

New data on tail lengths and variation along the caudal series in the non-avian dinosaurs

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Abstract

The caudal vertebral series of non-avian dinosaurs varied considerably in terms of overall length, total number of vertebrae, gross form and function. A new dataset confirms that there is little or no consistent relationship between tail length and snout-sacrum length; consequently, attempts to estimate one from the other are likely to be very error-prone. Patterns of changes in centra lengths across the caudal series vary among non-avian dinosaurs. However, despite this

variability, we show that some overarching patterns do emerge with a number of taxa showing (proximal to distal) a series of short centra, followed by a series of longer centra, with the remainder of the tail consisting of a long series of centra tapering in length. This pattern appears consistent with some functional constraints as the series of longer centra are coincident with the major attachments of femoral musculature. Notably, this arrangement is not present in early lineages and may have evolved independently in different dinosaurian groups, providing further support for the suggestion that the arrangement was of functional importance. Finally, we suggest that the methods developed here to separate out groups of similar units as part of a series may be widely applicable to assessments of entire vertebral series in a range of extinct and extant vertebrate taxa and, indeed, in any study of taxa exhibiting repeating units (for example, segmented invertebrates).

Introduction

The caudal vertebral series of the non-avian dinosaurs (hereafter simply ‘dinosaurs’) served many roles. Dinosaur tails had a biomechanical function in locomotion (e.g. Hutchinson, Ng-Thow-Hing & Anderson, 2007; Persons & Currie, 2011a) and balance (e.g. Hutchinson & Gatesy, 2001; Libby et al. 2012)), and some were specialized for behavioural roles including inter- and intraspecific combat (e.g. Mallison, 2011; Arbour 2009) and signaling (e.g. Persons, Currie & Norell, 2014). However, despite this importance, investigations of the osteological caudal anatomy of dinosaurs have been generally limited.

A major issue is the incomplete nature of dinosaur tails. Very few have been identified that are truly complete (i.e. represented by every single caudal vertebra in the series), and those that are complete show considerable variation both inter- and intraspecifically (Hone, 2012).

50 This makes comparisons between taxa and generalisations across clades difficult and limits the
51 confidence of any extrapolations.

52 Studies on dinosaur tails have often focused on tails as flexible structures (Pittman et al.,
53 2013) to support major muscle groups, in particular the caudofemoralis which serves as a major
54 driver in locomotion (Allen, Paxton & Hutchinson, 2009; Persons & Currie, 2011a). Previous
55 work has argued that the caudofemoralis has substantially influenced the form of anterior caudal
56 osteology, and adaptations suggested to be linked to the caudofemoralis include haemal spine
57 depth, prominent chevron and vertebral sulci (Persons and Currie 2011a, b; Cau and Serventi
58 2017), and, most frequently, the ‘transition point’ of the lateral processes (Russell, 1972; Gatesy,
59 1990; Gatesy and Thomason, 1995; Persons and Currie 2011b). The ‘transition point’ is the
60 region of the tail where the lateral processes end, and, by extension, where the caudofemoralis is
61 inferred to have terminated. The association of a major and functionally distinct muscle set with
62 one region of the tail suggests that dinosaur tails may have been modular, with different regions
63 along the tail functioning in different ways. This is obviously true of dinosaurs that bear highly-
64 derived caudal features, such as pygostyles or tail-clubs, but may also be true more generally,
65 and such derived caudal features may also be associated with less apparent morphological
66 diversity within other regions of the tail.

67 Here, we focus on a single aspect of the dinosaur caudal series: variation in anteroposterior
68 centrum length. Little work has been previously done examining patterns of centrum lengths,
69 although these have obvious influence on tail structure and by extension, may have influenced
70 function. Assuming otherwise equivalent form, a series of long vertebrae would, as a unit,
71 provide relative stiffness and stability to a tail (or at least parts of it), while series of shorter
72 vertebrae would provide a zone of greater relative flexibility (e.g. see Persons, Currie & Norrell,

2014). Compared to the rest of the axial column, the caudal series of vertebrates is generally simplified. The number of vertebrae is correlated with body size in many basal vertebrates (Head & Polly, 2007), but less so in those taxa where there is regionalization and functional constraint (as in birds and mammals – Wake, 1979). The tail however may also vary considerably, even in mammals – both in terms of caudal count and total length (e.g. Garland, 1985; Cavallini, 1995) – suggesting it is relatively free of such constraints.

Such possible variation in role and morphology has yet to be explored. Indeed, changes in caudal centra have typically been considered simple reductions along the length of the tail. For example, Sereno (1997, p185) says of *Psittacosaurus* that “[t]he caudal centra show a regular decrease in length from the first to the last centrum” and Gilmore (1936) gives a similar description of the first 40 caudals of *Apatosaurus*. Although such statements may have been deliberately simplified assessments of the condition seen in the respective tails, they do not reflect the available data. *Apatosaurus* for example, shows sections of increase in the proximal vertebrae (in terms of both proportional and absolute centrum lengths) (Fig. 1). Similarly, in the tail of *Psittacosaurus*, although the vertebrae never increase in absolute length, the vertebral series shows sections of stability in length and decreases are not always regular (Sereno, 1997).

Wide variations in the bauplans of dinosaurs (body size, bipeds and quadrupeds etc.) and various derived condition (tail clubs, pygostyles) may also be associated with greater diversity within tails than currently appreciated. As such, the pattern of vertebra length in the tails of dinosaurs is an area in need of assessment, and we observe that at least some dinosaur tails shown considerable variation in the arrangements of the lengths of series of caudal centra.

In this context, we hypothesise that there is high variation in tail length across the Dinosauria making total length difficult to predict (following Hone, 2012), and we would expect

96 that the structure of the tails of bipedal taxa differs from that of quadrupeds. We predict that
97 centrum length does not follow a simple decrease in length in successive vertebrae and that the
98 lateral processes are associated with a major change in tail function and therefore centrum
99 lengths.

100

101

102 Institutional Abbreviations

103

104 AMNH American Museum of Natural History, New York; BMNS Belgium Museum of Natural

105 Sciences, Brussels; CAGS Chinese Academy of Geological Sciences, Beijing; CM Carnegie

106 Museum of Natural History, Pittsburgh; CMN Canadian Museum of Nature, Aylmer; CYGYB /

107 CYNG Chaoyang Paleontological Museum, Chaoyang, Liaoning; FMNH Field Museum of

108 Natural History, Chicago; GIN / Gi-SPS Institute of Geology, Mongolian Academy of Sciences,

109 Ulan Baator; GMZ Grant Museum of Zoology, London; IGM Mongolian Academy of Sciences,

110 Ulan Baator; IVPP Institute of Vertebrate Paleontology and Paleoanthropology, Beijing; JME

111 Jura Museum, Eichstätt; JMP Henan Geological Museum, Henan Province; LPM Liaoning

112 Provincial Museum of Paleontology, Liaoning; MBR Museum für Naturkunde, Berlin; MNA

113 Museum of Northern Arizona, Flagstaff; MPC Mongolian Paleontological Centre, Mongolian

114 Academy of Sciences, Ulan Baator; NHM British Museum of Natural History, London; OMNH

115 Oklahoma Museum of Natural History, Norman; PIN Paleontological Institute, Russian

116 Academy of Sciences, Moscow; PMOL Paleontological Museum of Liaoning, Shenyang Normal

117 University, Shenyang; QM Qijiang Dinosaur National Geological Park Museum, Liaoning;

118 ROM Royal Ontario Museum, Toronto; RTMP Royal Tyrrell Museum of Palaeontology,

119 Drumheller; SC Italian State Collections; SMA Sauriermuseum Aathal, Aathal; UCMP

120 University of California Museum of Paleontology, Berkeley; USNM Smithsonian Museum of

Kommentiert [W1]: The Museum's abbreviation is "MfN". Collection numbers start "MB". "MB.R." refers to fossil reptiles.

The correct entry would thus be "MB.R. fossil reptiles collection of MfN (Museum für Naturkunde) Berlin"

Btw, the Archaeopteryx is MB.Av.001

Yes, it is annoying.... But that's what the rules are.

Kommentiert [W2]: Official institution code seems to be NHMUK by now
<https://www.gbif.org/grscicoll/institution/1d808a7c-1f9e-4379-9616-edb749ecf10e>

in the interest of machine learning and automated data collection, I'd recommend using the GBIF designators (as with MfN above)

121 Natural History, Washington, DC; YPM Yale Peabody Museum, New Haven; ZDM Zigong
122 Dinosaur Museum, Zigong.

123

124 **Materials & Methods**

125

126 We expanded on the dataset of Hone (2012), with additional data collected from direct
127 measurement of specimens, from measurements of photographs, and from the literature. We
128 identified previously overlooked and new material ourselves and also through suggestions from
129 various sources (see acknowledgements). It is possible that the inevitable variations and slight
130 inconsistencies of collecting data from specimens vs the literature or photographs may affect
131 narrow results. Therefore, we also took one specimen (a hadrosaur – TMP 1998.058.001) as a
132 test case for variation in measurements between first hand observations and photographs. Each
133 caudal centrum length was measured physically 10 times, and the same specimen was then
134 photographed and another 10 replicate measurements obtained from these photographs.
135 Segmented regressions were then fitted in the same way as the rest of the study, to both
136 independently estimate the break points and in particular their congruence to each other, and to
137 estimate the transition point (vertebra 12).

138 A complete tail was defined as one where every vertebrae was present down to the last
139 caudal. The last caudal can typically be identified by a rounded posterior face and a lack of
140 postzygopophyses and/or neural spine (Hone, 2012). Additional tails were regarded as complete
141 where, although one or more elements were not preserved, the absent material could be
142 accurately recorded because there was either an impression of the missing material in the matrix
143 or the missing material was bounded by other elements. Incomplete tails were also included
144 where it was felt that the missing material could be accurately reconstructed from other

specimens of the same genus or species. For example, a total tail length was calculated and included where two or more individual specimens were complete enough to suggest the animals had very similar body sizes, and where the tails of both included a series of overlapping elements (e.g. an anterior tail portion and a posterior tail portion, with both possessing the last chevron or last lateral process pair). Total tail length was taken as the sum total of all caudal centra lengths (either as measured on a specimen or described in a paper, or measured as a single piece for those specimens where the centra were closely appressed together). In most cases the live animals would have possessed intervertebral discs that would have increased tail length, but these cannot be easily estimated and so were simply excluded.

Kommentiert [W3]: bit of a stretch there if tails are highly variable between individuals.

But then, better this way than not at all.

Total femoral length was taken as a proxy for mass / body size (following Hone, 2012) for each specimen. Although other proxies (e.g. femur circumference) are stronger correlates of mass, femur length is appropriate for such datasets and the nature of many of the specimens (data collected from the literature, or compressed / crushed in preservation) means that length is often the only available measurement or the only one that can be obtained with any confidence. To examine the relationship between tail length and body size, we compared snout to sacrum length and tail length using a linear regression (see Hone, 2012). Since in some cases measurements came from different individuals, we scaled both against the femur of the specimen from which it was measured. This was also carried out for various subsets of the data to test the hypothesis that locomotion patterns of different groups would affect tail length. We therefore looked at four broad divisions of dinosaurs based on a general understanding of their locomotion: obligate bipeds (theropods, non-sauropodan sauropodomorphs), obligate quadrupeds (sauropods, thyroophoreans), bipeds and facultative bipeds (iguanodontids, hadrosaurs, psittacosaurids) together, and quadrupeds and facultative bipeds together.

Kommentiert [W4]: This is how such issues should be addressed: a clear, easily understood statement! Thank you!

(I've been reading too much shit lately where methods are unclear).

Kommentiert [W5]: Measured how?

168 In most cases, incomplete tails were not included in the analyses as it was considered
169 impossible to ascertain the missing material based on the variations in caudal counts and the
170 presence of both pygostyles and a lack of tapering in long series of caudals seen in some
171 dinosaur tails (see below). Even tails that appear to be tapering consistently to a tip may have
172 some considerable length still missing (as with e.g., *Diplodocus*). However, in an attempt to
173 maximise the limited available data, we also sourced tails that were incomplete, but considered
174 likely to be close to completeness. Such tails can at least be used to demonstrate minimum tail
175 lengths, as an incomplete tail that is as long as or longer than a complete tail still demonstrates a
176 genuine difference (data are provided in the Appendix).

177 The definition of what constitutes a ‘nearly’ complete tail is necessarily subjective given the
178 limitations of the available information, but the intention was to include only those judged to
179 have very few caudals missing and / or only a very short amount of the tail missing in terms of
180 length. In order to estimate this, we took into account the degree of tapering of the tail, the length
181 of material preserved and the length of the tail of close relatives. For example, not included is a
182 specimen of the diplodocid sauropod *Barosaurus* (McIntosh, 2005) which has 29 preserved
183 caudals that total over 6 m in length (against a femur of just 1.4 m in total length). However, the
184 last caudal in this preserved series is some 171 mm long and, while some sauropods have as few
185 as 35 caudals (Borsuk-Bialynicka 1977), a large amount of tail is considered likely missing in
186 *Barosaurus*, given the size of the caudals present and the considerably higher number of caudals
187 in other diplodocids (e.g. Gilmore, 1936). Note that the holotype of the small hadrosaur
188 *Tethyshadros* (Dalla Vecchia, 2009) was incorrectly considered complete in Hone (2012) and so
189 is not in the datasets.

Kommentiert [W6]: Name and shame ;)

190 The patterns of individual caudal centrum lengths that make up dinosaurian tails were
191 also analysed. Here data from the above specimens was supplemented with additional but
192 incomplete tails as the analysis looked at changes in individual centra as part of a series, rather
193 than the tail as a whole unit. Note that even tails that can be diagnosed as complete are not
194 always included in the analysis since either information on individual vertebrae lengths was not
195 available in the literature, or the divisions between the vertebrae could not be reliably measured
196 (e.g. the holotype of *Jinfengopteryx* – CAGS IG 040801).

197 To test the hypothesis that caudal centrum lengths do not follow a simple decrease in size
198 along the series we used segmented regression (also known as piecewise or broken stick
199 regression) to identify transitions in centrum length (break points). This was then compared with
200 the boundary between the muscular and non-muscular parts of the tail (transition point).
201 Essentially, this approach, where appropriate, fits a series of linear regressions to specific subsets
202 of the data. For example, in *Apatosaurus* (CM 3378), the first section covers vertebrae 1–20, the
203 second vertebrae 21–35, the third vertebrae 35–67 and the final section from vertebra 67–84 (Fig.
204 2). Clearly, however, in some cases a simple linear regression will provide a better fit to the data.

205 To test this, a Davies test (Davies, 2002) was used to test for a non-constant regression parameter
206 in the linear predictor (vertebra number) on centrum size using the R package segmented version
207 0.4-0.0 (Muggeo, 2003, 2008) implemented in R version 3.0.3 (R core team, 2014). In effect, this
208 allows us to fit a segmented regression where the data support this (see for example *Apatosaurus*
209 in Fig. 2) and a linear regression where there is no evidence to support a more complex fit (e.g.,
210 *Opistoceolocaudia* in Fig. 2).

211 Where the Davies test suggests that a segmented regression is appropriate, the next question
212 is how many segments to fit. Candidate models with 1–4 breaks were fitted using *segmented* and

Kommentiert [W7]: This what?

Please check entire MS for missing nouns!
(don't you hate style editors?)

Kommentiert [W8]: grammar

the best model selected on the basis of the Akaike Information Criterion (Akaike, 1974). In essence, this approach selects the model which best balances explanatory power with simplicity. An upper limit of four breaks was chosen since some specimens had 20 or fewer vertebrae, limiting the number of breaks that could be plausibly fitted.

In this study, models used the default parameters in *segmented*, with quantiles as the starting points for the iterative breakpoint analysis, but with 50 bootstrap samples and a maximum of 10 iterations. Candidate models that could not be fitted in *segmented* (usually because of gaps in the data) were discarded.

Results

Tail length vs snout-sacrum length

The model suggests that tail length is an extremely poor predictor of snout to sacrum length (Fig. 3) (linear regression of snout/sacrum to femur ratio on tail to femur ratio: $F_{1,21} = 0.11$, $p = 0.74$). For example, *Scutellosaurus* has a tail to femur ratio of 8.8, and with a femur length of 82 mm, this corresponds to an estimated snout-sacrum size between 263.0 and 485.1 mm though the real value is much closer to the upper bound of 405 mm. At the opposite end of the scale, the tail to femur ratio of 1.2 in *Epidexipteryx* would correspond to an estimated snout-sacrum range of 173.4 to 259.1 mm although the actual value is outside of even this broad range at 158 mm.

If we attempt to minimise problems due to intraspecific (ontogenetic) scaling or phylogenetic bias and restrict the analysis to the largest individual of each species (where the full dataset contains more than one individual), and when juveniles or indeterminate taxa are removed the same pattern is retained (linear regression: $F_{1,16} = 0.01$, $p = 0.91$). This is also true of the various subdivisions by locomotor style: bipeds alone (linear regression of snout-sacrum:

femur on tail to femur): $F(1,8)=0.01$, $p=0.92$; quadrupeds alone: $F(1,5)=0.2938$, $p=0.61$; bipeds plus facultative bipeds: $F(1,14)=0.331$, $p=0.57$; quadrupeds plus facultative bipeds: $F(1,11)=0.009$, $p=0.92$. In short, tail size is not clearly related to body size in non-avian dinosaurs, even allowing for broad distinctions in locomotor style.

Patterns of caudal vertebrae length

Across the Dinosauria, most tail sequences passed the Davies test and so could be reconstructed with one or more breaks to the series of individual centrum lengths. There was at least some consistency in the results within clades, with several specimens of single taxa showing similar patterns to one another (e.g. *Archaeopteryx* – Fig. 4) though others were inconsistent (e.g. *Coelophysis* – Fig. 5).

Break points

For 18 out of 25 specimens, the distance between the break point and transition point was lower than would be expected by chance (exact binomial test, $p=0.043$) (Fig. 6). Where multiple measurements were taken from one hadrosaur tail as a test of consistency of measurements, the congruence between break points as produced from direct measurements of the specimen and those taken from a photograph, was good. In both cases, the model fitted four break points (specimen (mean $\pm$ se): 12.0 $\pm$ 1.59, 45.8 $\pm$ 3.48, 61.5 $\pm$ 3.90, 74.7 $\pm$ 0.71; photographs 11.9 $\pm$ 1.99, 48.5 $\pm$ 1.29, 57.3 $\pm$ 1.07, 59.4 $\pm$ 1.04). In particular, both methods fitted a break point very close to the actual transition point, and even at the distal end, where there was slight disagreement, all four of the break points fitted from photographs were encompassed with the standard errors of

break points derived from the specimen itself (Fig. 7). This suggests that the data taken from photographs for various specimens will yield accurate data.

Discussion

Overall lengths of dinosaurian tails

Our hypothesis that there is high variation in tail lengths across the dinosaurs, and that tail lengths do not correlate well with body size (i.e. snout-sacrum length) was supported with very wide confidence limits for predictions of one based on the other (Fig.3). However, the prediction that there would be similarities between bipedal or quadrupedal taxa was not met. Even when considering facultatively bipedal or quadrupedal taxa with obligate biped and quadrupeds, no clear relationship between body size and tail length was recovered.

The data from the ‘near complete’ tails is of course limited in its use given these issues, though at least some of the specimens recorded here do suggest that there may be some consistency within groups. Additional data may alter this pattern and suggest a greater level of consistency, but for most dinosaur groups, attempting to estimate the total length of a tail from anything other than a near complete series is subject to a wide range of error and uncertainty, as seen even within some small clades (e.g., Scansoriopterygidae). Dinosaur tails were also likely evolutionally plastic and frequently assumed forms to serve specific functions (or specific combinations of functions) adding further to interspecific, and perhaps also intraspecific, variation.

Caudal length patterns in dinosaur tails

Considerable variation is seen not just in the overall and proportional sizes of dinosaur tails but also in the lengths of the individual caudal centra that comprise them. Although the distalmost

caudals of a series are generally smaller than more proximal ones, over a short section of consecutive elements there may be patterns of increasing length, stability, or decreasing length (and all three may occur in one individual e.g., *Apatosaurus* CM 563 – Gilmore, 1936). Although the datasets here are somewhat limited, they do cover a wide range of dinosaurian biology – large and small, herbivores and carnivores, bipeds and quadrupeds, long and short tails, and taxa from the Late Triassic to the end of the Cretaceous. Thus some considerable variation may be expected, but even so there are some clear patterns. Most notably, many dinosaurs show repeated series of, on average, increasing and decreasing centra lengths along the caudal series as demonstrated by the positions of break points and the associated regressions.

Most taxa show an early short series of tail vertebrae decreasing in length sequentially, then a short series increasing in length (typically including the longest centra in the tail), followed by a long series of progressive decrease. These include at least one specimen each of *Kentrosaurus* (Fig. 8), *Leptoceratops*, *Centrosaurus* (both Fig. 9), *Lufengosaurus* (Fig. 10), *Apatosaurus*, *Camarasaurus* (both Fig. 2), *Gorgosaurus*, *Tyrannosaurus* (both Fig. 11), *Ornithomimus*, *Nomingia* (both Fig. 12), *Microraptor*, and *Velociraptor* (both Fig. 13). Note that frequently the first and second caudal vertebrae may vary from this overarching pattern. While not universal, this pattern is widespread in the Dinosauria. Other specimens are not so far from this pattern (e.g., *Dilophosaurus* (Fig. 11), *Ingenia* (Fig. 12), *Ouranosaurus* (Fig. 14), *Lambeosaurus* (Fig. 15)). It may be possible that this pattern is even more prevalent but is, in some instances, hidden from the tests used here by some variation or lack of data. For example, the proximal caudals of *Diplodocus* and *Majungasaurus* are not recorded, and although those preserved do seem to conform to the pattern, it cannot be confirmed.

Other taxa ~~do~~ deviate considerably from the short-long-shortening pattern described above (e.g. *Plateosaurus* (Fig. 9), *Juravenator* (Fig. 11)), indeed the caudals of *Coelophysis* tend to increase in length for much of the series (Fig. 5). Various constraints may confound the basic pattern and affect the overall distribution. For example, the majority of the vertebrae in the dromaeosaurs *Velociraptor*, *Deinonychus* and *Microraptor* are bound by a complex series of extended zygapophyses and chevrons that stiffen the tail and perhaps free the vertebrae from normal functional constraints. This may explain some of the variation seen between specimens and genera (Fig. 13). However, the patterns of centrum lengths seen in the tails of all three specimens of *Archaeopteryx* and the putative glider *Microraptor* are strikingly similar and, although only a very limited set of data, ~~do~~ show a level of consistency not seen in other groups (Figs. 4, 13). This suggests at least the possibility that this similarity in form is connected to the shared tail function of control in flight. It has been noted by Gatesy and Dial (1996) that *Archaeopteryx* would benefit in flight control from a stiff tail that was only flexible at the very base and this is reflected here with a proximal section of short centra and then a very rapid jump to considerably longer centra.

In contrast, *Juravenator* is very different to most other taxa (Fig. 12), though this is perhaps the result of the holotype specimen being a juvenile. However, Chiappe and Göhlich (2010) noted that part the caudal length pattern of *Juravenator* (with a stable series then a series of short centra, then long, and then shorter again) may be consistent across at least some compsognathids. This suggest that *Juravenator* is perhaps not just an outlier on its own, but is representative of a pattern that is normal for the clade. Still, it remains unusual compared to most other dinosaurs.

Kommentiert [W9]: grammar? Confusing.

Error

328 Given the limited availability of data and the problems associated with sourcing information
329 from the literature, mounted specimens, or those with poor preservation, there is likely to be
330 some error in the data. Distortion, if systematic within a specimen, would still preserve the
331 pattern overall and if random (within or between specimens) should have no overall effect. This
332 is similar to any issues of measurements taken from the literature where different authors may
333 have used slightly different metrics to take the length of the caudal centra, but we would expect
334 consistency within specimens and thus preservation of patterns. As noted above, our own formal
335 assessment of the possible differences between the measurements from a specimen and from a
336 photograph produced similar results, especially for the prediction of the transition point which
337 was identical in both and correctly identified as caudal vertebra 12 (Fig. 7).

338 The vertebrae of smaller specimens may cause problems as these will be harder to measure
339 with equivalent accuracy. For example, the long sequence of identical values seen in
340 *Juravenator* could be because the animal is still a juvenile or may genuinely reflect the unusual
341 caudal anatomy of this genus (or of compsognathids as a whole). However, it could simply be
342 because the vertebrae are so small that variation between them (even when measuring to the
343 nearest 0.1 mm) was difficult to detect (as also perhaps seen in specimens of *Psittacosaurus*).
344 Similarly, the alternating sequence of long-short-long seen in various specimens of *Apatosaurus*
345 as described above, may simply be size related (it is easier to measure long vertebrae and find
346 clear differences between them). However, these errors in measurements are collectively likely
347 to be unbiased overall and so should not affect the results or general patterns reported here.

348 There is some consistency within clades, with for example two specimens of *Leptoceratops*
349 (despite differing caudal counts – Fig. 9), three specimens of *Archaeopteryx* (Fig. 4), and two
350 tyrannosaurids (Fig. 11) all showing similar patterns to one another, suggesting consistency in

the data and the analysis. Two specimens of *Velociraptor* are very similar, although a third is rather different, but similar to its near relative *Deinonychus* (Fig. 13).

Implications

Assuming equivalency of vertebral articulation, for a given unit of length of tail, more joints will increase flexibility and fewer joints will make it less flexible. Thus, shorter centra imply greater zonal flexibility and longer ones, greater zonal stiffness. As such, we can use the varying lengths of centra within different parts of dinosaur tails to infer differing levels of flexion.

The repeated pattern seen here of a series of short centra, then a series on long ones, and then finally a series of tapering caudals suggests that many dinosaurs had a flexible tail base, then a stiffened section and finally a more flexible section. Our hypothesis that the transition point (i.e. the termination of the attachment of the caudofemoralis musculature) is linked to a major change in tail function (as implied by centrum length) is borne out by our analyses. We recorded the last centrum to preserve a lateral process from specimens directly or where they were recorded in the literature. Comparing these to the data on serial variation shows that the transition point often coincides closely with a shift in pattern of centra length, (Fig.6) as determined by the changes in regression lines (e.g. *Lambeosaurus* (Fig. 15), *Juravenator*, *Gorgosaurus*, *Tyrannosaurus* (all Fig. 11), *Ornithomimus* (Fig. 12)).

Even in taxa where this pattern does not hold, there is still some evidence that the transition has an influence on caudal length, as the point recorded may be associated with a slight ‘hump’ in the data (i.e. a short increase and then decrease in vertebral length over just four or five vertebrae) as seen in e.g. *Plateosaurus* (Fig. 10) and *Nomingia* (Fig. 12). As the transition point is perhaps better thought of as a ‘zone’ (Persons & Currie 2011b), a little leeway must be

374 allowed and we would not expect a perfect correlation between the change in centrum length and
375 the last vertebra supporting a lateral process. Even so, it is clear that the calculated break points
376 in the series do often fall exactly or within one or two vertebrae of the last centrum with a lateral
377 process. Based on this discovery, it may be possible to deduce the transition point in some
378 specimens even if the lateral processes and chevrons are missing or damaged based on the
379 pattern of the lengths of centra. The series of long vertebra that correspond to most of the length
380 of the anterior tail up to the transition point would make the tail relatively stiff. This would
381 improve the efficiency of the caudofemoralis muscles as this stiffness would reduce energy loss
382 through movements between vertebrae and ensure that most effort of contract led to driving the
383 femur and not flexing the tail.

384 Posterior to the transition point, the requirement for great stiffness is presumably relaxed and
385 thus lead to the simple pattern of general reduction in size of successive centra moving
386 posteriorly. Simple selection for reduction in mass distally (with obvious exceptions such as taxa
387 bearing tail clubs) would lead to the pattern seen here and may be the typical primitive condition
388 for reptilian tails (see the data for *Varanus* and *Crocodylus* – Fig. 16, though clearly this is a very
389 limited dataset).

390 These two more posterior sections of the tail thus have simple mechanical explanations, but
391 this does not explain the series of short centra at the base of the tail. We suggest that this section
392 would allow the entire tail to flex as a unit, as clearly any proximal motion of the tail would also
393 affect any more distal portion of the tail. Thus a flexible section at the very base of the tail allows
394 the entire tail to be moved without compromising the stiffness of the successive section. This is
395 therefore likely a trade-off between flexion and stiffness. It should also be noted that the very
396 proximal section of the tail may also have been less strongly influenced by contractions of the

397 caudofemoral musculature, because the most proximal caudal vertebrae typically lack chevrons.
398 This would afford far less muscle attachment than in the immediately posterior section of the tail.
399

400 **Evolution of dinosaurian caudal centra series**

401 This short-long-decreasing pattern was likely acquired independently in multiple lineages of
402 dinosaurs. A number of Triassic and / or basal forms (*Coelophysis*, Fig. 5; *Plateosaurus*, Fig.
403 10), lack the pattern and retained the apparently primitive diapsid / archosaur condition of a
404 simple progressive decrease along the length of the tail. The repeated evolution of various
405 osteological structures able to passively stiffen the tail (e.g. elongate zygopophyses and chevrons
406 in some theropods, hyposphene-hypantra articulations in some sauropods, ossified tendons in
407 ornithischians) suggests that tail rigidity was favoured repeatedly in various groups of the
408 Theropoda, Sauropoda and Ornithischia. Thus, the apparent distribution of the short-long-
409 decreasing pattern seen here in later theropods, sauropods and ornithischians may have also
410 arisen independently from similar selective pressures favouring a small zone of high flexibility
411 immediately posterior to the hips and an extended zone of stiffness that helped improve
412 locomotory efficiency.

413 Despite the wide variations in patterns of elongation and constriction in centrum lengths,
414 it is clear that in at least some cases where there is a reasonable number of caudals preserved and
415 their positions known, it may be possible to reconstruct the missing ones with some confidence.
416 Repeated patterns within and between taxa, and long strings of caudals with a consistent pattern
417 of elongation or reduction means that the sizes of missing vertebrae may be estimated.
418 Potentially even the total length of a tail may be estimated if much of the series is preserved.
419 However, in general this is likely to be difficult – the variation seen here in the patterns of

420 increases and decreases, and the differing numbers of vertebrae in those various sets of increases
421 and decreases are highly variable and difficult to predict. In particular, the end of the tail is
422 difficult to assess. While clearly any regression of caudal size that was decreasing successively
423 would eventually suggest a centrum of near zero or negative length, at what point before this the
424 tail would actually terminate cannot be estimated. Gilmore (1936) notes with relation to the
425 ‘whiplash’ segment of the distal tail of *Apatosaurus* that “the uniformity in size of these terminal
426 rod-like caudals is such that any loss would be difficult to detect” and similarly, this general
427 problem of tail termination is further exacerbated by the presence of a pygostyle in some
428 maniraptoran theropods.

429 The variation in caudal counts in taxa also has implications for other aspects of research. For
430 example, taphonomic analyses may consider sorting or loss of elements by size and therefore
431 knowing how many vertebrae and of what size ranges a given taxon has may be important. In an
432 analysis of a bone bed dominated by the hadrosaur *Amurosaurus*, Lauters et al. (2008) looked at
433 the different numbers of element types preserved. They suggested that the vertebrae of
434 *Amurosaurus* were underrepresented in the bonebeds based on the estimated number of vertebrae
435 in the axial column. However, with very little articulation known for remains of *Amurosaurus*, it
436 cannot be easily estimated how long the tail was or how many caudals it possessed, with tails for
437 hadrosaurs known to have as few as around 50 caudals (Horner, Weishampel & Forster, 2004) to
438 over 75 (Lull & Wright, 1942). (There is of course also likely variation within the number of the
439 cervical, dorsal and sacral series, though based on Hone [2012], this is likely to be much less of
440 an issue than the caudal series). The results of Lauters et al. (2008) were robust and in this case
441 such an issue is not likely to have had a major effect on their results, but the uncertainty
442 surrounding the number of vertebrae in the axial column means that care should be taken when

443 performing such an analysis. We suggest that, unless the true axial count is known with
444 confidence, either caudals should not be counted, or upper and lower estimates of the number of
445 vertebrae in the column should be employed, or such considerations should be limited to the
446 lateral process bearing caudals (where the number is more certain).

447
448 **Conclusions**

449 Total tail length remains difficult to estimate for incomplete tails in the Dinosauria, and
450 there is some strong variation both between and within family-rank equivalent clades for various
451 taxa. However, there is some consistency in patterns of overall caudal lengths. Notably, the
452 proximal part of the tail often consists of relatively short vertebrae, followed by a series of longer
453 vertebrae and then a shift to decreasing centrum lengths beyond the transition point.

454 Although here used to investigate dinosaur tails, these methods have a much wider
455 applicability in terms of investigating patterns across series of vertebrae or other sequential
456 elements (e.g. rib length, scale size in reptiles, segment length in invertebrates etc.).

457
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467

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550
551

552 **Figure captions**

553

554 Figure 1. A complete caudal series for the tyrannosaurid *Gorgosaurus* (RTMP 91.36.500). One
555 of very few complete series that is also both articulated and preserved in three dimensions. Scale
556 bar is 200 mm.

557

558 Figure 2. Regressions for centrum lengths within the tails of members of Sauropoda. Here, and
559 for subsequent figures, predicted break points and their error bars are indicated at the bottom of
560 each graph where these have been calculated, and the transition point (where known) is indicated
561 by an arrow (the same point is inferred for both specimens of *Apatosaurus*). Both specimens of
562 *Apatosaurus* are from the CM.

563

564 Figure 3. Relative size of snout to sacrum against relative tail length. Snout to sacrum vs tail
565 length, with both measurements scaled to femur size (see Methods). Comparisons drawn from
566 the same individual are shown as black circles; those from different individuals as open circles.
567 The solid line shows the fitted (non-significant) regression; dashed lines show 95% confidence
568 intervals for this regression. The grey lines show the range and distribution of tail to femur ratio
569 for all of the species in our analysis. See also Table 1.

570

571 Figure 4. Regressions for centrum lengths within the tails for specimens of *Archaeopteryx*. The
572 different specimens can be identified by their museum prefixes.

573

574 Figure 5. Regressions for centrum lengths within the tails for specimens of *Coelophysis*. The
575 same transition point is inferred for all specimens. All three specimens are from the AMNH.

576

577 Figure 6. Mean distance between break point and transition point in 1000 randomisations, plotted
578 against the actual distance. The grey line shows the 1:1 line; red lines show standard errors. For
579 all but seven of the specimens, the actual distance was lower than the randomised distance (Exact
580 binomial test, $p=0.04$).

581

582 Figure 7. Segmented regressions for specimen TMP1998.058.001. Segments derived from
583 photographs (red) and from the specimen itself (blue). Both methods fitted a break point very
584 close to the actual transition point, and with the exception of a break point right at the distal end,
585 break points derived from one method overlapped with break points derived from the other.

586

587 Figure 8. Regressions for centrum lengths within the tails for members of the Thyrophorea. The
588 stegosaur *Kentrosaurus* above, and ankylosaur *Dyoplocephalus* below.

589

590 Figure 9. Regressions for centrum lengths within the tails for members of the Ceratopsidae. The
591 first two specimens of *Psittacosaurus* are from the AMNH and the two specimens of
592 *Leptoceratops* are from the CMN.

593

594 Figure 10. Regressions for centrum lengths within the tails for non-sauropodan members of the
595 Sauropodomorpha. Patterns of centrum lengths for a Jurassic and Triassic sauropodomorph.

596

597 Figure 11. Regressions for centrum lengths within the tails for members of the Theropoda.
598 Centrum length patterns for non-maniraptoran theropods.

599

600 Figure 12. Regressions for centrum lengths within the tails for members selected non-paravian
601 Maniraptora.

602

603 Figure 13. Regressions for centrum lengths within the tails for members of the Dromaeosauridae.
604 The different specimens of *Velociraptor* can be identified by their museum prefixes.

605

606 Figure 14. Regressions for centrum lengths within the tails for members selected non-
607 hadrosauroid Iguanodontia.

608

609 Figure 15. Regressions for centrum lengths within the tails for members selected Hadrosauridae.

610

611 Figure 16. Regressions for centrum lengths within the tails for two non-dinosaurian Reptiles –
612 *Crocodylus niloticus* and *Varanus niloticus*.

613

614

615

616

617 Table 1. Estimated ratio of body length (snout-to-sacrum) to tail length, with both scaled to
618 femur size, with upper and lower 95% confidence intervals (cf. Figure 3). Also shown are the
619 smallest and largest snout-sacrum sizes compatible with these confidence limits.

620

Genus	fit	lwr	upr	snout to sacrum (min)	snout to sacrum (max)
<i>Dryosaurus</i>	4.34	3.91	4.77	1290.6	1575.1
<i>Othneilosaurus</i>	4.38	3.93	4.84	1041.1	1282.5
<i>Jeholosaurus</i>	4.39	3.92	4.85	356.9	441.8
<i>Leaellynasaura</i>	4.71	2.43	6.99	170.3	489.6
<i>Stegosaurus</i>	4.29	3.70	4.88	2814.9	3707.8
<i>Scutellosaurus</i>	4.56	3.21	5.92	263.0	485.1
<i>Scleidosaurus</i>	4.40	3.90	4.91	1382.9	1741.9
<i>Pinacosaurus</i>	4.41	3.87	4.96	1546.6	1982.7
<i>Dyoplosaurus</i>	4.33	3.86	4.79	2169.3	2692.1
<i>Saichania</i>	4.37	3.94	4.80	1497.4	1823.0
<i>Edmontosaurus</i>	4.35	3.92	4.77	3841.6	4676.9
<i>Lambeosaurus</i>	4.32	3.84	4.80	4151.3	5181.7
<i>Corythosaurus</i>	4.33	3.86	4.79	4149.4	5149.5

Hadrosauridae_indet	4.35	3.92	4.77	2058.0	2505.5
Tenontosaurus	4.42	3.84	5.01	1802.8	2353.3
Parksosaurus	4.37	3.94	4.80	1024.4	1248.8
Psittacosaurus	4.31	3.79	4.83	594.9	757.9
Psittacosaurus	4.34	3.91	4.77	406.9	496.4
Psittacosaurus	4.33	3.89	4.78	252.9	310.6
Psittacosaurus	4.35	3.93	4.77	530.2	644.4
Archaeoceratops	4.26	3.51	5.01	680.3	971.6
Leptoceratops	4.33	3.86	4.79	1024.1	1268.9
Leptoceratops	4.30	3.74	4.86	860.5	1116.7
Leptoceratops	4.29	3.69	4.88	1075.2	1421.4
Protoceratops	4.31	3.79	4.83	98.5	125.5
Protoceratops	4.29	3.68	4.89	103.1	137.0
Centrosaurus	4.31	3.79	4.83	2803.9	3572.2
Anchiceratops	4.27	3.58	4.96	2651.9	3667.8
Lufengosaurus	4.37	3.94	4.80	2186.7	2665.7
Camarasaurus	4.36	3.94	4.79	2237.9	2718.6
Opisthocoelicaudia	4.33	3.87	4.78	5405.2	6673.4
Spinophorosaurus	4.41	3.87	4.94	4706.9	6007.3
Coelophysis	4.42	3.82	5.03	573.6	753.8
Gorgosaurus	4.37	3.94	4.80	2541.3	3098.0
Ornithomimid	4.33	3.89	4.78	1809.8	2221.5
Gallimimus	4.34	3.91	4.77	2600.8	3174.0
Ornithomimus	4.37	3.94	4.79	1670.9	2032.6
Sinocalliopteryx	4.41	3.87	4.95	917.9	1172.3
Caudipteryx	4.24	3.43	5.06	510.6	754.3
Caudipteryx	4.25	3.43	5.06	634.5	936.2
Nomingia	4.27	3.58	4.96	1021.4	1412.6
Mei	4.35	3.93	4.78	318.6	386.9
Jinfengopteryx	4.35	3.92	4.77	313.6	381.8
Anchiornis	4.45	3.71	5.20	NA	NA
Sinusonasus	4.34	3.90	4.78	522.0	640.0
Microraptor	4.39	3.92	4.85	NA	NA
Microraptor	4.33	3.87	4.79	379.3	469.0
Microraptor	4.44	3.75	5.13	322.9	441.3
Microraptor	4.42	3.84	5.00	199.8	259.9
Epidexipteryx	4.24	3.40	5.08	173.4	259.1
Eosinopteryx	4.32	3.82	4.81	153.0	192.3
Aurornis	4.34	3.91	4.77	254.0	310.3

<i>Archaeopteryx</i>	4.35	3.93	4.77	145.4	176.7
<i>Archaeopteryx</i>	4.33	3.87	4.79	214.1	264.6
<i>Changyuraptor</i>	4.34	3.91	4.77	629.2	768.5

APPENDICES:

Table 1. Master dataset of all data – Complete tail lengths, Snout-Sacrum lengths, Incomplete tail lengths, Centrum lengths, Transverse Processes, References.

Kommentiert [W10]: Please name "sheet1" ;)

SI Fig 1. Break points for ornithischian tails. Aligned caudal centra (black squares, spaces indicate missing vertebrae), break points as calculated (red points with error bars) and transition point (where known, blue triangles) for all ornithischians in the study.

SI Fig 2. Break points for sauropodomorph tails. Aligned caudal centra, break points as calculated and transition point (where known) for all sauropodomorphs in the study.

SI Fig 3. Break points for theropod tails. Aligned caudal centra, break points as calculated and transition point (where known) for all theropods in the study.