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I commend the authors for their extensive data set, compiled over many years of detailed fieldwork. In addition, the manuscript is clearly written in professional, unambiguous language. If there is a weakness, it is in the statistical analysis (as I have noted above) which should be improved upon before Acceptance.

Coral geometry and why it matters

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Clonal organisms like reef building corals exhibit a wide variety of colony morphologies and geometric shapes which can have many physiological and ecological implications. Colony geometry can dictate the relationship between dimensions of volume, surface area, and length, and their associated growth parameters. For calcifying organisms, there is the added dimension of two distinct ~~material~~ components of growth: biomass production and calcification. For reef building coral, basic geometric shapes can be used to model the inherent mathematical relationships between various growth parameters and how colony geometry determines which relationships are size-dependent or size-independent. Traditionally assumed to be size-independent, linear extension rates can vary as a function of colony size by virtue of its geometry (even with a constant calcification rate). Whether the ratio between mass and surface area remains constant or changes with colony size is the determining factor. For some geometric shapes, the coupling of biomass production (proportional to surface area productivity) and calcification (proportional to volume) can cause one aspect of growth to geometrically constrain the other. The nature of this relationship contributes to a species' life history strategy and has important ecological implications. At one extreme, thin diameter branching corals can maximize growth in surface area and resource acquisition potential, but this geometry requires high biomass production to cover the fast growth in surface area. At the other extreme, growth in large, hemispheroidal corals can be constrained by calcification. These corals grow surface area relatively slowly and may retain a surplus capacity for biomass production which can be allocated towards other anabolic processes. For hemispheroidal corals, the rate of surface area growth rapidly decreases as colony size increases. This ontogenetic relationship underlies the success of microfragmentation used to accelerate restoration of coral cover. However, ontogenetic changes in surface area productivity only applies to certain coral geometries where surface area to volume ratios rapidly decrease with colony size.

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Abstract

Clonal organisms like reef building corals exhibit a wide variety of colony morphologies and geometric shapes which can have many physiological and ecological implications. Colony geometry can dictate the relationship between dimensions of volume, surface area, and length, and their associated growth parameters. For calcifying organisms, there is the added dimension of two distinct material components of growth: biomass production and calcification. For reef building coral, basic geometric shapes can be used to model the inherent mathematical relationships between various growth parameters and how colony geometry determines which relationships are size-dependent or size-independent. Traditionally assumed to be size-independent, linear extension rates can vary as a function of colony size by virtue of its geometry (even with a constant calcification rate). Whether the ratio between mass and surface area remains constant or changes with colony size is the determining factor. For some geometric shapes, the coupling of biomass production (proportional to surface area productivity) and calcification (proportional to volume) can cause one aspect of growth to geometrically constrain the other. The nature of this relationship contributes to a species' life history strategy and has important ecological implications. At one extreme, thin diameter branching corals can maximize growth in surface area and resource acquisition potential, but this geometry requires high biomass production to cover the fast growth in surface area. At the other extreme, growth in large, hemispheroidal corals can be constrained by calcification. These corals grow surface area relatively slowly and may retain a surplus capacity for biomass production which can be allocated towards other anabolic processes. For hemispheroidal corals, the rate of surface area growth rapidly decreases as colony size increases. This ontogenetic relationship underlies the success of microfragmentation used to accelerate restoration of coral cover. However,

ontogenetic changes in surface area productivity only applies to certain coral geometries where surface area to volume ratios rapidly decrease with colony size.

Introduction

The colony morphology of clonal organisms varies widely between and within taxa and has many physiological and ecological implications associated with adaptation to environmental conditions (Jackson 1979). For reef building corals, colony morphology has many physiological and ecological implications associated with adaptation to environmental conditions including light, hydrodynamic regime, sedimentation, and subaerial exposure (Jackson 1979; Chappell 1980). While many coral species exhibit morphological phenotypic plasticity in response to environmental conditions, their general colony shape is often conserved and can be characteristic within a taxon (reviewed in Todd 2008; Zawada et al. 2019). Coral colony morphology can dictate a coral's internal light regime (e.g., Anthony et al. 2005; Kaniewska et al. 2008, 2014), hydrodynamics and mass transfer (e.g., Hossain and Staples 2019, 2020), and exposure to peripheral processes (Meeters et al. 1997; George et al. 2021). The general geometric shape of a colony can also dictate and constrain the quantitative relationships between various growth parameters which can have additional ecological implications. For corals, these common growth measurements included linear extension rates (length per unit time), areal growth rate (area per unit time), and calcification rate (mass per unit area per unit time) where calcification (G) is related to volume growth rate via average density ($M=\rho V$, where M is mass, V is volume, and ρ is mean density) (Pratchett et al. 2015).

For all calcifying organisms including reef building corals, there are two distinct components of growth/production: (1) organic or tissue biomass/biovolume and (2) inorganic or calcium carbonate skeleton (although there is a small fractional component of organic matter in coral skeletons) (DeCarlo et al. 2018). Each aspect of growth requires their own set of elemental resources which have characteristically different levels of availability depending on the habitat. For organisms like reef building corals (and coralline algae and sclerosponges), the growth in biomass (i.e., production) is proportional to growth in surface area (Anthony et al. 2002) while the growth in skeleton mass (i.e., calcification) is proportional to volume (via density). Therefore, biomass production is directly related surface area growth. In contrast, skeletal mass is proportional to volume (assuming a constant mean density), so a constant calcification rate leads to a constant volume growth rate (per unit surface area). The relationship between these two aspects of growth can be influenced by coral geometry may cause one aspect of growth to "geometrically" constrain the other which has important implications for life strategies.

For some geometric shapes, the surface area to volume ratio changes with size (Porter 1976) potentially causing ontogenetic changes in the ratio of biomass production to calcification and in the relationship between growth parameters causing them to size-dependent. One of the most common metrics of coral growth across all morphologies is linear extension rate due in part to the relative ease in which it can be measured and used for comparative purposes (reviewed in Pratchett et al. 2015). Linear extensions rates are generally assumed to be characteristics of a

species, independent of size (e.g., Hughes and Jackson 1985; Kinzie and Sarmiento 1986), and often used as a foundation of the census-based approach to calculate calcium carbonate reef budgets (e.g., Januchowski-Hartley et al. 2017; Perry et al. 2018, 2019; Molina-Hernandez et al. 2020; Cornwall et al. 2021). Changes in linear extensions rates are often interpreted as an environmental signal (e.g., Carricart-Ganivet et al. 2011). However, even with a constant calcification rate, linear extension rates can be colony size-dependent due to the dynamics of surface area to volume ratio which is dictated by the geometry of a coral colony (e.g., Kahng et al. 2023). Therefore, the relationship between linear extension rate and colony size for various geometric shapes is important to quantify and understand.

Recent reports have investigated the question whether coral growth is isometric by virtue of the colonial modular design or subject to allometric constraints like non-clonal metazoans (Edmunds 2006; Dornelas et al. 2017; Madin et al. 2020; Carlot et al. 2022; Medellín-Maldonado et al. 2022). If growth is allometric with an ontogenetic decrease in growth rate, there may be important implications for ecosystem function based on the reduction of age/size distributions of coral communities from mass mortality events during the Anthropocene (Dietzel et al. 2020; Carlot et al. 2021). While environmental factors in the form of spatial constraints, competition, or partial mortality due to stress or senescence obviously influence these growth parameters (Barnes 1973; Edmunds 2006), the inherent geometric relationships between growth parameters must be clarified to be able to quantitatively reconcile the different metrics of coral growth which are regularly measured using different techniques under a variety of conditions (Pratchett et al. 2015).

In this study, four common reef building coral morphologies are modeled using geometric shapes to illustrate the inherent mathematical relationships between various growth parameters and demonstrate how colony geometry can characteristically alter whether relationships are size-dependent or size-independent. Using previously published empirical values, the geometry-dependent relationships between organic (biomass production) and inorganic (calcification) growth are investigated, and the associated ecological implications are discussed.

Materials & Methods

To demonstrate the inherent mathematical relationships between various coral growth parameters, four geometric shapes were used to model how a constant calcification rate per unit area (G) affects linear extension rate (C) across time, change in surface area (ΔS), change in planar area (ΔP), and change in volume (ΔV). Surface area productivity ($SAP = \Delta S/S$) and planar area productivity ($PAP = \Delta P/S$) were calculated to demonstrate how quickly a coral generates area (per unit area) across time.

- Hemispheroids across the full range of eccentricity values (oblate, circular, prolate)
- Flat discs with constant thickness
- Branching corals with constant branch diameters (cylinder model)
- Conical branch/colony with constant aspect ratio (α = height/basal radius)



Size dependent relationships were illustrated by calculating parameters as a function of size (e.g., radius, thickness, length, or height). Average or common empirical values for G and density (ρ) were used from the literature for the various species modeled. To illustrate the effects of geometry independent of G and ρ values, SAP was calculated for all shapes using the same values for G and ρ . For this modeling exercise, favorable growth conditions were assumed with no partial mortality or spatial constraints on growth.

A hemispheroid shape was used to model the relationships between these parameters for massive corals (e.g., *Porites* spp.). The effect of the eccentricity (e) was calculated across the full range of possible values from oblate (flattened) to circular to prolate (tall) hemispheroids. For a circular hemisphere ($e=0$), the calcification rate ($G = \frac{\Delta V \rho}{S_t}$) and volume ($V = \frac{2}{3}\pi r^3$) equations were used to solve for extension rate ($C_t = r_{t+1} - r_t$). To calculate SAP ($\frac{\Delta S}{S_t} = \frac{S_{t+1} - S_t}{S_t}$), the calcification equations was solved for r_{t+1} and substituted into the equation where surface area $S_t = 2\pi r^2$. PAP ($\frac{\Delta P}{S_t} = \frac{P_{t+1} - P_t}{S_t}$) was solved using the equation for planar area ($P = \pi a^2$).

For a prolate hemispheroid with a circular base ($a=b$), the polar radius is larger than the equatorial radius ($c>a$), where c is the polar radius and a and b are the equatorial radii in the two horizontal dimensions. The surface area ($S = \pi a^2 + \frac{\pi a c}{e} \sin^{-1} e$) and volume ($V = \frac{2}{3}\pi a^2 c$) equations were used to solve for SAP using the definition for eccentricity ($e = \sqrt{1 - \frac{a^2}{c^2}}$), where $c>a$. PAP ($\frac{\Delta P}{S_t}$) was solved using the equation for planar area ($P = \pi a^2$). For an oblate hemispheroid with a circular base ($a=b$), the polar radius is less than the equatorial radius ($c<a$). The surface area ($S = \pi a^2 + \frac{\pi c^2}{2e} \ln \left(\frac{1+e}{1-e} \right)$) and volume ($V = \frac{2}{3}\pi a^2 c$) equations were used to solve for SAP using the definition for eccentricity ($e = \sqrt{1 - \frac{c^2}{a^2}}$), where $c<a$. PAP ($\frac{\Delta P}{S_t}$) was solved using the equation for planar area ($P = \pi a^2$). For graphing purposes, oblate eccentricity was denoted as negative values to distinguish it from prolate eccentricity. The effects of eccentricity and size (equatorial radius) on SAP and PAP were calculated.

A flat circular disk with radius (r) and height/thickness (h) was used to model plate-like corals such as those common in the lower photic zone (i.e., *Leptoseris* spp. and *Agaricia* spp.) (Kahng et al. 2019; Tamir et al. 2019; Gijsbers et al. 2022). The calcification rate ($G = \frac{\Delta V \rho}{S_t}$) and volume ($V = h\pi r^2$) equations were used to solve for extension rate ($C_t = r_{t+1} - r_t$). To calculate surface area productivity or SAP ($\frac{\Delta S}{S_t} = \frac{S_{t+1} - S_t}{S_t}$), the calcification equations was solved for r_{t+1} and substituted into the equation where surface area $S = \pi r^2$. The effect of skeletal thickness (h) on SAP was calculated within the range of values empirical values reported (Kahng et al. 2020).

A cylinder was used to model branching corals with constant average branch radius (r), (e.g., some branching *Acropora* spp.). As the colony grows, the sum of all branch lengths or total branch length (h_t) can be used to calculate skeletal volume, independent of the number of branches (β_t) or average branch length (h_t/β_t). The surface area ($S_t = 2\pi r h_t + \pi r^2$) can be calculated from the side of the cylinder using total branch length. Since each new branch base covers the side of its parent branch, there is no net increase in surface area from each new branch tip, with the exception of the area of the very first branch tip (πr^2). In this model, the ratios between growth in volume ($\Delta V = \pi r^2 [h_{t+1} - h_t]$), surface area ($\Delta S = 2\pi r [h_{t+1} - h_t]$), and total linear extension rate ($C_t = [h_{t+1} - h_t]$) remain constant which is consistent with empirical growth data for *Acropora cervicornis* (Million et al. 2021). The calcification rate ($G = \frac{\Delta V \rho}{S_t}$) and volume ($V = h\pi r^2$) equations were used to solve for average branch extension rate ($\frac{C_t}{\beta_t}$), where $C_t = h_{t+1} - h_t$. To calculate surface area productivity or SAP ($\frac{\Delta S}{S_t} = \frac{S_{t+1} - S_t}{S_t}$), the calcification equations was solved for h_{t+1} and substituted into the equation where surface area. The effect of branch diameter ($2r$) on SAP was calculated within the range of empirical values reported in the literature.

A cone with a constant aspect ratio was used to model a single branch of branching corals with conical branches. Some branching corals have branches that mimic high aspect cones. This same model also applies to some massive corals form colonies that can mimic low aspect cones. A constant aspect ratio ($\alpha = h_t/r_t$) during growth was assumed, where h is branch length/height and r is radius. The calcification rate ($G = \frac{\Delta V \rho}{S_t}$) and volume ($V = \frac{1}{3} h \pi r^2 = \frac{\pi h^3}{3\alpha^2}$) equations were used to solve for extension rate ($C_t = h_{t+1} - h_t$). To calculate surface area productivity or SAP ($\frac{\Delta S}{S_t} = \frac{S_{t+1} - S_t}{S_t}$), the calcification equations was solved for h_{t+1} and substituted into the equation where surface area. The effects of aspect ratio and cone length/height on SAP was calculated.

Results

The derivations of the mathematical relationships for each geometric shape are illustrated in [Appendix A](#). Given a constant calcification rate (G) and density (ρ), the size-dependence of the linear extension rate (C_t) for the four geometric shapes depends on whether the surface area to volume ratio remains constant or changes as the coral colony grows in size ([Table 1](#)). For a circular hemispheroid, the size-dependent relationship between calcification rate and (radial) linear extension rate can be expressed $G = \frac{\Delta V \rho}{S_t} = \frac{\rho(3C_t r_1^2 + 3C_t^2 r_t + C_t^3)}{3r_t^2}$, so as the colony reaches a larger size ($r_t \rightarrow \infty$), $G \rightarrow \rho C_t$. Therefore, the linear extension rate increases to an asymptotic maximum value of $C_t \rightarrow \frac{G}{\rho}$ ([Figure 1](#)). For hemispheroids with nonzero eccentricity, the relationships quantitatively depart from the circular hemisphere (equatorial radial extension rate slower for prolate and faster for oblate) but the asymptotic pattern is qualitatively the same.

For a circular flat disc with constant thickness (h), the linear extension rate increases linearly with colony size (radius), $C_t = r_t \left(\sqrt{\frac{G}{\rho h}} + 1 - 1 \right)$ (Figure 1) and exponentially across time (Kahng et al. 2023).

For a cone with constant aspect ratio, the linear extension rate for height increases asymptotically, $C_t = \sqrt[3]{\frac{3G\sqrt{\alpha^2+1}}{\rho}} h_t^2 + h_t^3 - h_t$, where $C_t = h_{t+1} - h_t$. For high aspect cones (e.g., $\alpha > 4$), the linear extension rate will not approach the asymptotic maximum value $\left(C_t \rightarrow \frac{G\sqrt{\alpha^2+1}}{\rho} \right)$ until branch length/height become unrealistically long (e.g., $h > 50$ cm) (Figure 1). The linear extension rate for basal radius also increases asymptotically, $C_t = \sqrt[3]{\frac{3G\sqrt{\alpha^2+1}}{\rho\alpha}} r_t^2 + r_t^3 - r_t$, where $C_t = r_{t+1} - r_t$. For low aspect cones (e.g., $\alpha < 0.5$), the linear extension rate will approach the asymptotic maximum value $\left(C_t \rightarrow \frac{G\sqrt{\alpha^2+1}}{\rho\alpha} \right)$ at relatively low values (e.g., $h > 25$ cm) (Figure 1).

For a branching coral with cylindrical branches of constant diameter, the relationship between calcification rate and total linear extension rate for all branches can be expressed as $C_t = \frac{2Gh_t}{\rho r} + \frac{G}{\rho}$, where h_t is the total lengths of all branches combined. Dividing both sides by the number of branches β_t provides the average branch extension rate $\frac{C_t}{\beta_t} = \frac{2Gh_t}{\rho r\beta_t} + \frac{G}{\rho\beta_t}$, where $\frac{C_t}{\beta_t}$ is average branch extension rate and $\frac{h_t}{\beta_t}$ is average branch length. As the colony grows more branches (i.e., $\rho\beta_t \gg G$), the average branch extension rate decreases asymptotically to a value proportional to average branch length, $\frac{C_t}{\beta_t} \rightarrow \frac{2Gh_t}{\rho r\beta_t}$. The proportionality constant decreases with increasing branch diameter.

Given a constant calcification rate (G) and density (ρ), the size-dependence of the surface area productivity (SAP) also depends on whether the surface area to volume ratio remains constant or changes as the coral colony grows in size (Table 1). For hemispheroids with constant eccentricity (e), the equations for SAP are listed below:

- Circular hemisphere $\frac{\Delta S}{S_t} = \frac{\left(\frac{3Gr_t^2}{\rho} + r_t^3 \right)^{2/3}}{r_t^2} - 1$
- Prolate hemispheroid $\frac{\Delta S}{S_t} = \frac{\left(\left(a_t^3 + \frac{a_t^2 3G\sqrt{(1-e^2)}}{2\rho} \left(1 + \frac{\sin^{-1}e}{e\sqrt{(1-e^2)}} \right) \right) \right)^{2/3}}{a_t^2} - 1$
- Oblate hemispheroid $\frac{\Delta S}{S_t} = a_t^{-2} \left(a_t^3 + \frac{3Ga_t^2 \left(1 + \frac{(1-e^2)}{2e} \ln \left(\frac{1+e}{1-e} \right) \right)}{2\rho\sqrt{1-e^2}} \right)^{2/3} - 1$

Using average G and ρ values for massive *Porites* (Lough and Barnes 2000; Lough 2008; Lough and Cantin 2014; Lough et al. 2016) were used to calculate SAP as a function of colony size (equatorial radius) and eccentricity (Figure 2). Flatter hemispheroids (i.e., larger c/a ratio)

have higher SAP than taller ones. For all hemispheroids, SAP quickly declines asymptotically with increasing size as a coral colony grows.

For a cone with constant aspect ratio, SAP is a size dependent and decreases asymptotically with increasing size in a manner analogous to hemispheroids,

$$\frac{\Delta S}{S_t} = \left(\frac{3G\alpha\sqrt{1+\frac{1}{\alpha^2}}}{\rho h_t} + 1 \right)^{2/3} - 1. \text{ Using average } G \text{ and } \rho \text{ values for branching } \textit{Acropora} \text{ (Hughes}$$

1987; Morgan and Kench 2012; Pratchett et al. 2015), the SAP for a single conical branch was calculated as a function of branch length and aspect ratio (Figure 3). Aspect ratio is positively correlated with SAP.

For a branching coral with cylindrical branches, SAP is a size independent and a function of calcification rate and branch radius/diameter (r), $\frac{\Delta S}{S_t} = \frac{2G}{\rho r}$. SAP declines with increasing branch thickness. Using average G and ρ values for branching *Acropora* spp. (Hughes 1987; Morgan and Kench 2012; Pratchett et al. 2015), the SAP was calculated as a function of branch thickness (Figure 4).

For a flat circular disc, SAP is a size independent and is a function of calcification rate and thickness (h), $\frac{\Delta S}{S_t} = \frac{G}{\rho h}$. Thinner colonies have a higher SAP. Using average G and ρ values for deep-water *Leptoseris* spp. from 70-111 m (Kahng et al. 2023), the SAP was calculated as a function of average skeletal thickness (Figure 5).

To isolate impact of geometry alone, SAP was calculated using equivalent values for G and ρ for the contrasting shapes (Figure 6). Flat, thin plate-like shapes have the highest SAP which is equivalent to planar area productivity (PAP) by virtue of their horizontal orientation. Cylindrical branching corals with small branch diameters also exhibit high SAP, especially in comparison to their massive coral counterparts (hemispheroids and low aspect cones) which have very low SAP as they reach larger size.

Discussion

Linear extension rates

Depending on coral colony morphology, inherent mathematical relationships determine which geometries can be expected to have constant (or near constant) linear extension rate (C_t) or size-dependent C_t which changes across time. In general, the stability of the quantitative relationship between calcification rate and linear extension rate depends on the surface area to volume ratio as the colony grows in size. Given a constant calcification rate, linear extension rate ~~to be~~ expected to be nearly constant for large hemispheroid coral colonies (e.g., radius >25 cm) and large branching coral colonies (e.g., >20 branches) with constant branch thickness and average branch length. However, when these colonies are small, decreases in the surface area to volume ratios are significant, so both radial extension rates of hemispheroidal corals and average branch extension rate for branching corals can be expected to decrease significantly during initial

growth (if calcification rate remains constant). Given an equivalent calcification rate and branch diameter, longer average branch lengths cause faster average branch linear extension rates. Similarly, thicker branch diameters cause slower average branch linear extension rates.

For conical shaped colonies with a constant calcification rate and aspect ratio (α), linear extension rates for both the height/length and the basal radius will decrease asymptotically with increasing height/length or radius respectively. For high aspect cones (e.g., $\alpha > 4$) like those of some branching corals, the natural lengths of conical branches are short relative to the values needed to approach the maximum extension rates. For low aspect cones (e.g., $\alpha < 0.5$) like some flattened morphologies of massive corals, the basal radius extension rates will approach the maximum values quickly relative to the size and longevity of these corals.

For disc-like colonies with constant calcification rate and mean thickness (h), radial extension rate can be expected to increase throughout the life of the colony linearly with colony size (radius) and exponentially across time (Kahng et al. 2023).

While the actual morphology of coral taxa may deviate considerably from these simple geometric shapes, the key factor which determines whether linear extension rates have a size dependent geometry is whether the ratio of mass (ρV) to surface area changes or remains constant as the colony grows and therefore, whether average density (ρ) remains constant. For massive *Porites* spp., skeletal density varies seasonally on a regular basis, but average density across longer timescales is more stable (Lough et al. 1990, 1992). A small ontogenetic decrease in density (i.e., 4% per 100 yrs) has been reported (Lough 2008). Within a colony, variations in skeletal density across time are generally less than 10% of mean values and several times lower than the percentage variation in calcification and extension rates (Lough and Barnes 2000; Razak et al. 2019). While calcification rate and extension rate correlate with each other, calcification rate does not correlate with density (Lough and Barnes 2000; Lough et al. 2016). With the recent advancements in 3D photogrammetry (e.g., Million et al. 2021) the mass to surface area ratio can be measured empirically for coral taxa that do not conform to a simple geometric shape. Likewise, the stability of skeletal density across time can also be measured empirically (e.g., via x-radiography and computerized tomography).

Because calcification rates for a given coral colony can vary considerably across time, the ontogenetic, size-dependent geometric effects on linear extension rate can be overshadowed. Significant interannual variability (e.g., ± 25 -50% of long-term mean) is commonly reported from retrospective analyses of massive corals (e.g., Kourandeh et al. 2018; Razak et al. 2019; Courtney et al. 2020; etc.). These temporal changes in calcification rate are associated with a variety of biotic and abiotic environmental factors. For hemispheroids and conical massive corals, the asymptotic maximum linear extension rates are directly proportional to calcification rate. For a flat circular disc, linear extension rates are directly proportional size (i.e., radius) and to (roughly) the square root of calcification rate, so size can have an exponentially larger impact.

Whether a particular growth metric is naturally isometric or allometric depends on both the individual metric and the colony geometry. Of course, the environmental history of each coral has a dominant effect on *in situ* net growth generating wide variability between conspecifics

across time (e.g., Madin et al. 2020). Nonetheless, the character (whether isometric/allometric) of one growth metric can be characteristically different than another due to their inherent mathematical relationship dictated by colony geometry. Likewise, the same growth metric may differ characteristically between coral taxa with contrasting geometries.

Organic and inorganic production

For all calcifying organisms, both biomass production and calcification are required for growth. While both require energy, each aspect of growth has different elemental resource requirements, and the availability of these elemental resources can vary significantly by habitat and depth. In oligotrophic waters associated with shallow coral reef ecosystems, the limiting elemental resources for coral biomass production are typically macronutrients like bioavailable nitrogen or soluble reactive phosphorus (Atkinson and Falter 2003; Karl and Church 2017). This limitation of essential macronutrients often results in a surplus and subsequent excretion of organic carbon production (i.e., photosynthate) in well-lit habitats (reviewed in Goldberg 2018). In contrast, the elemental resources for calcification (calcium ions and carbonate alkalinity) are generally not limiting in surface seawater (at normal pH) in tropical habitats. In clear, oligotrophic waters, the depth of the lower photic zone can coincide with the nutricline (or interaction with the nutricline via inertial oscillations) causing inorganic macronutrients to be less limiting or even replete (Kahng et al. 2019). However, available light energy to drive photosynthesis eventually becomes limiting with increasing depth.

For reef building corals, coralline algae, and sclerosponges, tissue biomass is limited to a finite layer associated with surface area of their skeleton. This design generates a geometric relationship and potential constraint between the two aspects of growth (skeletal mass and tissue biomass). If average tissue thickness and composition remain constant, the tissue biomass can be expected to be proportional to surface area. Therefore, the surface area productivity (growth of new surface area per unit surface area per unit time) can be a useful metric that can be used as a quantitative proxy for ontogenetic changes in biomass productivity (as the colony grows) and how geometry can constrain it.

For calcifying organisms with an external skeleton (i.e., shelled molluscs), calcification can directly relate to the growth of internal volume available for biomass (e.g., Raup and Graus 1972; Graus 1974) generating the potential for an analogous geometric constraint. However, ocean acidification studies have demonstrated that reduced calcification can occur without reductions in somatic growth due to reductions in shell thickness and structural integrity (reviewed in Gazeau et al. 2013). Phenotypic plasticity in shell thickness relative to tissue biomass (reviewed in Watson et al. 2012) further suggests that despite the potential geometric relationship between organic and inorganic production, the two aspects of growth are readily decoupled.

Ecological Implications of SAP

For clonal organisms with indeterminate growth, resource acquisition (i.e., energy and elemental resources) can dictate growth rate assuming physiological costs per unit biomass

remains constant (Sebens 1987). Within a stable environment in the absence of stress, space limitations, and disturbance, coral resource acquisition can be expected to scale with tissue surface area exposed to light for autotrophy and ambient water for heterotrophy (whether via polyp feeding or direct assimilation) and mass transfer (Porter 1976; Sebens 2003; Monismith 2007). Therefore, under optimal conditions maximum rates of production normalized to surface area (i.e., calcification and growth in biomass) can be expected to be independent of colony size. However, depending on colony morphology, portions of a colony's surface area may be subject to self-shading and/or reduced water motion (e.g., feeding and mass transfer) causing reductions and spatial heterogeneity in productivity per unit area (e.g., McFadden 1986).

Corals with high SAP can increase their area and therefore resource acquisition capacity quickly to fuel fast growth (both tissue biomass and calcification) when resources are not limiting. However, their growth requires high biomass production to cover the quickly expanding surface area. Therefore, biomass production may limit growth more than calcification with the latter being constrained by the former. This potential constraint has implications for tissue thickness (or biomass reserves) and resilience. The ability of branching corals, especially with species thin branch diameters, to recover from tissue damage or loss without negatively impacting growth can be expected to be less robust than corals with lower SAP. Many branching corals are known to have relative thin tissue thickness (e.g., Loya et al. 2001). These geometry-based predictions are consistent with the life history traits of fast-growing branching corals (e.g., *Acropora* spp.) and implies that their susceptibility to disturbance such as bleaching-related mortality may be due in part to the inherent tradeoff associated with their geometry (Loya et al. 2001; McClannahan et al. 2007; Darling et al. 2012). Where studied, some corals exhibit an inverse correlation between tissue layer thickness and calcification rate which is consistent with this geometric tradeoff (Lough et al. 2016).

Several coral taxa (e.g., massive *Porites* spp., etc.) have colonies that mimic a hemispheroidal or a low aspect conical shape. Large colonies with these shapes have very low SAP and grow surface area very slowly. Their biomass growth may be geometrically constrained by calcification thereby giving them a potential surplus in biomass production capacity in excess of growth requirements (Anthony et al. 2002). This slower biomass growth strategy may be tied to their thicker tissues (Loya et al. 2001) and be associated with a geometric tradeoff for greater resilience to bleaching (e.g., Loya et al. 2001; Hughes et al. 2018), a greater capacity to recovery from tissue damage/loss, and higher reproductive output per unit area (Alvarez-Noriega et al. 2016). However, during initial growth, their high SAP (and less surplus biomass production capacity) may contribute to the increased mortality rates of juveniles (Meesters et al. 1997).

The rapid, initial, ontogenetic change in SAP for massive corals (hemispheroidal or conical) underlies the success of microfragmentation as a technique for accelerating growth in coral cover (Forsman et al. 2015; Page et al. 2018). When large, massive corals are cut into small fragments, SAP is fundamentally increased by virtue of their geometry. Given an equivalent calcification rate, small colonies grow surface area multiple time faster (per unit surface area) than large conspecifics (Figure 2). Corals with an ontogenetic decrease in SAP likely experience an

ontogenetic shift in growth limitation from biomass production to calcification. This geometry-based prediction is consistent with empirical measurements of tissue thickness for massive *Porites* which increases with colony size (Barnes and Lough 1992). Based on geometry, microfragmentation will not alter SAP in branching corals (with constant branch diameter), foliose corals (with constant thickness), or thin encrusting corals.

Corals with high aspect conical branches appear to have intermediate SAP values depending on their aspect ratio and average branch length. Their SAP values are between those of cylindrical branching corals and hemispheroidal corals with commensurate ecological implications. The aforementioned implications for ontogenetic shift in hemispheroidal coral can also apply to conical branching corals if their average branch length increases with colony size.

The coral morphology which naturally enables the highest SAP are thin plate-like shapes. In shallow water exposed to wave stress, sedimentation, and overshadowing competition, this fragile morphology is not common. However, in the lower photic zone, dominant photosymbiotic coral taxa (e.g., *Leptoseris* spp. and *Agaricia* spp.) are often mimics the shape of a flat circular discs (reviewed in Kahng et al. 2019; Kramer et al. 2022). At these depths offshore, hydrodynamic forces from storm events and exposure to sedimentation is often attenuated. Space competition from fast growing photosynthetic taxa is also attenuated (reviewed in Kahng et al. 2010). Despite the very low calcification rates, the SAP for deep water *Leptoseris* spp. is higher than large, massive *Porites* spp. in shallow-water with their hemispheroidal shape (Kahng et al. 2023).

In oligotrophic, shallow-water environments, light available to drive daily photosynthesis is available from a wide range of angles due to scattering and the change in solar angle throughout the day (Kahng et al. 2019). However, in the lower photic zone, the angular width of usable light narrows centered around the vertical axis regardless of time of day. At these depths, horizontal planar area dictates the maximum amount of light that can be harvested by an organism. Therefore, the rate at which planar area is increased (i.e., planar area productivity, PAP) becomes a strategic attribute for phototrophy. The flattening of coral morphology with depth (both interspecies differences and intra species plasticity) reflects an adaptation to increase PAP at depth. For example, the flattening of massive coral colonies with increasing depth (e.g., Grigg 2006) increases both SAP and PAP. The coral colony morphology with a geometry that enables the highest PAP is a horizontally flat plate with a very thin skeletal thickness. This morphology is adopted by the deepest photosymbiotic corals around the world (i.e., *Leptoseris* spp.) and is consistent with phototrophic adaptation (Kahng et al. 2012).

Conclusions

The geometry of coral taxa can influence the inherent mathematical relationship between the various growth parameters and dictate whether some are size-dependent or size-independent. The size-dependent nature of surface area productivity which underlies the success of microfragmentation to accelerate coral cover is colony shape (and species) specific. The geometric coupling between biomass production and calcification differs characteristically between taxa and contributes to the diversity of life history traits of corals.

Acknowledgements

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Table 1 (on next page)

Table 1

Table 1. Changes in various parameters as coral colony grows in size for each geometric shape. Vertical arrows denote increase/decrease while slating arrows indicate asymptotic increase/decrease. Equal sign denotes constant values which do not change with colony size.

1

	Size metric	Surface area to volume ratio	Linear extension rate	Surface area productivity
Hemispheroid (constant eccentricity)	equatorial radius	↘	↗	↘
Disc (constant thickness)	radius	=	↑	=
Cone (constant aspect ratio)	height/length, basal radius	↘	↗	↘
Branching coral - cylindrical (constant branch diameter)	average branch length	=	↘	=

2

3

4

Figure 1

Figure 1

Figure 1. Size dependent linear extension rates. (*upper left*) Radial extension rate for circular hemisphere (eccentricity = 0) with constant calcification rate ($G = 1.6 \text{ g cm}^{-1} \text{ yr}^{-1}$) and density ($\rho = 1.4 \text{ g cm}^{-3}$). (*upper right*) Radial extension rate for circular disc with constant calcification rate ($G = 0.06 \text{ g cm}^{-1} \text{ yr}^{-1}$) and density ($\rho = 2.6 \text{ g cm}^{-3}$). (*lower left*) Height/length extension rate for cone with high aspect ratio ($\alpha = \text{height/radius} = 4$) with constant calcification rate ($G = 1.6 \text{ g cm}^{-1} \text{ yr}^{-1}$) and density ($\rho = 1.4 \text{ g cm}^{-3}$). (*lower right*) Radial extension rate for cone with low aspect ratio ($\alpha = 0.5$) with constant calcification rate ($G = 1.6 \text{ g cm}^{-1} \text{ yr}^{-1}$) and density ($\rho = 1.4 \text{ g cm}^{-3}$).

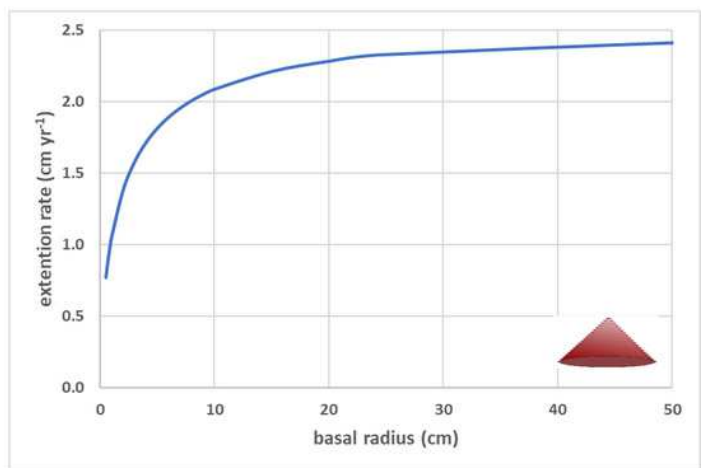
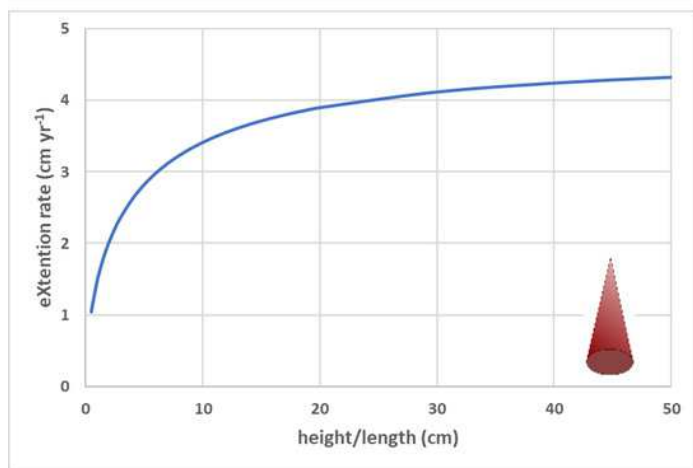
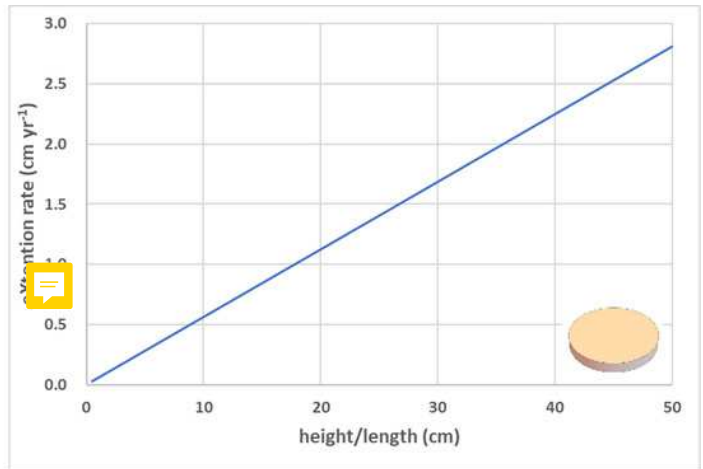
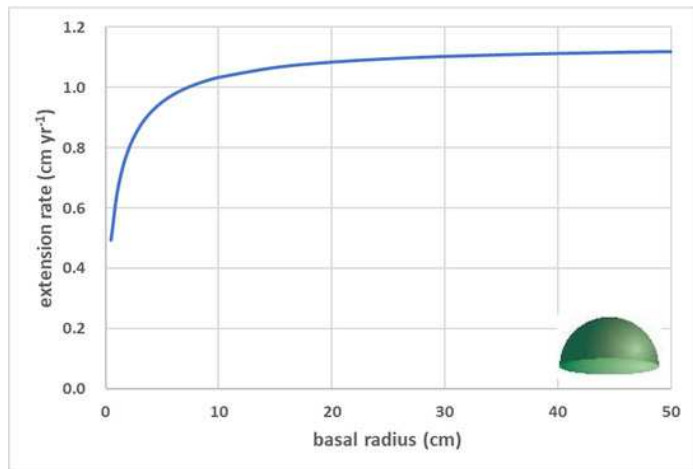


Figure 2

Figure 2

Figure 2. Surface area productivity (yr^{-1}) for a hemispheroid coral colony as a function of colony size (equatorial radius, a) and eccentricity (e) calculated using average values for massive *Porites*: $G = 1.64 \text{ g cm}^{-2} \text{ yr}^{-1}$, $\rho = 1.28 \text{ g cm}^{-3}$ (Lough 2008). For graphing continuity purposes, eccentricity values for oblate hemispheroids are denoted as negative.

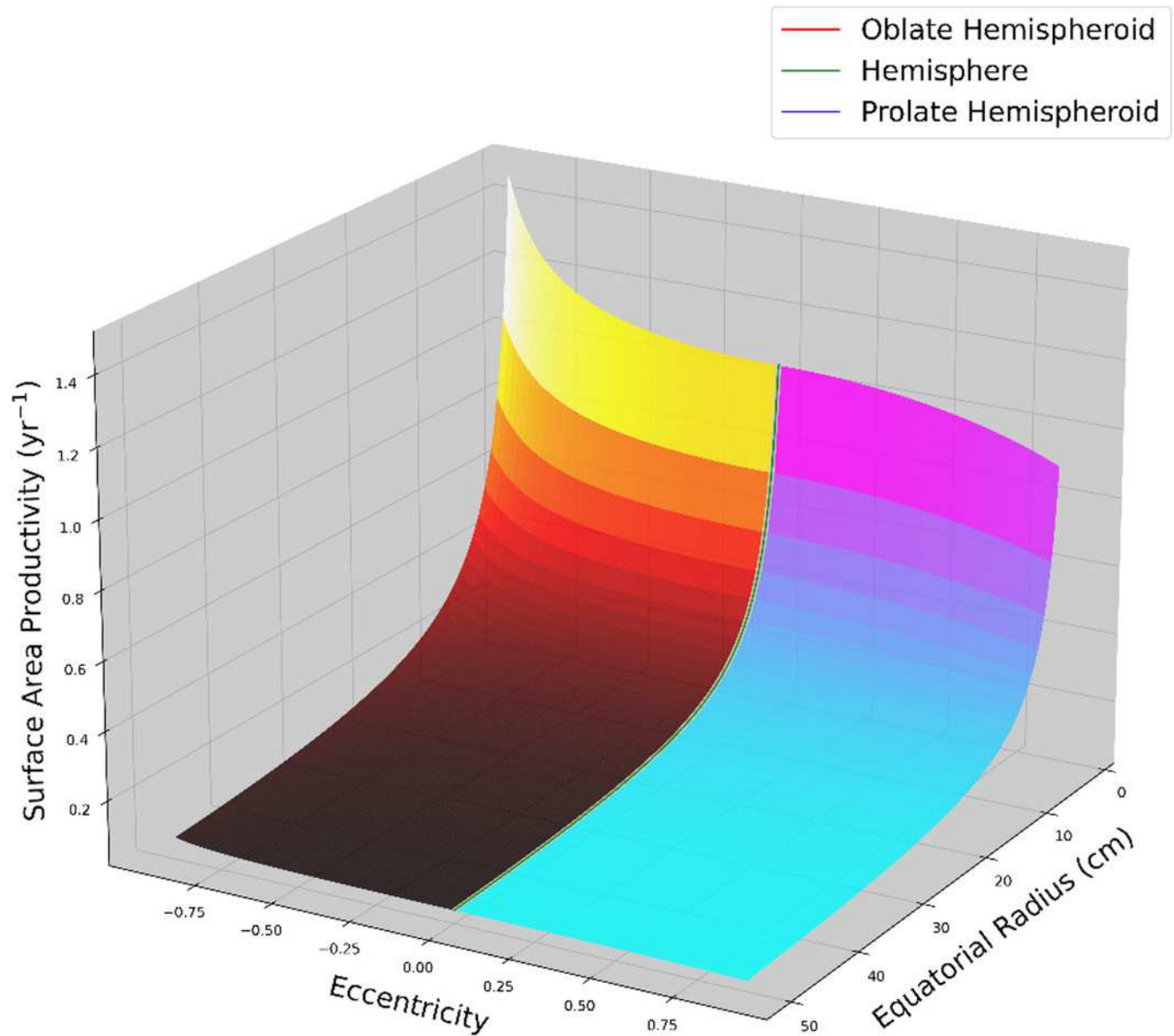


Figure 3

Figure 3

Figure 3. Surface area productivity (yr^{-1}) for a single conical coral colony as a function of height (or a single conical branch) and aspect ratio ($\alpha = \text{length/basal radius}$) using average values for branching *Acropora*: $G = 2.5 \text{ g cm}^{-2} \text{ yr}^{-1}$, $\rho = 1.4 \text{ g cm}^{-3}$ (Hughes 1987; Morgan and Kench 2012).

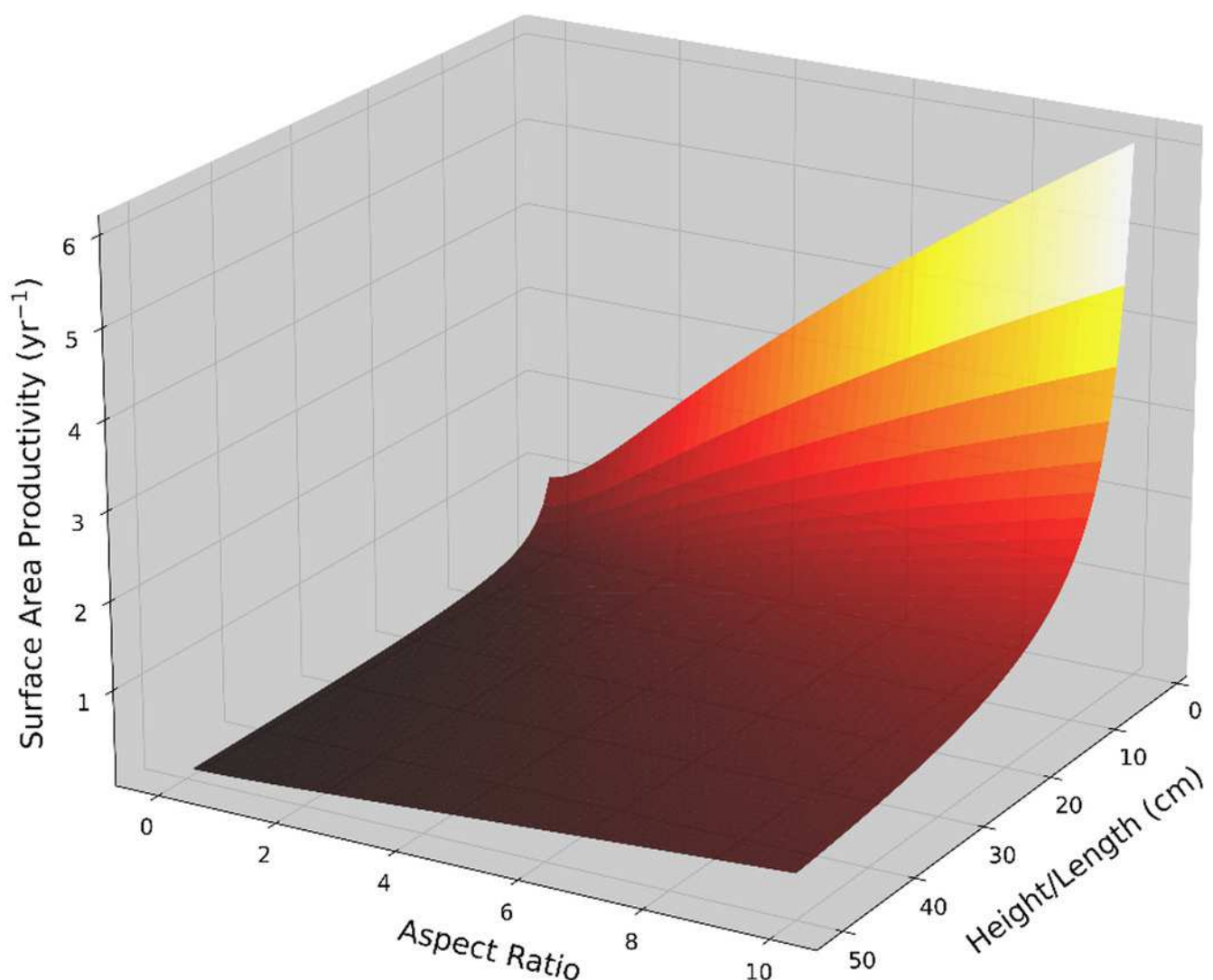


Figure 4

Figure 4

Figure 4. Surface area productivity (yr^{-1}) for a branching coral colony with cylindrical branches as a function of branch diameter using average values for branching *Acropora*: $G = 2.5 \text{ g cm}^{-2} \text{ yr}^{-1}$, $\rho = 1.4 \text{ g cm}^{-3}$ (Hughes 1987; Morgan and Kench 2012). The yellow shading indicates common values for branch diameter (Nadler et al. 2014).

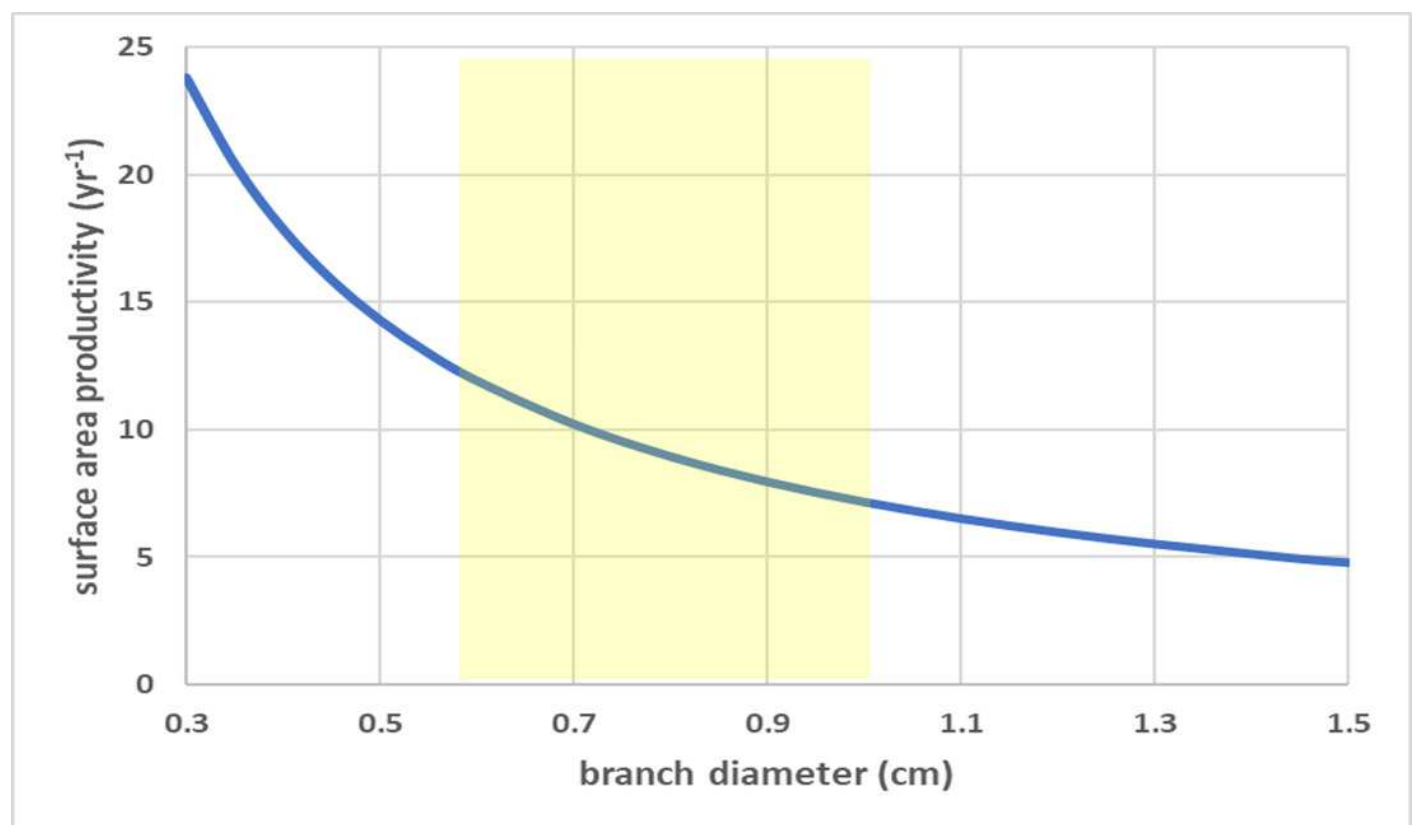


Figure 5

Figure 5

Figure 5. Surface area productivity for a flat plate-like colony as a function of average thickness using average values for branching deep-water *Leptoseris* spp. from 70-111 m in Hawaii: $G = 0.061 \text{ g cm}^{-2} \text{ yr}^{-1}$, $\rho = 2.67 \text{ g cm}^{-3}$ (Kahng et al. 2023). The yellow shading indicates common values for skeletal thickness diameter (Kahng et al. 2020).

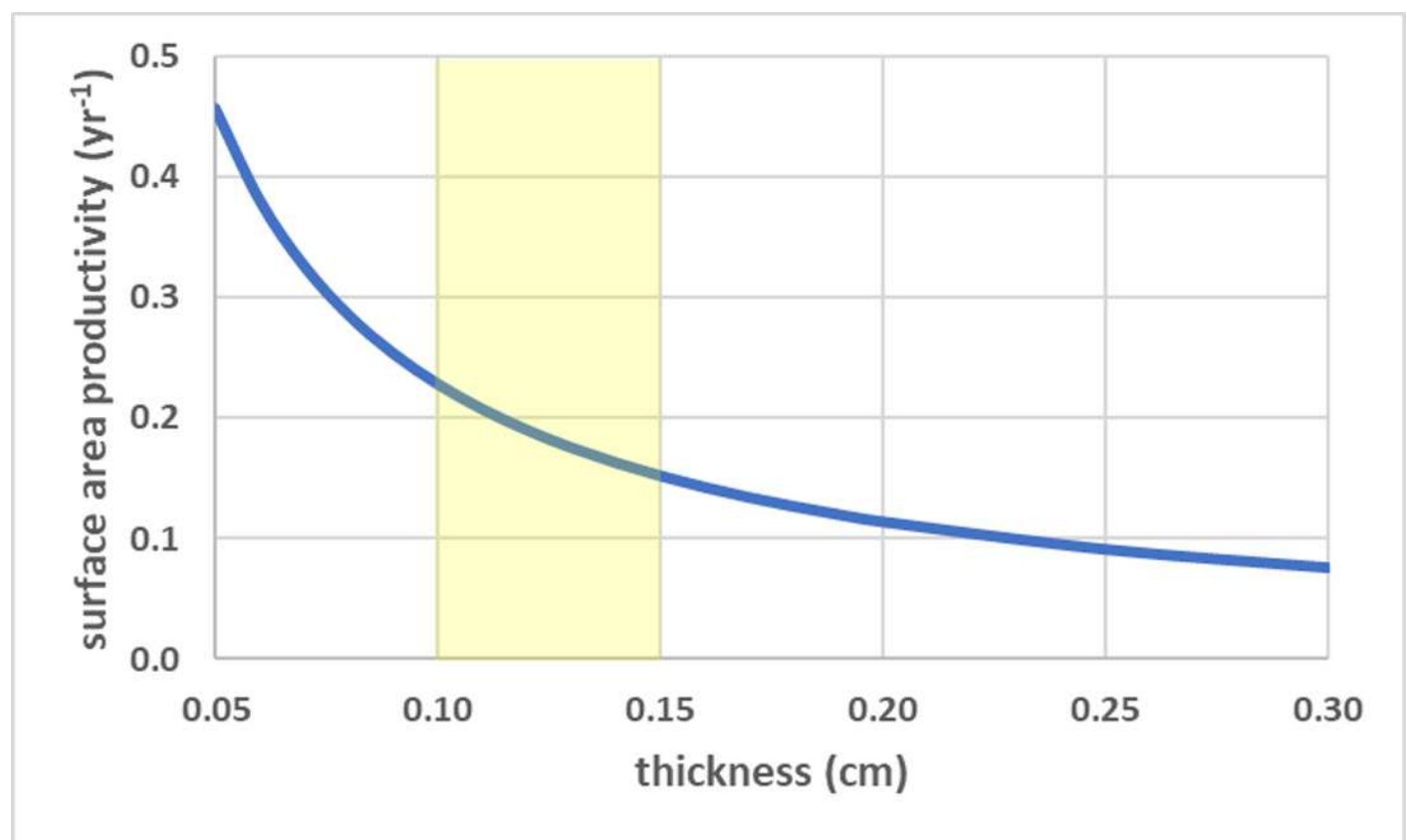


Figure 6

Figure 6

Figure 6. Surface area productivity (yr^{-1}) for three geometric shapes using equivalent values for calcification rate ($G=1.5 \text{ g cm}^{-2} \text{ yr}^{-1}$) and density ($\rho= 1.2 \text{ g cm}^{-3}$). (*upper left*) Flat disc, (*upper right*) cylindrical branching, (*lower left*) single conical branch with a range of aspect ratios (α), and (*lower right*) circular hemispheroid. Yellow shaded areas highlight common values for deep-water *Leptoseris* spp. skeletal thickness (*upper left*) and *Acropora* spp. branch diameter (*upper right*).

