

Predicting continuous ground reaction forces from accelerometers during uphill and downhill running: A recurrent neural network solution

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Background. Ground reaction forces (GRFs) are important for understanding human movement, but their measurement is generally limited to a laboratory environment. Previous studies have used neural networks to predict GRF waveforms during running from wearable device data, but these predictions are limited to the stance phase of level-ground running. A method of predicting the normal (perpendicular to running surface) GRF waveform using wearable devices across a range of running speeds and slopes could allow researchers and clinicians to predict kinetic and kinematic variables outside the laboratory environment.

Purpose. We sought to develop a recurrent neural network capable of predicting continuous normal (perpendicular to surface) GRFs across a range of running speeds and slopes from accelerometer data.

Methods. 19 subjects ran on a force-measuring treadmill at five slopes (0° , $\pm 5^\circ$, $\pm 10^\circ$) and three speeds (2.5, 3.33, 4.17 m/s) per slope with sacral- and shoe-mounted accelerometers. We then trained a recurrent neural network to predict normal GRF waveforms frame-by-frame. The predicted versus measured GRF waveforms had an average \pm SD RMSE of 0.16 ± 0.04 BW and relative RMSE of $6.4 \pm 1.5\%$ across all conditions and subjects.

Results. The recurrent neural network predicted continuous normal GRF waveforms across a range of running speeds and slopes with greater accuracy than neural networks implemented in previous studies. This approach may facilitate predictions of biomechanical variables outside the laboratory in near real-time and improves the accuracy of quantifying and monitoring external forces experienced by the body when running.

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19

20 **Abstract**

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22 but their measurement is generally limited to a laboratory environment. Previous studies have
23 used neural networks to predict GRF waveforms during running from wearable device data, but
24 these predictions are limited to the stance phase of level-ground running. A method of predicting
25 the normal (perpendicular to running surface) GRF waveform using wearable devices across a
26 range of running speeds and slopes could allow researchers and clinicians to predict kinetic and
27 kinematic variables outside the laboratory environment.

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30 normal (perpendicular to surface) GRFs across a range of running speeds and slopes from
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33 **Methods.** 19 subjects ran on a force-measuring treadmill at five slopes (0° , $\pm 5^\circ$, $\pm 10^\circ$) and three
34 speeds (2.5, 3.33, 4.17 m/s) per slope with sacral- and shoe-mounted accelerometers. We then
35 trained a recurrent neural network to predict normal GRF waveforms frame-by-frame. The
36 predicted versus measured GRF waveforms had an average \pm SD RMSE of 0.16 ± 0.04 BW and
37 relative RMSE of $6.4 \pm 1.5\%$ across all conditions and subjects.

38

39 **Results.** The recurrent neural network predicted continuous normal GRF waveforms across a
40 range of running speeds and slopes with greater accuracy than neural networks implemented in
41 previous studies. This approach may facilitate predictions of biomechanical variables outside the
42 laboratory in near real-time and improves the accuracy of quantifying and monitoring external
43 forces experienced by the body when running.

44 Introduction

45 Ground reaction forces (GRFs) are applied to the body when the foot is in contact with the
46 ground and their measurement has facilitated numerous insights into the etiology of running-
47 related injuries (Ceysens et al., 2019). However, measurement of GRFs is generally restricted to
48 a laboratory environment. To determine the effects of sport-specific environments on running
49 kinetics and kinematics, previous studies have replicated aspects of an athlete's competitive
50 environment (e.g., running surface, slope) within a laboratory environment (Voloshina & Ferris,
51 2015; Kipp, Taboga & Kram, 2017; Whiting et al., 2020). Alternatively, inertial measurement
52 units (IMUs; wireless wearable devices that measure magnetism, linear acceleration, and angular
53 velocity) have been used to measure athletes' leg joint angles, stride kinematics, and segmental
54 accelerations during competitive events (Reenalda et al., 2016; Ruder et al., 2019; Clermont et
55 al., 2019). Although IMUs cannot directly measure GRFs, previous studies have used
56 algorithms to estimate discrete biomechanical variables like peak vertical GRF, ground contact
57 time, vertical impulse, and vertical loading rate (Neugebauer, Hawkins & Beckett, 2012; Kiernan
58 et al., 2018; Ancillao et al., 2018; Derie et al., 2020; Alcantara et al., 2021) from IMU data.

59
60 Recently, neural networks have been used to predict GRF waveforms during running (Wouda et
61 al., 2018; Pogson et al., 2020; Dorschky et al., 2020; Johnson et al., 2021), from which a variety
62 of discrete variables can be calculated. Although predictions of the entire GRF waveform
63 represent a more versatile outcome compared to predicting a discrete variable, previous studies
64 have used neural network architectures that required waveforms to be normalized to the duration
65 of a step (Dorschky et al., 2020) or stance phase (Wouda et al., 2018; Johnson et al., 2021).
66 Temporal normalization is typically accomplished by identifying gait events in the GRF
67 waveform and segmenting the neural network's input signals, preventing the calculation of
68 biomechanical variables with a temporal component (e.g., ground contact time, step frequency,
69 vertical impulse, and loading rate) outside the laboratory where the GRF waveform is
70 unavailable. Additionally, previous studies have predicted GRF waveforms only during level-
71 ground running (Wouda et al., 2018; Pogson et al., 2020; Dorschky et al., 2020; Johnson et al.,
72 2021), limiting the application to environments that are flat (e.g., level treadmill or athletics
73 track). Road and trail running are internationally popular forms of physical activity (Running
74 USA, 2019; International Trail Running Association, 2020) and require runners to navigate a
75 variety of uphill and downhill slopes. A method that accurately predicts GRF waveforms from
76 wearable device data across a range of running slopes, while maintaining the temporal
77 component, could allow researchers, clinicians, and coaches to measure and monitor a variety of
78 kinetic and kinematic variables in outdoor environments.

79
80 Long Short-Term Memory (LSTM) networks (Hochreiter & Schmidhuber, 1997) are a type of
81 recurrent neural network that can overcome the traditional requirement of normalizing GRF
82 waveforms to the duration of stance phase because LSTM networks can recurrently predict
83 smaller, uniform portions of a larger sequence of any length. As such, a sequence of continuous

84 GRF data can be predicted if it can be broken up into uniform portions. For the prediction of a
85 given portion, LSTM networks use information from previous portions, effectively
86 “remembering” the portion’s context and have been used to predict sequential data during natural
87 language processing tasks (Wang & Jiang, 2016). In the field of Biomechanics, LSTM networks
88 have been used to make frame-by-frame predictions of GRF waveforms using motion capture
89 data (Mundt et al., 2020) and predictions of the center of mass position relative to center of
90 pressure from IMU data during walking (Choi, Jung & Mun, 2019). Developing an LSTM
91 network to predict GRF waveforms from wearable device data would allow researchers to
92 predict GRF waveforms not only during an isolated stance phase, but continuously for multiple
93 steps or the entire duration of a run. IMUs have already been used to longitudinally measure
94 biomechanical variables (Reenalda et al., 2016; Kiernan et al., 2018; Ruder et al., 2019;
95 Clermont et al., 2019) and applying an LSTM network to such data could effectively provide a
96 way to indirectly measure continuous GRF waveforms outside of the laboratory at a scale that
97 was previously unattainable. Improving means of remotely measuring biomechanical variables
98 with wearable devices may improve a clinician’s ability to identify injury risk factors, monitor
99 rehabilitation, or develop interventions (Gurchiek, Cheney, & McGinnis, 2019).

100

101 The purpose of this exploratory study was to develop an LSTM network that could predict
102 continuous normal (perpendicular to running surface) GRF waveforms across a range of running
103 speeds and slopes using data from accelerometers. We sought to develop a network that could
104 predict GRF waveforms with accuracy better than state-of-the-art predictions of time-normalized
105 vertical GRF data during level-ground running using data from multiple IMUs: a root mean
106 square error (RMSE) of 0.21 BW (Dorschky et al., 2020) and relative RMSE (rRMSE; RMSE
107 normalized to the average range of the compared waveforms; Eq. 1) of 13.92% (Johnson et al.,
108 2021).

109

110 **Materials & Methods**

111 **Subjects**

112 We analyzed a pre-existing dataset (Baggaley et al., 2019; Khassetarash et al., 2020; Vernillo et
113 al., 2020) where 21 subjects ran at a combination of running speeds and slopes. Two subjects
114 were excluded from the current analysis due to equipment data acquisition errors, leaving 19
115 subjects remaining (10 Male, 9 Female; 29 ± 9 years, 173 ± 9 cm, 68.1 ± 9.9 kg). All subjects
116 provided informed written consent and the experimental protocol was approved by the
117 University of Calgary Conjoint Health Research Ethics Board (#REB14-1117).

118

119 **Experimental Protocol**

120 Following a 5 min warm up at a self-selected speed, each subject completed thirty 30 s trials on a
121 force-measuring treadmill (2000 Hz; Bertec, OH, USA), which included five slopes (0° , $\pm 5^\circ$,
122 $\pm 10^\circ$) at three speeds (2.5, 3.33, 4.17 m/s) per slope, and three step frequencies (preferred and \pm
123 10%) at 3.33 m/s for each slope. Three custom biaxial accelerometers (2000 Hz) were adhered

124 with tape to subjects during all conditions: two on the right shoe and one on the sacrum. The
125 accelerometers on the shoe were only used to determine the foot strike pattern for each condition
126 using a previously validated method (Giandolini et al., 2014), which provided the percentage of a
127 trial's foot strikes classified as either rearfoot, midfoot, or forefoot strikes. The biaxial
128 accelerometer was placed on the sacrum such that the vertical axis in the accelerometer's local
129 coordinate system was oriented superiorly, but we did not perform a calibration to align
130 accelerometer and treadmill coordinate systems (Figure 1). We did not align the accelerometer
131 and treadmill coordinate systems because an LSTM network can likely learn the transformation
132 between the coordinate systems and requiring this preprocessing calibration may limit the utility
133 of an LSTM network outside a laboratory setting.

134

135 **Data Processing**

136 We analyzed 5 seconds of data (approximately 13 foot-ground contacts) from each trial and
137 downsampled the normal GRF, vertical sacral acceleration, and anteroposterior sacral
138 acceleration to 500 Hz to reduce the computational cost and match the sampling frequency of
139 prior studies (Day et al., 2021; Alcantara et al., 2021). We normalized GRFs to bodyweight
140 (BW) and filtered them using a 4th order low-pass Butterworth filter with a 30 Hz cut-off. We
141 filtered the sacral acceleration data with a 4th order low-pass Butterworth filter with a 20 Hz cut-
142 off. Preliminary analysis revealed that a 20 Hz cut-off improved prediction accuracy compared to
143 5 Hz, 10 Hz, 30 Hz, and no filter and preserved approximately 89% and 82% of the vertical and
144 anteroposterior signal power, respectively.

145

146 Vertical sacral accelerometer data were further processed so that all negative values were
147 replaced with zeros. Vertical center of mass acceleration is primarily negative during the aerial
148 phase of running (Blickhan 1989) and preliminary analysis revealed that replacing negative
149 vertical sacral accelerometer data with zeros helped the LSTM network avoid predictions of
150 negative normal GRFs during the aerial phase. For each condition, we used the 2500 frame (5 s
151 trial @ 500 Hz) sequences of vertical and anteroposterior sacral accelerometer data to predict the
152 simultaneously collected 2500 frame sequence of normal GRFs. The recurrent nature of the
153 LSTM network requires sequential data to be divided into smaller portions that are iteratively
154 used to make predictions. To accomplish this, we divided acceleration data for each trial into
155 overlapping windows with a 6 frame (12 ms) width and padded the beginning and end of each
156 trial's acceleration data with the first and final values, respectively, to ensure the number of
157 windows equaled the number of normal GRF frames (2500) and that the windows were centered
158 on the corresponding frame of the normal GRFs (Figure 1). Preliminary analysis revealed that a
159 window width of 6 frames was the smallest window we could use without decreasing LSTM
160 network prediction accuracy and we found no improvement in prediction accuracy when using
161 window sizes up to 60 frames (120 ms). Thus, the LSTM network iteratively predicted a single
162 frame of the normal GRF at time t using acceleration data from frames t_{-3} through t_{+2} (Figure 1).

163

164 **Feature Engineering**

165 A total of 13 features were used as inputs in the LSTM network (Figure 1). We calculated the
166 mean, standard deviation (SD), and range of vertical and anteroposterior acceleration data for
167 each 12 ms window and used them as input features. The use of summary statistics as input
168 features has been shown to maintain neural network accuracy while benefiting from a reduced
169 computational cost (Figo et al., 2010). These three summary statistics were normalized to a range
170 of 0 – 1 and represent 6 (3 features x 2 acceleration axes) of the 13 input features. The remaining
171 input features were selected due to their effect on running kinetics and kinematics: subject
172 height, body mass, running speed, slope, and percentage of steps classified as either rearfoot,
173 midfoot, or forefoot strikes (Almeida, Davis & Lopes, 2015; Khassestarash et al., 2020; Vernillo
174 et al., 2020; Vincent et al., 2020; Alcantara et al., 2021). We chose not to include step frequency
175 as an input feature, despite the presence of the $\pm 10\%$ preferred step frequency conditions, to
176 increase the variability in the data used to predict GRF waveforms. Doing so theoretically
177 represents a greater challenge for the LSTM network as there is additional variability between
178 trials that is not being explicitly accounted for with an input variable.

179

180 **Neural Network Architecture**

181 The neural network consisted of a Bidirectional LSTM and a multilayer perceptron (MLP) with
182 three fully connected layers containing 128, 384, and 320 neurons, respectively (Figure 2). The
183 Bidirectional LSTM consists of two LSTM layers where the order of the input sequence is
184 reversed for the second layer. Reversing the sequence for the second LSTM layer allows the
185 network to utilize information from future portions of the sequence just as the first LSTM layer
186 utilizes information from prior portions. The outputs from each LSTM layer are then averaged
187 before being passed along to the MLP. The number and size of the layers were determined using
188 the Hyperband hyperparameter optimization algorithm (Li et al., 2018) on the data of two
189 randomly selected subjects. The LSTM network was trained using a batch size of 32, learning
190 rate of 0.001, and mean square error loss function. Network weights and biases were updated
191 using the adaptive moment estimation (Adam) optimization algorithm at the end of each epoch
192 (Kingma & Ba, 2017) and training lasted a maximum of 1000 epochs or until the mean square
193 error failed to decrease by 0.001 BW after 30 consecutive epochs. The neural network was
194 developed using the Tensorflow (v2.2.0) python library (Abadi et al., 2016).

195

196 **Network Validation**

197 We assessed the accuracy and generalizability of the network using a Leave-One-Subject-Out
198 (LOSO) cross validation method (Halilaj et al., 2018). LOSO cross validation is a variation of K-
199 fold cross validation that requires the dataset to be subset by subject, with one subject's data
200 withheld for testing purposes and the rest of the subjects' data used to train the network. This
201 process is repeated until the network has been tested on every subject's data, ultimately
202 providing an ensemble of networks and their respective accuracy metrics. Performing LOSO
203 cross validation can be computationally costly, as the network must be trained and tested a

204 number of times equal to the number of subjects ($n = 19$), but the benefits of this method include
 205 the ensemble of accuracy metrics and assurance that a given subject's data are not included in
 206 both the training and testing subsets, which can artificially increase the reported accuracy of a
 207 network (Saeb et al., 2017; Chaibub Neto et al., 2019).

208

209 In addition to the LOSO cross validation method, we performed a test-train split of one
 210 representative subject's data according to slope ($\pm 5^\circ$ trials reserved for testing, 0° and $\pm 10^\circ$
 211 slopes used for training) to test the accuracy of the model when predicting speed-slope
 212 combinations that were not present during training. We selected Subject 14 as a representative
 213 subject because their RMSE during LOSO cross validation was similar to the average RMSE
 214 across all subjects (Figure 3) and their GRF waveforms illustrated an interaction between
 215 running slope and normal GRF impact peak magnitude (Gottschall & Kram, 2005). This single-
 216 subject validation method prioritizes accuracy over generalizability (ability to make accurate
 217 predictions for a variety of individuals) and represents a potential circumstance where an LSTM
 218 network is trained on data collected from a single athlete prior to their competitive season and
 219 later used to predict only that athlete's GRF data from wearable device data during their
 220 competitive season.

221

222 Prediction error for each trial's GRF waveforms was quantified as the root mean square error
 223 (RMSE) and relative RMSE (rRMSE), which is RMSE normalized to the average range of
 224 compared waveforms, expressed as a percentage and defined as

225

$$rRMSE = \frac{RMSE}{0.5 \times \sum_{i=1}^2 (\max(x_i) - \min(x_i))} \times 100, \quad (1)$$

226

227 where x_1 and x_2 are the GRF waveforms predicted by the LSTM network and measured by the
 228 force-measuring treadmill (Ren, Jones & Howard, 2008). Additionally, we used a threshold of
 229 5% BW to identify stance phase and calculated the active peak of the normal GRF waveform,
 230 normal impulse, normal GRF loading rate, contact time, and step frequency from the predicted
 231 and measured GRF data. The normal GRF active peak was calculated as the maximum normal
 232 GRF value occurring between 40 – 60% of stance phase because the magnitude of the impact
 233 peak can exceed the active peak during downhill running and occurs during early stance phase (0
 234 – 30%) (Gottschall & Kram, 2005; Vernillo et al., 2020). We calculated impulse as the integral
 235 of the normal GRF waveform during the stance phase with respect to time, loading rate as the
 236 average slope of the normal GRF waveform during the first 25 ms of stance phase (Yong et al.,
 237 2018), contact time as the duration when the normal GRF was greater than 5% BW, and step
 238 frequency as the number of initial foot-ground contacts per second. We report the mean absolute
 239 percent error (MAPE) of these discrete variables for each subject. Data analysis was performed
 240 in python (v3.6.9) and R (v4.0.4) using custom libraries (Wickham, 2009, 2019; Alcantara, 2019;

241 pandas development team, 2020; R Core Team, 2020; Wickham et al., 2020; Virtanen et al.,
242 2020; Harris et al., 2020).

243

244 We enforced two biomechanical boundaries upon the predicted GRF waveforms to ensure that
245 data fell within established biomechanical limits and could be used to calculate the discrete
246 biomechanical variables of interest. First, the predicted GRF waveform had to have an equal
247 number of foot-ground contacts as the GRF waveform measured by the force-measuring
248 treadmill, determined using the same 5% BW threshold. Second, the step frequency over the
249 duration of the predicted GRF waveform had to be ≤ 4 Hz. We selected these criteria based on
250 previous research of running biomechanics, as thresholds of 5% BW have been previously used
251 to identify the stance phase for the calculation of kinetic or kinematic variables (Day et al., 2021;
252 Alcantara et al., 2021) and during uphill and downhill running, step frequency is ≤ 4 Hz
253 (Cavagna et al., 1997; Snyder & Farley, 2011). Trials that failed to meet either of these criteria
254 were used to calculate the LSTM network's overall prediction failure rate and removed from
255 subsequent analyses.

256

257 **Results**

258 We analyzed 529 trials for the present study. The predicted GRF waveforms for 32 trials (6%)
259 failed to meet one or both criteria and were considered failed predictions. Specifically, we
260 identified 22 trials (4%) that required a threshold greater than 5% BW to identify an equal
261 number of steps between predicted and measured GRF waveforms and 10 trials (2%) that had a
262 step frequency greater than 4 Hz. Thus, 94% of GRF waveforms predicted by the LSTM network
263 fell within the imposed biomechanical boundaries.

264

265 Leave-One-Subject-Out cross validation revealed that the LSTM network predictions of each
266 subject's normal GRF waveforms had an average \pm SD RMSE of 0.16 ± 0.04 BW (Figure 3) and
267 rRMSE of $6.4 \pm 1.5\%$ compared to GRF waveforms measured by the force-measuring treadmill
268 across all conditions (Table 1). RMSE values were generally lower during slow uphill running
269 (2.5 m/s, $+10^\circ$; 0.13 BW) compared to fast downhill running (4.17 m/s, -10° ; 0.20 BW) (Figures
270 4 and 5). The MAPE for step frequency was $0.1 \pm 0.1\%$, contact time was $4.9 \pm 4.0\%$, impulse
271 was $6.4 \pm 6.9\%$, normal GRF active peak was $8.5 \pm 8.2\%$, and loading rate was $27.6 \pm 36.1\%$
272 (Table 2).

273

274 The prediction error for one representative subject's (Subject 14) normal GRF waveforms at $\pm 5^\circ$
275 during single-subject validation was lower than those resulting from the LOSO cross validation,
276 with an average \pm SD RMSE of 0.08 ± 0.02 BW and rRMSE of $3.3 \pm 0.9\%$. The MAPE of step
277 frequency ($0.1 \pm 0.1\%$), contact time ($3.0 \pm 2.3\%$), impulse ($2.5 \pm 1.9\%$), normal GRF active
278 peak ($2.7 \pm 2.0\%$), and loading rate ($17.6 \pm 16.9\%$) calculated from predicted GRF waveforms
279 were also generally lower than those resulting from LOSO cross validation.

280

281 Discussion

282 We developed a recurrent neural network capable of predicting continuous normal GRF
283 waveforms across a range of running speeds (2.5 – 4.17 m/s), slopes (0° , $\pm 5^\circ$, $\pm 10^\circ$), and step
284 frequencies (preferred, $\pm 10\%$) from accelerometer data. Our findings indicate that an LSTM
285 network with the runner's mass, height, running speed, slope, foot strike pattern, and sacral
286 acceleration as input features can predict normal GRF waveforms across a range of speeds and
287 slopes with an RMSE of 0.12 – 0.20 BW and rRMSE of 5.4 – 7.3% (Figure 4). For comparison,
288 previous studies report an RMSE of 0.39 ± 0.26 BW (Wouda et al., 2018), an RMSE of $0.21 \pm$
289 0.03 BW (Dorschky et al., 2020), and an rRMSE of 13.92% (Johnson et al., 2021) when using
290 neural networks to predict the stance phase vertical GRF waveform during level-ground running.
291 In contrast to previous studies, the LSTM network does not require preliminary stance phase
292 identification or time normalization, which preserves the temporal component of the predicted
293 GRF waveform. This characteristic of the LSTM network allowed us to calculate stride
294 kinematic variables like step frequency and contact time with a MAPE $< 5\%$. Additionally, the
295 recurrent nature of the LSTM network facilitates frame-by-frame predictions of GRF waveforms
296 and can be used to make predictions over any duration of running. Thus, an LSTM network
297 could be used to quantify changes in normal GRF waveforms over the course of a prolonged run
298 (e.g., a marathon race).

299

300 The accuracy of predicted GRF waveforms varied across speeds and slopes, with a combination
301 of faster running speeds and negative slopes producing greater RMSE values than slower
302 running speeds and positive slopes (Figure 4). The greater RMSE values during downhill
303 running may be due to the LSTM network's inability to account for changes in impact peak
304 magnitude across slopes (Figure 5). Previous studies have found that the presence of an impact
305 peak in the normal GRF waveform is subject-specific, affected by changes in running slope, and
306 associated with acceleration of the effective mass of the lower extremity during early stance
307 phase (McMahon, Valiant & Frederick, 1987; Gottschall & Kram, 2005; Vernillo et al., 2020).
308 Thus, predictions of normal GRF waveforms across slopes may be further improved by
309 incorporating accelerations measured at the feet or lower legs.

310

311 We also quantified the accuracy of the LSTM network when trained and tested on data from the
312 same subject. Although not a valid method of determining the LSTM network's generalizability,
313 single-subject validation provides insight into how well a personalized neural network could
314 predict an individual's GRF waveforms for unknown combinations of speed and slope in the
315 future. We found that predicted GRF waveforms of a representative subject (Subject 14) during
316 the $\pm 5^\circ$ slope conditions had an average \pm SD RMSE of 0.08 ± 0.02 BW, compared to $0.16 \pm$
317 0.03 BW during LOSO cross validation. These findings indicate that a subject-specific LSTM
318 network was twice as accurate as the LOSO cross validated LSTM network. A single-subject
319 approach may be particularly beneficial for researchers, coaches, or clinicians who have the
320 resources to train personalized LSTM networks and wish to monitor a specific athlete's

321 biomechanics over the course of a competitive season. For example, an athlete could run at a
322 variety of speeds and slopes while wearing accelerometers during a baseline data collection on a
323 force-measuring treadmill at the start of their competitive season and a personalized LSTM
324 network could be trained on their data. Then, if accelerometer data were collected from an
325 athlete during training runs, their normal GRF waveforms and a variety of discrete values could
326 be predicted and monitored longitudinally.

327

328 The MAPE values for step frequency, contact time, impulse, and normal GRF active peak were \leq
329 8.5%, but the loading rate MAPE was $27.6 \pm 36.1\%$. The lower MAPE values for step frequency,
330 contact time, impulse, and normal GRF active peak indicate that the LSTM network consistently
331 identified the general shape of the GRF waveform and the boundaries of the stance phase despite
332 changes in speed, slope, and step frequency. However, the network did not consistently predict
333 the presence of an impact peak during early stance phase (Figure 5, -10° trial), which affected the
334 predicted slope of the GRF waveform during early stance phase and thus the accuracy of loading
335 rate values. Although the prominence of an impact peak in the normal GRF waveform is affected
336 by foot strike pattern and slope (Gottschall & Kram, 2005), two of the inputs for the LSTM
337 network, the decreased accuracy when estimating loading rate may be because we did not
338 include accelerometer data from the lower extremities and impact accelerations are attenuated at
339 the sacrum compared to the tibia (Baggaley et al. 2019). A previous study found moderate-strong
340 correlations between axial tibial acceleration and vertical GRF impact peak magnitude ($r = 0.76$)
341 and timing ($r = 0.94$) during running (Hennig & Lafortune, 1991), and future research aimed at
342 improving the accuracy of loading rate estimates should include tibial acceleration as an input
343 feature. We did not include accelerometer data from the shoes as inputs for the LSTM network
344 because the data were not available for both feet.

345

346 Recurrent neural networks represent a promising strategy for predicting continuous normal GRFs
347 from wearable devices in outdoor environments. The LSTM network required data from three
348 accelerometers (one on the sacrum and two on the right shoe to determine foot strike pattern),
349 but we also performed a *post-hoc* analysis of prediction accuracy without the foot strike pattern
350 data to quantify the network's accuracy when only using data from one sacral accelerometer. The
351 *post-hoc* analysis revealed that excluding foot strike pattern data slightly increased the average \pm
352 SD RMSE from 0.16 ± 0.04 BW to 0.17 ± 0.05 BW and rRMSE from $6.4 \pm 1.5\%$ to $6.7 \pm 1.7\%$.
353 Excluding foot strike pattern data affected the MAPE of discrete variables by $< 3\%$ (Table 3).
354 These findings indicate that the LSTM network can predict normal GRF waveforms from a
355 single accelerometer on the sacrum more accurately than neural networks implemented in
356 previous studies (RMSE = 0.21 – 0.39 BW, rRMSE = 13.92%), which required data from 3 – 7
357 wearable devices (Wouda et al., 2018; Dorschky et al., 2020; Johnson et al., 2021).

358

359 We further analyzed the importance of input features to the LSTM network by calculating
360 prediction accuracy after systematically permuting each input feature across the trials for the

361 representative subject. This process of calculating Permutation Feature Importance (PFI)
362 effectively severs the learned relationship between an input feature for a given trial and the
363 corresponding GRF waveform (Molnar 2019). PFI is calculated as the ratio between the RMSE
364 of the LSTM network with a given feature permuted and the original prediction RMSE of the
365 LSTM network. After 100 permutations for each input feature, we found that the input feature
366 with the highest PFI was vertical acceleration (6.29), followed by anteroposterior acceleration
367 (1.62), foot strike pattern (1.14), slope, (1.13), speed (1.07), height (1.00), and body mass (1.00).
368 These findings indicate that the inclusion of body mass and height did not improve prediction
369 accuracy and that the LSTM network relies most on the acceleration data when predicting the
370 normal GRF waveform across a range of speeds and slopes.

371
372 Using a recurrent neural network in combination with accelerometers and a global positioning
373 system (GPS) device to obtain speed and slope data could potentially allow runners to receive
374 biomechanical feedback during an outdoor run. Watches with GPS capabilities are commonly
375 used by runners (Janssen et al., 2020), have been used to provide real-time feedback of step
376 frequency (Willy et al., 2016), and could provide running speed and slope data to the LSTM
377 network to predict GRF waveforms in near-real time (Scott, Scott & Kelly, 2016). Discrete
378 biomechanical variables could then be calculated from predicted normal GRF waveforms and
379 sent to a clinician, coach, researcher, or the runner themselves. A similar approach has been
380 implemented during outdoor walking and running using an integrated IMU-GPS device placed in
381 a backpack, but it is unclear how accurate or generalizable this approach is as the network was
382 trained and tested on data from three subjects and the reported accuracy metrics were combined
383 for walking and running (Davidson et al. 2019). To facilitate calculation of GRF-based variables
384 during outdoor running using accelerometers, we have made the LSTM networks, which were
385 trained on all subjects, with and without the need for foot strike data, publicly available at
386 www.github.com/alcantarar/Recurrent_GRF_Prediction. We have included a tutorial on how to
387 use an LSTM to continuously predict a signal from wearable device data, an approach that may
388 be used to improve a clinician's ability to remotely quantify a patient's GRFs or monitor
389 rehabilitation progress (Gurchiek, Cheney & McGinnis, 2019).

390
391 There are potential limitations to consider alongside our findings. The accelerometers used in the
392 present study were biaxial and the inclusion of mediolateral sacrum accelerations may have
393 further improved prediction as the mediolateral behavior of the center of mass is sensitive to
394 changes in running speed (Nilsson et al. 1989) and slope. Additionally, accelerometers were
395 adhered to subjects using tape and a less secure attachment method may introduce movement
396 artefact into the accelerometer data. Previous research suggests that attachment method can
397 affect peak tibial acceleration during running (Johnson et al., 2020), but the lower leg
398 experiences larger accelerations than the sacrum during running (Baggaley et al., 2019) and thus
399 is more sensitive to different attachment methods. However, variations in accelerometer
400 orientation between subjects may have contributed to the range of RMSE values (0.11 – 0.31

401 BW) during LOSO cross validation (Tan et al. 2019). Additionally, variations in soft tissue
402 movement artefact between the subjects used to train the LSTM network and other populations
403 may introduce prediction error (Peters et al. 2010). Using the LSTM network to predict normal
404 GRF waveforms from a sacral accelerometer adhered differently than in the present study may
405 affect prediction accuracy, but the 20 Hz low-pass filter we applied to the accelerometer data can
406 potentially mitigate this effect. Additionally, predictions made with the LSTM network may not
407 be generalizable for speeds or slopes that fall outside the range of the training data (2.5 – 4.17
408 m/s and $\pm 10^\circ$), for different running surfaces, as biomechanics change when running on steep
409 slopes (e.g. 20 – 40°) (Giovanelli et al., 2016; Whiting et al., 2020), for prolonged runs, on
410 variable terrain (Voloshina & Ferris, 2015), with changes in speed (Alcantara et al., 2021), or in
411 response to muscle fatigue (Derrick, Dereu & McLean, 2002). Lastly, the LSTM network was
412 trained on data collected on a stiff force-measuring treadmill and thus accelerometer data
413 collected during running on less stiff surfaces (e.g., grass) may result in greater prediction errors
414 given the effects of surface stiffness on running biomechanics and thus energy absorption
415 (Derrick, Hamill & Caldwell, 1998; Ferris, Louie & Farley, 1998).

416

417 **Conclusions**

418 We developed a recurrent neural network that used accelerometer data to predict continuous
419 normal GRF waveforms across a range of running speeds (2.5 – 4.17 m/s) and slopes (0° , $\pm 5^\circ$,
420 $\pm 10^\circ$) with an average \pm SD RMSE of 0.16 ± 0.04 BW and rRMSE of $6.4 \pm 1.5\%$. Unlike neural
421 networks implemented in prior studies, the recurrent neural network does not require preliminary
422 identification of the stance phase or temporal normalization and allows for near real-time
423 predictions of normal GRF waveforms during running. Accurate predictions of normal GRF
424 waveforms using wearable devices will improve the ability to longitudinally monitor
425 biomechanical variables in non-laboratory environments.

426

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625

Figure 1

Overview of the Long Short-Term Memory (LSTM) network's input features and function.

(A) The LSTM network's input features included body mass, height, running speed, slope, and percentage of a trial's steps classified as rearfoot (RFS), midfoot (MFS), or forefoot (FFS) strikes. **(B)** Vertical and anteroposterior sacral acceleration data were divided into overlapping 6 frame (12 ms) windows, one for each frame of the normal ground reaction force (GRF) data. The mean, standard deviation (SD), and range of vertical and anteroposterior sacral acceleration values were calculated for each window and used as input features to the LSTM network. For the prediction of a normal GRF value at a given time (t), the respective window of acceleration data begins at t_{-3} and ends at t_{+2} . **(C)** Normal GRFs were predicted frame-by-frame by the LSTM network using the 13 input features.

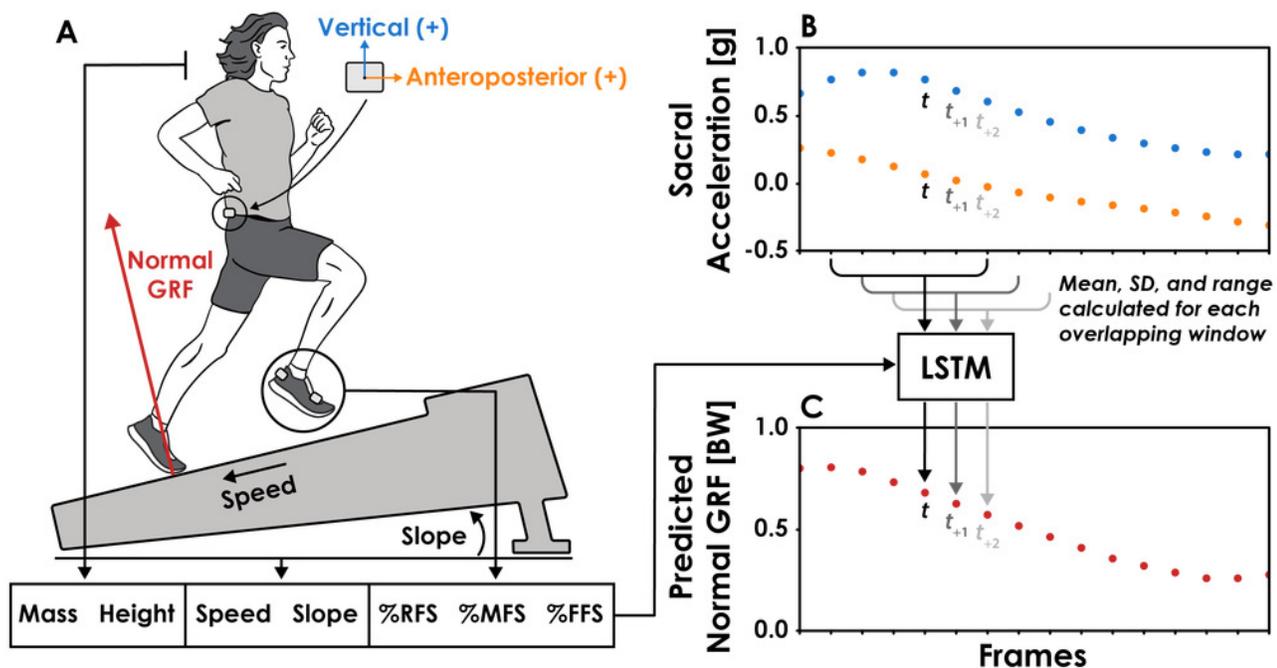


Figure 2

Neural Network Architecture

The Long Short-Term Memory (LSTM) network consisted of a Bidirectional LSTM layer with a hyperbolic tangent activation function followed by a multilayer perceptron (MLP) with rectified linear unit activation functions for three hidden layers with 128, 384, and 320 neurons, respectively. The Bidirectional LSTM layer is unraveled to illustrate its recurrent nature and dashed lines signify inputs (x) and outputs (h) at time t_{-1} and t_{+1} . A dropout rate of 20% was applied to the input layer of the network and a dropout rate of 40% was applied to the output of the Bidirectional LSTM layer to limit network overfitting. For each prediction of the normal ground reaction force (GRF) at a given time (t), the network received 13 features as inputs (x_t ; Figure 1), passed the output from the Bidirectional LSTM layer (h_t) to the MLP, and predicted a single value (y_t) with a linear activation function in the output layer.

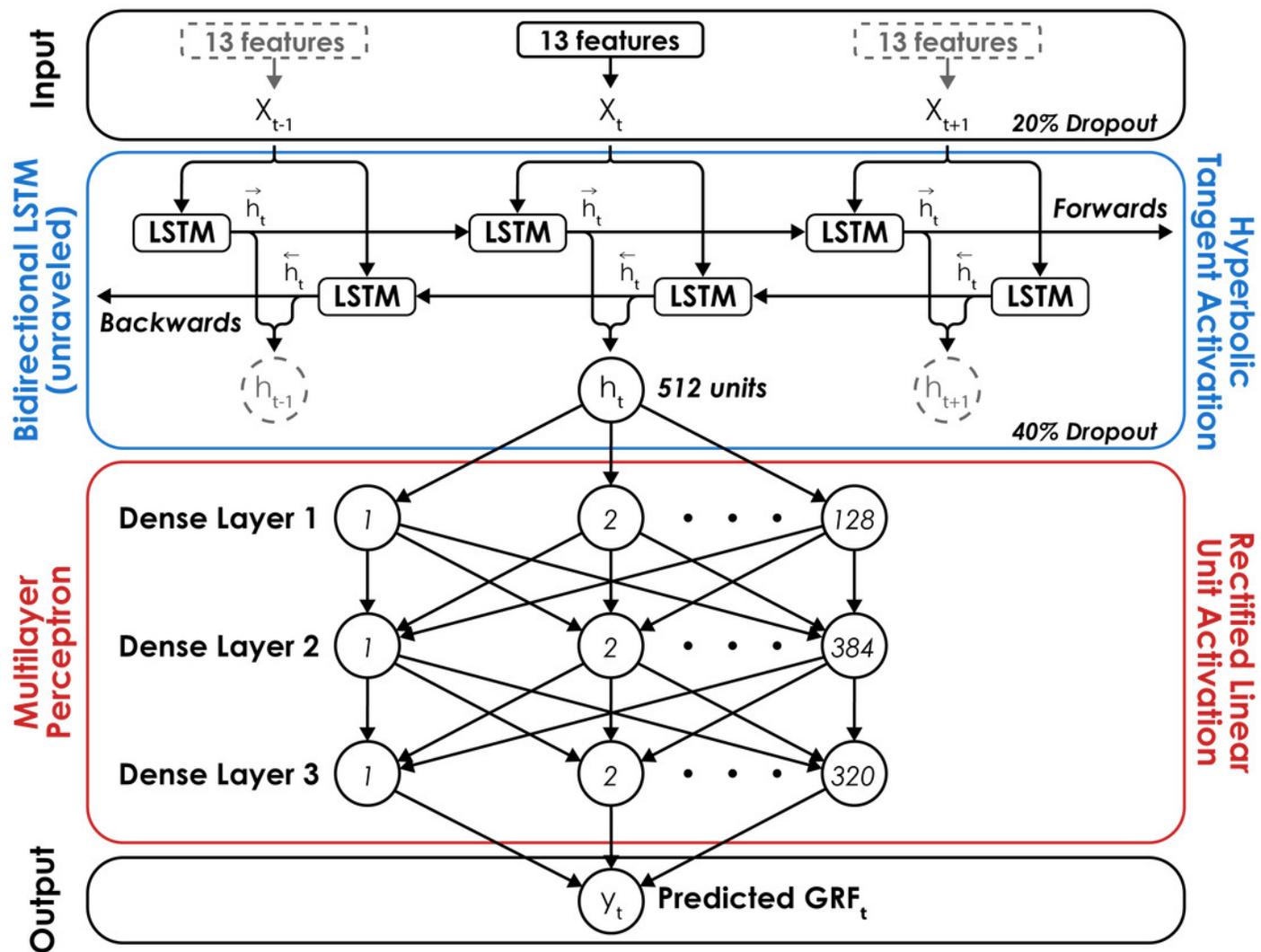


Figure 3

Ground reaction force waveform prediction error for each subject across all conditions

The average root mean square error (RMSE) across subjects was 0.16 BW (dotted line). Filled circles represent each trial, and the color indicates slope (0° , $\pm 5^\circ$, $\pm 10^\circ$) at three speeds (2.5, 3.33, 4.17 m/s). Open circles represent each subject's average RMSE, horizontal bars are the median RMSE, box plot edges indicate the interquartile range (IQR; 25th and 75th percentile), and the whiskers encompass values that fall within 1.5*IQR. Subjects are sorted from lowest to highest RMSE.

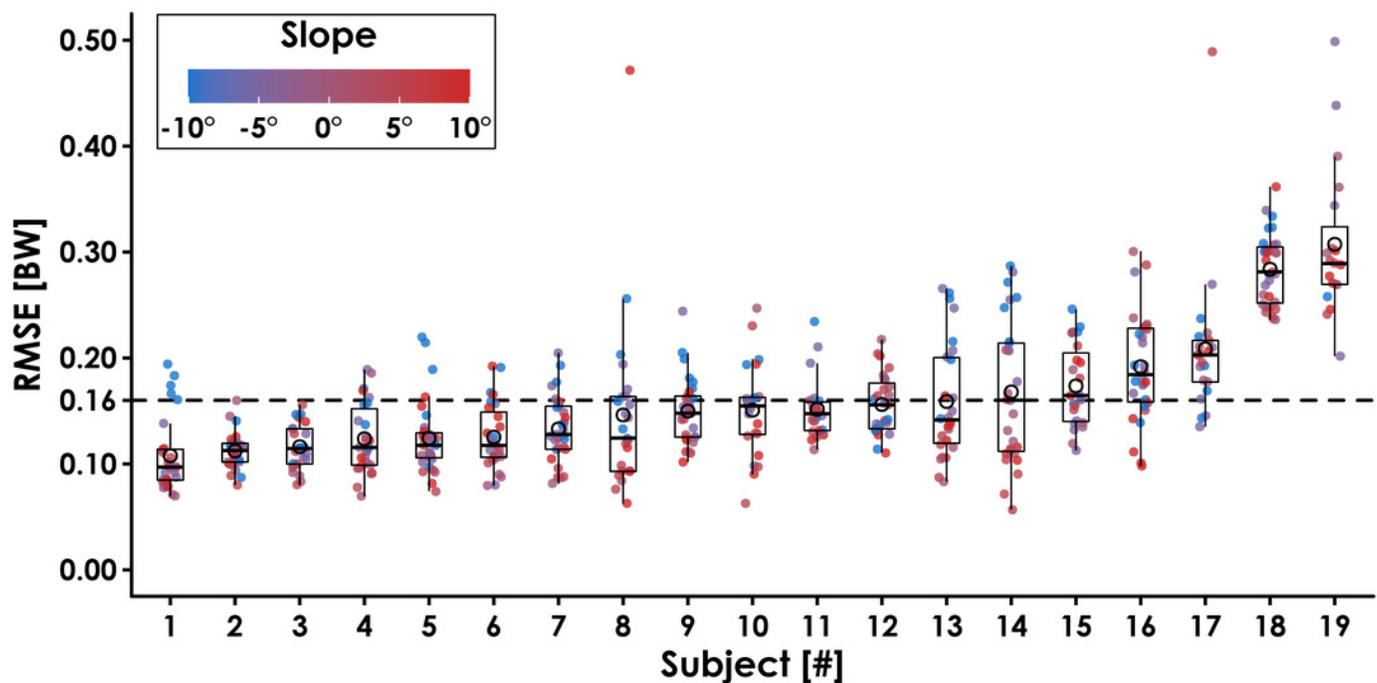


Figure 4

Ground reaction force waveform prediction error for each condition

The average \pm SD root mean square error (RMSE) of the predicted ground reaction force (GRF) waveforms compared to the GRF waveform measured by the force-measuring treadmill for each condition during leave-one-subject-out (LOSO) cross validation.

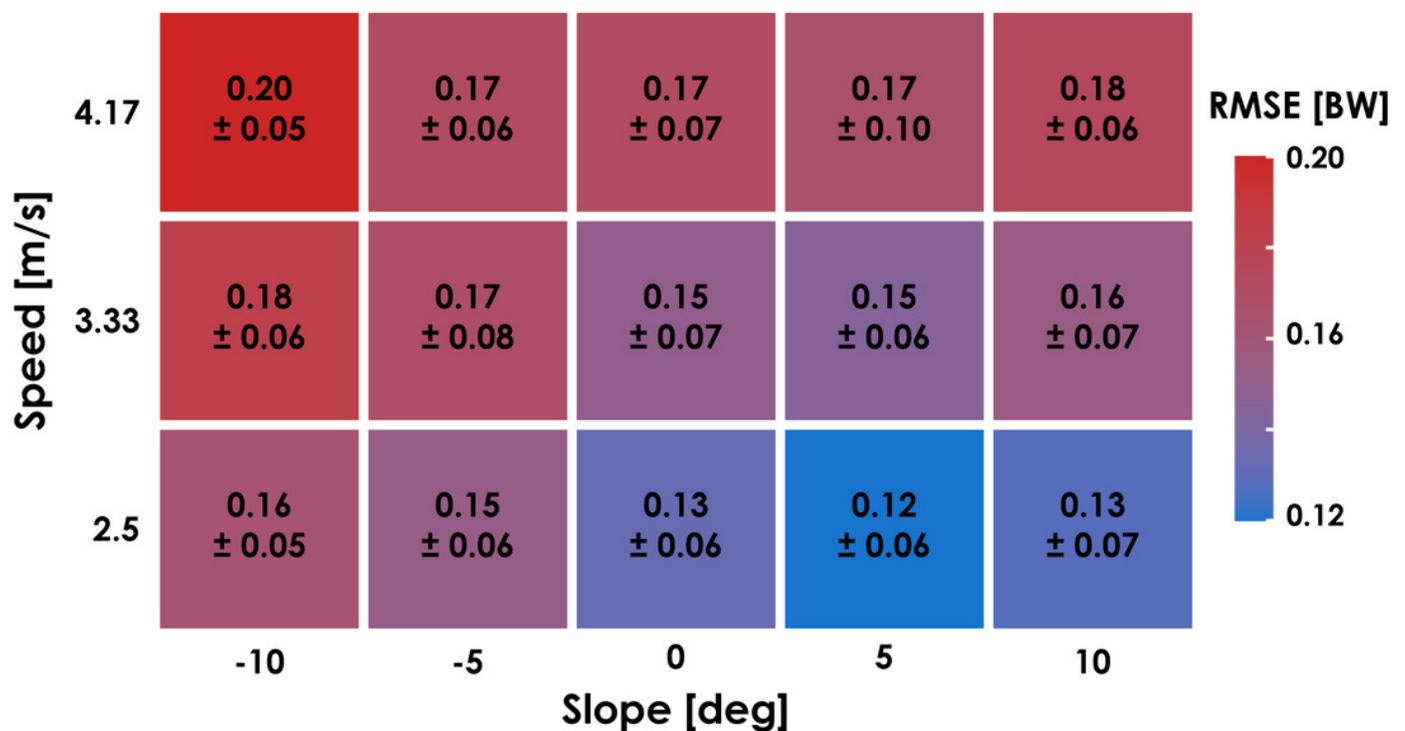


Figure 5

Predicted and measured normal GRF waveforms across slopes for a representative subject

Normal ground reaction force (GRF) waveforms predicted by the recurrent neural network (dashed red lines) and measured by the force-measuring treadmill (solid blue lines) at 3.33 m/s and all slopes (0° , $\pm 5^\circ$, $\pm 10^\circ$) are presented for Subject 14. Subject 14 was selected because they had similar RMSE values (0.17 ± 0.07 BW) as the average across all subjects (0.16 ± 0.04 BW) and their GRF waveforms illustrate an interaction between running slope and normal GRF impact peak magnitude.

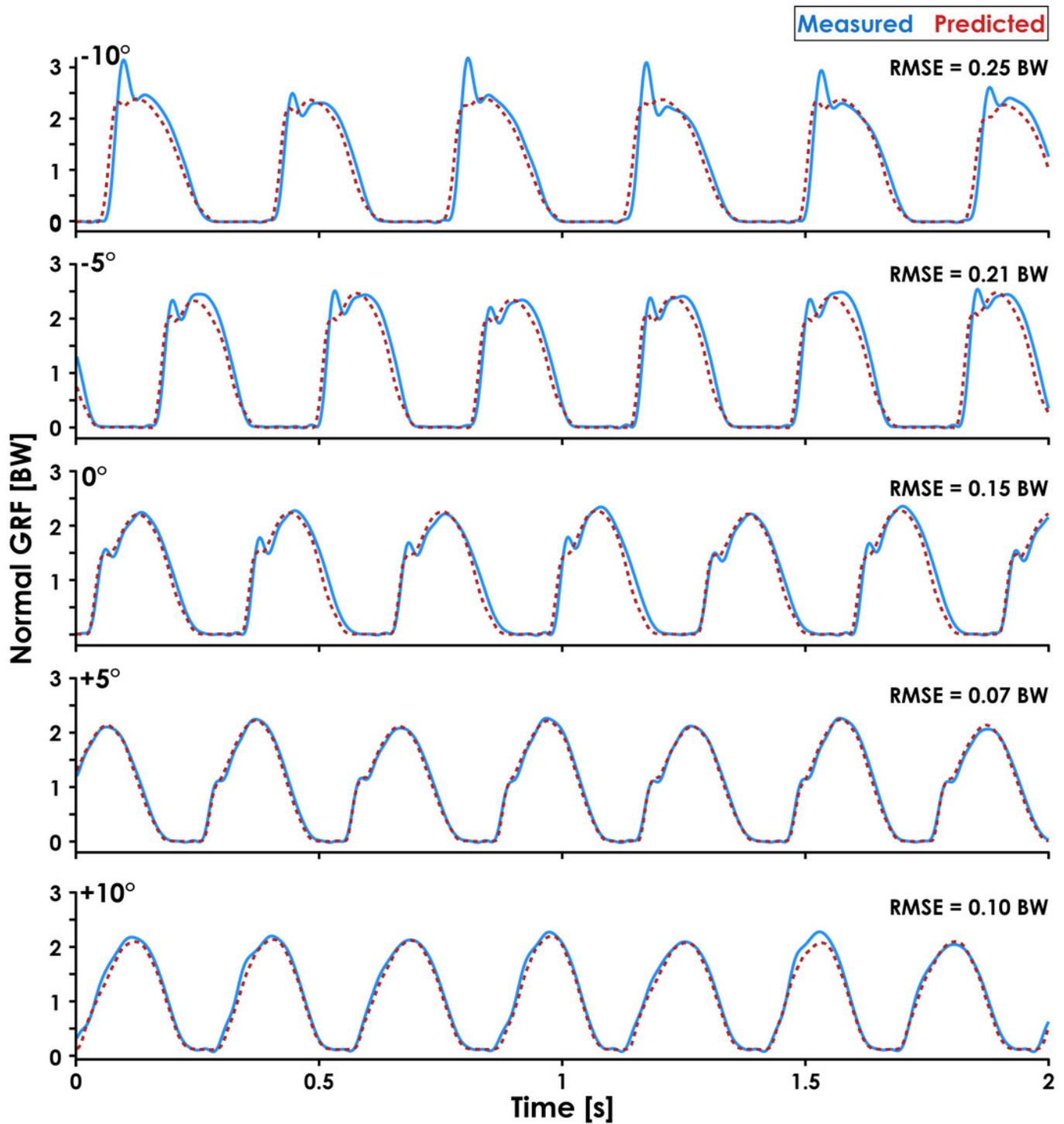


Table 1 (on next page)

Mean \pm SD root mean square error (RMSE) and relative RMSE (rRMSE) for normal GRF waveforms predicted by the LSTM network compared to the measured normal GRF waveforms for each subject.

Subject	RMSE [BW]	rRMSE [%]
1	0.11 ± 0.04	4.0 ± 1.1
2	0.11 ± 0.02	4.1 ± 0.7
3	0.12 ± 0.02	4.4 ± 0.9
4	0.12 ± 0.03	4.6 ± 1.2
5	0.12 ± 0.04	4.7 ± 0.9
6	0.12 ± 0.03	5.2 ± 1.4
7	0.13 ± 0.03	5.1 ± 1.2
8	0.15 ± 0.08	5.3 ± 3.3
9	0.15 ± 0.03	5.4 ± 1.0
10	0.15 ± 0.04	5.2 ± 1.3
11	0.15 ± 0.03	5.8 ± 0.8
12	0.16 ± 0.03	6.1 ± 1.1
13	0.16 ± 0.06	5.7 ± 1.5
14	0.17 ± 0.07	6.9 ± 2.5
15	0.17 ± 0.04	7.9 ± 2.0
16	0.19 ± 0.05	6.7 ± 1.7
17	0.21 ± 0.07	7.2 ± 2.5
18	0.29 ± 0.03	14.0 ± 1.7
19	0.31 ± 0.07	13.7 ± 2.7
Mean ± SD	0.16 ± 0.04	6.4 ± 1.5%

1

Table 2 (on next page)

Mean \pm SD of the discrete biomechanical variables.

Values were calculated from normal ground reaction force (GRF) waveforms predicted by the LSTM network (“Predicted”) and normal GRF waveforms measured from the force-measuring treadmill (“Measured”) across all speeds and subjects for each slope.

Slope	Step Frequency [Hz]		Contact Time [ms]		Impulse [BW*s]		Active Peak [BW]		Loading Rate [BW/s]	
	Predicted	Measured	Predicted	Measured	Predicted	Measured	Predicted	Measured	Predicted	Measured
-10°	3.1 ± 0.3	3.1 ± 0.3	215 ± 26	214 ± 29	0.33 ± 0.03	0.33 ± 0.05	2.38 ± 0.24	2.36 ± 0.40	64.7 ± 19.9	68.4 ± 20.6
-5°	3.1 ± 0.3	3.1 ± 0.3	222 ± 23	223 ± 27	0.34 ± 0.04	0.34 ± 0.04	2.41 ± 0.25	2.45 ± 0.36	54.9 ± 16.7	60.6 ± 19.4
0°	3.1 ± 0.3	3.1 ± 0.3	228 ± 24	229 ± 27	0.33 ± 0.04	0.34 ± 0.04	2.42 ± 0.22	2.51 ± 0.36	42.0 ± 12.8	49.0 ± 17.2
+5°	3.2 ± 0.3	3.2 ± 0.3	228 ± 25	232 ± 26	0.32 ± 0.03	0.33 ± 0.04	2.36 ± 0.21	2.40 ± 0.33	34.8 ± 8.5	39.3 ± 13.3
+10°	3.4 ± 0.3	3.4 ± 0.3	223 ± 26	227 ± 26	0.30 ± 0.04	0.30 ± 0.04	2.24 ± 0.22	2.20 ± 0.29	30.1 ± 8.3	31.3 ± 12.7

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Table 3(on next page)

Error metrics for the predicted waveforms and discrete variables when training the Long Short-Term Memory (LSTM) network with and without foot strike pattern as an input feature.

Root mean square error (RMSE) and relative RMSE (rRMSE) are presented for predicted normal ground reaction force (GRF) waveforms. Mean absolute percent error (MAPE) values are presented for the discrete variables calculated from normal GRF waveforms predicted by both LSTM networks.

	LSTM With Foot Strike (Sacral + Right Foot Accelerometers)	LSTM Without Foot Strike (Only Sacral Accelerometer)
GRF Waveform		
RMSE [BW]	0.16 ± 0.04	0.17 ± 0.05
rRMSE	6.4 ± 1.5%	6.7 ± 1.7%
Discrete Variables		
MAPE		
Step Frequency	0.1 ± 0.1%	0.1 ± 0.1%
Contact Time	4.9 ± 4.0%	5.6 ± 4.5%
Impulse	6.4 ± 6.9%	6.0 ± 7.1%
Active Peak	8.5 ± 8.2%	7.7 ± 6.3%
Loading Rate	27.6 ± 36.1%	30.3 ± 41.6%

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