Multi-scale immunoepidemiological modeling of within-host and between-host HIV dynamics: Systematic review of mathematical models

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Objective: The objective of this study is to conduct a systematic review of multi-scale HIV immunoepidemiological models to improve our understanding of the synergistic impact between the HIV viral-immune dynamics at the individual level and HIV transmission dynamics at the population level.

Background: While within-host and between-host models of HIV dynamics have been well studied at a single scale, connecting the immunological and epidemiological scales through multi-scale models is an emerging method to infer the synergistic dynamics of HIV at the individual and population levels.

Methods: We reviewed 9 articles using the PRISMA (Preferred Reporting Items for Systematic Reviews and Meta-Analyses) framework that focused on the synergistic dynamics of HIV immunoepidemiological models at the individual and population levels.

Results: HIV immunoepidemiological models simulate viral immune dynamics at the within-host scale and the epidemiological transmission dynamics at the between-host scale. They account for longitudinal changes in the immune viral dynamics of HIV+ individuals, and their corresponding impact on the transmission dynamics in the population. They are useful to analyze the dynamics of HIV super-infection, co-infection, drug resistance, evolution, and treatment in HIV+ individuals, and their impact on the epidemic pathways in the population. We illustrate the coupling mechanisms of the within-host and between-host scales, their mathematical implementation, and the clinical and public health problems that are appropriate for analysis using HIV immunoepidemiological models.

Conclusion: HIV immunoepidemiological models connect the within-host immune dynamics at the individual level and the epidemiological transmission dynamics at the population level. While multi-scale models add complexity over a single-scale model, they account for the time varying immune viral response of HIV+ individuals, and the corresponding impact on the time-varying risk of transmission of HIV+ individuals to other susceptibles in the population.

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Abstract

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21 and their corresponding impact on the transmission dynamics in the population. They are use-

22 ful to analyze the dynamics of HIV super-infection, co-infection, drug resistance, evolution,

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INTRODUCTION

HIV prevalence and mortality were 38.8 million and 1.2 million deaths respectively in 2015, with annual incidence being relatively constant at 2.6 million per year from 2005 to 2015 (Wang et al. (2016)). Access to big data and emergence of unanswered questions enable novel methods of mathematical models to connect within-host immune viral dynamics at the individual level, and the between-host epidemiological transmission of infectious diseases at the population level (Gog et al. (2015)). Mathematical models of HIV dynamics have been extensively studied using single-scale based models at the immunological and epidemiological scales (Perelson & Ribeiro (2013); Akpa & Oyejola (2010)). The immunological models focus on the within-host immune viral dynamics at the individual level, while the epidemiological models focus on the between-host transmission dynamics at the population level. Multi-scale immunoepidemiological modeling is an emerging method to study the synergistic dynamics of HIV at the individual and population levels (DebRoy & Martcheva (2008); Yeghiazarian et al. (2013); Handel & Rohani (2015)).

Epidemiological models

Epidemiological modeling of HIV infection started in 1985 (Curran et al. (1985)). Epidemiological models of HIV infections assign each individual to one of the following states: susceptible or infected. Infected individuals may transmit HIV to susceptible hosts with the same transmission rate over the course of disease, and experience specific duration of infection (Isham (1988); Hyman & Ann Stanley (1988); Haberman (1990)). However, time since infection, other co-infections, and a host's biological factors such as age, sex, genetic susceptibility, and immune status cause variation in infectiousness of HIV+ individuals (Cassels et al. (2008)). Host heterogeneity among different ages, gender and risk groups is significant due to the multiple routes of transmission – sexual transmission, intravenous transmission through needle sharing, blood transfusion, and mother-to-child vertical transmission.

Immunological models

Within-host models of HIV at the individual level study the dynamics of HIV and target immune cells – CD4+ T cells, macrophages, and dendritic cells. The complexity of the models vary from molecular level (Reddy & Yin (1999); Zarrabi et al. (2010); Hosseini & Mac Gabhann (2012)), cellular level (Anderson & May (1992); McLean (1993); Ho et al. (1995); Perelson et al. (1996); Kirschner (1996); De Boer & Perelson (1998); Banks et al. (2008); Hosseini & Mac Gabhann (2012); Perelson & Ribeiro (2013)), and tissue level (Spouge et al. (1996)). The within-host immunological models analyze the mechanisms of HIV pathogenesis and prognosis from acute, latent and late stages of HIV infection to AIDS phase.

Immunoepidemiological models

Figure 1 illustrates that the transmission dynamics of HIV in the population is dependent on the immune viral dynamics of HIV+ individuals. Immunoepidemiological models factor the HIV transmission dynamics at the population level as a function of within-host immune viral responses at the individual level (DebRoy & Martcheva (2008); Yeghiazarian et al. (2013); Hellriegel (2001)).

Clinical and public health significance

HIV immunoepidemiological models focus on solutions for the following questions of clinical and public health significance (Feng et al. (2011)):

- How does within-host immune-viral dynamics of HIV affect incidence at the population level?

- How does population level transmission dynamics of HIV affect viral evolution at the individual level?

In this study, we review the multi-scale modeling methods that connect the within-host and between-host scales of HIV models. Understanding the relation between these two scales is key to understand HIV prognosis, transmission risk, and intervention effectiveness (Pepin et al. (2010)).

METHODS

Search strategy

We searched the PubMed database for articles published from December 1, 1985 to June 1, 2017 with the terms: (HIV and ("multi-scale" or "immunoepidemiology" or "nested model" or ("within-host" and "between host") or ("within-host" and "among host") or ("within-host" and ("epidemiology" or "epidemiological")))).

Data abstraction and synthesis

The data abstraction and synthesis process was conducted by two authors (ND and RNB) independently, and includes the following four steps: identification, screening, eligibility, and inclusion. We resolved discordant decisions through consensus. During the identification step, articles were identified using the above search strategy. During the screening step, duplicate articles were removed, and titles and abstract of the remaining articles were screened to determine their relevance to our study. During the eligibility step, full texts of the articles were analyzed to determine their relevance to our study.

Inclusion and exclusion criteria

The inclusion criteria were articles focused on multi-scale immunoepidemiological modeling of HIV dynamics. The exclusion criteria were articles that focused on genetic epidemiology, molecular epidemiology, parasitology, ecology, evolutionary study, and experimental studies.

PRISMA process

Figure 2 illustrates the process flow diagram of identification, screening, eligibility, and inclusion of articles for the systematic review, using the PRISMA (Preferred Reporting Items for Systematic Reviews and Meta-Analyses) framework (Moher et al. (2009)). 89 articles were uniquely

103 identified, 66 articles were screened out, and 9 articles were found eligible to be included in this

104 systematic review. This systematic review includes a qualitative synthesis and does not include the

105 quantitative synthesis of a meta-analysis (not applicable for this study).

RESULTS

Table 1 illustrates the characteristics of HIV immunoepidemiological modeling studies included in this systematic review. The objective, model implementation, immunoepidemiological link between within-host and between-host models, and significant inferences of these studies are summarized in the table.

Within-Host Scale of HIV Immunoepidemiological Models

The within-host scale of HIV immunoepidemiological models simulate the immune-viral dynamics of HIV, which can later be used to determine the impact on transmission between hosts. We categorize the within-host models by whether they model a single strain of HIV, super-infection, drug resistance, evolution, co-infection and therapeutic interfering particles. The immunological scale includes the primary state variables of uninfected CD4+ T cells concentration (T), infected CD4+ T cells concentration (T^*) and viral load (V), and the corresponding parameters for the immune-viral dynamics between these state variables (Anderson & May (1992); Perelson et al. (1996); De Boer & Perelson (1998)).

HIV infection with single strain

In this approach, it is assumed that there is only one strain of HIV that infects the target cells. No additional features such as mutation, super-infection, or co-infection are considered at the within-host scale. We found three models that include only one strain of HIV at the within-host scale (Shen et al. (2015); Sun et al. (2016); Yeghiazarian et al. (2013)). An example of the basic dynamics are shown in Table 2, which also assumes that viral shedding rate (s) has negative effect on the viral load (V) within-host (DebRoy & Martcheva (2008)). This model can be modified to include the effects of drug therapy, which affect the viral production rate and the viral infectivity rate (Shen et al. (2015); Sun et al. (2016); Yeghiazarian et al. (2013)).

HIV super-infection

HIV super-infection occurs when individuals infected with a single HIV strain are infected with a second HIV strain. and Li included HIV infection with multiple strains in their model, with the assumption of complete competitive exclusion between the strains at the within-host scale. In this context, the strain with the larger reproduction rate becomes dominant. They studied the impact of virulence of different strains on the equilibrium at the individual and population scales (Martcheva & Li (2013)). Table 3 shows the schematic and formulation of this model.

HIV drug resistance

Drug resistance can be acquired through mutations of drug-sensitive strains within-host or through direct transmission of drug-resistant strains. Saenz and Bonhoeffer included HIV infection with drug resistant strains in their model, and studied the effects of antiretroviral treatment (ART) on both drug-sensitive and drug-resistant strains (Saenz & Bonhoeffer (2013)). Table 4 shows the schematic and formulation of this model.

HIV evolution

Studies have modeled HIV viral evolution within-host and its impact on transmission between hosts (Lythgoe et al. (2013); Doekes et al. (2017)). They investigate the trade-off between increased virus replication and virulence and decrease in virus transmission. Doekes et al also included long-lived reservoirs of latently infected CD4+ T cells to determine their impact on HIV within-host competition (Doekes et al. (2017)).

HIV co-infection

HIV co-infection with sexually transmitted infections among high risk groups (Abu-Raddad et al. (2008)), and/or co-infection with endemic infections such as malaria (Cuadros et al. (2011)) have direct impact on increasing the transmission rate of both infections. Cuadros and García-Ramos

152 incorporated HIV co-infection dynamics in the within-host immune model (Callaway & Perelson

153 (2002); Stafford et al. (2000); Nowak & May (2000)) to address increased immune response and

154 increased risk of transmission, and evaluated their impact on HIV epidemics (Cuadros & García-

155 Ramos (2012)). Table 5 shows the schematic and formulation of this model.

HIV and therapeutic interfering particles

157 Therapeutic interfering particles (TIPs) are an emerging drug therapy where therapeutic versions of

158 the pathogen are manufactured to attack viral replication processes and can be transmitted between

159 hosts (Metzger et al. (2011)). In the within-host model developed by Metzger et al, HIV and TIPs

160 are treated as separate viral strains. The model includes CD4+ T cells infected with HIV only,

161 CD4+ T cells infected with TIPs only, and CD4+ T cells dually infected with HIV and TIPs

162 (Metzger et al. (2011)).

Between-Host Scale of HIV Immunoepidemiological Models

164 Between-host scales of HIV immunoepidemiological models are based on the susceptible-infectious

165 (SI) epidemic model, which have been used extensively to study HIV transmission dynamics in a

166 homogeneous population and random mixing of susceptibles (S) and HIV+ individuals (I) (Isham

167 (1988)). Table 6 shows the schematic and formulation of the SI epidemic model. Studies have ex-

168 tended the homogeneous population structure of the SI model to incorporate different populations

169 of infected individuals. We categorize the studies by how they divide the infected population, and

170 thus how the transmission rates between these classes differ. We find heterogeneity in HIV trans-

171 mission rates depending on the stages of HIV infection (Cuadros & García-Ramos (2012); Yeghi-

172 azarian et al. (2013); Sun et al. (2016); Shen et al. (2015)), and the dynamics of super-infection

173 (Martcheva & Li (2013)), drug resistance (Saenz & Bonhoeffer (2013)), evolution (Lythgoe et al.

174 (2013); Doekes et al. (2017)), and therapeutic interfering particles (Metzger et al. (2011)).

Acute, latent and late stages of HIV infection

Previous studies have shown that transmission rates differ depending on whether the infected population is in the acute, latent, or AIDS stages (Hollingsworth et al. (2008)). This conclusion can be incorporated into immunoepidemiological models by categorizing the infected population into different stages (Cuadros & García-Ramos (2012); Yeghiazarian et al. (2013); Sun et al. (2016); Shen et al. (2015); Saenz & Bonhoeffer (2013)). Cuadros and García-Ramos extended the model so that the HIV+ sub-populations also differed by sexual-risk activity (Cuadros & García-Ramos (2012)). Yeghiazarian et al divided the infected population into stages to evaluate the timing of treatment initiation at the individual level, and its impact on HIV transmission at the population level. They assumed treatment initiation can start during any stage of HIV infection after diagnosis (Yeghiazarian et al. (2013)).

HIV super-infection

HIV infected individuals are categorized based on the strains of infection. Due to the assumption of competitive exclusion at the within-host level in the model developed by Martcheva and Li, susceptible individuals only become infected with one of the strains. Thus, only infected individuals having the dominant within-host strain can super-infect individuals with the lesser within-host strain (Martcheva & Li (2013)).

HIV drug resistance

Drug-resistant strains can emerge during antiretroviral therapy (ART) (Rong et al. (2007)), or can be transmitted between individuals who have never been exposed to ART (Hué et al. (2009)), which may lead to treatment failure if ART is begun (Hamers et al. (2011)). Saenz and Bonhoeffer thus categorize the infected population into those with only drug-sensitive or only drug-resistant strains with or without treatment, and those with drug-sensitive strains that develop drug-resistance while receiving treatment (Saenz & Bonhoeffer (2013)). Table 7 shows the schematic and formulation of

199 this model.

HIV evolution

201 Depending on virulence of the strain, infected individuals are categorized by the strain with which

202 they initially became infected (Doekes et al. (2017); Lythgoe et al. (2013)). Because it is assumed

203 that all other strains develop from an initial strain and only the most virulent strain is transmitted,

204 infected individuals can end up infecting others with a different strain than they were initially

205 infected. Table 8 shows the schematic and formulation of this model.

HIV and therapeutic interfering particles

207 The infected population is divided into classes of those infected with HIV only, those infected with

208 Therapeutic Interfering Particles (TIPs) only, and those infected dually with HIV and TIPs. The

209 infected population is also divided into these classes during different stages of infection (Metzger

210 et al. (2011)). Table 9 shows the schematic and formulation of this model.

Coupling Within-Host and Between-Host Scales of HIV Immunoepidemiological Models

213 The potential for transmission between HIV+ individuals to susceptibles is affected by the viral

214 load of infected hosts (Attia et al. (2009)). In all the models that we analyzed in this systematic

215 review, the transmission rate between hosts is dependent on the within-host viral load. We catego-

216 rize the models into those where the transmission rate is a function of viral load and those where

217 the equilibria of the within-host model are used to determine the transmission rate.

HIV transmission rate as a function of viral load

The within-host and between-host scales of HIV immunoepidemiological models are coupled by basing the transmission rate on the time-varying viral load since infection. The viral load (and thus the transmission rate) is high during the acute and late stages of HIV infection while being low during the latent stage (Hollingsworth et al. (2008); DebRoy & Martcheva (2008)). Table 10 shows the formulation of this model. Unlike the basic SI epidemiological model that assumes constant transmission rate (β), the between-host model assigns time-varying transmission rate, which is dependent on the non-linear viral immune dynamics of HIV in the within-host model.

In some models, the transmission rate depends on the viral load continuously over time (Shen et al. (2015); Martcheva & Li (2013); Saenz & Bonhoeffer (2013)). Saenz and Bonhoeffer also distinguished between drug-resistant and drug-sensitive strains and their corresponding impact on the transmission rate (Saenz & Bonhoeffer (2013)). Martcheva and Li made the death of infected individuals depend on the viral load over time, since the AIDS stage is associated with high viral load (Martcheva & Li (2013)).

In the context of HIV evolution, while the transmission rate varies through time depending on the viral load, the viral load is also modeled to distinguish between different strains (Doekes et al. (2017); Lythgoe et al. (2013)). The transmission rate depends on a predefined infectivity profile which changes depending on the stage of infection, and the frequency of the different viral strains in an infected population. Doekes et al made the transmission rate depend on the frequency of viral strains that were only in actively infected CD4+ T cells (Doekes et al. (2017)).

The within-host viral load can be used to individualize the transmission rate over time (Yeghi-azarian et al. (2013); Sun et al. (2016)). The CD4+ T cell count can also be used to determine the stage of infection (Yeghiazarian et al. (2013)).

HIV transmission rate using viral load equilibrium

Another method of linking the within-host and between-host scales is to use the within-host model to determine an equilibrium for the viral load. This equilibrium can then be used as a constant pa-

244 rameter in the between-host model, which can then be analyzed further by differing the parameters

245 of the within-host model (Metzger et al. (2011); Cuadros & García-Ramos (2012)). Cuadros and

246 García-Ramos accounted for the amplified viral load due to co-infection and the corresponding

247 increase in HIV transmission rate (Cuadros & García-Ramos (2012)). Metzger et al determined

248 the differing viral loads associated with HIV and TIPs, and their effect on the transmission proba-

249 bilities between infected populations (Metzger et al. (2011)).

Clinical and Public Health Implications

HIV virulence

252 Clinical studies have shown that HIV has evolved an intermediate level of virulence at the within-

253 host level that optimizes the transmission potential of the virus at the population level (Fraser et

254 al. (2007)). However, at the within-host level, HIV can evolve quickly (Lemey et al. (2006)),

255 virulence increases during the course of the infection (Kouyos et al. (2011)), and infections with

256 higher replicative capacities have higher virulence (Kouyos et al. (2011)). Replicative capacities

257 also increase over the course of infection, albeit slowly (Kouyos et al. (2011)). Because of this

258 behavior of HIV at the within-host level, it might be expected that HIV would evolve a high

259 virulence at the within-host level, even if it did not optimize the transmission potential at the

260 population level. To understand these seemingly contradictory results, immunoepidemiological

261 models were used, which incorporated these behaviors of HIV at the within-host level (Lythgoe et

262 al. (2013); Doekes et al. (2017)). The model developed by Lythgoe et al found that small rates of

263 within-host evolution optimize the transmission potential at the population level, whereas higher

264 rates of within-host evolution lead to high levels of virulence, but lower transmission potential

265 (Lythgoe et al. (2013)). Lythgoe et al suggest that the clinical observations seen in HIV may be

266 a result of a within-host fitness landscape that is complex to traverse, since this leads to smaller

267 rates of within-host evolution (Lythgoe et al. (2013)). They also suggest the effect of the adaptive

268 immune response may play a role in explaining the observed behavior (Lythgoe et al. (2013)).

269 Based off the results from Lythgoe et al, a similar model was constructed by Doekes et al, which

270 included a latent reservoir of CD4+ T cells at the within-host level (Doekes et al. (2017)). They

271 found that this latent reservoir may be responsible for delaying the evolutionary dynamics at the

272 within-host level, which then leads to the transmission potential being optimized (Doekes et al.

273 (2017)).

Antiretroviral therapy

275 While there is uncertainty over the timing of initiating antiretroviral therapy, some studies have

276 suggested there may be benefits to beginning treatment early (When To Start Consortium et al.

277 (2009); Cohen (2011)). Experimental studies also suggest that because ART reduces transmissi-

278 bility, increasing coverage levels may reduce the prevalence of HIV (Cohen (2011)). However,

279 drug-resistant strains can emerge, which can lead to treatment failure (Hué et al. (2009); Hamers et

280 al. (2011)). Immunoepidemiological models were used to understand these effects of ART, focus-

281 ing on treatment timing (Sun et al. (2016); Yeghiazarian et al. (2013)), coverage levels (Shen et al.

282 (2015)), and drug resistance (Saenz & Bonhoeffer (2013); Sun et al. (2016)). The models showed

283 that in general, initiating treatment early (Yeghiazarian et al. (2013); Sun et al. (2016)), increasing

284 coverage (Shen et al. (2015); Saenz & Bonhoeffer (2013)), and increasing effectiveness of ART

285 (Shen et al. (2015); Saenz & Bonhoeffer (2013)) reduces the prevalence of HIV.

286 However, in certain cases, increases in the prevalence of HIV may occur even with early treat-

287 ment initiation, increased coverage, and increased effectiveness of ART to drug-sensitive strains.

288 Models showed that as ART coverage levels increase, the prevalence of drug-resistant strains in-

289 crease, which cause an increase in HIV prevalence (Saenz & Bonhoeffer (2013)). Prevalence can

290 also increase if drug-resistant strains cause the drug efficacy to decrease significantly (Sun et al.

291 (2016)). These results imply that there may be an optimal therapy coverage level that will mini-

292 mize the number of infections (Saenz & Bonhoeffer (2013)). Therefore, in these cases, the models

293 suggest that HIV prevalence can be reduced by focusing efforts on decreasing the risk of drug

294 resistance emergence (Saenz & Bonhoeffer (2013)).

Clinical studies have observed that under certain conditions, the prevalence of HIV increases when ART coverage levels increase (Zaidi et al. (2013)). Zaidi et al hypothesize that since ART reduces viral load, patients may live longer, and thus have the ability to infect more people (Zaidi et al. (2013)). Immunoepidemiolgical models also observed this effect (Shen et al. (2015)), including a model of super-infection (Martcheva & Li (2013)). Both model outcomes are consistent with the hypothesis of Zaidi et al, since the models find that the increased prevalence is due solely to decreases in viral load (Shen et al. (2015); Martcheva & Li (2013)). The model developed by Shen et al found that this effect can be minimized if drug effectiveness is high (Shen et al. (2015)).

Therapeutic interfering particles

Clinical trials have shown that therapeutic interfering particles (TIPs) have the potential to reduce within-host viral load (Levine et al. (2006)) and transmit between hosts (Aaskov et al. (2006)). Experimental studies have also shown that HIV transmission rates between hosts depend on the within-host viral load (Fraser et al. (2007)). Based on these assumptions, an immunoepidemiological model is developed, which deploys TIPs to a small proportion (1%) of the population (Metzger et al. (2011)). The effect on HIV prevalence due to deploying TIPs is compared to deploying ART and to deploying a hypothetical HIV vaccine. When TIPs have the ability to transmit between hosts, the model shows deploying TIPs reduces HIV prevalence to lower levels than deploying ART therapy or deploying vaccines. However, the model shows that if TIPs do not have the ability to transmit between hosts, then there is minimal effect on the reduction of HIV prevalence (Metzger et al. (2011)). While more study of TIPs is needed, TIPs have the potential to be an effective therapy than either ART or vaccines.

HIV co-infection

Experimental studies suggest that co-infection may be responsible for increases seen in set-point viral load (spVL) at the within-host level over time (Modjarrad & Vermund (2010)). These increases due to co-infection vary substantially within-host (Kublin et al. (2005)). Also, the concen-

320 trations of co-infection in high-risk groups versus low-risk groups may affect how HIV spreads

321 in the general population (Abu-Raddad et al. (2008)). To study the mechanisms responsible for

322 these effects of co-infection, an immunoepidemiological model was developed (Cuadros & García-

323 Ramos (2012)). They found that populations with higher spVL lead to higher increases in viral

324 load due to co-infection, whereas populations with lower spVL leads to lower increases in viral

325 load due to co-infection. This leads to a greater chance of co-infection increasing the prevalence

326 of HIV in populations with high average spVL (Cuadros & García-Ramos (2012)). Therefore, the

327 effects of co-infection may be mitigated by identifying the viral factors that can reduce the spVL

328 in the population.

DISCUSSION

Mathematical implementation of HIV immunoepidemiological models

We conducted this systematic review of HIV immunoepidemiological models to improve our understanding and analysis of the synergistic dynamics of HIV prognoses at the individual level and the transmission dynamics at the population level. With respect to mathematical implementation, within-host models are implemented using ordinary differential equations which determine the HIV transmission rate for the between-host model. If the within-host model is used at equilibrium to determine constant parameters for the between-host model, ordinary differential equations are used for the between-host model as well (Cuadros & García-Ramos (2012); Metzger et al. (2011)). Integro-differential equations with delay are used in the between-host scales of HIV immunoepidemiological models to study HIV evolution dynamics (Lythgoe et al. (2013); Doekes et al. (2017)). Partial differential equations are used for the between-host model if the transmission rate changes continuously with the within-host viral load over time (Shen et al. (2015); Martcheva & Li (2013); Saenz & Bonhoeffer (2013)). Individual or agent-based based models analyze the HIV transmission dynamics between individual agents in a population, wherein the HIV transmission rates of each individual is determined by their specific within-host immune-viral dynamics (Sun et al. (2016); Yeghiazarian et al. (2013)).

Complexity of multi-scale models

Multi-scale HIV immunoepidemiological models have higher complexity in comparison to single-scale immune or epidemiology models (Mideo et al. (2008)). Thereby, the choice of immunoepidemiological models should be determined by problems with significant public health and clinical implications that can be addressed better by multi-scale models compared to single-scale models.

Clinical and public health relevant problems of HIV dynamics

Table 11 illustrates the clinical and public health relevant problems of HIV virulence, co-infection, super infection, drug resistance and treatment dynamics that can be potentially addressed using multi-scale models. Since the viral load among infected individuals varies with time during the acute, latent and late stages of HIV infection, immunoepidemiological models account for the time-varying viral load within host and their impact on transmission between hosts. Co-infection among HIV-infected individuals increases the average set-point of viral load in the population (Cuadros & García-Ramos (2012)). Super-infection of multiple HIV strains leads to oscillations in the population level which do not occur in the absence of super-infection; this effect is only observed using the multi-scale immunoepidemiological model (Martcheva & Li (2013)). The emergence of drug resistance within hosts impacts the optimal coverage levels of drug-sensitive treatment at the population level (Saenz & Bonhoeffer (2013)). Immunoepidemiological models can account for treatment initiation, compliance and interruption behavior among HIV-positive individuals as well as pre-exposure prophylaxis of high-risk HIV-negative individuals, and their impact on emergence of drug resistance in the population. The new knowledge gained from analysis of HIV immunoepidemiological dynamics add value in improving clinical and public health interventions for prevention and control of HIV epidemics.

Limitations

We reviewed English language articles on HIV immunoepidemiological models that were referenced in the PubMed database. The dynamics of the HIV immunoepidemiological models are dependent on the selection of parameters, and the coupling mechanisms of within-host immune-viral dynamics and between-host transmission dynamics. Verification and validation of HIV immunoepidemiological models (and multi-scale models in general) with empirical data is a challenge to be addressed in future studies. Also, the selection of optimal layers from the genomic, molecular, cellular, and organ levels at the micro-biological scale to the individual, family, community, national, and global levels at the macro-social scale is a challenge that need be addressed well in

377 future studies.

Conclusion

379 HIV immunoepidemiological models combine the immune-viral dynamics at the within-host im-

380 munological scale with the transmission dynamics at the between-host epidemiological scale to

381 analyze HIV dynamics of a single strain infection, co-infection, super-infection, evolution, drug

382 resistance, and treatment protocols in heterogeneous populations. Based on our understanding of

383 synergistic dynamics of HIV at the individual and population scales, we should select the optimal

384 layers of analysis from micro-biological to macro-social levels for multi-scale models to identify

385 and improve solutions to clinical and public health relevant problems of HIV dynamics.

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FIGURE LEGENDS

Figure 1

Within-host immune-viral dynamics and between-host transmission dynamics of HIV. HIV spreads in the population from infected individuals to susceptibles through sexual contact, intra-venous drug use, blood transfusion and mother-to-child vertical transmission. HIV immune-viral dynamics determine the time-varying viral load within each infected individual.

Figure 2

PRISMA flow-diagram. PRISMA (Preferred Reporting Items for Systematic Reviews and Meta-Analyses) flow-diagram of articles' identification, screening, eligibility and inclusion in the systematic review. A total of 9 studies are included in this systematic review of multi-scale immunoepidemiological modeling of within-host and between-host HIV dynamics.

Figure 1

Figure 1: Within-host immune-viral dynamics and between-host transmission dynamics of HIV.

HIV spreads in the population from infected individuals to susceptibles through sexual contact, intravenous drug use, blood transfusion and mother-to-child vertical transmission. HIV immune-viral dynamics determine the time-varying viral load within each infected individual.
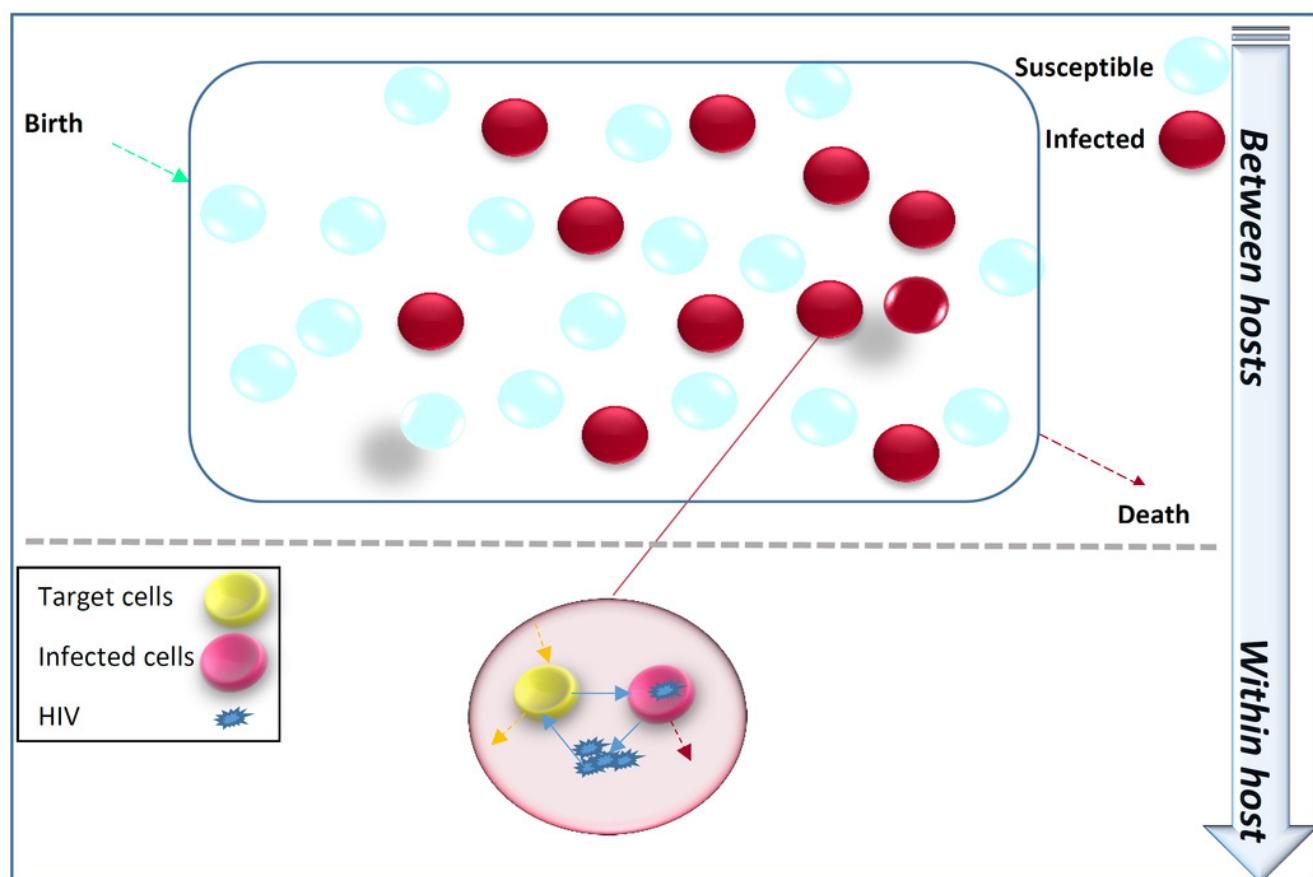
Figure 2

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PRISMA (Preferred Reporting Items for Systematic Reviews and Meta-Analyses) flow-diagram of articles' identification, screening, eligibility and inclusion in the systematic review. A total of 9 studies are included in this systematic review of multi-scale immunoepidemiological modeling of within-host and between-host HIV dynamics.

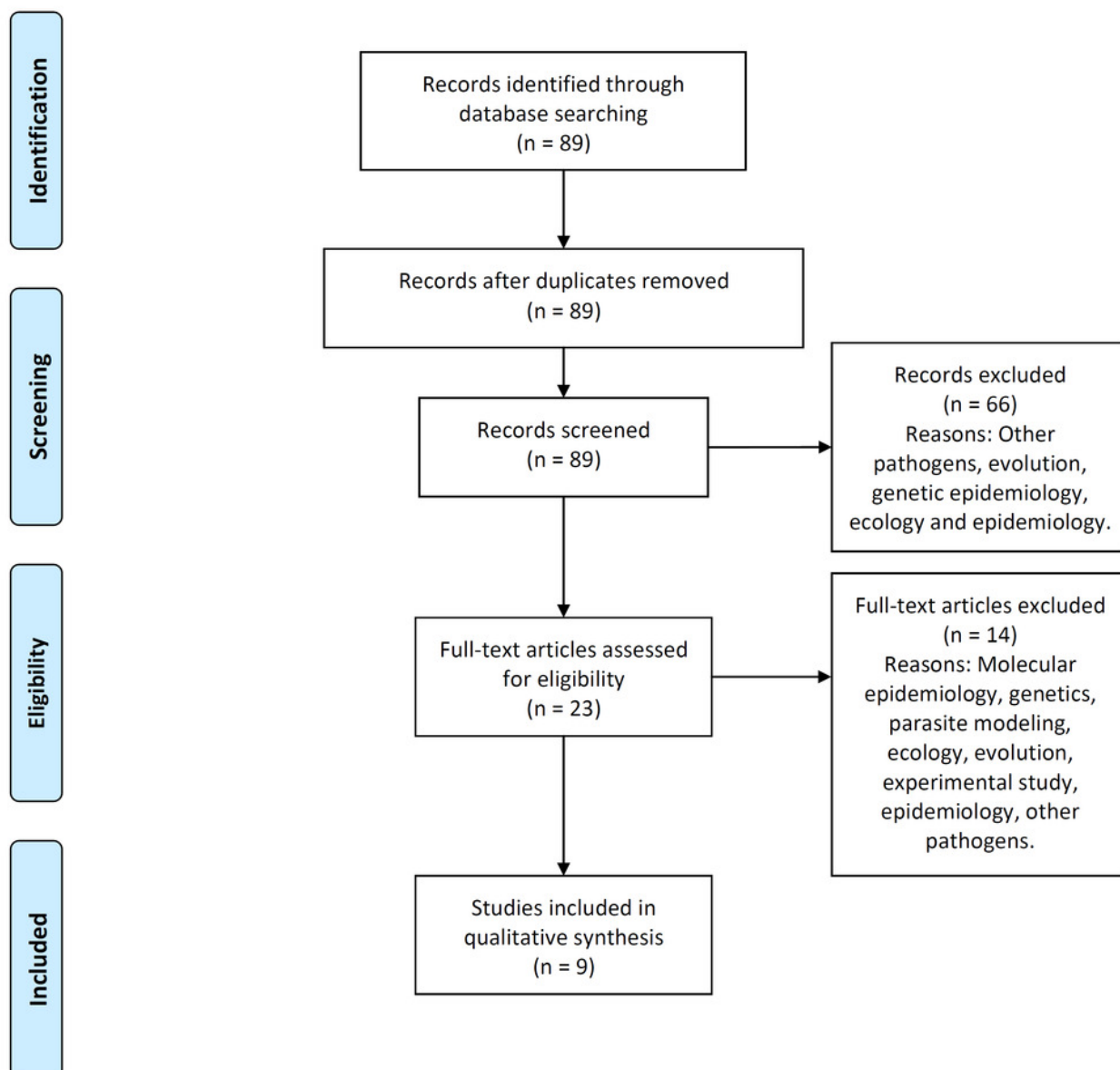



Table 1: Characteristics of HIV immunoepidemiological modeling studies.

The study topic, objective, model implementation, immunoepidemiological link between within-host and between-host models, and inferences of the studies included in the systematic review are summarized.

Table 1: **Characteristics of HIV immunoepidemiological modeling studies.** The study topic, objective, model implementation, immunoepidemiological link between within-host and between-host models, and inferences of the studies included in the systematic review are summarized.

Study	Topic	Objective	Implementation	Immunoepidemiological link	Inferences
Martcheva & Li (2013)	Super-infection	How does HIV super-infection affect population dynamics?	Partial differential equations	Transmission rate between hosts and death rate of individuals depend on viral load within host over time.	In certain cases, decreasing viral load can cause higher prevalence of HIV since infected individuals may live longer; oscillations at population level do not occur in superinfection, contrasting previous studies that did not use linked models.
Saenz & Bonhoeffer (2013)	Drug resistance	How do the dynamics of drug-sensitive and drug-resistant HIV strains within hosts affect the prevalence of drug-resistant strains in the population?	Partial differential equations	Transmission rate between hosts depends on viral load within host over time.	Increasing early initiation and coverage decreases total prevalence upto an optimal treatment coverage level but increases incidence and prevalence of drug resistant infections; above the optimal treatment coverage level, number of infections may not decrease in the long term and can even increase.
Lythgoe et al. (2013)	Evolution	How does competition between strains within-host affect evolution of HIV virulence?	Integro-differential equations with delay	Strain-specific infectivity rate between hosts depends on frequency of strains within-host.	Small rates of within-host evolution modestly increase HIV virulence while maximizing transmission potential; high rates of within-host evolution largely increase HIV virulence but lower transmission potential.
Doekes et al. (2017)	Evolution	How does latent reservoir of infected CD4+ T cells affect the types of strains of HIV that will evolve within and between hosts?	Integro-differential equations with delay	Strain-specific infectivity rate between hosts depends on frequency of strain in actively infected CD4+ T cells within-host.	Relatively large latent reservoirs cause delay to within-host evolutionary processes, which select for moderately virulent strains that optimize transmission at the population level; with no reservoir, highly virulent strains are selected for within-host that do not optimize transmission at the population level.

Study	Topic	Objective	Implementation	Immunoepidemiological link	Inferences
Cuadros & García-Ramos (2012)	Co-infection	How does co-infection affect the HIV replication capacity?	Ordinary differential equations	Transmission rate between hosts depends on steady-state of viral load within host.	Impact of co-infection increases as average set-point viral load of population increases.
Yeghiazarian et al. (2013)	ART	How does the timing of antiretroviral therapy (ART) in individuals affect the spread of HIV?	Individual-based model	Transmission rate to each susceptible partner depends on viral load of infected individual.	Beginning ART during acute infection is most effective for reducing spread of HIV.
Shen et al. (2015)	ART	How does antiretroviral therapy (ART) affect HIV prevalence?	Partial differential equations	Transmission rate depends on saturated viral load within-host, and varies between stages of infection.	While ART decreases the viral load and infectiousness of each infected host, in certain cases, this can lead to higher spread of HIV throughout the population because these infected individuals live longer; HIV can still be controlled in these cases if drug effectiveness is high.
Sun et al. (2016)	ART	How does antiretroviral therapy (ART) affect HIV prevalence?	Individual-based model	Transmission rate to each susceptible partner depends on viral load of infected individual.	Initiating ART early causes lower transmission of HIV in population; however, when ART efficacy decreases with emergence of drug resistance, early treatment leads to higher HIV spread in the population because the prevalence of drug resistant strains increases rapidly.
Metzger et al. (2011)	TIPs	How does introduction of therapeutic interfering particles (TIPs) affect HIV prevalence?	Ordinary differential equations	Transmission rate between hosts depends on steady-states of TIP and HIV viral loads within-host.	Deploying TIPs in even small numbers of infected individuals reduces the prevalence of HIV to low levels due to TIPs' ability to transmit between hosts and target high-risk groups; using TIPs reduces challenges of antiretroviral therapy and vaccines, and complements them.

Table 2: HIV infection with single strain.

Within-host layer of HIV multi-scale model with assumption of single strain HIV infection. The uninfected CD4+ T cells get infected by the free virions and produce HIV virus. CD4+ T cells have the constant reproduction and death rates. HIV induces death rate of infected cells. HIV population increases by production of virus by infected cells, and decreases because of the virus clearance and shedding rate.

Model diagram

Equations

$$\frac{dT}{d\tau} = \lambda - kTV - dT$$

$$\frac{dT^*}{d\tau} = kTV - (\mu + d)T^*$$

$$\frac{dV}{d\tau} = N(\mu + d)T^* - (c + s)V - kTV$$

Parameters

λ	Reproduction rate of uninfected cells
k	Infection rate of uninfected cells
d	Natural death rate of uninfected cells
μ	HIV induced death rate of infected cells
N	HIV production by infected cells
s	Shedding rate of virus
c	HIV clearance rate

Table 2: **HIV infection with single strain.** Within-host layer of HIV multi-scale model with assumption of single strain HIV infection. The uninfected CD4+ T cells get infected by the free virions and produce HIV virus. CD4+ T cells have the constant reproduction and death rates. HIV induces death rate of infected cells. HIV population increases by production of virus by infected cells, and decreases because of the virus clearance and shedding rate.

Table 3: HIV super-infection.

The within-host layer of HIV multi-scale model illustrates the impact of infection with multiple strains of HIV. This model includes the uninfected, infected target CD4+ T cells with different strains, and different strains of free HIV virions. An individual may get infected with drug-resistant and/or drug-susceptible strains. Also, mutations may happen within-host leading to emergence of drug-resistant strains.

Model diagram

λ

| CD4+ T cells (T) | $k_i TV_i$ | Infected CD4+ T cells with strain i (T_i) |

dT $(\mu_i + d)T_i$

HIV strain i (V_i) $N_i(\mu_i + d)T_i$

$(c + s_i)V_i$

Equations

$$\frac{dT}{d\tau} = \lambda - k_i TV_i - dT$$

$$\frac{dT_i}{d\tau} = k_i TV_i - (\mu_i + d)T_i$$

$$\frac{dV_i}{d\tau} = N_i(\mu_i + d)T_i - (c + s_i)V_i - k_i TV_i$$

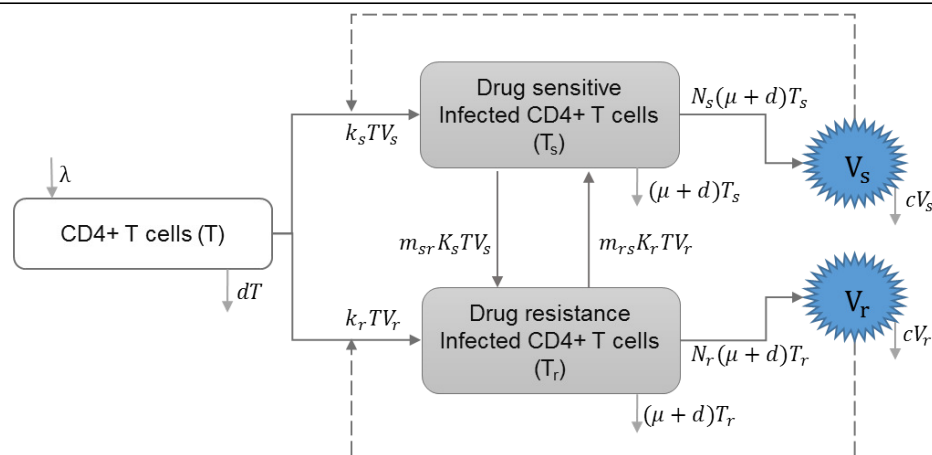
Parameters

λ	Reproduction rate of uninfected cells
k_i	Infection rate of uninfected cells by virus strain i
μ_i	HIV induced death rate of infected cell with strain i
N_i	HIV Production of virus i by infected cells
s_i	Shedding rate of virus strain i
d	Natural death rate of uninfected cells
c	HIV clearance rate

Table 3: **HIV super-infection.** The within-host layer of HIV multi-scale model illustrates the impact of infection with multiple strains of HIV. This model includes the uninfected, infected target CD4+ T cells with different strains, and different strains of free HIV virions. An individual may get infected with drug-resistant and/or drug-susceptible strains. Also, mutations may happen within-host leading to emergence of drug-resistant strains.

Table 4: HIV drug resistance.

The within-host layer of HIV multi-scale model illustrates the uninfected and infected target CD4+ T cells, including drug-sensitive and drug-resistant strains. Mutations from drug-sensitive to drug-resistant or drug-resistant to drug-sensitive strains are studied in this model, and the impact of treatment is also included.

Model diagram

Equations

$$\frac{dT}{d\tau} = \lambda - (1 - \epsilon_{rt})k_s T V_s - (1 - p_{rt}\epsilon_{rt})k_r T V_r - dT$$

$$\frac{dT_s}{d\tau} = (1 - m_{sr})(1 - \epsilon_{rt})k_s T V_s + m_{rs}(1 - p_{rt}\epsilon_{rt})k_r T V_r - (\mu + d)T_s$$

$$\frac{dT_r}{d\tau} = m_{sr}(1 - \epsilon_{rt})k_s T V_s + (1 - m_{rs})(1 - p_{rt}\epsilon_{rt})k_r T V_r - (\mu + d)T_r$$

$$\frac{dV_s}{d\tau} = (1 - \epsilon_{pi})N_s(\mu + d)T_s - cV_s$$

$$\frac{dV_r}{d\tau} = (1 - p_{pi}\epsilon_{pi})N_r(\mu + d)T_r - cV_r$$

Parameters

λ	Reproduction rate of uninfected cells
k_s	infection rate of uninfected cells by drug-sensitive strain
k_r	infection rate of uninfected cells by drug-resistant strain
d	Natural death rate of uninfected cells
μ	HIV induced death rate of infected cells
c	HIV clearance rate
ϵ_{rt}	Efficacy of reverse transcriptase inhibitor treatment
ϵ_{pi}	Efficacy of protease inhibitor treatment
V_s	Drug sensitive strain of HIV
V_r	Drug resistant strain of HIV
m_{sr}	A proportion of infected cells with drug-sensitive strain that produce drug resistant virions
m_{rs}	A proportion of infected cell with drug-resistant strain that produce drug sensitive virions
p_{rt}	Relative rate of reverse transcriptase inhibitor efficacy for drug resistant strain
p_{pi}	Relative rate of protease inhibitor efficacy for drug resistant strain
N_s	Reproduction of HIV virus by drug-sensitive strain
N_r	Reproduction of HIV virus by drug-resistant strain

Table 4: **HIV drug resistance.** The within-host layer of HIV multi-scale model illustrates the uninfected and infected target CD4+ T cells, including drug-sensitive and drug-resistant strains. Mutations from drug-sensitive to drug-resistant or drug-resistant to drug-sensitive strains are studied in this model, and the impact of treatment is also included.

Table 5: HIV co-infection.

The within-host layer of HIV multi-scale model illustrates the impact of co-infection. This model includes the uninfected and infected target CD4+ T cells, and free virions. Co-infection increases immune response and the infection rate of immune cells. Therefore, the set-point viral load is higher compared to the case of no co-infection.

Model diagram

Equations

$$\frac{dT}{d\tau} = \lambda - kTV - dT + \left[1 - \frac{T_m + T + T^*}{T_{max}}\right]r_T T$$

$$\frac{dT^*}{d\tau} = kTV - (\mu + d)T^* + k_{Tm}VT_m$$

$$\frac{dV}{d\tau} = N(\mu + d)T^* - cV$$

Parameters

λ	Reproduction rate of uninfected cells
k	Infection rate of uninfected cells
d	Natural death rate of uninfected cells
μ	HIV induced death rate of infected cells
N	HIV production by infected cells
c	HIV clearance rate
T_m	Activated immune cells against co-infection
T_{max}	Maximum number of immune cells
r_T	Growth rate of non-specific immune cells
k_{Tm}	Infection rate of co-infection

Table 5: **HIV co-infection.** The within-host layer of HIV multi-scale model illustrates the impact of co-infection. This model includes the uninfected and infected target CD4+ T cells, and free virions. Co-infection increases immune response and the infection rate of immune cells. Therefore, the set-point viral load is higher compared to the case of no co-infection.

Table 6: Susceptible-Infected (*S I*) epidemic model.

The between-host layer of HIV multi-scale model illustrates the random mixing of susceptibles and infected individuals. Susceptibles get infected by the infected individuals. HIV transmission rate depends on the HIV viral load at the within-host scale.

Model diagram

Equations

$$\frac{dS}{dt} = b - \beta S I - \delta S$$

$$\frac{dI}{dt} = \beta S I - (\alpha + \delta)I$$

Parameters

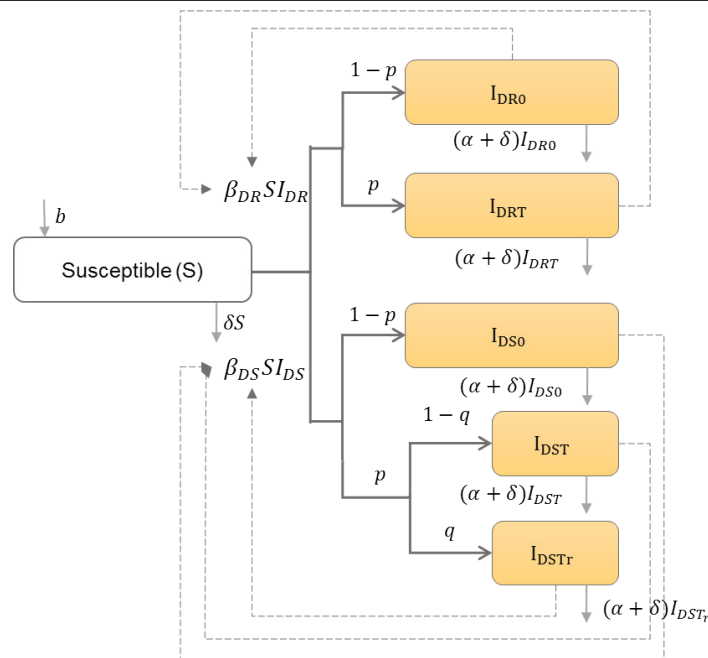
S	Number of individuals in the susceptible class
I	Number of individuals in the infected class
b	Natural birth rate in the population
β	HIV transmission rate in the population
α	Disease induced mortality rate
δ	Natural death rate in the population

Table 6: **Susceptible-Infected ($S I$) epidemic model.** The between-host layer of HIV multi-scale model illustrates the random mixing of susceptibles and infected individuals. Susceptibles get infected by the infected individuals. HIV transmission rate (β) depends on the HIV viral load at the within-host scale.

Table 7 **(on next page)**

Table 7: HIV drug resistance and treatment impact.

HIV transmission dynamics between drug-sensitive and drug-resistant infected individuals are illustrated. Infected individuals may get infected by the drug-sensitive or drug-resistant strains. A proportion p of infected individuals get treatment, and among the infected individuals with drug-sensitive strains, a proportion q of them develop drug resistance.

Model diagram

Equations

$$\frac{dS}{dt} = b - \beta_{DR} S I_{DR} - \beta_{DS} S I_{DS} - \delta S$$

$$\frac{dI_{DR0}}{dt} = (1-p)\beta_{DR} S I_{DR} - (\alpha + \delta)I_{DR0}$$

$$\frac{dI_{DRT}}{dt} = p\beta_{DR} S I_{DR} - (\alpha + \delta)I_{DRT}$$

$$\frac{dI_{DS0}}{dt} = (1-p)\beta_{DS} S I_{DS} - (\alpha + \delta)I_{DS0}$$

$$\frac{dI_{DST}}{dt} = p(1-q)\beta_{DS} S I_{DS} - (\alpha + \delta)I_{DST}$$

$$\frac{dI_{DSTr}}{dt} = pq\beta_{DS} S I_{DS} - (\alpha + \delta)I_{DSTr}$$

Parameters

b	Natural birth rate in the population
I_{DR0}	Number of individuals infected with drug-resistant strain and do not receive treatment
I_{DRT}	Number of individuals infected with drug-resistant strain and receive treatment
I_{DS0}	Number of individuals infected with drug-sensitive strain and do not receive treatment
I_{DST}	Number of individuals infected with drug-sensitive strain and receive treatment
I_{DSTr}	Number of individuals infected with drug-sensitive strain, receive treatment, and develop resistance
β_{DR}	Drug-resistant HIV transmission rate in the population
β_{DS}	Drug-sensitive HIV transmission rate in the population
α	HIV induced mortality rate
δ	Natural death rate in the population
p	Proportion of infected individuals who receive treatment
q	Proportion of infected individuals who receive treatment and develop resistance
I_{DR}	$I_{DR0} + I_{DRT}$
I_{DS}	$I_{DS0} + I_{DST} + I_{DSTr}$

Table 7: **HIV drug resistance and treatment impact.** HIV transmission dynamics between drug-sensitive and drug-resistant infected individuals are illustrated. Infected individuals may get infected by the drug-sensitive or drug-resistant strains. A proportion p of infected individuals get treatment, and among the infected individuals with drug-sensitive strains, a proportion q of them develop drug resistance.

Table 8: HIV evolution.

HIV transmission dynamics between infected individuals with different strains are illustrated. Infected individuals with strains i may get infected with another strain j and transmit the dominant strain of HIV.

Model diagram

Equations

$$S(t) \quad = b - \sum_{i=1}^{n} \int_0^{T_i} H_i(t - \tau)e^{-\delta\tau}d\tau$$

$$I_i(t) \quad = \int_0^{T_i} H_i(t - \tau)e^{-\delta\tau}d\tau - (\alpha + \delta)I_i$$

$$H_i(t) \quad = \frac{S(t)}{N(t)} \sum_{j=1}^{n} \int_0^{T_i} \beta_{ij}(\tau)H_j(t - \tau)e^{-\delta\tau}d\tau$$

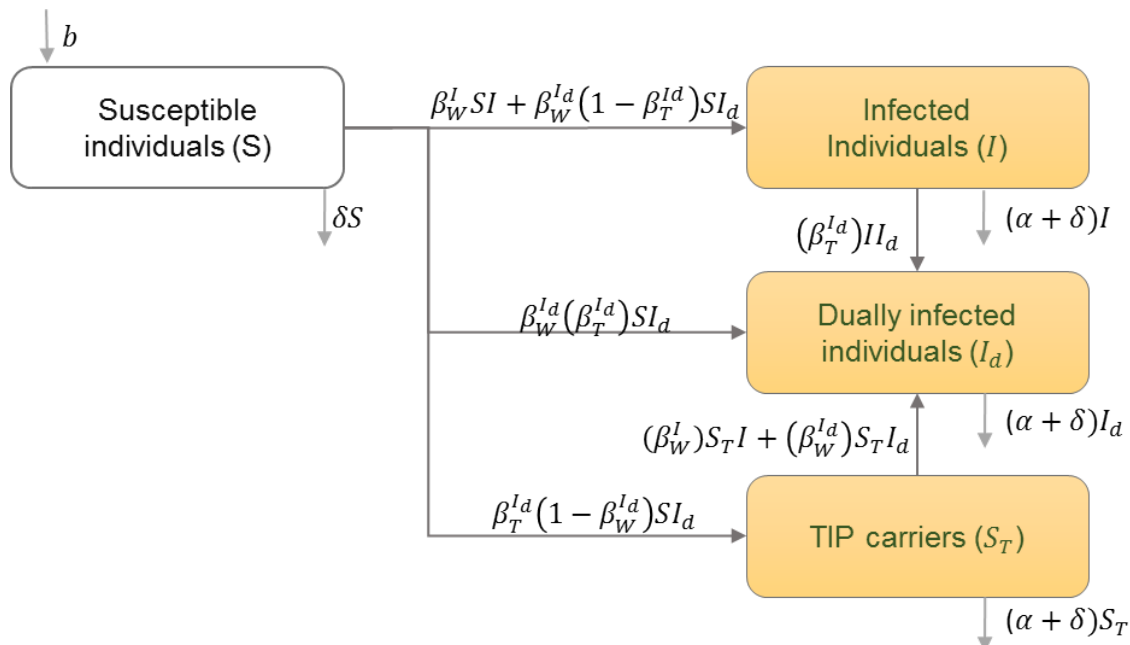
Parameters

b	Natural birth rate in the population
T_i	Time of death after initiation of infection
H_i	The rate at which new type-i infection occur
δ	Natural mortality rate
I_i	Number of individuals infected with strain i
β_{ij}	Infectivity of strain i in a host originally infected with strain j at time τ since infection.

Table 8: **HIV evolution.** HIV transmission dynamics between infected individuals with different strains are illustrated. Infected individuals with strains i may get infected with another strain j and transmit the dominant strain of HIV.

Table 9: HIV and therapeutic interfering particles (TIPs).

HIV transmission dynamics between infected individuals with wild type of HIV and TIPs are illustrated. Individuals can get infected with wild type of HIV, TIPS, or both. Infected individuals can get reinfected with both types.

Model diagram

Equations

$$\frac{dS}{dt} = b - \beta_W^I SI - \beta_W^{I_d}(1 - \beta_T^{I_d})SI_d - \beta_W^{I_d}\beta_T^{I_d}SI_d - \beta_T^{I_d}(1 - \beta_W^{I_d})SI_d - \delta S$$

$$\frac{dI}{dt} = \beta_W^I SI + \beta_W^{I_d}(1 - \beta_T^{I_d})SI_d - \beta_T^{I_d}II_d - (\alpha + \delta)I$$

$$\frac{dI_d}{dt} = \beta_W^{I_d}\beta_T^{I_d}SI_d + \beta_W^I S_T I + \beta_W^{I_d}S_T I_d + \beta_T^{I_d}II_d - (\alpha + \delta)I_d$$

$$\frac{dS_T}{dt} = \beta_T^{I_d}(1 - \beta_W^{I_d})SI_d - \beta_W^I S_T I - \beta_W^{I_d}S_T I_d - (\alpha + \delta)S_T$$

Parameters

b Natural birth rate in the population
I Number of infected individuals with only the wild type of HIV
I_d Individuals infected with both HIV and TIPs
S_T Individuals infected with only TIPs
β_W^I Transmission rate of wild type HIV from HIV infected individuals
$\beta_W^{I_d}$ Transmission rate of wild type HIV from dually infected individuals
$\beta_T^{I_d}$ Transmission rate of TIPs from dually infected individuals

Table 9: **HIV and therapeutic interfering particles (TIPs).** HIV transmission dynamics between infected individuals with wild type of HIV and TIPs are illustrated. Individuals can get infected with wild type of HIV, TIPS, or both. Infected individuals can get reinfected with both types.

Table 10: Coupling mechanism of within-host and between-host scales of HIV dynamics.

The within-host and between-host layers of HIV multi-scale model are linked using partial differential equations. The HIV viral immune dynamics model (see Table 2) determines the time-varying within-host viral load, which impacts the transmission rate. Another method to determine the HIV transmission rate is based on the viral load equilibrium.

	Equations
$\frac{dS}{dt}$	$= b - S \int_0^\infty \beta(\tau)I(\tau,t)d\tau - \delta S$
$\frac{\partial I}{\partial t} + \frac{\partial I}{\partial \tau}$	$= -m(V(\tau))I(\tau,t)$
$I(0,t)$	$= S \int_0^\infty \beta(\tau)I(\tau,t)d\tau$
	Parameters
S	Number of individuals in the susceptible class
$I(\tau,t)$	Number of infected individuals structured by time since infection (τ)
b	Natural birth rate in the population
$\beta(\tau)$	HIV transmission rate ($r.V(\tau)$)
m	Coefficient on dependence of induced mortality due to disease on the host viral load.

Table 10: **Coupling mechanism of within-host and between-host scales of HIV dynamics.** The within-host and between-host layers of HIV multi-scale model are linked using partial differential equations. The HIV viral immune dynamics model (see Table 2) determines the time-varying within-host viral load, which impacts the transmission rate ($\beta(\tau) = r.V(\tau)$; r is a constant coefficient). Another method to determine the HIV transmission rate is based on the viral load equilibrium.

Table 11: Clinical and public health relevant problems of HIV dynamics.

Clinical and public health relevant problems of HIV dynamics that can be potentially addressed using multi-scale models.

- How does the time-varying viral load and shedding rate since HIV infection impact the transmission rate between hosts?

- How does co-infection among HIV-infected individuals impact the HIV dynamics in the population?

- How does super-infection of multiple HIV strains among infected individuals impact the HIV dynamics in the population?

- How does within-host mutations of drug-sensitive and drug-resistant strains impact the HIV evolution in the population?

- How does timing of treatment initiation among infected individuals impact the HIV dynamics in the population?

- How does treatment compliance and interruption behavior of HIV-positive individuals impact HIV dynamics in the population?

- What is the impact of pre-exposure prophylaxis of high-risk HIV-negative individuals on HIV dynamics in the population?

- How can multi-scale HIV models be verified and validated with empirical data?

- How can the optimal layers from micro-biological (genomic, molecular, cellular, organ) to macro-social (individual, family, community, national, global) levels for multi-scale models of HIV dynamics be selected appropriately?

Table 11: **Clinical and public health relevant problems of HIV dynamics.** Clinical and public health relevant problems of HIV dynamics that can be potentially addressed using multi-scale models.