated measurements of the same chick's growth rate over
65 time. In both cases, we might expect that measurements within a statistical unit (here,
66 an individual, or a female's clutch) might be more similar than measurements from
67 different units. Explicit modelling of the random effects structure will aid correct inference
68 of fixed effects, depending on which level of the system's hierarchy is being
69 manipulated. In our example, if the fixed effect varies or is manipulated at the level of the
70 clutch, then pseudoreplicated measurements of each chick can be controlled carefully
71 using random effects. Alternatively, if fixed effects vary at the level of the chick, then

72 non-independence among clutches or mothers can be accounted for. Random effects
73 typically represent some grouping variable (Breslow and Clayton 1993) and allow the
74 estimation of variance in the response variable within and among these groups. This
75 reduces the probability of false positives (Type I error rates) and false negatives (Type II
76 error rates, e.g. Crawley 2013). Second, inferring the magnitude of variation within and
77 among statistical clusters or hierarchical levels can be highly informative in its own right.
78 In our bird example, understanding whether there is more variation in a focal trait among
79 females within a population, rather than among populations, might be a central goal of
80 the study.

81 LMMs are powerful yet complex tools. Software advances have made these tools
82 accessible to the non-expert and have become relatively straightforward to fit in widely
83 available statistical packages such as R (R Core Team 2016). Here we focus on the
84 implementation of LMMs in R, although the majority of the techniques covered here can
85 also be implemented in alternative packages including SAS (SAS Institute, Cary, NC) &
86 SPSS (SPSS Inc., Chicago, IL). It should be noted however that due to different
87 computational methods employed by different packages there maybe differences in the
88 model outputs generated. These differences will generally be subtle and the overall
89 inferences drawn from the model outputs should be the same.

90 Despite this ease of implementation, the correct use of LMMs in the biological
91 sciences is challenging for several reasons: i) they make additional assumptions about
92 the data to those made in more standard statistical techniques such as general linear
93 models (GLMs), and these assumptions are often violated (Bolker et al 2009); ii)
94 interpreting model output correctly can be challenging, especially for the variance
95 components of random effects (Bolker et al 2009; Zuur et al 2009); iii) model selection
96 for LMMs presents a unique challenge, irrespective of model selection philosophy,
97 because of biases in the performance of some tests (e.g. Wald tests, AIC comparisons)
98 introduced by the presence of random effects (Vaida & Blanchard 2005; Dominicus et al
99 2006; Bolker et al 2009). Collectively, these issues mean that the application of LMM
100 techniques to biological problems can be risky and difficult for those that are unfamiliar
101 with them. There have been several excellent papers in recent years on the use of
102 generalized linear mixed effects models (GLMMs) in biology (Bolker et al 2009), the use
103 of information theory and multi-model inference for studies involving LMMs (Grueber et
104 al 2011), best practice for data exploration (Zuur et al 2009) and for conducting statistical

105 analyses for complex datasets (Zuur & Ieno 2016; Kass et al 2016). At the interface of
106 these excellent guides lies the theme of this paper: an updated guide for the uninitiated
107 through the model fitting and model selection processes when using LMMs. A secondary
108 but no less important aim of the paper is to bring together several key references on the
109 topic of LMMs, and in doing so act as a portal into the primary literature that derives,
110 describes and explains the complex modelling elements in more detail.

111 We provide a best practice guide covering the full analysis pipeline, from
112 formulating hypotheses, specifying model structure and interpreting the resulting
113 parameter estimates. The reader can digest the entire paper, or snack on each
114 standalone section when required. First, we discuss the advantages and disadvantages
115 of including both fixed and random effects in models. We then address issues of model
116 specification, and choice of error structure and/or data transformation, a topic that has
117 seen some debate in the literature (e.g. O'Hara & Kotze 2010; Ives 2015). We also
118 address methods of model selection, and discuss the relative merits and potential pitfalls
119 of using information theory (IT), AIC and multi-model inference in ecology and evolution.
120 At all stages, we provide recommendations for the most sensible manner to proceed in
121 different scenarios.

122 Understanding Fixed and Random Effects

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124 A key decision of the modelling process is specifying model predictors as fixed or
125 random effects. Unfortunately, the distinction between the two is not always obvious,
126 and is not helped by the presence of multiple, often confusing definitions in the literature
127 (see Gelman and Hill 2007 p. 245). Absolute rules for how to classify something as a
128 fixed or random effect generally are not useful because that decision can change
129 depending on the goals of the analysis (Gelman and Hill 2007). We can illustrate the
130 difference between fitting something as a fixed (M1) or a random effect (M2) using a
131 simple example of a researcher who takes measurements of mass from 100 animals
132 from each of 5 different groups ($n = 500$) with a goal of understanding differences among
133 groups in mean mass. We use notation equivalent to fitting the proposed models in the
134 statistical software *R* (R Core Team 2016), with the LMMs fitted using the R package
135 *lme4* (Bates et al. 2015):

136

137

```
M1 <- glm (mass ~ group)
```

138

```
M2 <- lmer(mass ~ 1 + (1|group))
```

139

140 Fitting 'group' as a fixed effect in model M1 assumes the 5 'group' means are all
141 independent of one another, and share a common residual variance. Conversely, fitting
142 group as a random intercept model in model M2 assumes that the 5 measured group
143 means are only a subset of the realised possibilities drawn from a 'global' set of
144 population means that follow a Normal distribution with its own mean (μ_{group} , Fig. 1A) and
145 variance (σ^2_{group}). Therefore, LMMs model the variance hierarchically, estimating the
146 processes that generate among-group variation in means, as well as variation within
147 groups. Treating groups from a field survey as only a subset of the *possible* groups that
148 could be sampled is quite intuitive, because there are likely many more groups (e.g.
149 populations) of the study species in nature than the 5 the researcher measured.
150 Conversely if one has designed an experiment to test the effect of three different
151 temperature regimes on growth rate of plants, specifying temperature treatment as a
152 fixed effect appears sensible because the experimenter has deliberately set the variable
153 at a given value of interest. That is, there are no unmeasured groups with respect to that
154 particular experimental design.

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160 *Controlling for non-independence among data points*

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This is one of the most common uses of a random effect. Complex biological data sets often contain nested and/or hierarchical structures such as repeat measurements from individuals within and across units of time. Random effects allow for the control of non-independence by constraining non-independent 'units' to have the same intercept and/or slope (Zuur et al 2009; Zuur & Ieno 2016). Fitting only random intercepts, or both random intercepts and slopes, will be decided by the goals of the analysis and the dependency structure of the data (Zuur & Ieno 2016). Fitting *only* a random intercept allows group means to vary, but assumes all groups have a common slope for a fitted

169 covariate (fixed effect). Fitting random intercepts *and* slopes allows the slope of a
170 predictor to vary based on a separate grouping variable. For example, one hypothesis
171 might be that the probability of successful breeding for an animal is a function of its body
172 mass. If we had measured animals from multiple sampling sites, we might wish to fit
173 'sampling site' as a random intercept, and estimate a common slope (change in
174 breeding success) for body mass across all sampling sites by fitting it as a fixed effect:

```
175 M3 <- glmer(successful.breed ~ body.mass + (1|sample.site)
```

176 Conversely, we might wish to test the hypothesis that the strength of the effect (slope) of
177 body mass on breeding success varies depending on the sampling location i.e. the
178 change in breeding success for a 1 unit change in body mass is not consistent across
179 groups (Figure 1B). Here, 'body mass' is specified as a random slope by moving it into
180 the random effects structure:

```
181 M4 <- glmer(successful.breed ~ body.mass + (body.mass |  
182 sample.site)
```

183 Schielzeth & Forstmeier (2009) warn that constraining groups to share a common slope
184 can inflate Type I and Type II errors. Consequently, Grueber et al (2011) recommend
185 always fitting both random slopes and intercepts where possible. Whether this is
186 feasible or not will depend on the data structure (see 'Costs to Fitting Random Effects'
187 section below). Figure 1 describes the differences between random intercept models
188 and those also containing random slopes.

189 *Further reading: Zuur & Ieno (2016) shows examples of the difficulties in*
190 *identifying the dependency structure of data and how to use flow charts / graphics to*
191 *help decide model structure. Kery (2010, Ch 12) has an excellent demonstration of how*
192 *to fit random slopes, and how model assumptions change depending on specification of*
193 *a correlation between random slopes and intercepts or not. Schielzeth & Forstmeier*
194 *(2009) and van de Pol & Wright (2009) are useful references for understanding the utility*
195 *of random slope models.*

196 *Improving the accuracy of parameter estimation*

197 Random effect models use data from all the groups to estimate the mean and variance
198 of the global distribution of group means. Assuming all group means are drawn from a
199 common distribution causes the estimates of their means to drift towards the global
200 mean μ_{group} . This phenomenon, known as *shrinkage* (Gelman & Hill 2007; Kery 2010),
201 can also lead to smaller and more precise standard errors around means. Shrinkage is
202 strongest for groups with small sample sizes, as the paucity of within-group information
203 to estimate the mean is counteracted by the model using data from other groups to
204 improve the precision of the estimate. This ‘partial pooling’ of the estimates is a principal
205 benefit of fitting something as a random effect (Gelman & Hill 2007). However, it can feel
206 strange that group means should be shrunk towards the global mean, especially for
207 researchers more used to treating sample means as independent fixed effects.
208 Accordingly, one issue is that variance estimates can be hugely imprecise when there
209 are fewer than 5 levels of the random grouping variable (intercept or slope; see Harrison
210 2015). However, thanks to the Central Limit Theorem, the assumption of Gaussian
211 distribution of group means is usually a good one, and the benefits of hierarchical
212 analysis will outweigh the apparent costs of shrinkage.

213 *Estimating variance components*

214 In some cases, the variation among groups will be of interest to ecologists. For example,
215 imagine we had measured the clutch masses of 30 individual birds, each of which had
216 produced 5 clutches ($n=150$). We might be interested in asking whether different
217 females tend to produce consistently different clutch masses (high among-female
218 variance for clutch mass). To do so, we might fit an intercept-only model with Clutch
219 Mass as the response variable and a Gaussian error structure:

```
220 Model <- lmer(ClutchMass ~ 1 + (1|FemaleID))
```

221 By fitting individual ‘FemaleID’ as a random intercept term in the LMM, we estimate the
222 among-female variance in our trait of interest. This model will also estimate the residual
223 variance term, which we can use in conjunction with the among-female variance term to
224 calculate an ‘intra-class correlation coefficient’ that measures individual repeatability in
225 our trait (see Nakagawa & Schielzeth 2010). While differences among individuals can be
226 obtained by fitting individual ID as a fixed effect, this uses a degree of freedom for each

227 individual ID after the first, severely limiting model power, and does not benefit from
228 increased estimation accuracy through shrinkage. More importantly, repeatability scores
229 derived from variance components analysis can be compared across studies for the
230 same trait, and even across traits in the same study. Variance component analysis is a
231 powerful tool for partitioning variation in a focal trait among biologically interesting
232 groups, and several more complex examples exist (see Nakagawa & Schielzeth 2010;
233 Wilson et al 2010; Houslay & Wilson 2017). In particular, quantitative genetic studies rely
234 on variance component analysis for estimating the heritability of traits such as body
235 mass or size of secondary sexual characteristics (Wilson et al 2010). We recommend
236 the tutorials in Wilson et al (2010) and Houslay & Wilson (2017) for a deeper
237 understanding of the power and flexibility of variance component analysis.

238 *Making predictions for unmeasured groups*

239 Fixed effect estimates prevent us from making predictions for new groups because the
240 model estimates are only relevant to groups in our dataset (e.g. Zuur et al 2009 p. 327).
241 Conversely, we can use the estimate of the global distribution of population means to
242 predict for the average group using the mean of the distribution μ_{group} for a random
243 effects model (see Fig. 1). We could also sample hypothetical groups from our random
244 effect distribution, as we know its mean and SD (Zuur & Ieno 2016). Therefore, whether
245 something is fitted as a fixed or random effect can depend on the goal of the analysis:
246 are we only interested in the mean values for each group in our dataset, or do we wish
247 to use our results to extend our predictions to new groups? Even if we do not want to
248 predict to new groups, we might wish to fit something as a random effect to take
249 advantage of the shrinkage effect and improved parameter estimation accuracy.

250

251 **Considerations When Fitting Random Effects**

252 Random effect models have several desirable properties (see above), but their use
253 comes with some caveats. First, they are quite 'data hungry'; requiring at least 5 'levels'
254 (groups) for a random intercept term to achieve robust estimates of variance (Gelman &
255 Hill 2007; Harrison 2015). With <5 levels, the mixed model may not be able to estimate
256 the among-population variance accurately. In this case, the variance estimate will either
257 collapse to zero, making the model equivalent to an ordinary GLM (Gelman & Hill 2007
258 p. 275) or be non-zero but incorrect if the small number of groups that were sampled are

259 not representative of true distribution of means (Harrison 2015). Second, models can be
260 unstable if sample sizes across groups are highly unbalanced i.e. if some groups
261 contain very few data. These issues are especially relevant to random slope models
262 (Grueber et al 2011). Third, an important issue is the difficulty in deciding the
263 “significance” or “importance” of variance among groups. The variance of a random
264 effect is inevitably at least zero, but how big does it need to be to be considered of
265 interest? Fitting a factor as a fixed effect provides a statement of the significance of
266 differences (variation) among groups relatively easily. Testing differences among levels
267 of a random effect is made much more difficult for frequentist analyses, though not so in
268 a Bayesian framework (Kery 2010, see ‘*Testing Significance of Random Effects*’
269 section). Finally, an issue that is not often addressed is that of mis-specification of
270 random effects. GLMMs are powerful tools, but incorrectly parameterising the random
271 effects in the model could yield model estimates that are as unreliable as ignoring the
272 need for random effects altogether. An example would be failure to recognise non-
273 independence caused by nested structures in the data e.g. multiple clutch measures
274 from a single bird. A second example would be testing the significance of fixed effects at
275 the wrong ‘level’ of hierarchical models that ultimately leads to pseudoreplication and
276 inflated Type I error rates. That is, if we take 10 measurements from each of 10 leaves
277 to measure plant hormone concentration, even if we control for measurement non-
278 independence with a random intercept for ‘leaf ID’, do we calculate our residual degrees
279 of freedom at the data level (max $n=100$), or the grouping level (max $n=10$)?

280 *Further reading: Harrison (2015) shows how poor replication of the random*
281 *intercept groups can give unstable model estimates. Zuur & Ieno (2016) discuss the*
282 *importance of identifying dependency structures in the data.*

283 Deciding Model Structure for GLMMs

284 Choosing Error Structures and Link Functions

285 Linear models make various statistical assumptions, including additivity of the linear
286 predictors, independence of errors, equal variance of errors (homoscedasticity) and
287 Normality of errors (Gelman & Hill 2007 p. 46; Zuur et al 2009 p. 19). Ecologists often
288 deal with response variables that violate these assumptions, and face several decisions

289 about model specification to ensure models of such data are robust. The price for
290 ignoring violation of these assumptions tends to be an inflated Type I error rate (Zuur et
291 al 2010; Ives 2015). In some cases, however, transformation of the response variable
292 may be required to ensure these assumptions are met. For example, an analytical goal
293 may be to quantify differences in mean mass between males and females, but if the
294 variance in mass for one sex is greater than the other, the assumption of homogeneity of
295 variance is violated. Transformation of the data can remedy this (Zuur et al 2009),
296 'mean-variance stabilising transformations' ensure the variance around the fitted mean
297 of each group is similar, making the models more robust. Alternatively, modern statistical
298 tools such as the 'varIdent' function in the R package *nlme* can allow one to explicitly
299 model differences in variance between groups to avoid the need for data transformation.
300 *Further reading: Zuur et al (2010) provide a comprehensive guide on using data*
301 *exploration techniques to check model assumptions, and give advice on*
302 *transformations.*

303 For non-Gaussian data, our modelling choices become more complex. Non-
304 Gaussian data structures include Poisson-distributed counts (number of eggs laid,
305 number of parasites); binomial-distributed constrained counts (number of eggs that
306 hatched in a clutch; prevalence of parasitic infection in a group of hosts) and Bernoulli-
307 distributed binary traits (e.g. infected with a parasite or not). Gaussian models of these
308 data would violate the assumptions of normality of errors and homogenous variance. To
309 model these data, we have two initial choices: i) we can apply a transformation to our
310 non-Gaussian response to 'make it' approximately Gaussian, and then use a Gaussian
311 model; or ii) we can apply a GL(M)M and specify the appropriate error distribution and
312 link function. The link function takes into account the (assumed) empirical distribution of
313 our data by transformation of the linear predictor within the model. It is critical to note
314 that transformation of the raw response variable is not equivalent to using a link function
315 to apply a transformation in the model. Data-transformation applies the transformation to
316 the raw response, whilst using a link function transforms the fitted mean (the linear
317 predictor). That is, *the mean of a log-transformed response (using a data*
318 *transformation) is not identical to the logarithm of a fitted mean (using a link function).*

319 The issue of transforming non-Gaussian data to fit Gaussian models to them is
320 contentious. For example, arcsin square-root transformation of proportion data was once

321 extremely common, but recent work has shown it to be unreliable at detecting real
322 effects (Warton & Hui 2011). Both logit-transformation (for proportional data) and
323 Binomial GLMMs (for binary response variables) have been shown to be more robust
324 (Warton & Hui 2011). O'Hara & Kotze (2010) argued that log-transformation of count
325 data performed well in only a small number of circumstances (low dispersion, high mean
326 counts), which are unlikely to be applicable to ecological datasets. However, Ives (2015)
327 recently countered these assumptions with evidence that transformed count data
328 analysed using LMMs can often outperform Poisson GLMMs. We do not make a case
329 for either here, but acknowledge the fact that there is unlikely to be a universally best
330 approach; each method will have its own strengths and weakness depending on the
331 properties of the data (O'Hara & Kotze 2010). Checking the assumptions of the LMM or
332 GLMM is an essential step. An issue with transformations of non-Gaussian data is
333 having to deal with zeroes as special cases (e.g. you can't log transform a 0), so
334 researchers often add a small constant to all data to make the transformation work, a
335 practice that has been criticised (O'Hara & Kotze 2010). GLMMs remove the need for
336 these 'adjustments' of the data. The important point here is that transformations change
337 the entire relationship between Y and X (Zuur et al 2009), but different transformations
338 do this to different extents and it may be impossible to know which transformation is best
339 without performing simulations to test the efficacy of each (Warton & Hui 2011; Ives
340 2015).

341 *Further reading: Crawley (2013 Ch 13) gives a broad introduction to the various error*
342 *structures and link functions available in the R statistical framework. O'Hara & Kotze*
343 *(2010); Ives (2015) and Warton et al (2016) argue the relative merits of GLMs vs log-*
344 *transformation of count data; Warton & Hui (2011) address the utility of logit-*
345 *transformation of proportion data compared to arcsin square-root transformation.*

346 **Choosing Random Effects I: Crossed or Nested?**

347 A common issue that causes confusion is this issue of specifying random effects as
348 either 'crossed' or 'nested'. In reality, the way you specify your random effects will be
349 determined by your experimental or sampling design (Schielzeth & Nakagawa 2013). A
350 simple example can illustrate the difference. Imagine a researcher was interested in
351 understanding the factors affecting the clutch mass of a passerine bird. They have a

352 study population spread across 5 separate woodlands, each containing 30 nest boxes.
353 Every week during breeding they measure the foraging rate of females at feeders, and
354 measure their subsequent clutch mass. Some females have multiple clutches in a
355 season and contribute multiple data points. Here, female ID is said to be *nested within*
356 *woodland*: each woodland contains multiple females unique to that woodland (that never
357 move among woodlands). The nested random effect controls for the fact that i) clutches
358 from the same female are not independent, and ii) females from the same woodland
359 may have clutch masses more similar to one another than to females from other
360 woodlands

361
$$\text{Clutch Mass} \sim \text{Foraging Rate} + (1|\text{Woodland}/\text{Female ID})$$

362 Now imagine that this is a long-term study, and the researcher returns every year for 5
363 years to continue with measurements. Here it is appropriate fit year as a *crossed*
364 random effect, because every woodland appears multiple times in every year of the
365 dataset, and females that survive from one year to the next will also appear in multiple
366 years.

367
$$\text{Clutch Mass} \sim \text{Foraging Rate} + (1|\text{Woodland}/\text{Female ID}) + (1|\text{Year})$$

368 Understanding whether your experimental/sampling design calls for nested or crossed
369 random effects is not always straightforward, but it can help to visualise experimental
370 design by drawing it (see Schielzeth and Nakagawa 2013 Fig. 1), or tabulating your
371 observations by these grouping factors (e.g. with the *'table'* command in R) to identify
372 how your data are distributed. Finally, we caution that whether two factors are nested or
373 crossed affects the ability of GLMMs to estimate the interaction variance between those
374 two groups on the outcome variable. Crossed factors can accurately estimate the
375 interaction variance between the two, whereas nested factors automatically pool the
376 interaction variance in the second (nested) factor (Schielzeth and Nakagawa 2013). We
377 do not expand on this important issue here but direct the reader to Schielzeth and
378 Nakagawa 2013 for an excellent treatment of the topic.

379 **Choosing Random Effects II: Random Slopes for Continuous Variables**

380 Fitting random slope models in ecology is not very common. Often, researchers fit
381 random intercepts to control for non-independence among measurements of a statistical
382 group (e.g. birds within a woodland), but allow a continuous variable to have a common
383 slope across all experimental units. Schielzeth & Forstmeier (2009) argue that including
384 random slopes controls Type I error rate for continuous predictors (yields more accurate
385 p values), but also give more power to detect among individual variation. Barr et al
386 (2013) argue that researchers should fit the maximal random effects structure possible
387 for the data. That is, if there are four continuous predictors under consideration, all four
388 should be allowed to have random slopes. However, we believe this is unrealistic
389 because random slope models require large numbers of data to estimate variances and
390 covariances accurately (Bates et al 2015). Ecological datasets can often struggle to
391 estimate a single random slope, diagnosed by a perfect correlation (1 or -1) between
392 random intercepts and slopes (Bates et al 2015). Therefore, the approach of fitting the
393 'maximal' complexity of random effects structure (Barr et al 2013) is perhaps better
394 phrased as fitting the most complex mixed effects structure allowed by your data (Bates
395 et al 2015), which may mean no random slopes at all. If fitting a random slope model,
396 always inspect the correlation coefficient between the intercepts and slopes in the
397 variance/covariance summary returned by packages like *lme4* to look for evidence of
398 perfect correlations, indicative of insufficient data to estimate the model.

399 *Further Reading: Forstmeier and Schielzeth (2009) is essential reading for*
400 *understanding how random slopes control Type I error rate, and Bates et al (2015) gives*
401 *sound advice on how to iteratively determine optimal complexity of random effect*
402 *structure.*

403 **Choosing Fixed Effect Predictors and Interactions**

404 One of the most important decisions during the modelling process is deciding which
405 predictors and interactions to include in models. Best practice demands that each model
406 should represent a specific *a priori* hypothesis concerning the drivers of patterns in data
407 (Burnham & Anderson 2002; Forstmeier & Schielzeth 2011), allowing the assessment of
408 the relative support for these hypotheses in the data irrespective of model selection
409 philosophy. The definition of "hypothesis" must be broadened from the strict pairing of

410 null and alternative that is classically drilled into young pupils of statistics and
411 experimental design. Frequentist approaches to statistical modelling still work with
412 nested pairs of hypotheses. Information theorists work with whole sets of competing
413 hypotheses. Bayesian modellers are comfortable with the idea that every possible
414 parameter estimate is a hypothesis in its own right. But these epistemological
415 differences do not really help to solve the problem of “which” predictors should be
416 considered valid members of the full set to be used in a statistical modelling exercise. It
417 is therefore often unclear how best to design the most complex model, often referred to
418 as the *maximal model* (which contains all factors, interactions and covariates that might
419 be of any interest, Crawley 2013) or as the *global model* (a highly parameterized model
420 containing the variables and associated parameters thought to be important of the
421 problem at hand, Burnham & Anderson 2002; Grueber et al 2011). We shall use the
422 latter term here for consistency with terminology used in information-theory (Grueber et
423 al 2011).

424 Deciding which terms to include in the model requires careful and rigorous a
425 *priori* consideration of the system under study. This may appear obvious; however
426 diverse authors have noticed a lack of careful thinking when selecting variables for
427 inclusion in a model (Peters 1991, Chatfield 1995, Burnham & Anderson 2002). Lack of
428 *a priori* consideration, of what models represent, distinguishes rigorous hypothesis
429 testing from ‘fishing expeditions’ that seek significant predictors among a large group of
430 contenders. Ideally, the global model should be carefully constructed using the
431 researchers’ knowledge and understanding of the system such that only predictors likely
432 to be pertinent to the problem at hand are included, rather than including all the data the
433 researcher has collected and/or has available. This is a pertinent issue in the age of ‘big
434 data’, where researchers are often overwhelmed with predictors and risk skipping the
435 important step of *a priori* hypothesis design. In practice, for peer reviewers it is easy to
436 distinguish fishing expeditions from *a priori* hypothesis sets based on the evidence base
437 presented in introductory sections of research outputs.

438 **How Complex Should My Global Model Be?**

439 The complexity of the global model will likely be a trade-off between the number
440 of measured observations (the n of the study) and the proposed hypotheses about how

441 the measured variables affect the outcome (response) variable. Lack of careful
442 consideration of the parameters to be estimated can result in overparameterised
443 models, where there are insufficient data to estimate coefficients robustly (Southwood &
444 Henderson 2000, Quinn & Keough 2002, Crawley 2013). In simple GLMs,
445 overparameterisation results in a rapid decline in (or absence of) degrees of freedom
446 with which to estimate residual error. Detection of overparameterisation in LMMs can be
447 more difficult because each random effect uses only a single degree of freedom,
448 however the estimation of variance among small numbers of groups can be numerically
449 unstable. Unfortunately, it is common practice to fit a global model that is simply as
450 complex as possible, irrespective of what that model actually represents; that is a
451 dataset containing k predictors yields a model containing a k -way interaction among all
452 predictors and simplify from there (Crawley 2013). This approach is flawed for two
453 reasons. First, this practice encourages fitting biologically-unfeasible models containing
454 nonsensical interactions. It should be possible to draw and/or visualise what the fitted
455 model 'looks like' for various combinations of predictors – being unable to draw the
456 expected fitted lines of a 3-way interaction means refraining from fitting a model
457 containing one. Second, using this approach makes it very easy to fit a model too
458 complex for the data. At best, the model will fail to converge, thus preventing inference.
459 At worst, the model will “work”, risking false inference. Guidelines for the ideal ratio of
460 data points (n) to estimated parameters (k) vary widely (see Forstmeier & Schielzeth
461 2011). Crawley (2013) suggests a minimum n/k of 3, though we argue this is very low
462 and that an n/k of 10 is more conservative. A 'simple' model containing a 3-way
463 interaction between continuous predictors and a single random intercept needs to
464 estimate 8 parameters, so requires a dataset of a *minimum* n of 80. Interactions can be
465 especially demanding, as fitting interactions between a multi-level factor and a
466 continuous predictor can result in poor sample sizes for specific treatment combinations
467 even if the total n is quite large (Zuur et al 2010), which will lead to unreliable model
468 estimates.

469 *Grueber et al (2011) show an excellent worked example of a case where the*
470 *most complex model is biologically feasible and well-reasoned, containing only one 2-*
471 *way interaction. Nakagawa and Foster (2004) discuss the use of power analyses, which*
472 *will be useful in determining the appropriate n/k ratio for a given system.*
473

474 *Assessing Predictor Collinearity*

475 With the desired set of predictors identified, it is wise to check for collinearity among
476 predictor variables. Collinearity among predictors can cause several problems in model
477 interpretation because those predictors explain some of the same variance in the
478 response variable, and their effects cannot be estimated independently (Quinn and
479 Keough. 2002; Graham 2003): First, it can cause model convergence issues as models
480 struggle to partition variance between predictor variables. Second, positively correlated
481 variables can have negatively correlated regression coefficients, as the marginal effect
482 of one is estimated, given the effect of the other, leading to incorrect interpretations of
483 the direction of effects (Figure 2). Third, collinearity can inflate standard errors of
484 coefficient estimates and make 'true' effects harder to detect (Zuur et al 2010). Finally,
485 collinearity can affect the accuracy of model averaged parameter estimates during multi-
486 model inference (Freckleton 2011; Cade 2015). Examples of collinear variables include
487 climatic data such as temperature and rainfall, and morphometric data such as body
488 length and mass. Collinearity can be detected in several ways, including creating
489 correlation matrices between raw explanatory variables, with values >0.7 suggesting
490 both should not be used in the same model (Dormann et al. 2013); or calculating the
491 variance inflation factor (VIF) of each predictor that is a candidate for inclusion in a
492 model (details in Zuur et al 2010) and dropping variables with a VIF higher than a certain
493 value (e.g. 3; Zuur et al 2010, or 10, Quinn & Keogh 2002). One problem with these
494 methods though is that they rely on a user-selected choice of threshold of either the
495 correlation coefficient or the VIF, and use of more stringent (lower) is probably sensible.
496 Some argue that one should always prefer inspection of VIF values over correlation
497 coefficients of raw predictors because strong multicollinearity can be hard to detect with
498 the latter. When collinearity is detected, researchers can either select one variable as
499 representative of multiple collinear variables (Austin 2002), ideally using biological
500 knowledge/ reasoning to select the most meaningful variable (Zuur et al 2010); or
501 conduct a dimension-reduction analysis (e.g. Principal Components Analysis; James &
502 McCullough 1990), leaving a single variable that accounts for most of the shared variance
503 among the correlated variables. Both approaches will only be applicable if it is possible
504 to group explanatory variables by common features, thereby effectively creating broader,
505 but still meaningful explanatory categories. For instance, by using mass and body length
506 metrics to create a 'scaled mass index' representative of body size (Peig & Green 2009).

507 *Standardising and Centering Predictors*

508 Transformations of predictor variables are common, and can improve model
509 performance and interpretability (Gelman & Hill 2007). Two common transformations for
510 continuous predictors are i) predictor centering, the mean of predictor x is subtracted
511 from every value in x , giving a variable with mean 0 and SD on the original scale of x ;
512 and ii) predictor standardising, where x is centred and then divided by the SD of x , giving
513 a variable with mean 0 and SD 1. Rescaling the mean of predictors containing large
514 values (e.g. rainfall measured in thousands of mm) through centering/standardising will
515 often solve convergence problems, in part because the estimation of intercepts is
516 brought into the main body of the data themselves. Both approaches also remove the
517 correlation between main effects and their interactions, making main effects
518 interpretable when models also contain interactions (Schielzeth 2010). Note that this
519 collinearity among coefficients is distinct from collinearity between two separate
520 predictors (see above). Centering and standardising by the mean of a variable changes
521 the interpretation of the model intercept to the value of the outcome expected when x is
522 at its mean value. Standardising further adjusts the interpretation of the coefficient
523 (slope) for x in the model to the change in the outcome variable for a 1 SD change in the
524 value of x . Scaling is therefore a useful, indeed recommended, tool to improve the
525 stability of models and likelihood of model convergence, and the accuracy of parameter
526 estimates, but care must be taken in the interpretation and graphical representation of
527 outcomes.

528 *Further reading: Schielzeth (2010) provides an excellent reference to the*
529 *advantages of centering and standardising predictors. Gelman (2008) provides strong*
530 *arguments for standardising continuous variables by 2 SDs when binary predictors are*
531 *in the model. Gelman & Hill (2007 p. 56, 434) discuss the utility of centering by values*
532 *other than the mean.*

533 **Quantifying GLMM Fit and Performance**

534 Once a global model is specified, it is vital to quantify model fit and report these metrics
535 in the manuscript. The global model is considered the best candidate for assessing fit
536 statistics such as overdispersion (Burnham & Anderson 2002). Information criteria

537 scores should not be used as a proxy for model fit, because a large difference in AIC
538 between the top and null models is not evidence of a good fit. AIC tells us nothing about
539 whether the basic distributional and structural assumptions of the model have been
540 violated. Similarly a high R^2 value is in itself only a test of the magnitude of model fit and
541 not an adequate surrogate for proper model checks. Just because a model has a high
542 R^2 value does not mean it will pass checks for assumptions such as homogeneity of
543 variance. We strongly encourage researchers to view *model fit* and *model adequacy* as
544 two separate but equally important traits that must be assessed and reported. Model fit
545 can be poor for several reasons, including the presence of overdispersion, failing to
546 include interactions among predictors, failing to account for non-linear effects of the
547 predictors on the response, or specifying a sub-optimal error structure and/or link
548 function. Here we discuss some key metrics of fit and adequacy that should be
549 considered.

550

551 *Inspection of Residuals and Linear Model Assumptions*

552 Best practice is to examine plots of fitted values vs residuals for the entire model, as well
553 as model residuals versus all explanatory variables to look for patterns (Zuur et al 2010;
554 Zuur & Ieno 2016). In addition, there are further model checks specific to mixed models.
555 First, inspect fitted values versus residuals for each grouping level of a random intercept
556 factor (Zuur et al 2009). This will often prove dissatisfying if there are few data/residuals
557 per group, however this in itself is a warning flag that the assumptions of the model
558 might be based on weak foundation. Note that for the GLMMs it is wise to use
559 normalised/Pearson residual when looking for patterns as they account for the mean-
560 variance relationship of generalized models (Zuur et al 2009). Another feature of fit that
561 is very rarely tested for in (G)LMMs is the assumption of normality of deviations of the
562 conditional means of the random effects from the global intercept. Just as a quantile-
563 quantile (QQ) plot of linear model residuals should show points falling along a straight
564 line (e.g. Crawley 2013), so should a QQ plot of the random effect means (Schielzeth &
565 Nakagawa 2013).

566 *Further reading: Zuur et al (2010) given an excellent overview of the assumptions of*
567 *linear models and how to test for their violation. See also Gelman & Hill (2007 p. 45).*
568 *The R package 'sjPlot' (Lüdtke 2017) has built in functions for several LMM*
569 *diagnostics, including random effect QQ plots. Zuur et al (2009) provides a vast*

570 *selection of model diagnostic techniques for a host of model types, including GLS,*
571 *GLMMs and GAMMS.*

572

573 *Overdispersion*

574 Models with a Gaussian (Normal) error structure do not require adjustment for
575 overdispersion, as Gaussian models do not assume a specific mean-variance
576 relationship. For generalized mixed models (GLMMs) however (e.g. Poisson, Binomial),
577 the variance of the data can be greater than predicted by the error structure of the model
578 (e.g. Hilbe 2011). Overdispersion can be caused by several processes influencing data,
579 including zero-inflation, aggregation (non-independence) among counts, or both (Zuur et
580 al 2009). The presence of overdispersion in a model suggests it is a bad fit, and
581 standard errors of estimates will likely be biased unless overdispersion is accounted for
582 (e.g. Harrison 2014). The use of canonical binomial and Poisson error structures, when
583 residuals are overdispersed, tends to result in Type I errors because standard errors are
584 underestimated. Adding an observation-level random effect (OLRE) to overdispersed
585 Poisson or Binomial models can model the overdispersion and give more accurate
586 estimates standard errors (Harrison 2014; 2015). However, OLRE models may yield
587 inferior fit and/or biased parameter estimates compared to models using compound
588 probability distributions such as the Negative-Binomial for count data (Hilbe 2011;
589 Harrison 2014) or Beta-Binomial for proportion data (Harrison 2015), and so it is good
590 practice to assess the relative fit of both types of model using AIC before proceeding
591 (e.g. Zuur et al 2009). Researchers very rarely report the overdispersion statistic (but
592 see Elston et al 2001), but it should be made a matter of routine. See 'Assessing Model
593 Fit Through Simulation' Section for advice on how to quantify and model overdispersion.

594 *Further reading: Crawley (2013 page 580-581) gives an elegant demonstration of*
595 *how failing to account for overdispersion leads to artificially small standard errors and*
596 *spurious significance of variables. Harrison (2014) quantifies the ability of OLRE to cope*
597 *with overdispersion in Poisson models. Harrison (2015) compares Beta-Binomial and*
598 *OLRE models for overdispersed proportion data.*

599 R^2

600 In a linear modelling context, R^2 gives a measure of the proportion of explained variance
601 in the model, and is an intuitive metric for assessing model fit. Unfortunately, the issue of

602 calculating R^2 for (G)LMMs is particularly contentious; whereas residual variance can
603 easily be estimated for a simple linear model with no random effects and a Normal error
604 structure, this is not the case for (G)LMMs. In fact, two issues exist with generalising R^2
605 measures to (G)LMMs: i) for generalised models containing non-Normal error structures,
606 it is not clear how to calculate the residual variance term on which the R^2 term is
607 dependent; and ii) for mixed effects models, which are hierarchical in nature and contain
608 error (unexplained variance) at each of these levels, it is uncertain which level to use to
609 calculate a residual error term (Nakagawa & Schielzeth 2013). Diverse methods have
610 been proposed to account for this coefficient in GLMMs, including so-called ‘pseudo- r^2 ’
611 measures of explained variance (e.g. Nagelkerke 1991, Cox & Snell 1989), but their
612 performance is often unstable for mixed models and can return negative values
613 (Nakagawa & Schielzeth 2013). Gelman & Pardoe (2006) derived a measure of R^2 that
614 accounts for the hierarchical nature of LMMs and gives a measure for both group and
615 unit level regressions (see also Gelman & Hill 2007 p. 474), but it was developed for a
616 Bayesian framework and a frequentist analogue does not appear to be widely
617 implemented. The method that has gained the most support over recent years is that of
618 Nakagawa & Schielzeth (2013).

619 The strength of the Nakagawa & Schielzeth (2013) method for GLMMs is that it
620 returns two complimentary R^2 values: the marginal R^2 encompassing variance explained
621 by only the fixed effects, and the conditional R^2 comprising variance explained by both
622 fixed and random effects i.e. the variance explained by the whole model (Nakagawa &
623 Schielzeth 2013). Ideally, both should be reported in publications as they provide
624 different information; which one is more ‘useful’ may depend on the rationale for
625 specifying random effects in the first instance. Recently, Nakagawa, Johnson &
626 Schielzeth (2017) expanded their R^2 method to handle models with compound
627 probability distributions like the Negative Binomial error family. Note that when
628 observation-level random effects are included (see ‘Overdispersion’ section above), the
629 conditional R^2 becomes less useful as a measure of explained variance because it
630 includes the extra-parametric dispersion being modelled, but has no predictive power
631 (Harrison 2014).

632 *Further reading: Nakagawa & Schielzeth (2013) provide an excellent and*
633 *accessible description of the problems with, and solutions to, generalising R^2 metrics to*
634 *GLMMs. The Nakagawa & Schielzeth (2013) R^2 functions have been incorporated into*

635 *several packages, including ‘MuMIn’ (Bartoń 2016) and ‘piecewiseSEM’ (Lefcheck*
636 *2015), and Johnson (2014) has developed an extension of the functions for random*
637 *slope models. See Harrison (2014) for a cautionary tale of how the GLMM R^2 functions*
638 *are artificially inflated for overdispersed models.*

639

640 *Stability of Variance Components and Testing Significance of Random Effects*

641 When models are too complex relative to the amount of data available, GLMM variance
642 components can collapse to zero (they cannot be negative). This is not a problem *per*
643 *se*, but it’s important to acknowledge that in this case the model is equivalent to a
644 standard GLM. Reducing model complexity by removing interactions will often allow
645 random effects variance component estimates to become >0 , but this is problematic if
646 quantifying the interaction is the primary goal of the study. REML (restricted maximum
647 likelihood) should be used for estimating variance components of random effects in
648 Gaussian GLMMs as it produces less biased estimates compared to ML (maximum
649 likelihood) (Bolker et al 2009). However, when comparing two models with the same
650 random structure but different fixed effects, ML estimation cannot easily be avoided. The
651 RLRsim package (Scheipl, 2016) can be used to calculate restricted likelihood ratio tests
652 for variance components in mixed and additive models. Crucially, when testing the
653 significance of a variance component we are ‘testing on the boundary’ (Bolker et al
654 2009). That is the null hypothesis for random effects ($\sigma=0$) is at the boundary of its
655 possible range (it has to be ≥ 0), meaning p-values from a likelihood ratio test are
656 inaccurate. Dividing p values by 2 for tests of single variance components provides an
657 approximation to remedy this problem (Verbenke & Molenberghs, 2000).

658 Finally, estimating degrees of freedom for tests of random effects using Wald, t or
659 F tests or AICc is difficult, as a random effect can theoretically use anywhere between 1
660 and $N - 1$ df (where N is the number of random-effect levels) (Bolker et al. 2009).

661 Adequate F and P values can be calculated using Satterthwaite (1946) approximations
662 to determine denominator degrees of freedom implemented in the package ‘lmerTest’
663 (Kuznetzova et al. 2014, see further details in section ‘Model Selection and Multi-Model
664 Inference’ below).

665 *Assessing Model Fit through Simulation*

666 Simulation is a powerful tool for assessing model fit (Gelman & Hill 2007; Kery 2010;
667 Zuur & Ieno 2016), but is rarely used. The premise here is simple: when simulating a
668 dataset from a given set of parameter estimates (a model), the fit of the model to those
669 *simulated* 'ideal' data should be comparable to the model's fit to the real data (Kery
670 2010). Each iteration yields a simulated dataset that allows calculation of a statistic of
671 interest such as the sum of squared residuals (Kery 2010), the overdispersion statistic
672 (Harrison 2014) or the percentage of zeroes for a Poisson model (Zuur & Ieno 2016). If
673 the model is a good fit, after a sufficiently large number of iterations (e.g. 10,000) the
674 distribution of this test statistic should encompass the observed statistic in the real data.
675 Significant deviations outside of that distribution indicate the model is a poor fit (Kery
676 2010). Figure 3 shows an example of using simulation to assess the fit of a Poisson
677 GLMM. After fitting a GLMM to count data, we may wish to check for overdispersion
678 and/or zero-inflation, the presence of which might suggest we need to adjust our
679 modelling strategy. Simulating 10,000 datasets from our model reveals that the
680 proportion of zeroes in our real data is comparable to simulated expectation (Figure 3A).
681 Conversely, simulating 1000 datasets and refitting our model to each dataset, we see
682 that the sum of the squared Pearson residuals for the real data is far larger than
683 simulated expectation (Figure 3B), giving evidence of overdispersion (Harrison 2014).
684 We can use the simulated frequency distribution of this test statistic to derive a mean
685 and 95% confidence interval for the overdispersion by calculating the ratio of our test
686 statistic to the simulated values (Harrison 2014). The dispersion statistic for our model is
687 3.16 [95% CI 2.77 – 3.59]. Thus, simulations have allowed us to conclude that our model
688 is overdispersed, but that this overdispersion is not due to zero-inflation. All R code for
689 reproducing these simulations is provided in Online Supplementary Material.

690 *Further reading: The R package 'SQuID' (Allegue et al 2017) provides a highly*
691 *flexible simulation tool for learning about, and exploring the performance of, GLMMs.*
692 *Rykiel (1996) discusses the need for validation of models in ecology.*

693 *Dealing with missing data*

694 Often when collecting ecological data it is not always possible to measure all of the
695 predictors of interest for every measurement of the dependant variable. Such missing
696 data is a common feature of ecological datasets, however the impacts of this have
697 seldom been considered in the literature (Nakagawa & Freckleton 2011). Incomplete

698 data is often dealt with by deleting data point with missing predictor data (Nakagawa &
699 Freckleton 2008), although this may results in biased parameter estimates and reduces
700 statistical power (Nakagawa & Freckleton 2008). Nakagawa & Freckleton (2011)
701 recommend multiple imputation (MI) as a mechanism for handling missing data, and
702 highlight the ability of this technique for more accurate estimates, particularly for IT-AIC
703 approaches.
704 *Further reading: See Nakagawa & Freckleton (2008) for a review on the risks of ignoring*
705 *incomplete data. Nakagawa & Freckleton (2011) demonstrate the effects of missing data*
706 *during model selection procedures, and provide an overview of R packages available for*
707 *MI.*

708 Model Selection and Multi-Model Inference

709 Several methods of model selection are available once there is a robust global model
710 that satisfies standard assumptions of error structure and hierarchical independence
711 (Johnson & Omland 2004). We discuss the relative merits of each approach briefly here,
712 before expanding on the use of information-theory and multi-model inference in ecology.
713 We note that these discussions are not meant to be exhaustive comparisons, and we
714 encourage the reader to delve into the references provided for a comprehensive picture
715 of the arguments for and against each approach.

716 *Stepwise Selection, Likelihood Ratio Tests and P values*

717 A common approach to model selection is the comparison of a candidate model
718 containing a term of interest to the corresponding 'null' model lacking that term, using a
719 p value from a likelihood ratio test (LRT), referred to as null-hypothesis significance
720 testing (NHST; Nickerson 2000). Stepwise deletion involves using the NHST framework
721 to drop terms sequentially from the global model, and arrive at a 'minimal adequate
722 model' (MAM) containing only significant predictors (see Crawley 2013). NHST and
723 stepwise deletion have come under heavy criticism; they can overestimate the effect
724 size of 'significant' predictors (Whittingham et al 2006; Forstmeier & Schielzeth 2011)
725 and force the researcher to focus on a single best model as if it were the only
726 combination of predictors with support in the data. Although we strive for simplicity and
727 parsimony, this assumption is not reasonable in complex ecological systems (e.g.

728 Burnham, Anderson & Huyvaert 2011). It is common to present the MAM as if it arose
729 from a single *a priori* hypothesis, when in fact arriving at the MAM required multiple
730 significance tests (Whittingham et al 2006; Forstmeier & Schielzeth 2011). This cryptic
731 multiple testing can lead to hugely inflated Type I errors (Forstmeier & Schielzeth 2011).
732 Perhaps most importantly, LRT can be unreliable for fixed effects in GLMMs unless both
733 total sample size and replication of the random effect terms is high (see Bolker et al
734 2009 and references therein), conditions which are often not satisfied for most
735 ecological datasets. However, there are still cases where NHST may be the most
736 appropriate tool for inference (Murtaugh 2014). For example, in controlled experimental
737 studies a researcher may wish to test the effect of a limited number of treatments and
738 support estimates of effect sizes with statements of statistical significance using model
739 simplification (Mundry 2011). Importantly, Murtaugh (2009) found that the predictive
740 ability of models assessed using NHST was comparable to those selected using
741 information-theoretic approaches (see below), suggesting that NHST remains a valid
742 tool for inference despite strong criticism (see also Murtaugh 2014). Our advice is that
743 NHST remains an important tool for analyses of experiments and for inferential surveys
744 with small numbers of well-justified *a priori* hypotheses and with uncorrelated (or weakly
745 correlated) predictors.

746 *Further reading: See Murtaugh's (2014) excellent 'in Defense of P values', as*
747 *well as the other papers on the topic in the same special issue of Ecology. Stephens et*
748 *al (2005) & Mundry (2011) argue the case for NHST under certain circumstances such*
749 *as well-designed experiments. Halsey et al (2015) discuss the wider issues of the*
750 *reliability of p values relative to sample size.*

751 *Information-Theory and Multi-Model Inference*

752 Unlike NHST, which leads to a focus on a single best model, model selection using
753 information theoretic (IT) approaches allows the degree of support in the data for several
754 competing models to be ranked using metrics such as Akaike's Information Criterion
755 (AIC). Information criteria attempt to quantify the Kullback-Leibler distance (KLD), a
756 measure of the relative amount of information lost when a given model approximates the
757 true data-generating process. Thus, relative difference among models in AIC should be
758 representative in relative differences in KLD, and the model with the lowest AIC should
759 lose the least information and be the best model in that it optimises the trade-off

760 between fit and complexity (e.g. Richards 2008). A key strength of the IT approach is
761 that it accounts for ‘model selection uncertainty’, the idea that several competing models
762 may all fit the data similarly (Burnham & Anderson 2002; Burnham, Anderson &
763 Huyvaert 2011). This is particularly useful when competing models share equal
764 “complexity” (i.e. number of predictors, or number of residual degrees of freedom): in
765 such situations, NHST is impossible because there is no “null”. Where several models
766 have similar support in the data, inference can be made from all models using model-
767 averaging (Burnham & Anderson 2002; Johnson & Omand 2004; Grueber et al 2011).
768 Model averaging incorporates uncertainty by weighting the parameter estimate of a
769 model by that model’s Akaike weight (often referred to as the probability of that model
770 being the best Kullback-Leibler model given the data, but see Richards 2005). Multi-
771 model inference places a strong emphasis on *a priori* formulation of hypotheses
772 (Burnham & Anderson 2002; Dochterman & Jenkins 2011; Lindberg et al 2015), and
773 model-averaged parameter estimates arising from multi-model inference are thought to
774 lead to more robust conclusions about the biological systems compared to NHST
775 (Johnson & Omland 2004, but see Richards et al 2011). These strengths over NHST
776 have meant that the use of IT approaches in ecology and evolution has grown rapidly in
777 recent years (Lindberg et al 2015; Barker & Link 2015; Cade 2015). We do not expand
778 on the specific details of the difference between NHST and IT here, but point the reader
779 to some excellent reference on the topic. Instead, we use this section to highlight recent
780 empirical developments in the best practice methods for the application of IT in ecology
781 and evolution.

782 *Further reading: Grueber et al (2011) and Symonds & Moussalli (2011) give a*
783 *broad overview of multi-model inference in ecology, and provide a worked model*
784 *selection exercise. Heygi & Garamszegi (2011) provide a detailed comparison of IT and*
785 *NHST approaches. Burnham, Anderson & Huyvaert (2011) demonstrate how AIC*
786 *approximates Kullback-Leibler information and provide some excellent guides for the*
787 *best practice of applying IT methods to biological datasets. Vaida & Blanchard (2005)*
788 *provide details on AIC should be implemented for the analysis of clustered data.*

789 *Global Model Reporting*

790 Because stepwise deletion can cause biased effect sizes, presenting means and SEs of
791 parameters from the global model should be more robust, especially when the n/k ratio

792 is low (Forstmeier & Schielzeth 2011). An alternative approach to NHST is to perform
793 'full model tests' (comparing the global model to an intercept only model) before
794 investigating single-predictor effects, as this controls the Type I error rate (Forstmeier &
795 Schielzeth 2011). Reporting the full model also helps reduce publication bias towards
796 strong effects, providing future meta-analyses with estimates of both significant and non-
797 significant effects (Forstmeier & Schielzeth 2011). Global model reporting should not
798 replace other model selection methods, but provides a robust measure of how likely
799 significant effects are to arise by sampling variation alone.

800 **Practical Issues with Applying Information Theory to Biological Data**

801 *1. Using All-Subsets Selection*

802 All-Subsets selection is the act of fitting a global model, often containing every possible
803 interaction, and then fitting every possible nested model. On the surface, all-subsets
804 might appear to be a convenient and fast way of 'uncovering' the causal relationships in
805 the data. All-subsets selection of enormous global models containing large numbers of
806 predictors and their interactions makes analyses extremely prone to Type I errors and
807 'overfitted' models. Burnham & Anderson (2002) caution strongly against all-subsets
808 selection, and instead advocate 'hard thinking' about the hypotheses underlying the
809 data. If adopting an all subsets approach, it is worth noting the number of models to
810 consider increases exponentially with the number of predictors, where 5 predictors
811 require 2^5 (32) models to be fitted, whilst 10 predictors requires 1024 models, both
812 *without* including any interactions.

813 The inflation of Type I error rate through all-subsets selection is simple to
814 demonstrate. Figure 4 shows the results of a simulation exercise where we created
815 datasets containing various numbers of continuous and categorical variables, fitted a
816 global model containing all predictors as main effects and no interactions; and then
817 performed ASS on that model in the 'MuMIn' package in *R*. Note that MuMIn refers to
818 ASS as 'dredging' (the 'dredge' command), and this *model* dredging is separate from
819 *data* dredging sensu Burnham & Anderson (2002). All simulated predictors were
820 samples drawn from populations representing the null hypothesis, i.e. having zero
821 influence on the response variable. We considered all models with an AIC score of

822 within 6 of the best-supported AIC model to be equally well supported (also referred to
823 as the $\Delta 6$ AIC top model set, Richards 2008) (detailed methods available in Online
824 Supplementary Material). We assumed a Type I error had occurred when the 95%
825 confidence intervals for model averaged parameter estimates from the $\Delta 6$ AIC set did not
826 cross zero. The higher the number of terms in the model, the higher the Type I error
827 rate, reaching a maximum of over 60% probability of falsely including a predictor in the
828 top model set that was unrelated to the response variable. Importantly, we found that the
829 rate of increase (slope) in Type I error with added continuous predictors was modified by
830 the number of categorical variables (Fig. 4), meaning the change in Type 1 error rate per
831 continuous predictor was highest with smaller numbers of categorical variables. Note
832 that many factors contribute to this high Type I error rate observed here. For example,
833 just because one level of a factor has 95% intervals that do not span zero does not
834 mean that the factor as a whole has any explanatory power. See also Forstmeier &
835 Schielzeth (2011) for a discussion of cryptic testing of multiple hypotheses in a single
836 model.

837 These results help to illustrate why dredging should not be used, and why global
838 models should not contain huge numbers of variables and interactions without prior
839 thought about what the models represent for a study system. In cases where all-subsets
840 selection from a global model is performed, it is important to view these model selection
841 exercises as exploratory (Symonds & Moussali 2011), and hold some data back from
842 these exploratory analyses to be used for cross-validation with the top model(s) (see
843 Dochterman and Jenkins 2011 and references therein). Here, 90% of the data can be
844 used to fit the model(s), with the remaining 10% used for confirmatory analysis to
845 quantify how well the model(s) perform for prediction (Zuur & Ieno 2016). Such an
846 approach requires a huge amount of data (Dochterman and Jenkins 2011), but cross-
847 validation to validate a model's predictive ability is rare and should result in more robust
848 inference (see also Fieberg & Johnson 2015).

849 Therefore, best practice is to consider only a handful of hypotheses and then build a
850 single statistical model to reflect each hypothesis. This makes inference easier because
851 the resulting top model set will likely contain fewer parameters, and certainly fewer
852 spuriously 'significant' parameters (Burnham & Anderson 2002; Arnold 2010). However,
853 we argue all subsets selection may be sensible in a limited number of circumstances
854 when testing causal relationships between explanatory variables and the response

855 variable. For example, if the most complex model contains two main effects and their
856 interaction, performing all subsets selection on that model is identical to building the four
857 competing models (including the null model) nested in the global model, all of which may
858 be considered likely to be supported by the data. It is worth remembering that the Type I
859 error rate can quickly exceed the nominal 5% threshold if these conditions are not met
860 (Fig. 4). Moreover, a small number of models built to reflect well-reasoned hypotheses
861 are only valid if the predictors therein are not collinear (see 'Collinearity' section below).
862 All-subsets selection using the R package *MuMIn* (Bartoń 2016) will not automatically
863 check for collinearity, and so the onus falls on the researcher to be thorough in checking
864 for such problems.

865 2. *Deciding Which Information Criterion To Use*

866 Several information criteria are available to rank competing models, but their
867 calculations differ subtly. Commonly applied criteria include Akaike's Information
868 Criterion (AIC), the small sample size correction of AIC for when $n/k < 40$ (AICc), and the
869 Bayesian Information Criterion (BIC). QAIC is an adjustment to AIC that accounts for
870 overdispersion, and should be used when overdispersion has been identified in a model
871 (see 'Overdispersion section' above). Note QAIC is not required if the overdispersion in
872 the dataset has been modelled using zero-inflated models, observation-level random
873 effects, or compound probability distributions. Bolker et al (2009) and Grueber et al
874 (2011) provide details of how to calculate these criteria.

875 AIC maximises the fit/complexity trade-off of a model by balancing the model fit
876 with the number of estimated parameters. AICc and BIC both penalise the IC score
877 based on total sample size n , but the degree of penalty for AICc is less severe than BIC
878 for moderate sample sizes, and more severe for very low sample size (Brewer et al
879 2016). Whilst AIC tend to select overly complex models, Burnham and Anderson (2002)
880 criticised BIC for selecting overly simplistic models (underfitting). BIC is also criticised
881 because it operates on the assumption that the true model is in the model set under
882 consideration, whereas in ecological studies this is unlikely to be true (Burnham &
883 Anderson 2002; 2004). Issues exist with both AIC and BIC in a GLMM context for
884 estimating the number of parameters for a random effect (Bolker et al 2009; Grueber et
885 al 2011), and although degrees of freedom corrections to remedy this problem exist it is
886 not always clear what method is being employed by software packages (see Bolker et al

887 2009 Box 3). Brewer et al (2016) show how the optimality of AIC, AICc and BIC for
888 prediction changes with both sample size and effect size of predictors (see also
889 Burnham and Anderson 2004). Therefore, the choice between the two metrics is not
890 straightforward, and may depend on the goal of the study i.e. model selection vs
891 prediction, see Grueber et al 2011 Box 1.

892 3. *Choice of Δ AIC Threshold*

893 Once all models have been ranked by an information criterion, it is common practice to
894 identify a “top model set” containing all models assumed to have comparable support in
895 the data, normally based on the change in AIC values relative to the best AIC model
896 (Δ AIC). Historically, Burnham & Anderson (2002) recommended that only models with
897 Δ AIC between 0-2 should be used for inference, but subsequent work has shown that at
898 least Δ 6 AIC is required to guarantee a 95% probability that the best (expected)
899 Kullback-Leibler Distance model is in the top model set (Richards 2008; see also
900 Burnham et al 2011). Alternatively, models can be ranked by their Akaike weights and all
901 those with an Akaike weight ≥ 0.95 retained in the “95% confidence set” (Burnham &
902 Anderson 2002; Symonds & Moussali 2011). Using high cut-offs is not encouraged, to
903 avoid overly complex model sets followed by invalid results (Richards 2008; Grueber et
904 al. 2011) but deciding on how many is too many remains a contentious issue (Grueber et
905 al. 2011). We suggest Δ 6 as a minimum following Richards (2005; 2008).

906 4. *Using the Nesting Rule to Improve Inference from the Top Model Set*

907 It is well known that AIC tends towards overly complex models (‘overfitting’, Burnham &
908 Anderson 2002). As AIC only adds a 2 point penalty to a model for inclusion of a new
909 term, Arnold (2010) demonstrated that adding a nuisance predictor to a well-fitting model
910 leads to a Δ AIC value of the new model of ~ 2 , therefore appearing to warrant inclusion
911 in the top model set (see section above). Therefore, inference can be greatly improved
912 by eliminating models from the top model set that are more complex versions of nested
913 models with better AIC support, known as the nesting rule (Richards 2005; 2008;
914 Richards et al 2011). Doing so greatly reduces the number of models to be used for
915 inference, and improves parameter accuracy (Arnold 2010; Richards et al 2008).
916 Symonds & Moussali (2011) caution that its applicability has not yet been widely
917 assessed over a range of circumstances, but the theory behind its application is sound

918 and intuitive (Arnold 2010). One potential problem is that once models have removed
919 from the top model set, interpretation of the Akaike weights for the remaining models
920 becomes difficult, and thus model-averaged estimates using these weights may not be
921 sensible.

922 *5. Using Akaike Weights to Quantify Variable Importance*

923 With a top model set in hand, it is common practice to use the summed Akaike weights
924 of every model in that set in which a predictor of interest occurs as a measure of
925 ‘variable importance’ (e.g. Grueber et al 2011). Recent work has demonstrated that this
926 approach is flawed because Akaike weights are interpreted as relative model
927 probabilities, and give no information about the importance of individual predictors in a
928 model (Cade 2015), and fail to distinguish between variables with weak or strong effects
929 (Galipaud et al 2014; 2017). The sum of Akaike weights as a measure of variable
930 importance may at best be a measure of how likely a variable would be included after
931 repeated sampling of the data (Burnham & Anderson 2002; Cade 2015, but see
932 Galipaud et al 2017). A better measure of variable importance would be to compare
933 standardised effect sizes (Schielzeth 2010; Cade 2015).

934 *6. Model Averaging when Predictors Are Collinear*

935 The aim of model averaging is to incorporate the uncertainty of the size and presence of
936 effects among a set of candidate models with equal support in the data. Model
937 averaging using Akaike weights proceeds on the assumption that predictors are on
938 common scales across models and are therefore comparable. Unfortunately, the nature
939 of multiple regression means that the scale and sign of coefficients will change across
940 models depending on the presence or absence of other variables in a focal model (Cade
941 2015). The issue of predictor scaling changing across models is particularly exacerbated
942 when predictors are collinear, even when VIF values are low (Burnham and Anderson
943 2002; Lukacs, Burnham & Anderson 2010; Cade 2015). Cade (2015) recommends
944 standardising model parameters based on partial standard deviations to ensure
945 predictors are on common scales across models prior to model averaging (details in
946 Cade 2015). We stress again the need to assess multicollinearity among predictors in
947 multiple regression modelling before fitting models (Zuur & Ieno 2016) and before

948 model-averaging coefficients from those models (Lukacs, Burnham & Anderson 2010;
949 Cade 2015)
950

951 Conclusion

952 We hope this article will act as both a guide, and as a gateway to further reading, for
953 both new researchers and those wishing to update their portfolio of analytic techniques.
954 Here we distill our message into a bulleted list.

955 1. Modern mixed effect models offer an unprecedented opportunity to explore complex
956 biological problems by explicitly modelling non-Normal data structures and/or non-
957 independence among observational unit. However, the LMM and GLMM toolset should
958 be used with caution.

959 2. Rigorous testing of both model fit (R^2) and model adequacy (violation of assumptions
960 like homogeneity of variance) must be carried out. We must recognise that satisfactory
961 fit does not guarantee we have not violated the assumptions of LMM, and vice versa.
962 Interpret measures of R^2 for (G)LMMs with hierarchical errors cautiously, especially
963 when OLRE are used.

964 3. Collinearity among predictors is difficult to deal with and can severely impair model
965 accuracy. Be especially vigilant if data are from field surveys rather than controlled
966 experiments, as collinearity is likely to be present.

967 4. Data dredging or 'fishing expeditions' are very risky and inflate the number of false
968 positives enormously. Including all combinations of predictors in a model requires strong
969 *a priori* justification.

970 5. When including a large number of predictors is necessary, backwards selection and
971 NHST should be avoided, and ranking via AIC of all competing models is preferred. A
972 critical question that remains to be addressed is whether model selection based on
973 information theory is superior to NHST even in cases of balanced experimental designs
974 with few predictors.

975 6. Data simulation is a powerful but underused tool. If the analyst harbours any
976 uncertainty regarding the fit or adequacy of the model structure, then the analysis of

977 data simulated to recreate the perceived structure of the favoured model can provide
978 reassurance, or justify doubt.

979 7. Wherever possible, provide diagnostic assessment of model adequacy, and metrics of
980 model fit, even if in Supplementary Material.

981 8. Other modelling approaches such as Bayesian inference are available, and allow
982 much greater flexibility in choice of model structure, error structure and link function.
983 However, the ability to compare among competing models is underdeveloped, and
984 where these tools do exist, they are not yet accessible enough to non-experts to be
985 useful.

986

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990 References

- 991 Allegue H, Araya-Ajoy YG, Dingemanse NJ, Dochtermann NA, Garamszegi LZ,
992 Nakagawa S, Reale D, Schielzeth H, Westneat DF. 2017. Statistical Quantification
993 of Individual Differences (SQuID): an educational and statistical tool for
994 understanding multilevel phenotypic data in linear mixed models. *Methods in*
995 *Ecology and Evolution* 8:257-67.
- 996 Arnold TW. 2010. Uninformative parameters and model selection using Akaike's
997 Information Criterion. *The Journal of Wildlife Management* 74: 1175-1178.
- 998 Austin MP. 2002. Spatial prediction of species distribution: an interface between
999 ecological theory and statistical modelling. *Ecological Modelling* 157: 101–118.
- 1000 Barker RJ, Link WA. 2015. Truth, models, model sets, AIC, and multimodel inference: A
1001 Bayesian perspective. *The Journal of Wildlife Management* 79: 730–738.
- 1002 Barr DJ, Levy R, Scheepers C, Tily HJ. 2013. Random effects structure for confirmatory
1003 hypothesis testing: Keep it maximal. *Journal of memory and language* 68:255-78.
- 1004 Bartoń K. 2016. MuMIn: Multi-Model Inference. R package version
1005 1.15.6. <https://CRAN.R-project.org/package=MuMIn>
- 1006 Bates D, Maechler M, Bolker B, Walker S. 2015. Fitting Linear Mixed-Effects Models
1007 Using lme4. *Journal of Statistical Software* 67: 1-48.
- 1008 Bates D, Kliegl R, Vasishth S, Baayen H. 2015. Parsimonious mixed models. *arXiv*
1009 *preprint arXiv:1506.04967*.
- 1010 Bolker BM, Brooks ME, Clark CJ, Geange SW, Poulsen JR, Stevens MHH, White JSS.
1011 2009. Generalized linear mixed models: a practical guide for ecology and evolution.
1012 *Trends in Ecology and Evolution* 24: 127–135.
- 1013 Breslow NE, Clayton DG. 1993. Approximate inference in generalized linear mixed
1014 models. *Journal of the American statistical Association* 88: 9-25.
- 1015 Brewer MJ, Butler A, Cooksley SL. 2016. The relative performance of AIC, AICC and
1016 BIC in the presence of unobserved heterogeneity. *Methods in Ecology and Evolution* 7:
1017 679-692.
- 1018 Burnham KP, Anderson DR. 2002. Model Selection and Multimodel Inference: A
1019 Practical Information-Theoretic Approach, Second. Springer-Verlag, New York.

- 1020 Burnham KP, Anderson DR. 2004. Multimodel inference: understanding AIC and BIC in
1021 model selection. *Sociological Methods & Research* 33: 261-304.
- 1022 Burnham KP, Anderson DR, Huyvaert KP. 2011. AIC model selection and multimodel
1023 inference in behavioral ecology: Some background, observations, and comparisons.
1024 *Behavioral Ecology and Sociobiology* 65: 23–35.
- 1025 Cade BS. 2015. Model averaging and muddled multimodel inferences. *Ecology* 96:
1026 2370–2382.
- 1027 Chatfield C. 1995. Model uncertainty, data mining and statistical inference (with
1028 discussion). *Journal of the Royal Statistical Society, Series A* 158: 419-66.
- 1029 Cox DR, Snell EJ. 1989. *The Analysis of Binary Data*, 2nd ed. London: Chapman and
1030 Hall.
- 1031 Crawley (2013) *The R Book*. Second Edition. Wiley, Chichester UK.
- 1032 Dochtermann NA, Jenkins SH. 2011. Developing multiple hypotheses in behavioural
1033 ecology. *Behavioral Ecology and Sociobiology* 65: 37-45.
- 1034 Dominicus A, Skrondal A, Gjessing HK, Pedersen NL, Palmgren J. 2006. Likelihood ratio
1035 tests in behavioral genetics: problems and solutions. *Behavior Genetics* 36: 331–340.
- 1036 Dormann CF, Elith J, Bacher S, Buchmann C, Carl G, Carré G, Marquéz JR, Gruber B,
1037 Lafourcade B, Leitão PJ, Münkemüller T. 2013. Collinearity: a review of methods to deal
1038 with it and a simulation study evaluating their performance. *Ecography* 36: 027–046.
- 1039 Ellison AM. 2004. Bayesian inference in ecology. *Ecology letters* 7: 509-520.
- 1040 Elston, DA, Moss R, Boulinier T, Arrowsmith C, Lambin X, 2001. Analysis of aggregation,
1041 a worked example: numbers of ticks on red grouse chicks. *Parasitology* 122: 563-569.
- 1042 Fieberg J, Johnson DH. 2015. MMI: Multimodel inference or models with management
1043 implications? *The Journal of Wildlife Management* 79: 708–718.
- 1044 Forstmeier W, Schielzeth H. 2011. Cryptic multiple hypotheses testing in linear models:
1045 Overestimated effect sizes and the winner’s curse. *Behavioral Ecology and Sociobiology*
1046 65: 47–55.
- 1047 Freckleton RP. 2011. Dealing with collinearity in behavioural and ecological data: model
1048 averaging and the problems of measurement error. *Behavioral Ecology and*
1049 *Sociobiology* 65: 91-101.
- 1050 Galipaud M, Gillingham MAF, David M, Dechaume-Moncharmont FX. 2014. Ecologists
1051 overestimate the importance of predictor variables in model averaging: a plea for
1052 cautious interpretations. *Methods in Ecology and Evolution* 5, 983-991.

- 1053 Galipaud M, Gillingham MAF, Dechaume-Moncharmont FX. 2017. A farewell to the sum
1054 of Akaike weights: The benefits of alternative metrics for variable importance estimations
1055 in model selection. *Methods in Ecology and Evolution* 00:1–11.
1056 <https://doi.org/10.1111/2041-210X.12835>
- 1057 Gelman A, Hill J. 2007. Data analysis using regression and hierarchical/multilevel
1058 models. New York, NY, USA: Cambridge University Press.
- 1059 Gelman A. 2008. Scaling regression inputs by dividing by two standard
1060 deviations. *Statistics in Medicine* 27: 2865-2873.
- 1061 Gelman A, Pardoe I. 2006. Bayesian measures of explained variance and pooling in
1062 multilevel (hierarchical) models. *Technometrics* 48: 241-251.
- 1063 Graham ME (2003) Confronting multicollinearity in multiple linear regression. *Ecology*
1064 84: 2809-2815
- 1065 Grueber CE, Nakagawa S, Laws RJ, Jamieson IG. 2011. Multimodel inference in
1066 ecology and evolution: Challenges and solutions. *Journal of Evolutionary Biology* 24:
1067 699–711.
- 1068 Harrison XA. 2014. Using observation-level random effects to model overdispersion in
1069 count data in ecology and evolution. *PeerJ* 2: e616.
- 1070 Harrison XA. 2015. A comparison of observation-level random effect and Beta-Binomial
1071 models for modelling overdispersion in Binomial data in ecology & evolution. *PeerJ*, 3:
1072 p.e1114.
- 1073 Halsey LG, Curran-Everett D, Vowler SL, Drummond GB. 2015. The fickle P value
1074 generates irreproducible results. *Nature Methods* 12: 179-185.
- 1075 Hegyi G, Garamszegi LZ. 2011. Using information theory as a substitute for stepwise
1076 regression in ecology and behaviour. *Behavioral Ecology and Sociobiology* 65: 69-76.
- 1077 Hilbe JM. 2011. *Negative binomial regression*. Cambridge University Press.
- 1078 Houslay T, Wilson A. 2017. Avoiding the misuse of BLUP in behavioral ecology.
1079 *Behavioral Ecology* arx023 doi:10.1093/beheco/arx023
- 1080 Ives AR. 2015. For testing the significance of regression coefficients, go ahead and log-
1081 transform count data. *Methods in Ecology and Evolution* 6:, 828-835.
- 1082 James FC, McCullugh CF. 1990. Multivariate Analysis In Ecology And Systematics:
1083 Panacea Or Pandora Box. *Annual Review of Ecology and Systematics* 21: 129–166.
- 1084 Johnson JB, Omland KS. 2004. Model selection in ecology and evolution. *Trends in*
1085 *Ecology and Evolution* 19: 101–108.

- 1086 Johnson PCD. 2014. Extension of Nakagawa & Schielzeth's R^2 GLMM to random slopes
1087 models. *Methods in Ecology and Evolution* 5: 944-946.
- 1088 Kass RE, Caffo BS, Davidian M, Meng XL, Yu B, Reid N. 2016. Ten simple rules for
1089 effective statistical practice. *PLoS computational biology* 12: p.e1004961.
- 1090 Keene ON. 1995. The log transform is special. *Statistics in Medicine* 14: 811–819.
- 1091 Kéry M. 2010. Introduction to WinBUGS for ecologists: Bayesian approach to
1092 regression, ANOVA, mixed models and related analyses. Academic Press.
- 1093 Kuznetsova A, Brockhoff PB, Christensen RHB. 2014. Package 'lmerTest'. Test for
1094 random and fixed effects for linear mixed effect models (lmer objects of lme4 package).
1095 R package ver.2.
- 1096 Lefcheck JS. 2015. piecewiseSEM: Piecewise structural equation modeling in R for
1097 ecology, evolution, and systematics. *Methods in Ecology and Evolution* 7: 573-579.
- 1098 Lindberg MS, Schmidt JH, Walker J. 2015. History of multimodel inference via model
1099 selection in wildlife science. *The Journal of Wildlife Management* 79: 704–707.
- 1100 Low-Décarie E, Chivers C, Granados M. 2014. Rising complexity and falling explanatory
1101 power in ecology. *Frontiers in Ecology and the Environment* 12: 412-418.
- 1102 Lüdtke D. 2017. SjPlot: Data Visualization for Statistics in Social Science. 2017 R
1103 package version, 2.4.0.
- 1104 Lukacs PM, Burnham KP, Anderson DR. 2010. Model selection bias and Freedman's
1105 paradox. *Annals of the Institute of Statistical Mathematics* 62: 117–125.
- 1106 Mundry R. 2011. Issues in information theory-based statistical inference—a commentary
1107 from a frequentist's perspective. *Behavioral Ecology and Sociobiology* 65: 57-68.
- 1108 Murtaugh PA. 2007. Simplicity and complexity in ecological data analysis. *Ecology* 88:
1109 56-62.
- 1110 Murtaugh PA. 2009. Performance of several variable-selection methods applied to real
1111 ecological data. *Ecology Letters* 10: 1061-1068.
- 1112 Murtaugh PA. 2014. In defense of P values. *Ecology* 95: 611-617
- 1113 Nagelkerke NJ. 1991. A note on a general definition of the coefficient of determination.
1114 *Biometrika* 78: 691-692.
- 1115 Nakagawa S, Foster T. 2004. The case against retrospective statistical power analyses
1116 with an introduction to power analysis. *Acta Ethologica* 7: 103-108.
- 1117 Nakagawa S, Freckleton RP. 2008. Missing inaction: the dangers of ignoring missing
1118 data. *Trends in Ecology and Evolution* 23(11): 592-596.

- 1119 Nakagawa S, Freckleton RP. 2011. Model averaging, missing data and multiple
1120 imputation: a case study for behavioural ecology. *Behavioral Ecology and Sociobiology*
1121 65: 103-116.
- 1122 Nakagawa S, Schielzeth H. 2010. Repeatability for Gaussian and non-Gaussian data: a
1123 practical guide for biologists. *Biological Reviews* 85: 935-956
- 1124 Nakagawa S, Schielzeth H. 2013. A general and simple method for obtaining R² from
1125 generalized linear mixed-effects models. *Methods in Ecology and Evolution* 4: 133-142.
- 1126 Nakagawa S., Johnson PC, Schielzeth H. 2017. The coefficient of determination R² and
1127 intra-class correlation coefficient from generalized linear mixed-effects models revisited
1128 and expanded. *Journal of The Royal Society Interface* 14(134), p.20170213.
- 1129 Nickerson RS. 2000. Null Hypothesis Significance Testing: A Review of an Old and
1130 Continuing Controversy. *Psychological Methods* 5: 241-301.
- 1131 O'Hara RB, Kotze DJ. 2010. Do not log-transform count data. *Methods in Ecology and*
1132 *Evolution* 1: 118-122.
- 1133 Peters RH. 1991. *A critique for ecology*. Cambridge University Press.
- 1134 Peig J, Green AJ. 2009. New perspectives for estimating body condition from
1135 mass/length data: the scaled mass index as an alternative method. *Oikos* 118: 1883-
1136 1891.
- 1137 Quinn GP, Keough MJ. 2002. *Experimental design and data analysis for biologists*.
1138 Cambridge University Press.
- 1139 R Core Team. 2016. R: A language and environment for statistical computing. R
1140 Foundation for Statistical Computing, Vienna, Austria. URL <https://www.R-project.org/>.
- 1141 Richards SA. 2005. Testing ecological theory using the information-theoretic approach:
1142 examples and cautionary results. *Ecology* 86: 2805-2814.
- 1143 Richards SA. 2008. Dealing with overdispersed count data in applied ecology. *Journal of*
1144 *Applied Ecology* 45 218–227.
- 1145 Richards, SA, Whittingham MJ, Stephens PA. 2011. Model selection and model
1146 averaging in behavioural ecology: the utility of the IT-AIC framework. *Behavioral Ecology*
1147 *and Sociobiology* 65: 77–89.
- 1148 Rykiel EJ. 1996. Testing ecological models: The meaning of validation. *Ecological*
1149 *Modelling* 90: 229-244.
- 1150 Satterthwaite FE. 1946. An approximate distribution of estimates of variance
1151 components. *Biometrics Bulletin* 2(6): 110-114.

- 1152 Scheipl F, & Bolker, B. 2016. RLRsim: Exact (Restricted) Likelihood Ratio Tests for
1153 Mixed and Additive Models *Computational Statistics & Data Analysis*. R package version
1154 3.1-3. <https://cran.r-project.org/web/packages/RLRsim/index.html>
- 1155 Schielzeth H, Forstmeier W. 2009. Conclusions beyond support: overconfident
1156 estimates in mixed models. *Behavioral Ecology* 20: 416-420.
- 1157 Schielzeth H, Nakagawa S. 2013. Nested by design: model fitting and interpretation in a
1158 mixed model era. *Methods in Ecology Evolution* 4: 14-24
- 1159 Schielzeth H. 2010. Simple means to improve the interpretability of regression
1160 coefficients. *Methods in Ecology and Evolution* 1: 103-113
- 1161 Southwood TRE, Henderson PA. 2000. *Ecological methods*. John Wiley &
1162 Sons. Stephens PA, Buskirk SW, Hayward GD, Martinez Del Rio C. 2005. Information
1163 theory and hypothesis testing: a call for pluralism. *Journal of Applied Ecology* 42: 4-12.
- 1164 Symonds MRE, Moussalli A. 2011. A brief guide to model selection, multimodel inference
1165 and model averaging in behavioural ecology using Akaike's information criterion.
1166 *Behavioral Ecology and Sociobiology* 65: 13–21.
- 1167 Vaida F, Blanchard S. 2005. Conditional Akaike information for mixed-effects models.
1168 *Biometrika* 92: 351–370
- 1169 van de Pol M, Wright J. 2009. A simple method for distinguishing within-versus between-
1170 subject effects using mixed models. *Animal Behaviour* 77: 753-758.
- 1171 Verbenke G, Molenberghs G. 2000. Linear mixed models for longitudinal data. New
1172 York, Springer.
- 1173 Warton D, Hui F. 2011. The arcsine is asinine: the analysis of proportions in ecology.
1174 *Ecology* 92: 3-10
- 1175 Warton DI, Lyons M, Stoklosa J, Ives AR. 2016. Three points to consider when choosing
1176 a LM or GLM test for count data. *Methods in Ecology and Evolution* 7: 882-90.
- 1177 Wilson AJ, Réale D, Clements MN, Morrissey MM, Postma E, Walling CA, Kruuk LEB,
1178 Nussey DH. 2010. An ecologist's guide to the animal model. *Journal of Animal Ecology*
1179 79: 13–26.
- 1180 Wood SN, Goude Y, Shaw S. 2015. Generalized additive models for large data
1181 sets. *Journal of the Royal Statistical Society: Series C (Applied Statistics)* 64:139-155.
- 1182 Whittingham MJ, Stephens PA, Bradbury RB, Freckleton RP 2006. Why do we still use
1183 stepwise modelling in ecology and behaviour? *Journal of Animal Ecology* 75: 1182-1189.

- 1184 Zuur AF, Ieno EN, Walker NJ, Saveliev AA, Smith GM. 2009 *Mixed Effects Models and*
1185 *Extensions in Ecology with R* Springer, New York
- 1186 Zuur AF, Ieno EN, Elphick CS. 2010. A protocol for data exploration to avoid common
1187 statistical problems. *Methods in Ecology and Evolution* 1: 3-14.
- 1188 Zuur AF, Ieno EN, 2016. A protocol for conducting and presenting results of regression-
1189 type analyses. *Methods in Ecology and Evolution* 7: 636-645.

Figure 1(on next page)

Differences between Random Intercept vs Random Slope Models

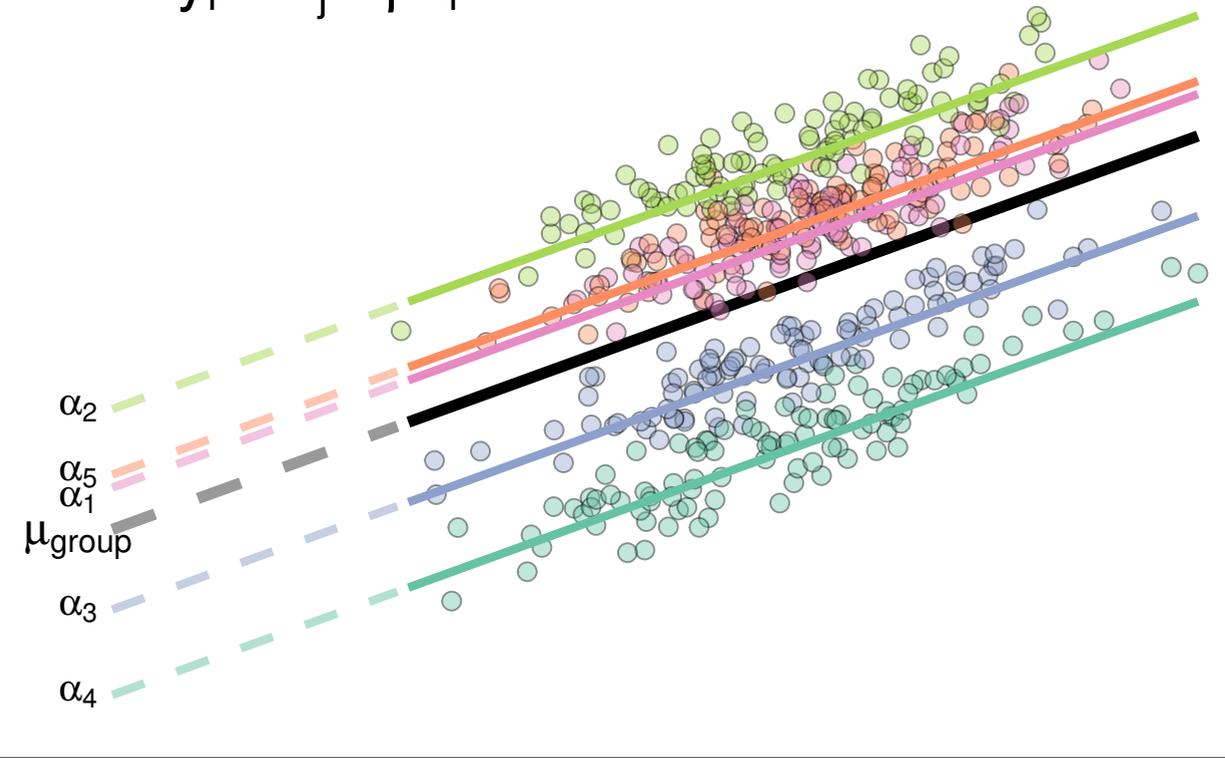
(A) A random-intercepts model where the outcome variable y is a function of predictor x , with a random intercept for group ID (coloured lines). Because all groups have been constrained to have a common slope, their regression lines are parallel. Solid lines are the regression lines fitted to the data. Dashed lines trace the regression lines back to the y intercept (0 in this case). Point colour corresponds to group ID of the data point. The black line represents the global mean value of the distribution of random effects.

A

Dependent Variable y

Random Intercepts

$$y_i = \alpha_j + \beta x_i$$



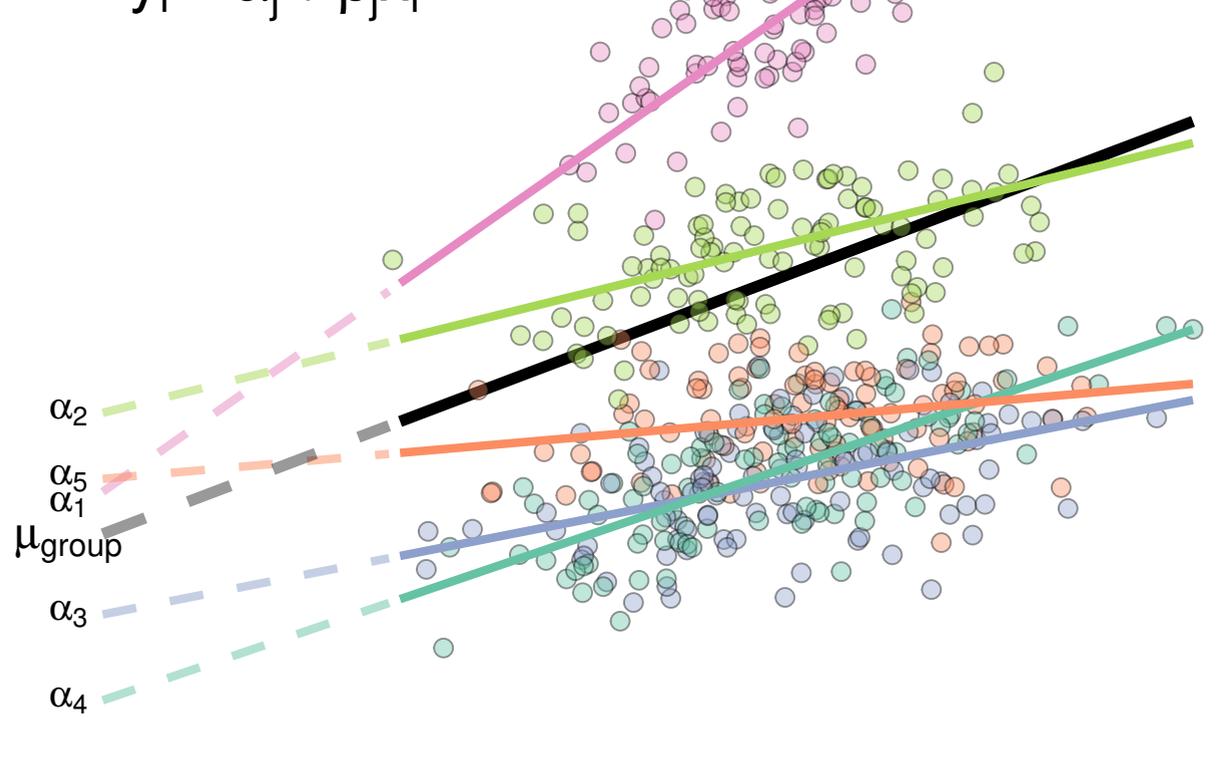
Predictor Variable x

B

Dependent Variable y

Random Intercepts and Slopes

$$y_i = \alpha_j + \beta_j x_i$$



Predictor Variable x

Figure 2(on next page)

The effect of collinearity on model parameter estimates.

We simulated 10,000 iterations of a model $y \sim x1 + x2$, where $x1$ had a positive effect on y ($\beta_{x1} = 1$, vertical dashed line). $x2$ is collinear with $x1$ with either a moderate ($r = 0.5$, A) or strong correlation ($r = 0.9$, B). With moderate collinearity, bias in estimation of β_{x1} is minimal, but variance in estimation of β_{x2} is large. When collinearity is strong, bias in estimation of β_{x1} is large, with 14% of simulations estimating a negative coefficient for the effect of $x1$. For more elaborate versions of these simulations, see Freckleton (2011)

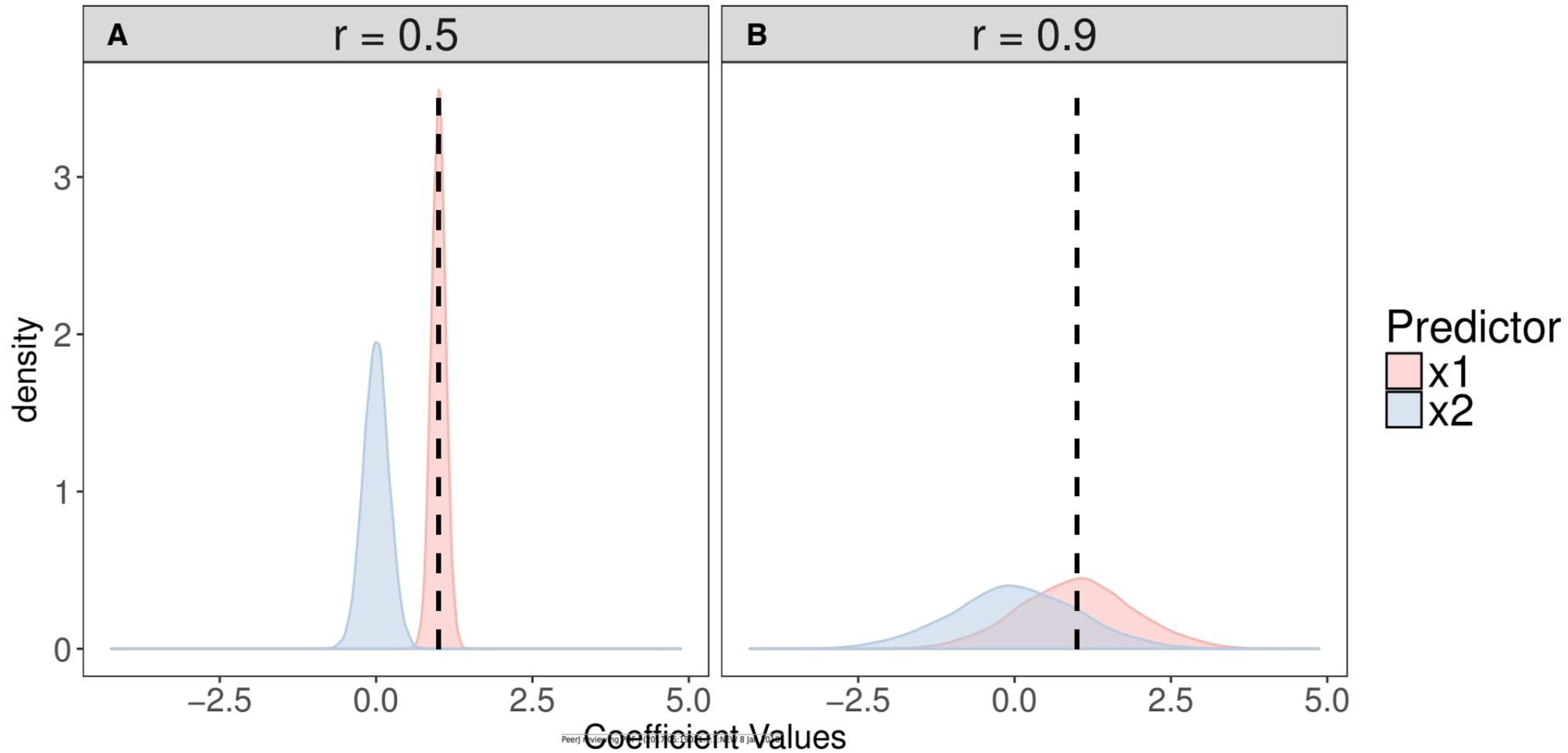


Figure 3(on next page)

Using Simulation to Assess Model Fit for GLMMs

(A) Histogram of the proportion of zeroes in 10,000 datasets simulated from a Poisson GLMM. Vertical red line shows the proportion of zeroes in our real dataset. There is no strong evidence of zero-inflation for these data. (B) Histogram of the sum of squared Pearson residuals for 1000 parametric bootstraps where the Poisson GLMM has been re-fitted to the data at each step. Vertical red line shows the test statistic for the original model, which lies well outside the simulated frequency distribution. The ratio of the real statistic to the simulated data can be used to calculate a mean dispersion statistic and 95% confidence intervals, which for these data is mean 3.16, 95% CI 2.77 - 3.59. Simulating from models provides a simple yet powerful set of tools for assessing model fit and robustness.

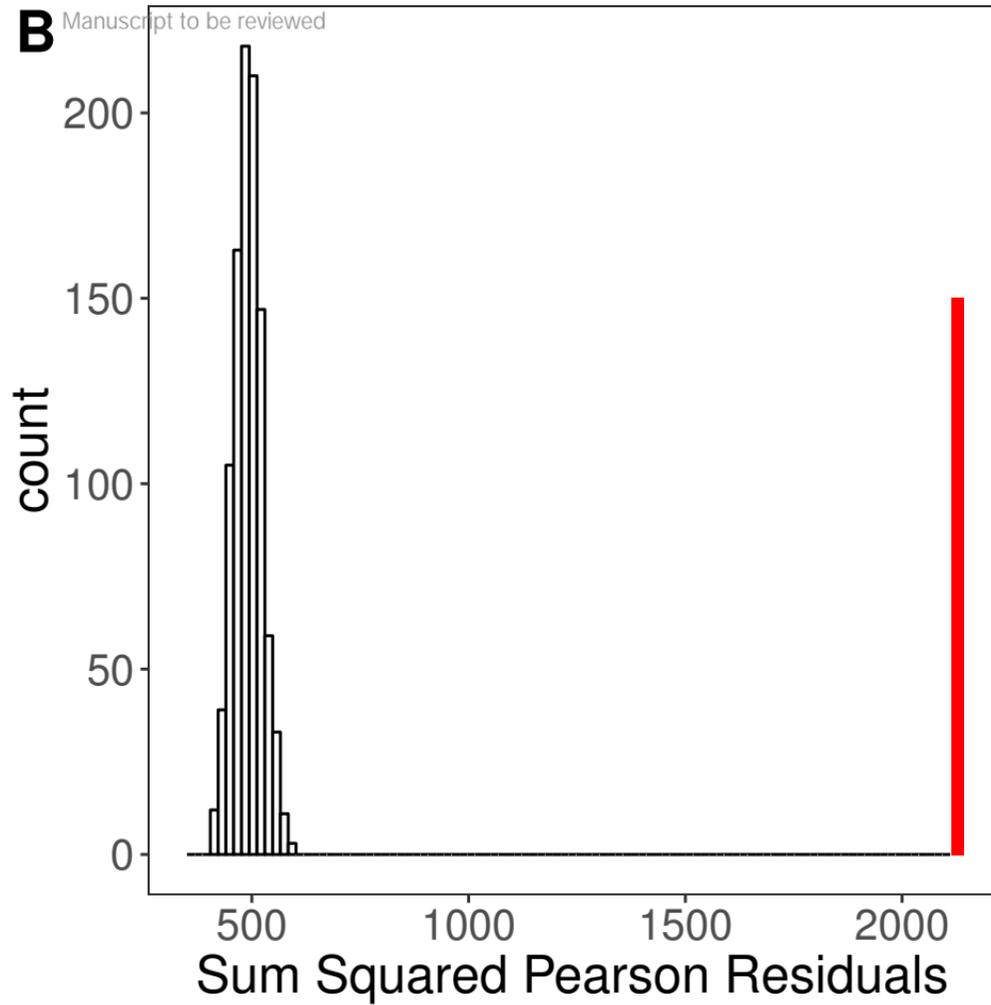
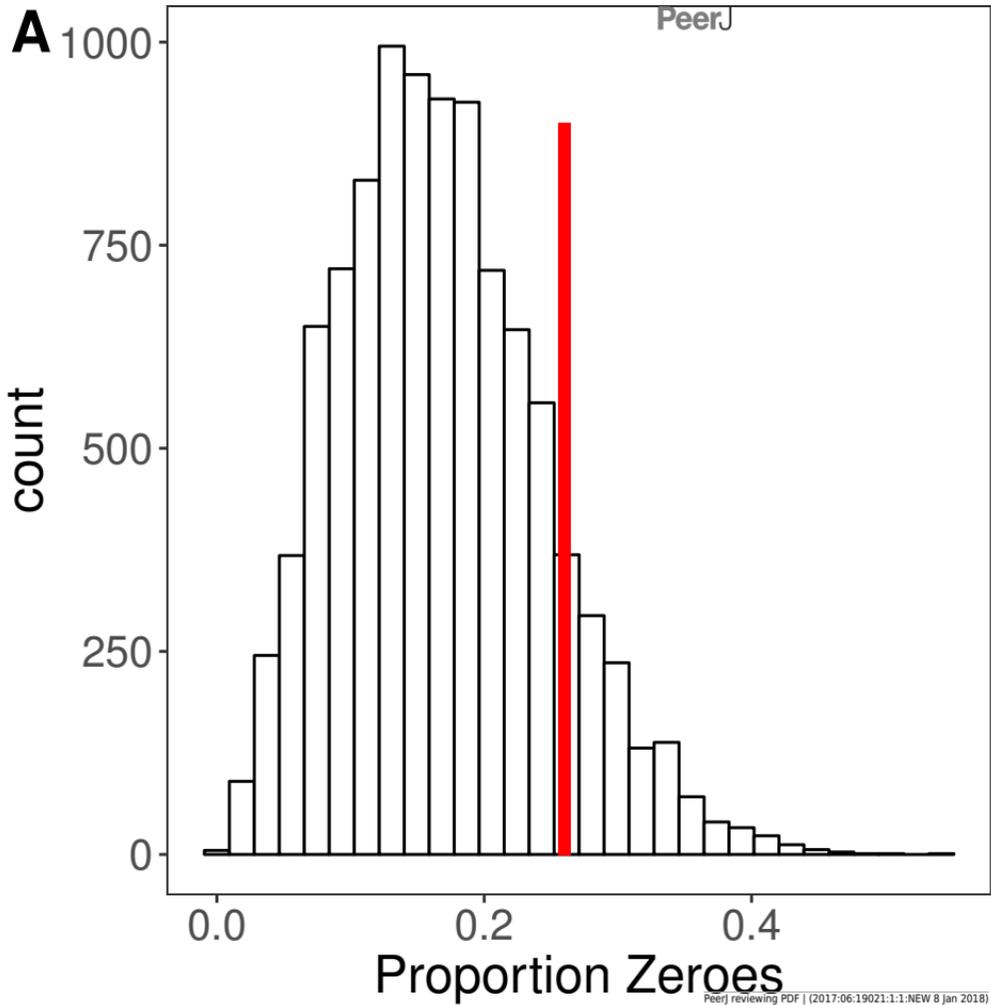


Figure 4(on next page)

The effect of data dredging on Type 1 Error Rate as a function of the number of continuous and categorical variables included in the global model

Adding both categorical and continuous predictors to the models (increasing complexity) increases the Type I error rate (95% confidence intervals of model averaged parameter estimates do not cross zero). The slope of the increase in Type I error rate with increase in the number of continuous predictors is modified by how many categorical predictors there are in the model, with steeper increases in Type 1 error rate for lower numbers of categorical predictors. However, the Type I error rate was highest overall for global models containing the largest numbers of parameters. For full details of the simulation methodology, see supplementary file S1).

