

Segmentation of multi-temporal polarimetric SAR data based on mean-shift and spectral graph partitioning

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Abstract: Polarimetric SAR (PolSAR) image segmentation is a key step in its interpretation. For the targets with time series changes, the single-temporal PolSAR image segmentation algorithm is difficult to provide correct segmentation results for its target recognition, time series analysis and other applications. For this, a new algorithm for multi-temporal PolSAR image segmentation is proposed in this paper. Firstly, the over-segmentation of single-temporal PolSAR images is carried out by the mean-shift algorithm, and the over-segmentation results of single-temporal PolSAR are combined to get the over-segmentation results of multi-temporal PolSAR images. Secondly, the edge detectors are constructed to extract the edge information of single-temporal PolSAR images and fuse them to get the edge fusion results of multi-temporal PolSAR images. Then, the similarity measurement matrix is constructed based on the over-segmentation results and edge fusion results of multi-temporal PolSAR images. Finally, the normalized cut criterion is used to complete the segmentation of multi-temporal PolSAR images. The performance of the proposed algorithm is verified based on three temporal PolSAR images of Radarsat-2, and compared with the segmentation algorithm of single-temporal PolSAR image. Experimental results revealed the following findings: (1) The proposed algorithm effectively realizes the segmentation of multi-temporal PolSAR images, and achieves ideal segmentation results. Moreover, the segmentation details are excellent, and the region consistency is good. The objects which can't be distinguished by the single-temporal PolSAR image segmentation algorithm can be segmented. (2) The segmentation accuracy of the proposed multi-temporal algorithm is up to 86.5%, which is significantly higher than that of the single-temporal PolSAR image segmentation algorithm. In general, the segmentation result of proposed algorithm is closer to the optimal segmentation. The

optimal segmentation of farmland parcel objects to meet the needs of agricultural production is realized. This lays a good foundation for the further interpretation of multi-temporal PoISAR image.

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26 combined to get the over-segmentation results of multi-temporal PolSAR images. Secondly, the
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28 and fuse them to get the edge fusion results of multi-temporal PolSAR images. Then, the similarity
29 measurement matrix is constructed based on the over-segmentation results and edge fusion results
30 of multi-temporal PolSAR images. Finally, the normalized cut criterion is used to complete the
31 segmentation of multi-temporal PolSAR images. **The performance of the proposed algorithm** is
32 verified based on three temporal PolSAR images of Radarsat-2, and compared with the
33 segmentation algorithm of single-temporal PolSAR image. **Experimental results revealed the**

34 following findings: (1) The proposed algorithm effectively realizes the segmentation of multi-
35 temporal PolSAR images, and achieves ideal segmentation results. Moreover, the segmentation
36 details are excellent, and the region consistency is good. The objects which can't be distinguished
37 by the single-temporal PolSAR image segmentation algorithm can be segmented. (2) The
38 segmentation accuracy of the proposed multi-temporal algorithm is up to 86.5%, which is
39 significantly higher than that of the single-temporal PolSAR image segmentation algorithm. In
40 general, the segmentation result of proposed algorithm is closer to the optimal segmentation. The
41 optimal segmentation of farmland parcel objects to meet the needs of agricultural production is
42 realized. This lays a good foundation for the further interpretation of multi-temporal PolSAR
43 image.

44 1 Introduction

45 Polarimetric SAR (PolSAR) is an advanced remote sensing earth observation system. It detects ground
46 targets by emitting and receiving electromagnetic waves in different polarimetric states, and can obtain
47 rich scattering information of targets (Ersahin, Cumming & Ward, 2010). PolSAR image segmentation is a
48 key step in its interpretation, and its performance directly affects the subsequent processing such as feature
49 extraction, target recognition, ground **target** classification and so on (Yu, 2012). Therefore, the research on
50 PolSAR image segmentation algorithm has always been the focus and hotspot of PolSAR image processing
51 technology.

52 In recent years, **numerous** studies have put forward many segmentation algorithms according to the
53 characteristics of PolSAR images. According to the core technology used, the existing PolSAR segmentation
54 methods are roughly divided into the following four categories: (1) Segmentation methods based on graph
55 theory, such as spectral graph partitioning (SGP) / spectral clustering (Ersahin, Cumming & Ward, 2010),
56 max-flow min-cut method (Zhou et al, 2020), etc.; (2) Segmentation method based on region growth, such
57 as simple linear iterative clustering (Zou et al, 2016), simple nonlinear iterative clustering (Ma et al., 2021),
58 watershed algorithm (Marcin, 2017), etc.; (3) Segmentation method based on threshold, such as simple
59 threshold division method (Otsu, 2007), maximum between-class variance (Shao et al., 2013), etc.; (4)
60 Segmentation method based on specific theory, such as markov random fields (Duan et al., 2017), level set
61 (Mohammadimanesh et al., 2019), neural network (Fowlkes et al., 2004), etc. Among them, the methods
62 based on SGP have become a research hotspot in recent years due to its advantages of clustering in
63 arbitrary-shaped sample spaces and converging to the global optimal solution, but its computational time
64 and space costs are relatively high. Many scholars have carried out research on this problem, and some of
65 them use sampling approximation techniques, such as Nyström sampling method proposed by Fowlkes et
66 al. (2004), which can effectively improve the efficiency of SGP, but the implementation process of this
67 algorithm is complicated and the effect is not ideal for images with low signal-to-noise ratio. Other scholars
68 solve this problem through combined segmentation algorithm. For example, the segmentation algorithm
69 that combines watershed and spectral clustering proposed by Ma & Jiao (2008); PolSAR image
70 segmentation algorithm based on mean shift (MS) and SGP (MS-SGP) proposed by Zhao et al. (2015). This
71 kind of combination algorithm usually first uses a local optimization algorithm to quickly realize the over-
72 segmentation of PolSAR image, and then the global optimization of SGP algorithm is used to achieve
73 excellent segmentation effect. Since the SGP is based on the over-segmentation regions (super-pixel) instead
74 of the original pixels, the computational cost of SGP is effectively reduced. This kind of combination
75 algorithm combines the advantages and disadvantages of local and global optimization segmentation
76 algorithms, and is the research focus of PolSAR image segmentation algorithms in recent years.

77 However, most of the existing PolSAR image segmentation algorithms are only for single-temporal
78 PolSAR images. For the **targets** with time series changes, single-temporal PolSAR image can't provide
79 enough information for segmentation. For example, crops of different types and different sowing times are
80 easy to show similar characteristics on single-temporal PolSAR images, so it is impossible to segment field
81 parcel objects that meet the needs of agricultural production based on single-temporal PolSAR images.
82 Based on multi-temporal PolSAR images, the scattering characteristics of crops in different growth periods

83 can be obtained, which is expected to solve the above problems.

84 In recent years, some scholars have begun to explore multi-temporal PolSAR image segmentation
85 algorithms. For example, Zou (2015) proposed a variational level set segmentation algorithm for multi-
86 temporal PolSAR images, which can effectively improve the recognition accuracy of ground **targets**. Deng
87 et al. (2014) obtained more robust and accurate segmentation results by combining stationary wavelet
88 transform and algebraic multigrid method for hierarchical segmentation of multi-temporal PolSAR images.
89 Ma et al. (2021) realized super-pixel cooperative segmentation of dual-temporal SAR images through
90 simple nonlinear iterative clustering. Alonso-Gonzalez, Lopez-Martinez & Salembier (2014) proposed a
91 data processing method of PolSAR time series based on **binary partition trees**. Overall, there are relatively
92 few segmentation algorithms suitable for multi-temporal PolSAR images. **Moreover, most segmentation**
93 **algorithms are based on local optimization to process the image, which will produce super-pixel regions**
94 **and can't achieve optimal segmentation. However, as far as agricultural application is concerned, as the**
95 **basic farming unit of agricultural production, accurate identification of farmland parcels is conducive to**
96 **the realization of crop production planning, management and benefit evaluation. In addition, the**
97 **polarization features extracted from farmland parcel units can avoid the influence of outliers, and are more**
98 **accurate than the polarization features extracted from over-segmented objects based on homogeneous pixel**
99 **clustering. Thus, it is more beneficial to the application of crop target identification and time series analysis.**
100 **Obviously, the super-pixels produced by over-cutting can't meet the above production needs. Therefore,**
101 **an optimal segmentation algorithm that can segment the basic units of farmland parcels is needed. At this**
102 **time, based on multi-temporal PolSAR images and combined with the advantage that SGP algorithm can**
103 **cluster in the sample space of arbitrary shape and converge to the global optimal solution, it is expected to**
104 **achieve optimal segmentation and solve the above problems.**

105 In view of the above analysis, a new algorithm suitable for multi-temporal PolSAR image
106 segmentation is proposed based on the MS-SGP segmentation algorithm of single-temporal PolSAR image
107 (Zhao et al., 2015). On the basis of combining the advantages and disadvantages of local optimization and
108 global optimization segmentation algorithm, this algorithm comprehensively uses the rich polarimetric
109 and temporal information of multi-temporal PolSAR images to realize image segmentation. The algorithm
110 combines the over-segmentation results of single-temporal PolSAR images generated by MS algorithm.
111 Furthermore, the edge information extracted by edge detector is fused. In order to obtain the over-
112 segmentation result and edge fusion result of the multi-temporal PolSAR image. Based on this, the
113 similarity measurement matrix is constructed to realize the segmentation of multi-temporal PolSAR
114 images. In order to verify the performance of this algorithm, it is applied to the segmentation of time series
115 PolSAR images of Radarsat-2, and the segmentation effect and accuracy of single-temporal and multi-
116 temporal PolSAR image segmentation algorithms are compared and analyzed.

117 2. Materials and Methods

118 2.1 Materials

119 2.1.1 PolSAR data and the test site

120 The data used in this experiment are a time series Radarsat-2 PolSAR (C-band) images acquired on
121 May 23, August 3, and August 27, 2013, respectively. The acquired three images have the same sensor
122 parameters such as the ascending orbit, the imaging mode of FQ18, the incident angle of 37.5° , and the
123 azimuth and range resolution with 4.96 m and 4.73 m, respectively. The study area is covered by the
124 acquired is Shangkuli Farm ($119^\circ 07' \sim 121^\circ 49' E$, $50^\circ 01' \sim 53^\circ 26' N$) between city Erguna and Genhe, Inner
125 Mongolia. Part of the farmland region is selected as for our experiment. The selected farmland region was
126 planted mainly with rape (*Brassica napus* L), wheat (*Triticum aestivum* L) and other crops. Fig. 1 shows
127 the PolSAR image (PauliRGB) for the experiments. Due to the difference in factors such as height, moisture
128 content, and appearance of the same crop at different crop growth stages, different backscattering
129 coefficients of the same farmland parcel with same crop at different growth stages occurred in the time
130 series images like (a), (b), and (c) in Fig. 1. They show different color on multi-temporal PolSAR images.

131 **Figure 1.** Pauli RGB display of PolSAR data at different temporal in experimental region. The data are three temporal
132 PolSAR images of Radarsat-2 (C-band) acquired on May 23, August 3, and August 27, 2013, respectively. (a) 20130523,
133 (b) 20130803, (c) 20130827.

134 2.1.2 Reference map for segmentation evaluation

135 Reference map for segmentation evaluation, which is generated based on ground campaigned data
136 and expert knowledge, is shown here as Fig. 2. In this study, the segmentation evaluation reference map
137 will be used to evaluate the accuracy, so as to verify the performance of the proposed multi-temporal MS-
138 SGP segmentation algorithm. For the generation process of Fig. 2, readers are referred to the details in Zhao
139 et al. (2015). There are mainly five types of land cover in this region, including rape, wheat, shrubs, bare
140 soil and other types. Among them, bare soil shows three different scattering characteristics due to different
141 factors such as roughness, ridge direction and water content, so it can be subdivided into three categories.

142 **Figure 2.** Reference map for Segmentation Evaluation.

143 2.2 Multi-temporal polarimetric SAR segmentation method

144 According to the data characteristics of multi-temporal PolSAR images, a multi-temporal MS-SGP
145 segmentation algorithm suitable for multi-temporal PolSAR images is proposed on the basis of single-
146 temporal MS-SGP segmentation algorithm. The technical flow is shown in Fig. 3. **Firstly, the PolSAR data
147 is pre-processed. Secondly, MS algorithm is used to pre-segment the image to obtain the initial
148 segmentation unit, and the edge extraction algorithm is used to provide segmentation clues for SGP. Then,
149 the similarity measurement matrix is constructed based on the segmentation unit and segmentation clues,
150 and then the normalized cut criterion is used to complete the segmentation of image. Finally, the
151 segmentation results are evaluated in detail based on the reference segmentation map obtained from the
152 ground survey data.**

153 **Figure 3.** Technical flow chart of multi-temporal MS-SGP segmentation algorithm.

154 2.2.1 Pre-segmentation

155 1) MS method for single-temporal SAR image over-segmentation

156 MS is an iterative algorithm for nonparametric kernel density estimation (Fukunaga & Hostetler,
157 1975). Firstly, the offset mean value of the current point is calculated in the feature space, and the point is
158 moved according to its offset mean value. Then, taking the location of the above moved point as the input
159 of the new starting point and repeating the procedure until it converges to the convergence point of
160 probability density function. The offset mean value is calculated as follows:

$$161 \quad M_h(x) = \frac{\sum_{i=1}^n G[(x_i - x) / h] w(x_i) (x_i - x)}{\sum_{i=1}^n G[(x_i - x) / h] w(x_i)} \quad (1)$$

162 where h is the window size of the kernel function, G is the kernel function, in this paper, Gaussian
163 function is selected as kernel function. $w(x_i) \geq 0$ is weight function assigned to each sampling point x_i ,
164 $x = (x_r, x_s)$ where x_s is a two-dimensional space vector, which include the coordinate information of each
165 pixel, x_r is the feature vector (He et al., 2008). Three polarimetric scattering components decomposed by
166 PolSAR Pauli are used as the features vector of x_r . The kernel function is shown as Eq. (2).

$$167 \quad G_{h_s, h_r} = \frac{C}{h_s^2 h_r^3} g\left(\frac{\mathbf{P} x_s^2}{h_s} \mathbf{P}\right) g\left(\frac{\mathbf{P} x_r^2}{h_r} \mathbf{P}\right) \quad (2)$$

168 Where h_s and h_r are window sizes for space vector and feature vector of each pixel, respectively C is
169 normalized constant, $g(\mathbf{g})$ is a Gaussian function (Zhao et al., 2015). The detailed steps and parameter
170 setting principles of PolSAR image segmentation using MS algorithm can be found in the literature He et
171 al. (2008) and Zou et al. (2009).

172 2) Over-segmentation regions merging of multi-temporal images

173 Over-segmentation regions of multi-temporal images are merged by the over-segmentation regions of
174 each single-temporal PolSAR image. The merging strategy is shown in Fig. 4. Each square describes a pixel
175 in images, the value of the square means the attribute of the object in the images. Different values or colors
176 in the squares discriminate the different objects in the images.

177 Even the over-segmentation result of the merged multi-temporal PolSAR image contains more regions
178 than that of the single-temporal PolSAR image, the number of the regions in it is still less than the number
179 of the pixels in the original image.

180 **Figure 4.** Schematic diagram of merging over-segmentation regions of multi-temporal PolSAR images. (a) Over-
181 segmentation regions of single-temporal image A (4 regions). (b) Over-segmentation regions of single-temporal image
182 B (3 regions). (c) Merging results of multi-temporal images (8 regions).

183 2.2.2 Edge information extraction

184 The construction of similarity measurement matrix needs to select appropriate features as
185 segmentation clues, which is not only the core of transforming image segmentation problem into graph
186 segmentation problem, but also the premise of segmentation. Edge information is very important
187 information in image segmentation, especially when excellent segmentation results can't be obtained by
188 using information such as image gray level and color. For PolSAR images, the strong multiplicative noise

189 makes the segmentation method based on pixel-based region growth unable to achieve application
 190 purpose, and relatively stable edge information is a excellent choice. Through the edge intensity
 191 information between pixels, the similarity between two pixels can be effectively measured. Therefore, the
 192 edge information of multi-temporal PolSAR images is used as the segmentation clue of SGP.

193 1) Edge information extraction of single-temporal

194 In this paper, referring to the method proposed by Schou et al. (2003) and Zhao et al. (2015), edge
 195 detectors in four directions ($0^\circ, 45^\circ, 90^\circ, 135^\circ$) are set, as shown in Fig. 5. The window size can be determined
 196 according to the actual situation ($3 \times 3, 5 \times 5, \dots$).

197 **Figure 5.** Schematic diagram of edge detector. Edge detectors are set in four directions. (a) 0° direction, (b) 45° direction,
 198 (c) 90° direction, (d) 135° direction.

199 Assuming that the central pixel of the edge detector is the edge, there should be a strong difference
 200 between the regions on both sides of the central pixel. Therefore, the Wishart test statistics suitable for
 201 PolSAR data is utilized to measure the difference between two regions. In the Wishart algorithm, the
 202 maximum likelihood-ratio function is utilized to test the equality of center covariance matrices of two
 203 regions. The hypothesis test equation is

$$204 \quad H_0: \Sigma_i = \Sigma_j \quad \text{versus} \quad H_1 \quad \Sigma_i \neq \Sigma_j \quad (3)$$

205 Where Σ_i and Σ_j are the center covariance matrices of the i th and j th regions, respectively. Let Θ_i and Θ_j
 206 be the sample covariance matrix data sets of the i th and j th regions, respectively. It is assumed that sample
 207 covariance matrices are spatially independent, therefore, the difference measure between the i th and j th
 208 regions can be derived from the likelihood ratio test. The test statistic equation is

$$209 \quad Q = \frac{L_{H_0}(\hat{\Sigma}|\Theta_i, \Theta_j)}{L_{H_1}(\hat{\Sigma}_i, \hat{\Sigma}_j|\Theta_i, \Theta_j)} = \frac{|\hat{\Sigma}_i|^{nN_i} |\hat{\Sigma}_j|^{nN_j}}{|\hat{\Sigma}|^{n(N_i+N_j)}} \quad (4)$$

210 where $L_{H_0}(\mathbf{g})$ and $L_{H_1}(\mathbf{g})$ are likelihood functions under different assumptions, respectively. Σ is the
 211 center covariance matrices of the whole region. $\hat{\Sigma}$, $\hat{\Sigma}_i$ and $\hat{\Sigma}_j$ are maximum likelihood estimators of Σ ,
 212 Σ_i and Σ_j , respectively. N_i and N_j are the numbers of samples in the i th and j th regions, respectively. n
 213 is the number of looks. If the value of Q is too low, the null hypothesis H_0 is rejected. Thus, the difference
 214 measure between the i th and j th regions can be defined as

$$215 \quad D(S_i, S_j) = -\frac{1}{n} \ln Q = (N_i + N_j) \ln \left| \frac{\hat{\Sigma}}{\hat{\Sigma}_i} \right| - N_i \ln \left| \frac{\hat{\Sigma}}{\hat{\Sigma}_i} \right| - N_j \ln \left| \frac{\hat{\Sigma}}{\hat{\Sigma}_j} \right| \quad (5)$$

216 where S_i and S_j represent the i th and j th regions, respectively. The difference measure D is symmetric. If
 217 $i = j$, $D(S_i, S_j)$ has a minimum value equaling to zero. If the i th and j th regions are more dissimilar, the
 218 value of $D(S_i, S_j)$ is higher. Details of the derivation of edge extraction algorithm can be found in, Cao et
 219 al. (2007) and Liu et al. (2013).

220 The Eq. (5) is used to calculate the $D(S_i, S_j)$ in four directions of each pixel, that is, the edge intensity
 221 values in different directions, and retain the maximum edge intensity value D_{\max} and its edge direction θ^* .
 222 After edge extraction, the polarimetric information of PolSAR image is transformed into edge information.

223 2) Multi-temporal edge information fusion

224 First, it is necessary to further optimize the edge extraction results of the single-temporal PolSAR
 225 image to determine the boundary elements and avoid positioning deviations. For any pixel x on the
 226 image, the maximum edge intensity value $D_{\max}(x)$ and edge direction $\theta^*(x)$ orientation have been
 227 determined. Compare the edge intensity values of the pixels on both sides perpendicular to the edge
 228 direction $\theta^*(x)$. If the maximum edge intensity value $D_{\max}(x)$ of pixel x is greater than or equal to the
 229 edge intensity value of pixels on both sides, then keep the value, otherwise, set to zero. For example, as
 230 shown in Fig. 6.a and 6.b, assuming that $\theta^*(x)$ is 0° , $D_{\max}(x)$ can be preserved only if it is greater than
 231 or equal to the edge intensity values of the upper and lower pixels. Similarly, if the $\theta^*(x)$ is 90° , the
 232 $D_{\max}(x)$ can be retained only if it is greater than or equal to the edge intensity values of the left and right
 233 pixels. Then, based on the edge optimization results of different time temporal, the edge intensity values
 234 of pixels in the same position are compared, and the maximum value is taken as the multi-temporal edge
 235 value, that is, the edge information fusion of multi-temporal PolSAR images is completed. The fusion result
 236 is shown in Fig. 6.c. The result of multi-temporal edge information fusion will provide segmentation clues
 237 for subsequent SGP of multi-temporal PolSAR images.

238 **Figure 6.** Schematic diagram of single-temporal edge optimization and multi-temporal edge fusion. (a) Edge
 239 optimization schematic diagram of single-temporal A. (b) Edge optimization schematic diagram of single-temporal B.
 240 (c) Schematic diagram of multi-temporal edge fusion.

241 2.2.3 Construction of similarity measurement matrix

242 On the basis of dividing the original pixels of the multi-temporal PolSAR image into many over-
 243 segmentation region units with similar statistical characteristics, it is necessary to find a pixel that can
 244 represent the spatial position of the entire over-segmentation region. The calculation method is shown in
 245 Fig. 7.

246 **Figure 7.** The centre location of over-segmentation regional. S is a segmentation region, p is the internal pixel of an
 247 over-segmentation region S , α is the azimuth angle, $L(\alpha)$ is the distance from the pixel P to the boundary of the region
 248 when the azimuth angle is α .

249 In the Fig. 7, p is the internal pixel of an over-segmentation region S , $L(\alpha)$ is the distance from the pixel
 250 p to the boundary of the region when the azimuth angle is α , when the value of α is determined, the
 251 extensibility of the pixel p in the over-segmentation region S can be expressed as:

$$252 \quad E(p \in S) = \prod_{i=1}^n L(\alpha \times i), \quad n = 2\pi / \alpha \quad (6)$$

253 where the pixel corresponding to $\max\{E(p \in S)\}$ is the pixel representing the S space position of the entire
 254 over-segmentation region. If the over-segmentation region is a regular shape (such as a rectangle, a circle,
 255 etc.), the pixel corresponding to $\max\{E(p \in S)\}$ is the geometric centre of the region.

256 After obtaining the representative central pixel of the over-segmentation region of the multi-temporal
 257 PolSAR image, then, the edge fusion information of the multi-temporal PolSAR image can be used to
 258 measure the degree of similarity between the regions. The basic idea is shown in Fig. 8.

259 **Figure 8.** Illustration of extracting the dissimilarity information from edge maps. (a) A subset of a C-band PolSAR
 260 image (Pauli RGB). (b) Part of the original image marked by the box; S_1 , S_2 and S_3 are three over-segmentation

261 regions; p_1 and p_2 are in the same class, and p_1 and p_3 are in different classes. (c) Edge map of image (b) after the
 262 oriented nonmaximal suppression; somewhere along l_1 , the value of edge map strength is high, which suggests that p_1
 263 and p_3 are in different classes; along l_2 , the values of edge map strength are all low, proposing that p_1 and p_2 are
 264 probably in the same class.

265 Fig. 8.a shows the Pauli RGB display of the PolSAR image, Fig. 8.b is the local region, S_1 , S_2 and S_3
 266 are three segmentation regions. p_1 , p_2 and p_3 are the corresponding spatial representative pixels. The
 267 similarity measure between the two regions can be represented by the maximum edge intensity value on
 268 the line between the representative pixels, as shown in Fig. 8.c. There are obvious edges between pixels p_1
 269 and p_3 , and the similarity will be lower. Correspondingly, the similarity between pixel p_1 and p_2 is higher.

270 Therefore, based on multi-temporal edge fusion information, the difference between any two pixels x
 271 , y can be defined $D_c(x, y)$. As shown in the following equation (Leung & Malik, 1998; Ersahin, Cumming
 272 & Ward, 2010; Ersahin, Cumming & Ward, 2014).

$$273 \quad D_c(x, y) = D^*(z^*), \quad z^* = \arg \max_{z \in l} D^*(z) \quad (7)$$

274 where $D^*(g)$ denotes the strength of edge maps after the oriented nonmaximal suppression, l is the line
 275 joining x and y , and z^* is the location where the strength of edge maps after the oriented nonmaximal
 276 suppression is maximum along l . Then, the pairwise affinity is defined using a gaussian kernel (Shi &
 277 Malik, 2000; Ersahin, Cumming & Ward, 2010; Ersahin, Cumming & Ward, 2014).

$$278 \quad W(x, y) = \exp \left\{ \frac{-D_c^2(x, y)}{2\sigma_C^2} \right\} \quad (8)$$

279 where σ_C is the scaling parameter for the kernel. Based on this, the construction of the similarity
 280 measurement matrix between the over-segmentation regions of the multi-temporal PolSAR image can be
 281 completed.

282 2.2.4 Normalized cuts

283 In the normalized cuts algorithm, Shi & Malik (2000) formulated visual grouping as a graph
 284 partitioning problem. The basic principle of graph-based partitioning schemes is to represent a set of points
 285 in an arbitrary feature space using an undirected graph $G = \{V, E\}$, where V is for the vertices and E is
 286 for the edges between the vertices. Each vertex corresponds to a point in the feature space, and the edge
 287 between two vertices, e.g., x and y , is associated with a weight $W(x, y)$, that indicates the affinity of the
 288 pair. Image segmentation can be formulated as the best partitioning of the feature space into two regions,
 289 A and B , based on the minimum cut criterion. The cost function cut as follows is minimized

$$290 \quad cut(A, B) = \sum_{x \in A, y \in B} W(x, y) \quad (9)$$

291 where $W(x, y)$ is the pairwise affinity between x and y .

292 Since minimizing the cost function in Eq. (9) favors cutting out small and isolated partitions, Shi &
 293 Malik (2000) proposed a new measure of partitioning cost. Instead of using value of total edge weight
 294 connecting the two regions, the new measure defines the partitioning cost as a fraction of the total edge
 295 connections to all the nodes in the graph. It is referred to as the normalized cut, $Ncut$ as follows

$$296 \quad Ncut(A, B) = \frac{cut(A, B)}{assoc(A, V)} + \frac{cut(B, A)}{assoc(B, V)} = \frac{cut(A, B)}{\sum_{x \in A, v \in V} W(x, v)} + \frac{cut(B, A)}{\sum_{y \in B, v \in V} W(y, v)} \quad (10)$$

297 where $A \cup B = V$, and $assoc(A, V)$ is the total connection from nodes in A to all nodes in the graph and
 298 $assoc(B, V)$ is similarly defined. The principle of the normalized cuts algorithm is to minimize the
 299 partitioning cost measure $Ncut$. How to solve the minimization problem and more details related to the
 300 normalized cuts algorithm can be found in Shi & Malik (2000).

301 2.2.5 Method of segmentation evaluation

302 At present, there are many methods of segmentation evaluation, each of which has different
 303 advantages, disadvantages and applicable objects. In this paper, the improved method of maximum
 304 overlapping area proposed in reference Zhao et al. (2015) is used to evaluate the results of image
 305 segmentation. The segmentation accuracy calculated by this method reflects the degree of over-
 306 segmentation and under-segmentation of the image. The basic principle is shown in Fig. 9.

307 Firstly, for a reference segmentation region SS , there may be multiple segmentation regions to be
 308 evaluated (A, B, C, K) overlapping with it. Assuming that the overlapping region of the segmented

309 region to be evaluated A and SS is the largest, the overlapping region is recorded as A_{SS} , then $(1 - A_{SS}/A)$

310 is defined as the under segmentation ratio (USR). Then, the percentage of correctly segmented pixels can
 311 be calculated by limiting the value of USR. That is, only the pixels with the largest overlap region and the
 312 under-segmentation ratio not greater than USR will be counted as the number of pixels for correct

313 segmentation. For example, as shown in Fig. 9, if we set $USR = 0.3$, then $(1 - A_{SS}/A) = (1 - 9/16) = 0.44 > 0.3$,

314 it can be considered that the A_{SS} region is a wrongly segmented. At this time, there is no correctly

315 segmented pixel for the reference region SS , and its segmentation accuracy is 0. When setting $USR = 0.5$,

316 $(1 - A_{SS}/A) = (1 - 9/16) < 0.5$, the A_{SS} region can be considered as the correct segmented pixel. For the

317 reference region SS , the segmentation accuracy is the ratio of the number of pixels in the region A_{SS} to

318 the number of pixels in the region SS . Finally, the segmentation accuracy of the whole image is the average

319 of the segmentation accuracy of all reference segmentation regions.

320 **Figure 9.** Illustration chart of segmentation evaluation principle. SS is the reference segmentation region; A, B and C
 321 are the segmentation regions, respectively; A_{SS} is the region with the largest overlapping area between the segmentation

322 region A to be evaluated and the reference segmentation region SS .

323 3. Results

324 3.1 Segmentation experiment

325 The PolSAR images of three temporal are pre-processed by radiometric calibration, image registration,
326 multi-look, filter and geocode. First of all, the main purpose of radiometric calibration in PolSARpro6.0
327 software (<https://earth.esa.int/web/polsarpro/home>) is to determine the relationship between the grayscale
328 of radar image and the standard backscatter coefficient. Secondly, the registration of multi-temporal images
329 is carried out in Gamma software (<https://www.gamma-rs.ch/>). The detailed registration process can be
330 found in the literature Wang (2013). The image after registration is processed with 2×2 window multi-look
331 processing in PolSARpro6.0 software, the pixel sizes in azimuth and range of PolSAR image after multi-
332 look are about 9.92m and 9.47m respectively. In order to reduce the influence of speckle noise, this paper
333 uses Mean-Shift filtering method to filter, and its window is set to 5×5 . Finally, the digital elevation model
334 (DEM) data of 30m resolution in the study area is used for geocoding in Gamma software. The projection
335 of Radarsat-2 image is transformed into "UTM_Zone_51N" projection under WGS84 coordinate system,
336 and resampled to obtain PolSAR polarization covariance matrix data with a spatial resolution of 10m.

337 Then, the single-temporal PolSAR images are over-segmented by MS. In this paper, based on the
338 existing literature reference (He et al., 2008; Zou et al., 2009 & Zhao et al., 2015). The kernel function window
339 values h_s and h_r of pixel space vector and feature vector are set to 7 and 6.5. And the minimum
340 segmentation region parameter M plays a role in controlling the size of the segmentation region. The setting
341 of this parameter only needs to ensure the over-segmentation degree of the image, which has a large setting
342 space. In this paper, considering the operation cost of SGP for multi-temporal PolSAR images, a certain
343 degree of attempt and comparison is made according to experience, and the segmentation results are
344 qualitatively evaluated based on visual evaluation. The parameter M which ensures that each of the three
345 temporal PolSAR images can be over-segmented and has a small computational cost is determined as the
346 optimal parameter selected in this paper. As shown in Fig. 10.a-c, the number of over-segmentation regions
347 of MS for different temporal is 118, 102 and 111, respectively, under setting of different M (M : 235, 235,
348 192). Based on this, the over-segmentation results produced by the initial segmentation of three temporal
349 PolSAR images are merged, and the number of over-segmentation regions after merging is 1411. The
350 merging result of multi-temporal over-segmentation regions is shown in Fig. 10.d, with the 20130803 Pauli
351 RGB as the display image.

352 In addition, the central position of the over-segmentation region is calculated according to Eq. (6). That
353 is, the pixels that can represent the spatial position of the over-segmentation region of the single-temporal
354 and multi-temporal PolSAR images are obtained. The result is shown as the yellow point in Fig. 11. It can
355 be seen that these points are in the relative center of the region.

356 **Figure 10.** MS pre-segmentation results of single-temporal PolSAR images and merging results of multi-temporal
357 segmentation regions. The h_s and h_r of the three temporal are set to 7 and 6.5, respectively; M is set to 235, 235 and

358 192, respectively; and the number of blocks in the over-segmentation region of MS is 118, 102 and 111, respectively.
359 Fig. 10.d shows the merging results of multi-temporal segmentation regions is 1411, and the Pauli RGB of 20130803 is
360 used as the display image. (a) 20130523, $h_s = 7$, $h_r = 6.5$, $M=235$, $N=118$; (b) 20130803, $h_s = 7$, $h_r = 6.5$, $M=235$, $N=102$; (c)
361 20130827, $h_s = 7$, $h_r = 6.5$, $M=192$, $N=111$; (d) multi-temporal, $N=1411$.

362 **Figure 11.** Over-segmentation regional center of single-temporal and multi-temporal PolSAR images. (a) 20130523; (b)
363 20130803; (c) 20130827; (d) multi-temporal.

364 While the over-segmentation of multi-temporal PolSAR images is carried out, the edge information of
365 multi-temporal PolSAR images is also extracted to obtain the segmentation clues of SGP. Firstly, the edge
366 information of the single-temporal PolSAR image is extracted based on the edge detector, and the window
367 is set to 7×7 . Then, edge optimization based on rough edge extraction. Based on the edge optimization
368 results of different temporal, the edge intensity values of pixels in the same position are compared, and the
369 maximum value is taken as the multi-temporal edge value. As shown in Fig. 12. Among them, the edge
370 information of the farmland parcels in the yellow rectangle in Fig. 12.a, the parcels in the green rectangle
371 in Fig. 12.b and the parcels in the red rectangle in Fig. 12.c are clearer and more complete compared with
372 the same position of the other two images. The edge information of the three temporal PolSAR images is
373 fused, so that the result after the fusion Fig. 12.d contains rich edge information of the multi-temporal
374 PolSAR image. The edge fusion results are used as the segmentation clues for the subsequent SGP, which
375 can achieve better segmentation results than single-temporal PolSAR images.

376 **Figure 12.** Single-temporal PolSAR image edge extraction results and multi-temporal edge fusion results. (a) 20130523;
377 (b) 20130803; (c) 20130827; (d) multi-temporal edge fusion results.

378 Through the above-mentioned pixel points representing the spatial position of the over-segmentation
379 regions of the multi-temporal PolSAR image Fig. 11.d and the edge fusion result of the multi-temporal
380 PolSAR image Fig. 12.d, the similarity measurement matrix can be constructed. Then, the segmentation of
381 the multi-temporal PolSAR image is completed by the normalized cut criterion. In this step, the
382 segmentation scale can be controlled by setting the number of final segmentation regions. **After a certain
383 degree of attempt and comparison according to the experience, and the qualitative evaluation of the
384 segmentation results based on visual evaluation, it can be found that the optimal segmentation effect can
385 be achieved when the number of segmentation regions is set to 47. At this time,** the farmland parcels of
386 different sizes are well segmented and become independent objects. **In addition,** the details of segmentation
387 results are excellent, and the regional consistency is well maintained. The final segmentation result is
388 shown in Fig. 13. In order to show the effect of the multi-temporal MS-SGP segmentation algorithm, the
389 PauliRGB of three temporal PolSAR images are all used as the display image, respectively.

390 **Figure 13.** Segmentation results of multi-temporal PolSAR images. The number of segmentation regions is set to 47. (a)
391 20130523, $N=47$; (b) 20130803, $N=47$; (c) 20130827, $N=47$.

392 **In terms of the operation cost of the algorithm, the experimental image consists of 374 rows and 205
393 columns, with a total of 76670 pixels. If the traditional pixel-based SGP is adopted to complete the**

394 segmentation of multi-temporal PolSAR images, the similarity measurement matrix of 76670×76670 size
395 needs to be established through C_{76670}^2 operations, while the proposed method only needs C_{1411}^2 operations
396 to establish a similarity measurement matrix of 1411×1411 size. Thus, the requirements of computing space
397 and time are reduced by about 3000 times. It can be seen that the pre-segmentation with MS can reduce the
398 operation cost of SGP to a certain extent, and the global optimization strategy of SGP also is used to achieve
399 excellent segmentation effect.

400 3.2 Quantitative evaluation and analysis

401 In the previous section, multi-temporal MS-SGP segmentation algorithm is used to obtain the
402 segmentation results of multi-temporal PolSAR images. In order to evaluate the segmentation algorithm
403 more objectively, a quantitative method is used to evaluate the pros and cons of the segmentation results.
404 Firstly, the accuracy of the segmentation results of multi-temporal PolSAR images are evaluated based on
405 the obtained segmentation reference images (Fig. 2), as shown in Fig. 14. It is calculated that when $USR =$
406 0.3 , the segmentation accuracy of multi-temporal PolSAR image is 86.5%. Fig. 14 is a distribution diagram
407 of correctly segmentation pixels in multi-temporal PolSAR images. Among them, the yellow region is the
408 pixel of correct segmentation, the indigo region is the pixel of wrong segmentation, and the blue region is
409 the pixel that do not participate in segmentation evaluation. It can be seen that the multi-temporal MS-SGP
410 segmentation algorithm proposed in this paper can achieve preferable segmentation results. The farmland
411 parcel unit of the experimental region can be segmented relatively completely, making it an independent
412 farmland parcel object. The regional consistency is excellent, which lays a good foundation for the next
413 image interpretation.

414 **Figure 14.** Correct segmentation pixel distribution map of multi-temporal PolSAR image. ($USR=0.3$). The segmentation
415 accuracy is 86.5%.

416 In order to clarify the influence of the parameter setting of each link on the segmentation accuracy of
417 the multi-temporal MS-SGP segmentation algorithm proposed in this paper, the variation of segmentation
418 accuracy with the number of final segmentation regions and the number of MS over-segmentation regions
419 is analyzed, as shown in Fig. 15 and 16. Finally, in order to further discuss the influence of the choice of
420 temporal on the segmentation accuracy, the segmentation accuracy of different combinations of single-
421 temporal and multi-temporal is compared, as shown in Fig. 17. Based on the above analysis, users can fully
422 understand the performance of the algorithm.

423 The trend of the segmentation accuracy of the multi-temporal MS-SGP segmentation algorithm with
424 the number of final segmentation regions is shown in Fig. 15. Except for the different settings of the final
425 number of segmentation regions, the other parameter settings are consistent with those in Fig. 10. It can be
426 seen that when the number of regions is in the range of 20-40, the segmentation accuracy shows an
427 increasing trend with the increase of the number of regions. Then it reached a peak and stabilized in the
428 range of 40-120 regions, and then showed a downward trend. It can be seen that the segmentation effect is
429 the best and stable when the number of regions in the map is in the range of 40-120, which is the

430 segmentation scale that users can choose. In addition, Fig. 15 also verifies that the segmentation evaluation
431 index used in this article can reflect both over-segmentation and under-segmentation. Whether the number
432 of regions is too small or too many, the segmentation accuracy will be low.

433 **Figure 15.** Segmentation accuracy of multi-temporal MS-SGP segmentation algorithm changes with the number of
434 regions.

435 The trend of the segmentation accuracy of the multi-temporal MS-SGP segmentation algorithm with
436 the number of merged MS over-segmentation regions is shown in Fig. 16. Except for the different number
437 of merged MS over-segmentation regions, the other parameter settings are the same as those in Fig. 13. It
438 can be seen that the segmentation accuracy exhibits a fluctuating growth trend with the increase of the
439 number of regions and stabilizes after reaching a peak. It shows that the number of regions in the over-
440 segmentation stage of MS should not be too small, and it is necessary to avoid the impact of under-
441 segmentation on the subsequent segmentation effect. The specific parameter setting should firstly ensure
442 the realization of over-segmentation, and secondly consider the influence of the number of regions on the
443 operation cost.

444 **Figure 16.** Segmentation accuracy of multi-temporal MS-SGP segmentation algorithm changes with the merging
445 number of MS over-segmentation regions.

446 The variation trend of segmentation accuracy in the combination of temporal is shown in Fig. 17. The
447 temporal data are three images acquired on May 23, August 3, and August 27, 2013. Except for the different
448 temporal combination, the other parameter settings are the same as those in Fig. 10 and Fig. 13. It can be
449 seen that the segmentation accuracy of the two-date combination is greater than that of the single-temporal,
450 but is less than the segmentation accuracy of the three temporal combination. This shows that the addition
451 of multi-temporal information can effectively improve the segmentation accuracy and obtain the ideal
452 segmentation effect.

453 **Figure 17.** Segmentation accuracy with different temporal combination.

454 *3.3 Comparison and analysis of single-temporal segmentation results*

455 In order to further verify the effectiveness of the proposed method, the single-temporal MS-SGP
456 segmentation algorithm is used to segment three temporal PolSAR images. Furthermore, the segmentation
457 results of multi-temporal MS-SGP segmentation algorithm and single-temporal MS-SGP segmentation
458 algorithm are compared and analyzed. For the single-temporal PolSAR image, the representative pixels of
459 spatial position of over-segmentation region (Fig. 11. a-c) and edge information (Fig. 12. a-c) of three
460 temporal were used as input of SGP. The number of segmentation regions in the final SGP is consistent
461 with that in Fig. 13, which is 47. The results are shown in Fig. 18.

462 **Figure 18.** Segmentation results of single-temporal PolSAR images. The number of segmentation regions is set to 47.
463 (a) 20130523, N=47; (b) 20130803, N=47; (c) 20130827, N=47.

464 Figure 18.a shows the segmentation results of the first temporal (20130523) PolSAR image. Due to the

465 most crops had just been sown when the images were obtained in this period, the backscattering in this
466 region was mainly soil surface scattering. Therefore, it is easy to be segmented when the difference of soil
467 backscattering coefficient between different farmland parcels is large. As shown by the farmland parcel in
468 the black rectangle, it has different color representations from the surrounding field parcels, and the
469 difference is obvious. At this time, the farmland parcel has been well segmented and has become an
470 independent object. However, the farmland parcels at the same location in the two temporal images of Fig.
471 18.b and Fig. 18.c are not segmented. The reason is that the rape in the two images is in the filling stage and
472 mature stage respectively, growing well and the vegetation structure is similar. A large region of rape
473 planting farmland parcels have similar backscattering coefficients and have the same color representation
474 on images. However, the ridge that actually distinguishes the boundary of the farmland parcels can't be
475 reflected in the image due to its limited width (about 0.5m) (Zou, Li & Tian, 2014). Therefore, it is not
476 possible to effectively segment different field parcel units based on single-temporal PolSAR images.

477 Although the region in the yellow rectangle in Fig. 18.a contains two types of ground targets, rape and
478 shrubs. However, due to the small difference of backscattering coefficient and similar color representation
479 of soil surface in this area, its separability is poor and it can't be effectively segmented. On the other hand,
480 the rape and shrub in the same region of the two images of Fig. 18.b and Fig. 18.c were well segmented,
481 because that rape grows vigorously in these two images, and its backscattering is stronger, which is
482 obviously higher than other ground targets. At this time, the backscattering coefficients of ground targets
483 and their color representations in images are quite different between rape and shrub, so rape and shrub
484 can be well separated.

485 **Figure 19.** Correct segmentation pixel distribution map of single-temporal PolSAR image. (USR=0.3). The segmentation
486 accuracy are 42.4%, 43.8% and 21.8%, respectively.

487 Based on the obtained segmentation reference images (Fig. 2), the accuracy of segmentation results of
488 single-temporal PolSAR images is evaluated, as shown in Fig. 19. It is calculated that when $USR = 0.3$, the
489 segmentation accuracy of single-temporal PolSAR image are 42.4%, 43.8% and 21.8%, respectively. It can
490 be seen that the segmentation results of single-temporal PolSAR images show a large area of wrong
491 segmentation, and the final segmentation accuracy is poor. It can be seen that the segmentation effect of
492 the multi-temporal MS-SGP segmentation algorithm proposed in this paper (Fig. 14) is better than that of
493 the single-temporal MS-SGP segmentation algorithm.

494 It is not difficult to see from Fig. 18 and Fig. 19. In each period of images, the difference of surface
495 scattering, secondary scattering and volume scattering between two types of objects or multiple types of
496 objects is small, so it is difficult to effectively identify all objects by using single-temporal PolSAR images
497 (Deng et al., 2014). Through the segmentation of multi-temporal PolSAR images, it is found that the
498 backscattering coefficients of some two types of objects may be close in one period of images, but quite
499 different in the other period of images. Therefore, it is beneficial to improve the segmentation accuracy to
500 try to combine multi-stage images and make comprehensive use of the characteristics of images in different
501 periods for multi-temporal MS-SGP segmentation. At the same time, it can distinguish the planting time
502 sequence information and the growth status information of the ground **targets** which cannot be identified

503 in the traditional algorithm, which is of great significance for the monitoring of crops.

504 **4. Discussion**

505 Under the technical framework of SGP, this paper proposes a new algorithm for multi-temporal
506 PolSAR image segmentation, which is used to solve the segmentation problems in some specific difficult
507 scenes which can't be realized by single-temporal PolSAR image segmentation algorithm. Furthermore,
508 through the same type of comparative experiments between the previously proposed single-temporal MS-
509 SGP segmentation algorithm by Zhao et al. (2015) and the multi-temporal MS-SGP segmentation algorithm
510 proposed in this paper, the effectiveness of the proposed algorithm is verified. The experimental results
511 show that the optimal segmentation is realized based on multi-temporal PolSAR images and combined
512 with the global optimization of SGP algorithm. Thereby solving the problem that single-temporal PolSAR
513 images and the super-pixels generated by local optimization algorithms both can't meet the needs of
514 agricultural production. This lays a good foundation for the further interpretation of multi-temporal
515 PolSAR image.

516 The algorithm constructs an edge detector based on the Wishart statistical distribution of polarization
517 covariance data and hypothesis testing, and extracts the edge information of PolSAR image as the
518 segmentation clue of SGP. Compared with the method proposed by Ersahin, Cumming & Ward (2010) to
519 extract edge information by selecting amplitude or intensity images with different polarization channels
520 and using edge detection operator, the proposed edge extraction algorithm can make full use of the full
521 polarization information of PolSAR images. Among them, the strength of edge information depends on the
522 difference of polarization information between targets. For single-temporal PolSAR images, there are cases
523 in which different targets show similar polarization characteristics, and mis-segmentation is easy to occur
524 when the edge information is weak. At this time, based on multi-temporal PolSAR images, the scattering
525 characteristics of ground targets in different growth periods can be obtained, which can solve the above
526 problems. In other words, this paper fuses the edge information of single-temporal PolSAR images to make
527 them get useful supplement to each other, so as to obtain more complete and clear edge fusion results than
528 any single-temporal PolSAR images, which can be used as the segmentation clue of subsequent multi-
529 temporal PolSAR images SGP. The targets which can't be distinguished by single-temporal PolSAR image
530 segmentation algorithm can be segmented. However, this method also has some shortcomings. The
531 registration accuracy of multi-temporal PolSAR images directly affects the result of edge fusion. In
532 addition, this process will inevitably introduce some noise problems, so that the multi-temporal edge
533 fusion results have a certain degree of "pepper and salt" phenomenon, which is also reflected in the final
534 segmentation results (Fig. 13). Therefore, in the next research, texture and spatial features should be
535 comprehensively considered, so as to explore whether the introduction of other features is helpful to the
536 segmentation of multi-temporal PolSAR images.

537 In this paper, the experiment of multi-temporal MS-SGP segmentation of crops with time series
538 changing characteristics was carried out by using three temporal Radarsat-2 images. Compared with the
539 local optimization segmentation algorithms such as level set (Zou, 2015), simple nonlinear iterative
540 clustering (Ma et al, 2021) and binary partition trees (Alonso-Gonzalez, Lopez-Martinez & Salembier, 2014)

541 currently applicable to multi temporal PolSAR images, the proposed algorithm makes use of the
542 advantages of SGP algorithm, which can cluster in arbitrary shape sample space and converge to the global
543 optimal solution, the optimal segmentation of farmland parcel object to meet the needs of agricultural
544 production is realized. Although in terms of classification, change detection and other applications, the
545 super-pixels generated by the local optimization algorithm have met the application requirements.
546 However, for agricultural applications, as the smallest unit of farmers' production and management,
547 accurate identification of farmland parcels is conducive to the realization of crop production planning,
548 management and benefit evaluation. However, the shape feature of the over-segmented object based on
549 homogeneous pixel clustering is not meaningful, nor does it have any social attributes, that is, it is not
550 convenient for production and application; In addition, the polarization features extracted from farmland
551 parcel units can avoid the influence of outliers caused by mixed pixels and internal variation, and are more
552 accurate than those extracted by over-segmented objects. Thus, it is more beneficial to carry out
553 applications such as crop target identification. Many studies have also shown that the parcel-oriented crop
554 classification method has higher classification accuracy than the over-segmented object-oriented
555 classification method. Therefore, according to the characteristics of crop planting structure, many scholars
556 adopt the classification method of taking farmland parcel as the basic unit to improve the classification
557 accuracy. However, how to determine the optimal segmentation result still needs to select its relevant
558 parameters according to experience. Although the setting range of related parameters is relatively wide, it
559 still needs to go through a certain degree of attempt and comparison to achieve the optimal segmentation
560 effect. Therefore, how to choose the optimal parameter configuration according to the image characteristics
561 or develop a segmentation algorithm with adaptive parameters is the focus of in-depth research.

562 However, due to the difficulty of obtaining real verification data of multi-temporal PolSAR images,
563 this paper is only discussed in a relatively small study area. In the follow-up, we will try to extend the
564 algorithm to the practical application of large areas, which is of great significance and value to solve the
565 problems of farmland parcel boundary extraction and target recognition in large crop planting areas.
566 However, the application of this algorithm to a large research area will bring high computational cost to a
567 certain extent, so it is necessary to use a high-performance computer or block the image. Moreover, more
568 prior knowledge will be needed to determine the correlative parameter. In addition, there will be higher
569 requirements for the registration accuracy of multi-temporal PolSAR images, so as to avoid excessive
570 influence of "salt and pepper" phenomenon on the results of multi-temporal edge fusion. Therefore, the
571 application of the algorithm to large research areas is the focus of in-depth research in the future.

572 5. Conclusions

573 Aiming at the problem that the single-temporal PolSAR image segmentation algorithm is difficult to
574 provide correct segmentation results for applications such as target recognition and time series analysis of
575 ground targets with time series changes. This paper proposes a new algorithm for multi-temporal PolSAR
576 image segmentation, and uses the three temporal Radarsat-2 PolSAR data to verify the effectiveness of this
577 algorithm. The experimental results show that the multi-temporal MS-SGP segmentation algorithm
578 proposed in this paper comprehensively utilizes the abundant ground targets polarimetric and temporal

579 information of multi-temporal PolSAR images. The algorithm can segment the ground **targets** that can't be
580 distinguished using single-temporal PolSAR images and realize the accurate identification of farmland
581 parcel units. At the same time, the segmentation accuracy of this method reaches 86.5%, which is
582 significantly improved compared with the single-temporal PolSAR image segmentation accuracy, and the
583 segmentation result is closer to the segmentation result of reference image.

584 **The algorithm proposed in this paper still has some shortcomings, such as the selection of optimal**
585 **parameters in the whole segmentation algorithm, the applicability of the algorithm, and whether other**
586 **features can be introduced, which need to be further studied.**

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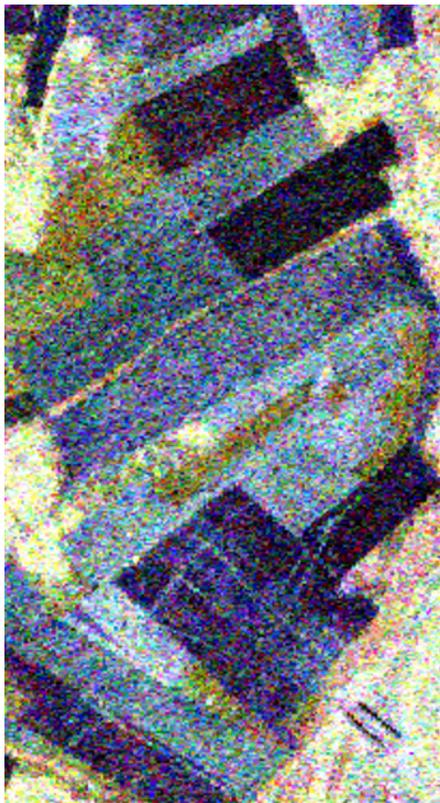
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Figure 1

Pauli RGB display of PolSAR data at different temporal in experimental region.

The data are three temporal PolSAR images of Radarsat-2 (C-band) acquired on May 23, August 3, and August 27, 2013, respectively. (a) 20130523, (b) 20130803, (c)20130827.



a



b



c

Figure 2

Reference map for Segmentation Evaluation .

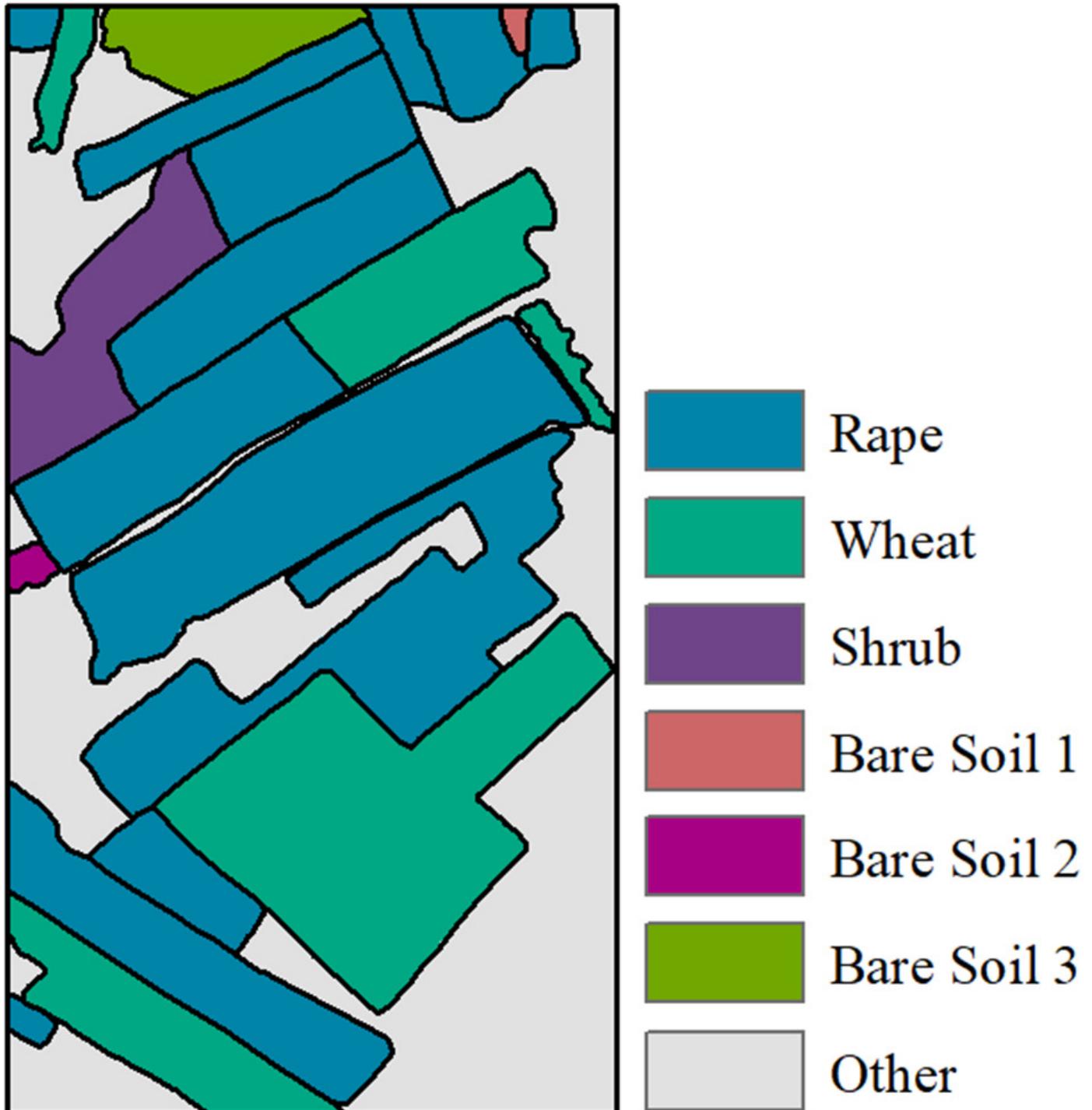


Figure 3

Technical flow chart of multi-temporal MS-SGP segmentation algorithm.

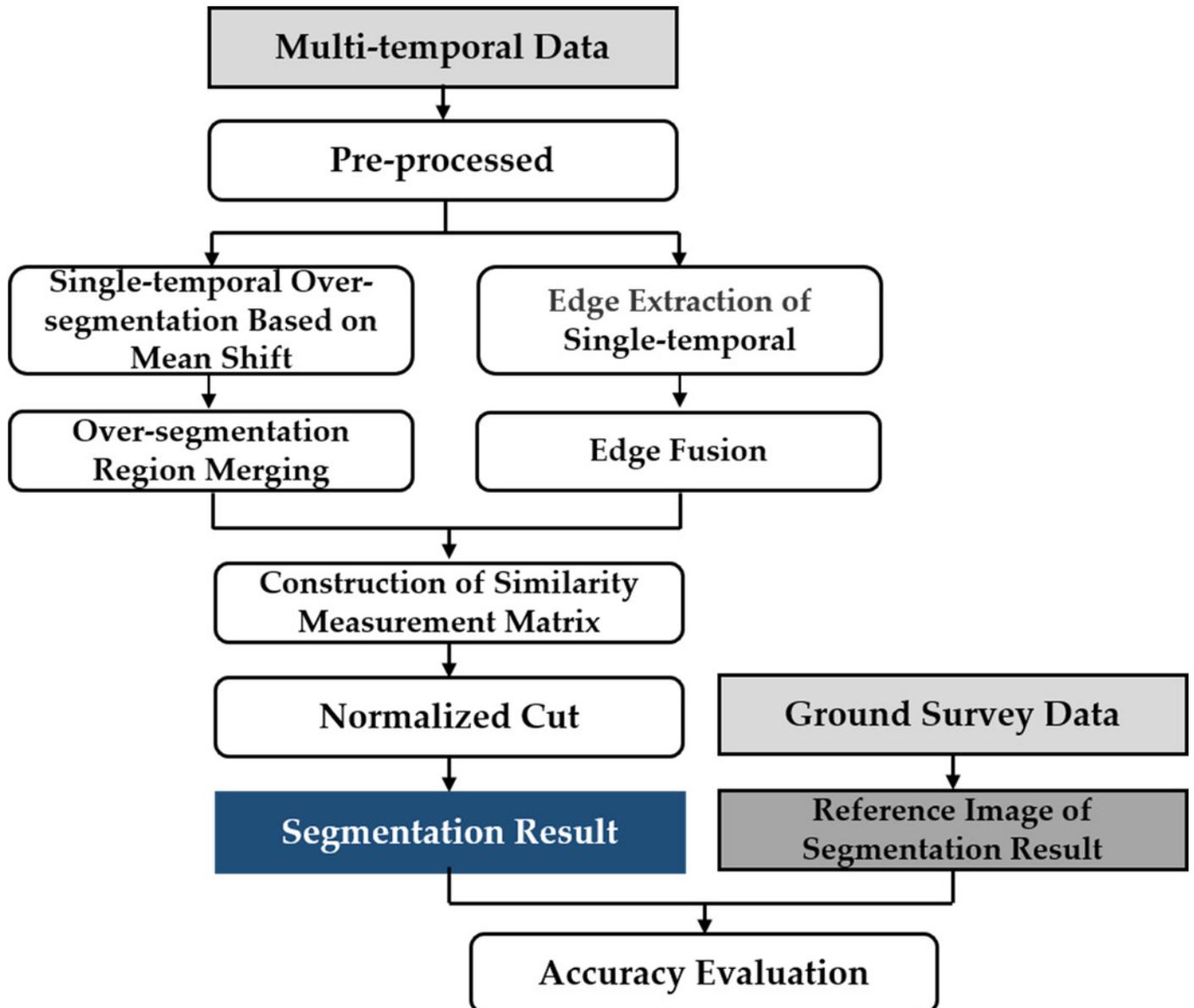


Figure 4

Schematic diagram of merging over-segmentation regions of multi-temporal PolSAR images.

(a) Over-segmentation regions of single-temporal image A (4 regions). (b) Over-segmentation regions of single-temporal image B (3 regions). (c) Merging results of multi-temporal images (8 regions).

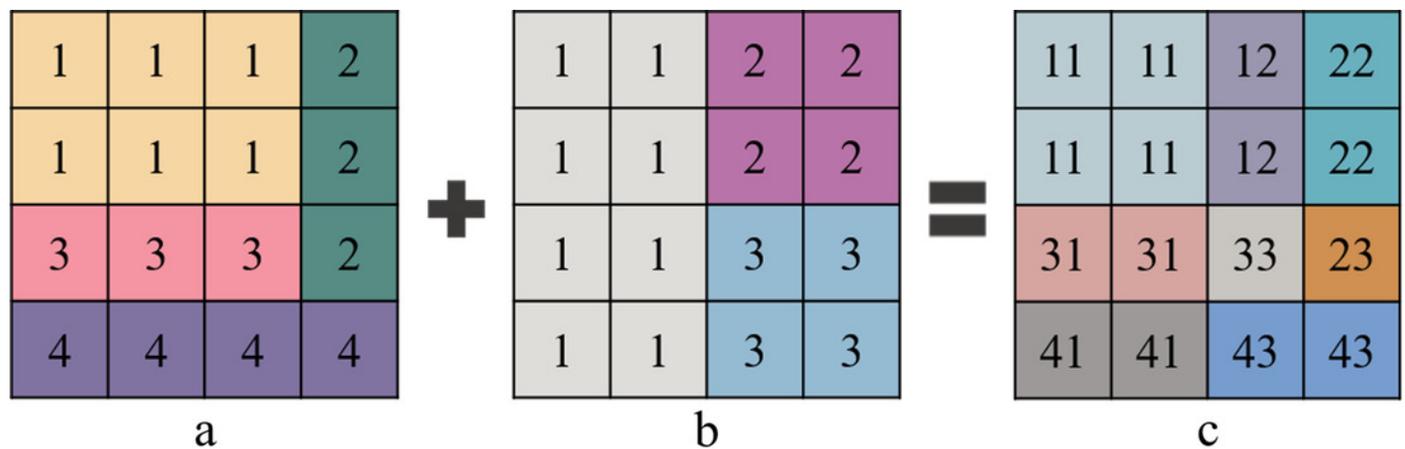


Figure 5

Schematic diagram of edge detector.

Edge detectors are set in four directions. (a) 0° direction, (b) 45° direction, (c) 90° direction, (d) 135° direction.

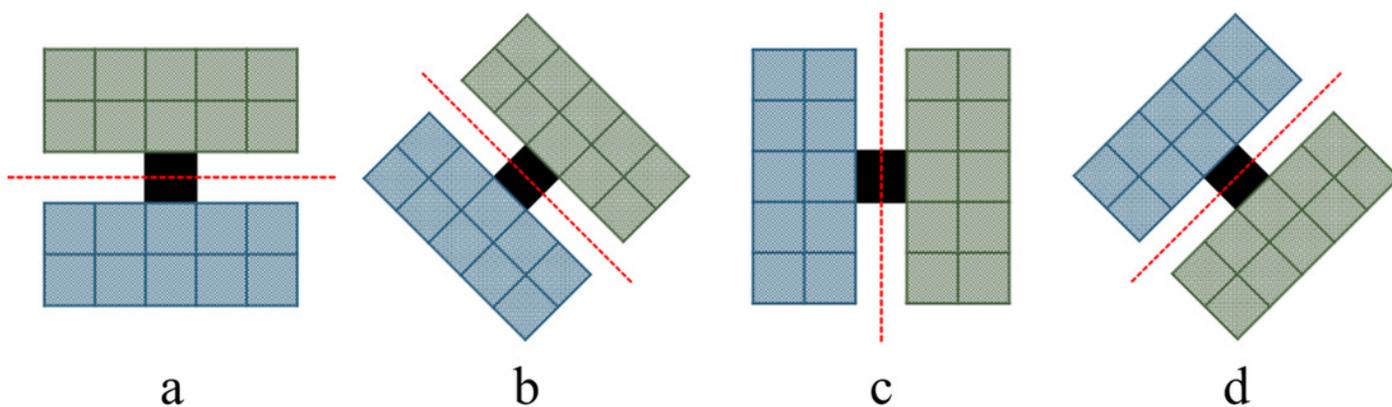


Figure 7

The centre location of over-segmentation regional.

S is a segmentation region, p is the internal pixel of an over-segmentation region S , α is the azimuth angle, $L(\alpha)$ is the distance from the pixel p to the boundary of the region when the azimuth angle is α .

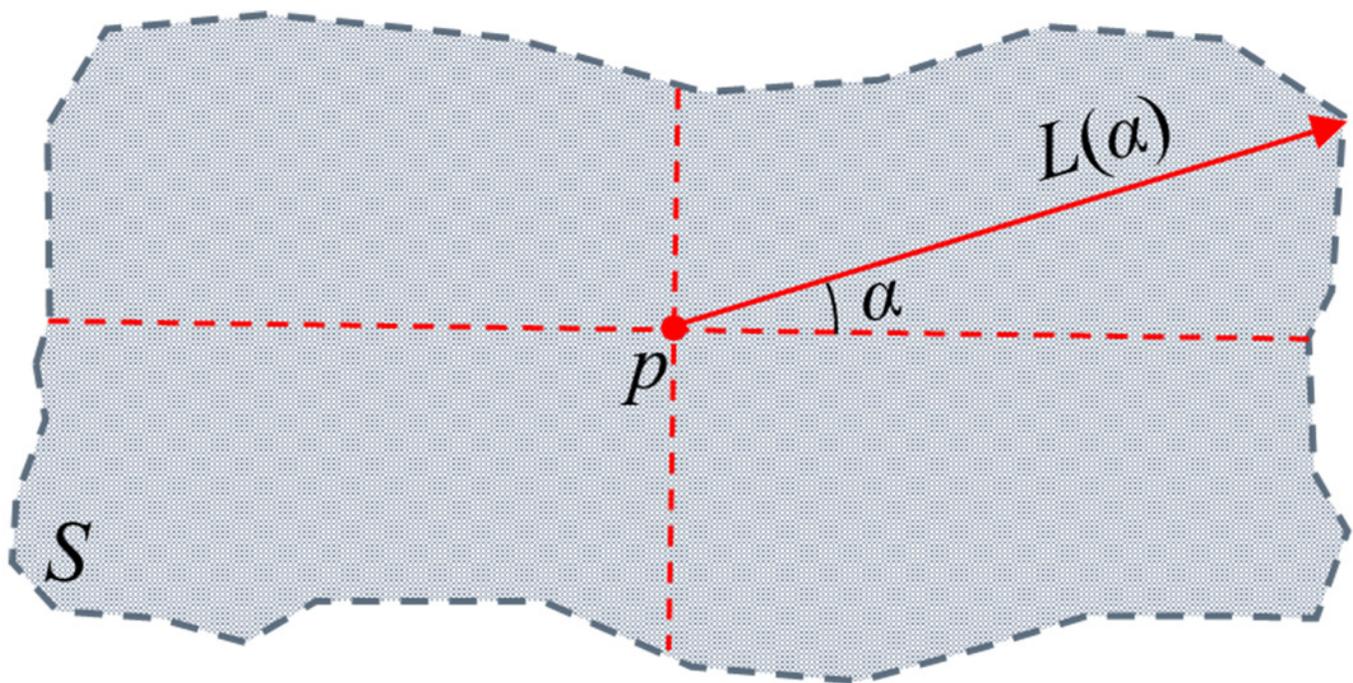
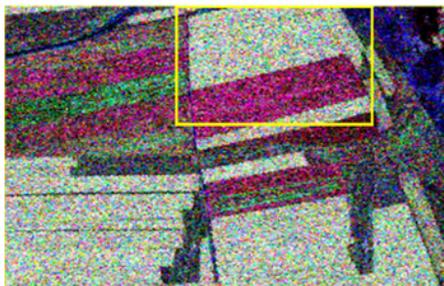


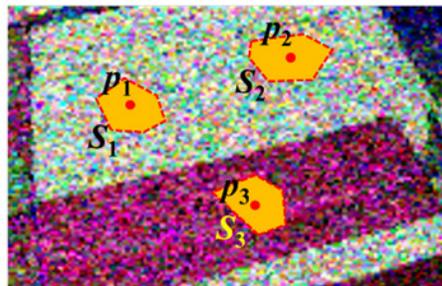
Figure 8

Illustration of extracting the dissimilarity information from edge maps.

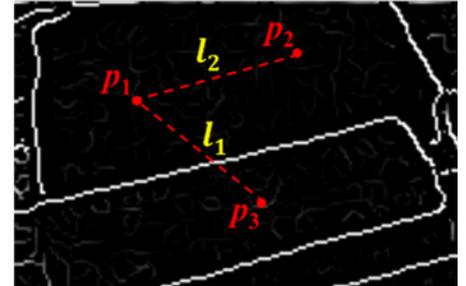
(a) A subset of a C-band PolSAR image (Pauli RGB). (b) Part of the original image marked by the box; S_1 , S_2 and S_3 are three over-segmentation regions; p_1 and p_2 are in the same class, and p_1 and p_3 are in different classes. (c) Edge map of image (b) after the oriented nonmaximal suppression; somewhere along l_1 , the value of edge map strength is high, which suggests that p_1 and p_3 are in different classes; along l_2 , the values of edge map strength are all low, proposing that p_1 and p_2 are probably in the same class.



a



b



c

Figure 9

Illustration chart of segmentation evaluation principle.

SS is the reference segmentation region; A , B and C are the segmentation regions, respectively; A_{SS} is the region with the largest overlapping area between the segmentation region A to be evaluated and the reference segmentation region SS .

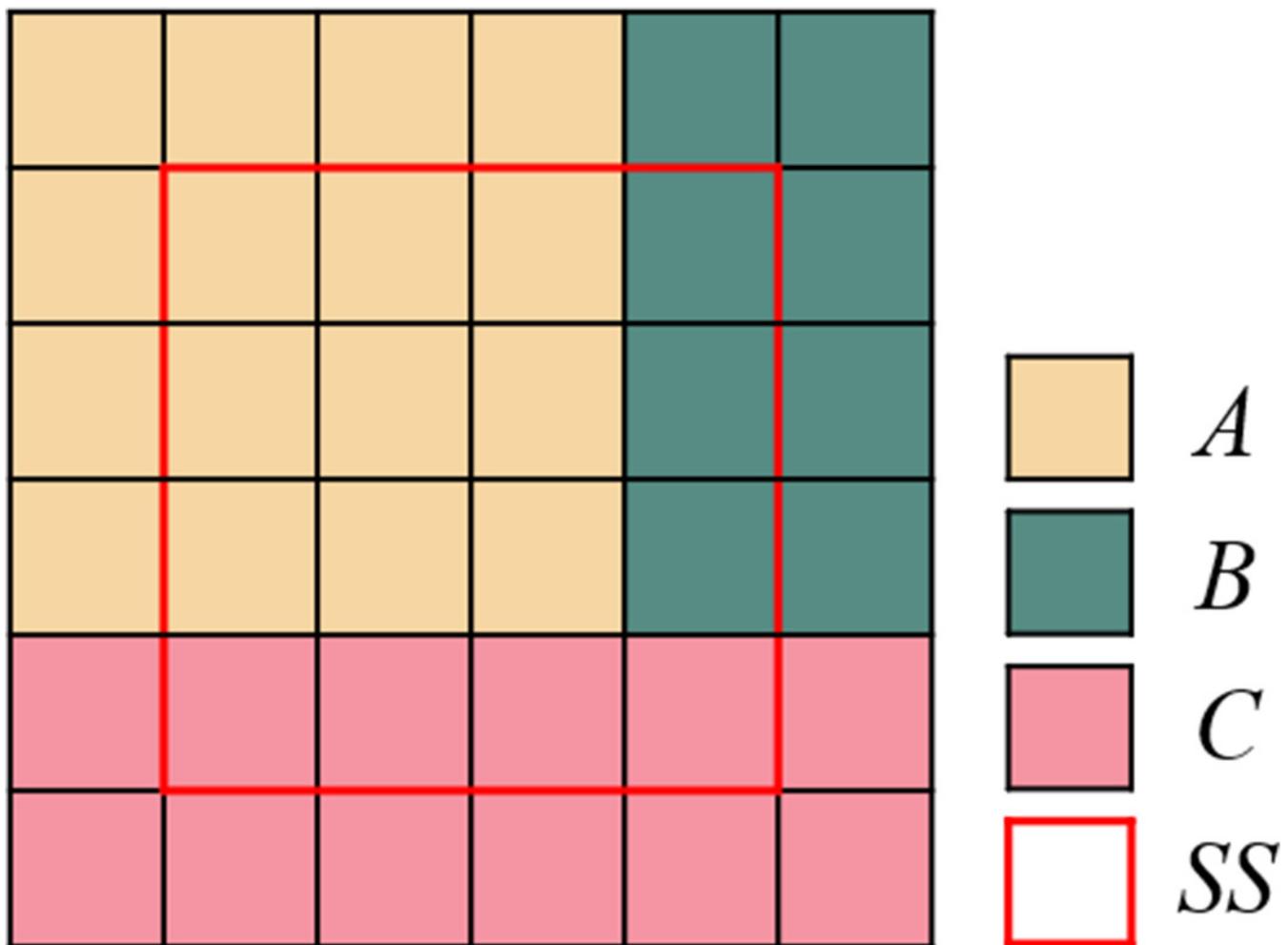


Figure 10

MS pre-segmentation results of single-temporal PolSAR images and merging results of multi-temporal segmentation regions.

The h_s and h_r of the three temporal are set to 7 and 6.5, respectively; M is set to 235, 235 and 192, respectively; and the number of blocks in the over-segmentation region of MS is 118, 102 and 111, respectively. Fig. 10.d shows the merging results of multi-temporal segmentation regions is 1411, and the Pauli RGB of 20130803 is used as the display image.

(a) 20130523, $h_s = 7$, $h_r = 6.5$, $M=235$, $N=118$; (b) 20130803, $h_s = 7$, $h_r = 6.5$, $M=235$, $N=102$; (c) 20130827, $h_s = 7$, $h_r = 6.5$, $M=192$, $N=111$; (d) multi-temporal, $N=1411$.

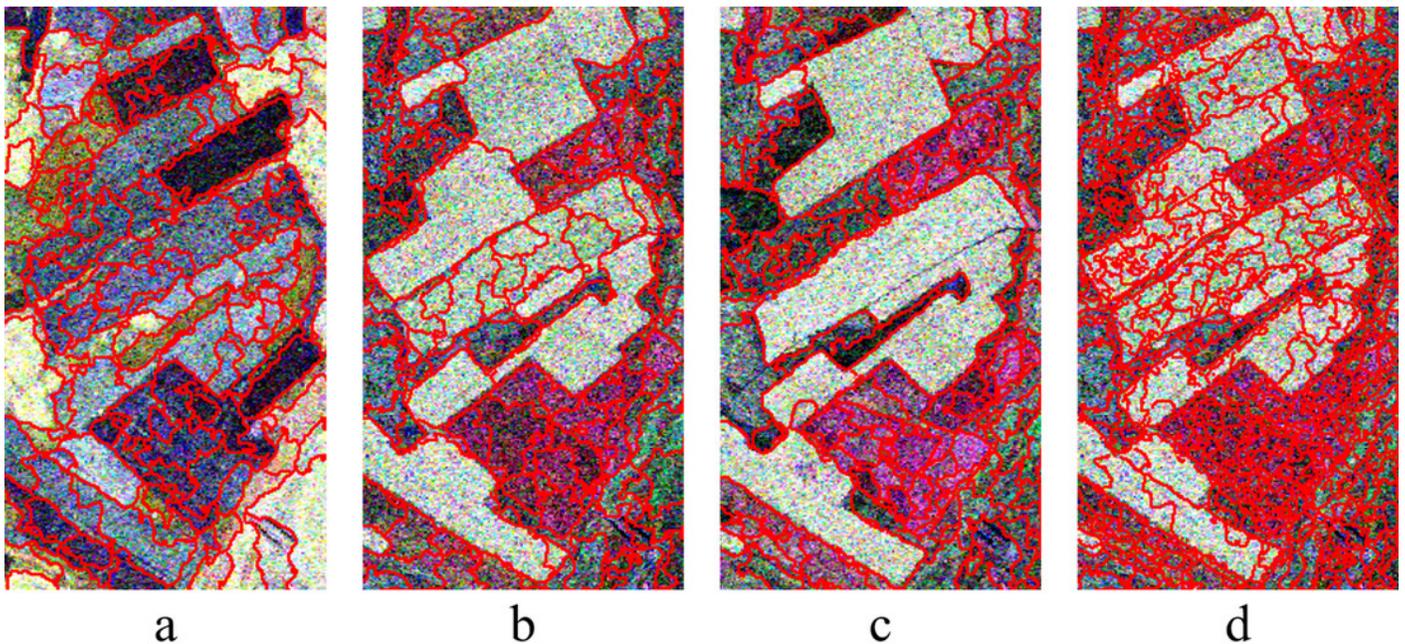


Figure 11

Over-segmentation regional center of single-temporal and multi-temporal PolSAR images.

(a) 20130523; (b) 20130803; (c) 20130827; (d) multi-temporal.

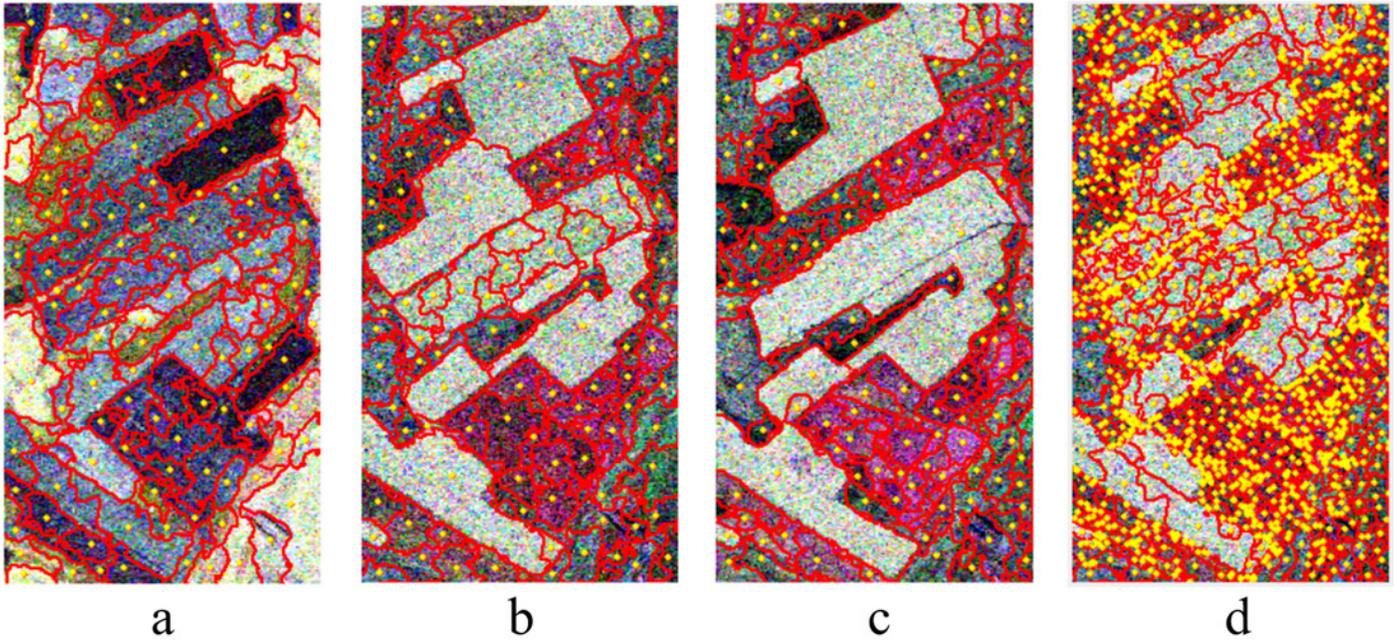


Figure 12

Single-temporal PolSAR image edge extraction results and multi-temporal edge fusion results.

(a) 20130523; (b) 20130803; (c) 20130827; (d) multi-temporal edge fusion results.

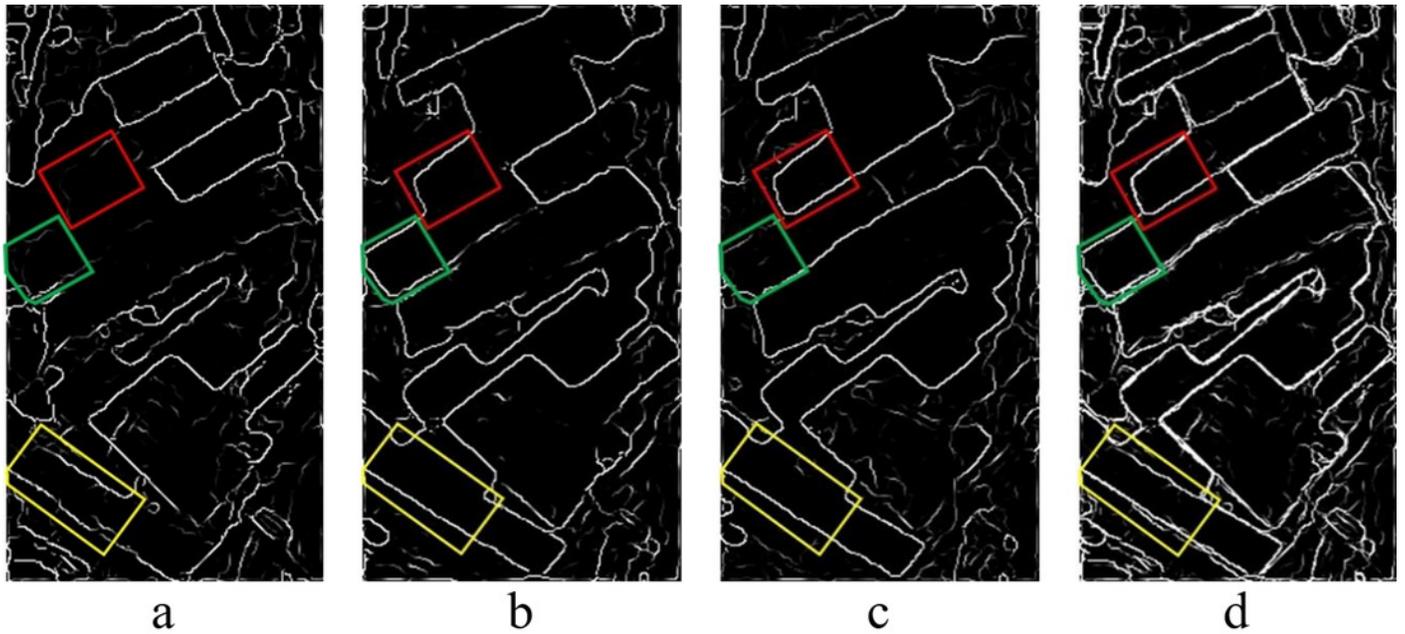


Figure 13

Segmentation results of multi-temporal PolSAR images.

The number of segmentation regions is set to 47. (a) 20130523, N=47; (b) 20130803, N=47; (c) 20130827, N=47.

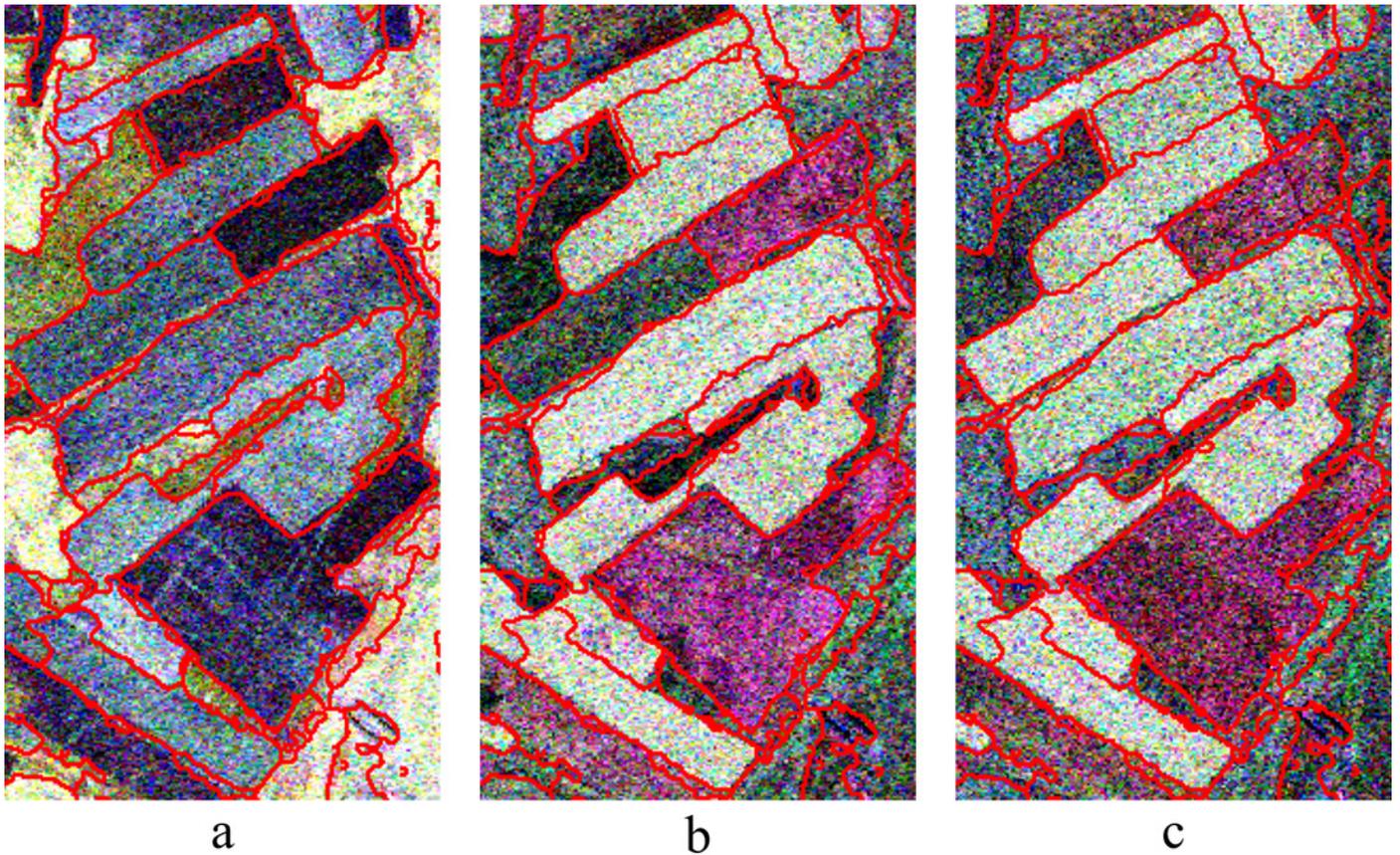


Figure 14

Correct segmentation pixel distribution map of multi-temporal PolSAR image.
(USR=0.3).

The segmentation accuracy is 86.5%.

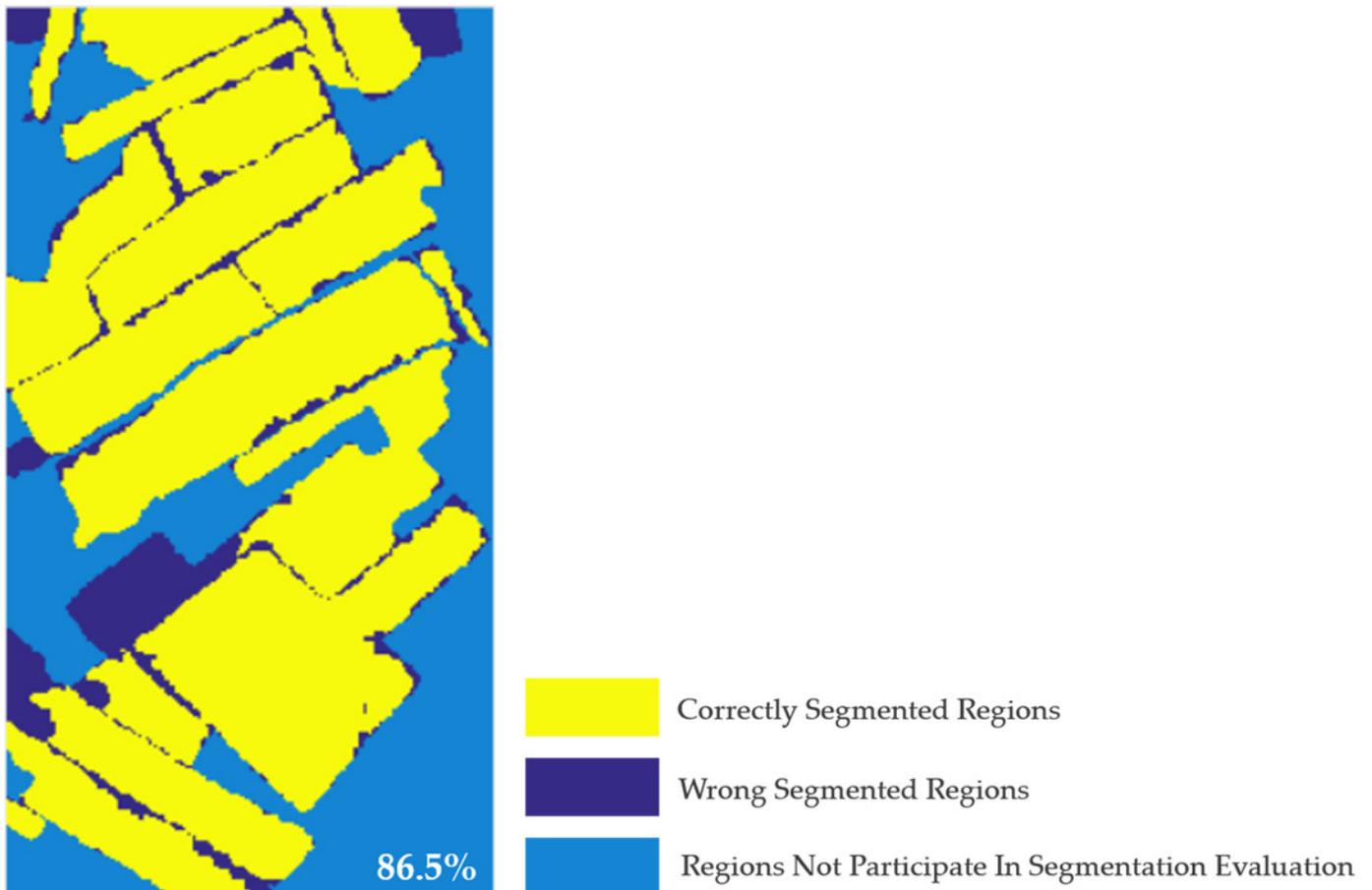


Figure 15

Segmentation accuracy of multi-temporal MS-SGP segmentation algorithm changes with the number of regions.

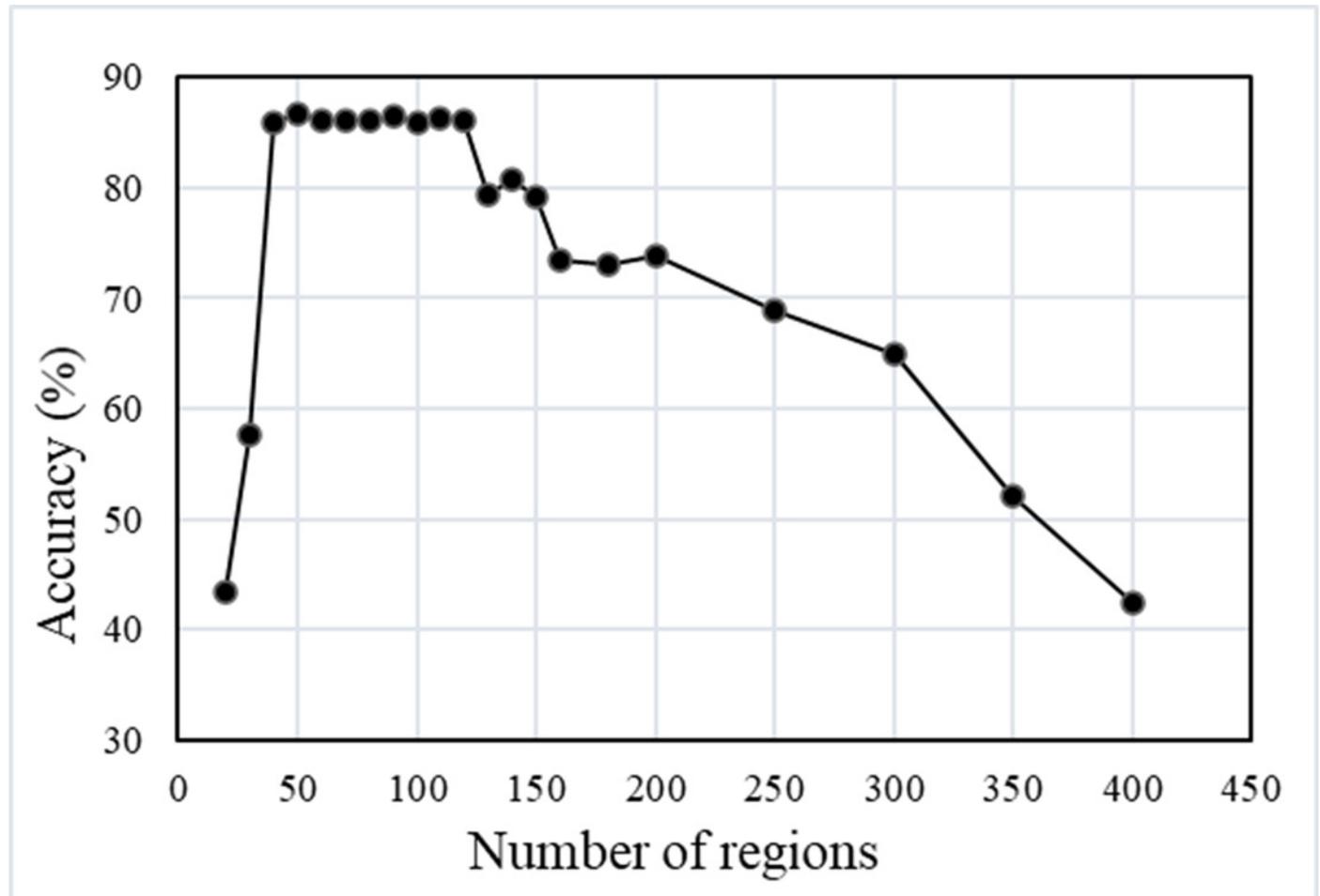


Figure 16

Segmentation accuracy of multi-temporal MS-SGP segmentation algorithm changes with the merging number of MS over-segmentation regions.

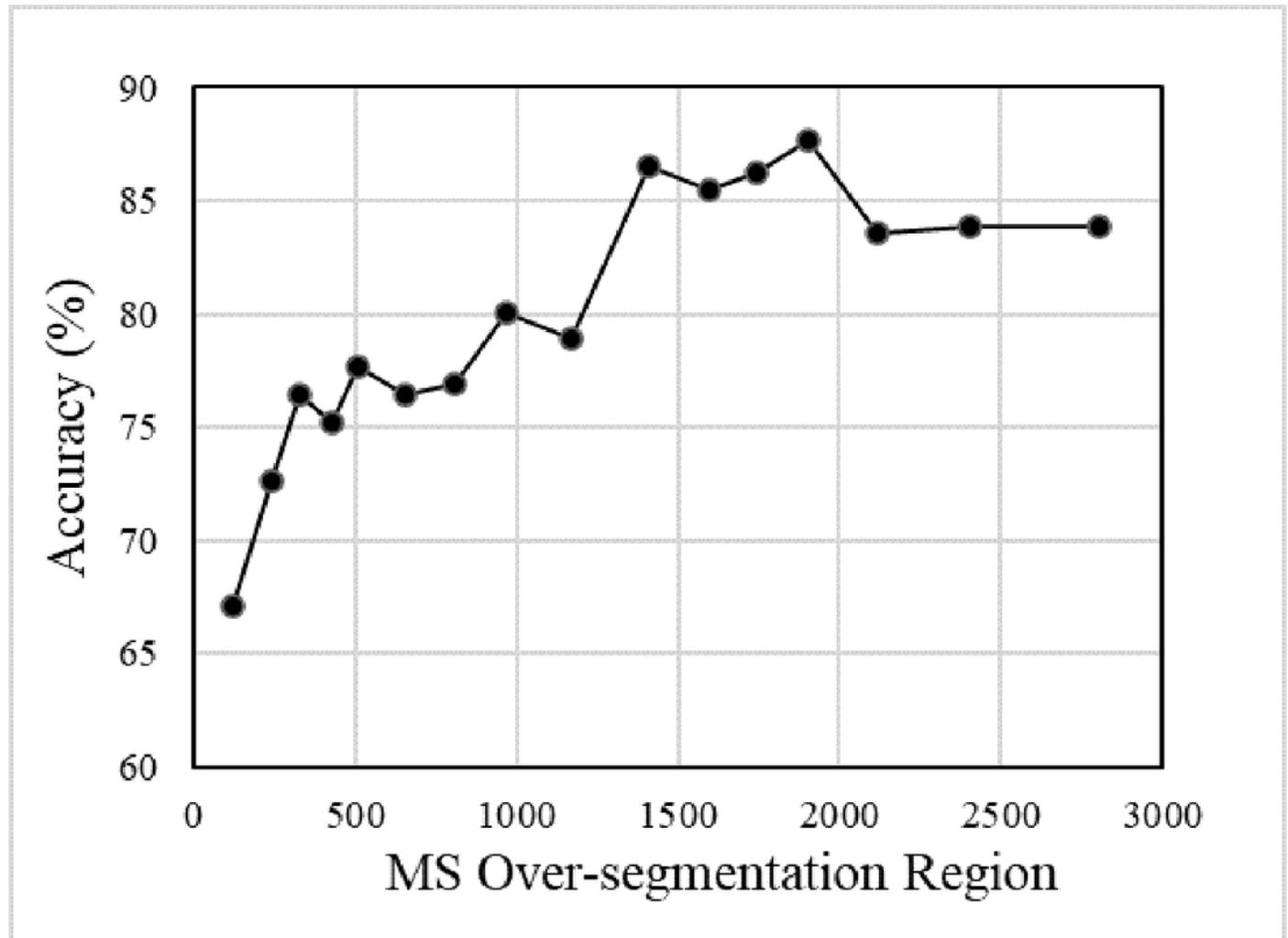


Figure 17

Segmentation accuracy with different temporal combination.

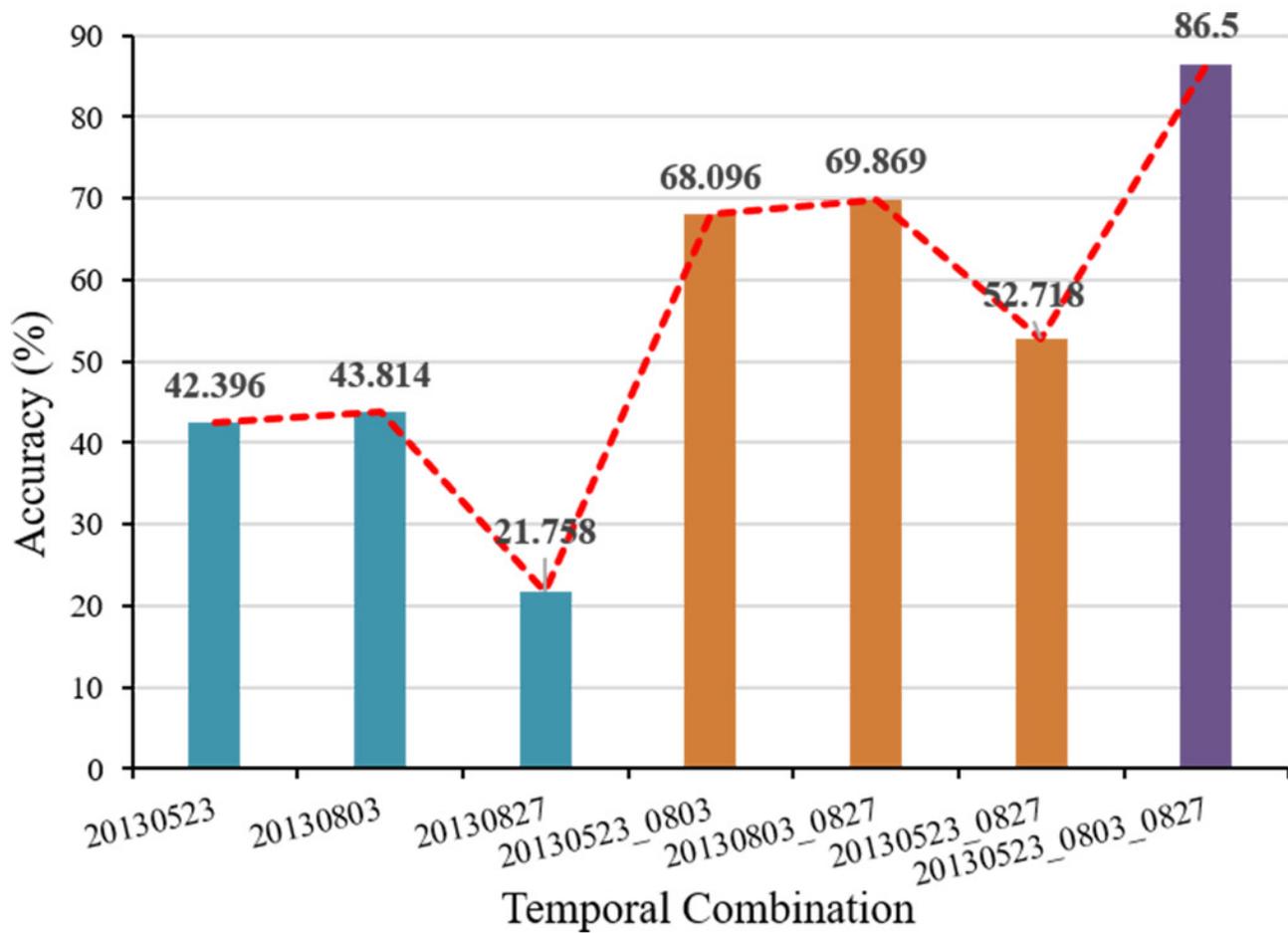


Figure 18

Segmentation results of single- temporal PolSAR images.

The number of segmentation regions is set to 47. (a) 20130523 , N=47; (b) 20130803, N=47; (c) 20130827, N=47.

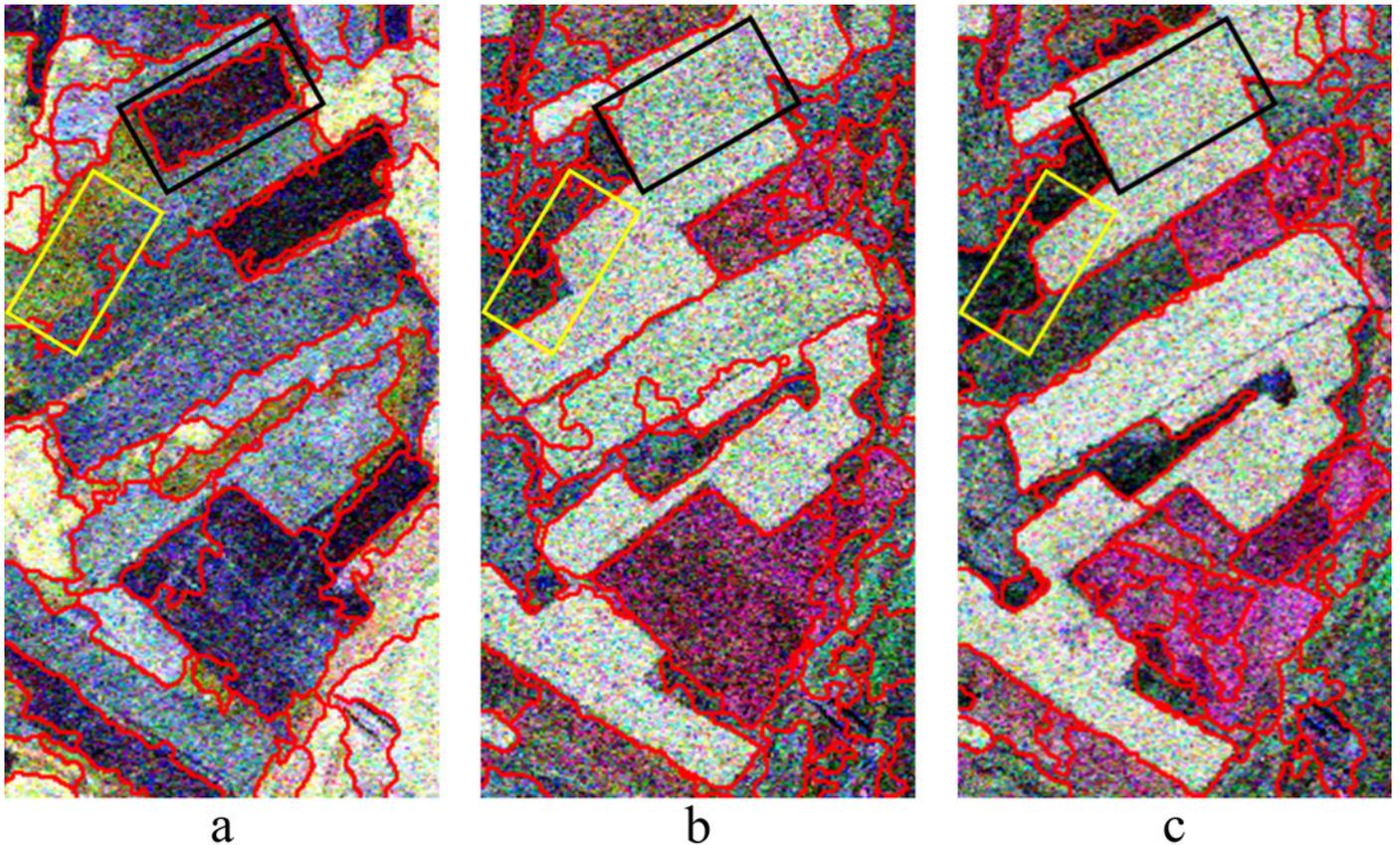


Figure 19

Correct segmentation pixel distribution map of single-temporal PolSAR image. (USR=0.3).

The segmentation accuracy are 42.4%, 43.8% and 21.8%, respectively.

